First Evidence for Direct CP Violation

CERN-Dortmund-Edinburgh-Mainz-Orsay-Pisa-Siegen Collaboration

Talk given by A.C. SCHAFFER

*Presented at the XXIII Rencontres de Moriond*
*Les Arcs, France, 6-13 March 1988*

U.E.R
de
l'Université Paris - Sud

Institut National
de Physique Nucléaire
et
de Physique des Particules

Bâtiment 200 - 91405 ORSAY Cedex
FIRST EVIDENCE FOR DIRECT CP VIOLATION

CERN-Dortmund-Edinburgh-Mainz-Orsay-Pisa-Siegen Collaboration

Talk given by A.C. SCHAFFER

CERN, Geneva, Switzerland
G. Dietrich and W. Heinem
Institut für Physik, Universität Dortmund, Fed. Rep. Germany
R. Black, D.J. Candlin, I. Muir, K.J. Peach, B. Pijlgrims, I.P. Shipsey and W. Stephenson
Physics Department, University of Edinburgh, UK
H. Blümner, M. Kasemann, K. Kleinheinrich, B. Panzer and B. Renk
Institut für Physik, Universität Mainz, Fed. Rep. Germany
Laboratoire de l'Accélérateur Lineaire, Université de Paris-Sud, Orsay, France
A. Bigi, M. Calvetti, R. Carosi, R. Castill, C. Cerri, G. Gargani, E. Massa, A. Nappi and G.M. Pierazzini
Dipartimento di Fisica e Sezione INFN, Pisa, Italy
C. Becker, D. Heyland, M. Holder, G. Quast, M. Rost, W. Weils and G. Zech

2) On leave from SLAC, Stanford, Calif., USA (work supported in part by the U.S. Department of Energy contract DE-AC03-76SF00515).
3) Present address: Scuola Normale Superiore e Sezione INFN, Pisa, Italy.
5) Present address: LAL, Université Paris-Sud, Orsay, France.
8) Present address: FWO, University of Amsterdam, The Netherlands.
9) Present address: Syracuse University, NY, USA.
10) Present address: Dipartimento di Fisica e Sezione INFN, Perugia, Italy.
a) Funded by the German Federal Minister for Research and Technology (BMFT) under contract 05 4M3318.
b) Funded by Institut National de Physique des Particules et de Physique Nucléaire, France.
c) Funded by the German Federal Minister for Research and Technology (BMFT) under contract 034 S 014.

ABSTRACT

The double ratio \( R \) of the relative decay rates of the short- and long-lived neutral kaons into two charged and two neutral pions was measured to be \( 0.980 \pm 0.004 \pm 0.005 \). The deviation of \( R \) from unity implies CP violation in the transition of the CP-odd \( K_2 \) into two pions with \( \epsilon'/\epsilon = (3.3 \pm 1.1) \times 10^{-3} \).
Since its first observation in the decay of the long-lived neutral kaon into two pions [1], CP violation remains one of the enigmas in particle physics. While CP violation is manifest in neutral kaon decays, the search for CP-violating effects elsewhere has been unsuccessful. In the phenomenology of CP violation in the neutral kaon system [2] it is convenient to define the CP eigenstates $K_1 = (K^0 + \bar{K}^0)/\sqrt{2}$ and $K_2 = (K^0 - \bar{K}^0)/\sqrt{2}$ with $K_1 = + CP \ K_1$ and $K_2 = - CP \ K_2$. The short- and long-lived $K^0$ are the mass eigenstates which can be written as $K_S = K_1 + \epsilon \ K_2$ and $K_L = K_2 + \epsilon \ K_1$. The parameter $\epsilon$ describes CP violation induced by kaon state mixing. Direct CP violation may also occur in the decay of the $K_2$ into two pions with a relative amplitude of [2]

$$\epsilon' = i/\sqrt{2} \ \text{Im} \ (A_2/A_0) \ e^{i(\delta_2 - \delta_0)},$$

where $A_0$ and $A_2$ are the amplitudes for the decay into isospin 0 and 2 two-pion states; $\delta_0$ and $\delta_2$ are the corresponding $\pi\pi$ scattering phase shifts at the mass of the $K^0$. With these definitions the ratios of $K_L$ and $K_S$ decay amplitudes into $2\pi^0$ and $\pi^+\pi^-$ respectively are

$$\eta_{00} = \langle 2\pi^0 | T | K_L \rangle / \langle 2\pi^0 | T | K_S \rangle = |\eta_{00}| e^{i\Phi_{00}} = \epsilon - 2\epsilon'$$

and

$$\eta_{+ -} = \langle \pi^+\pi^- | T | K_L \rangle / \langle \pi^+\pi^- | T | K_S \rangle = |\eta_{+ -}| e^{i\Phi_{+ -}} = \epsilon + \epsilon'.$$

The relevant experimental measurements are the magnitudes and phases of these two parameters, and the real part of $\epsilon$ determined from the charge asymmetry in semileptonic $K_L$ decays: $|\eta_{+ -}| = 2.27 \pm 0.02 \times 10^{-3}$ [3]; $\Phi_{+ -} = 44.6 \pm 1.2^\circ$ [4]; $|\eta_{00}|/|\eta_{+ -}| = 1.00 \pm 0.01$ [5]; $\Phi_{00} = 55 \pm 5^\circ$ [6]; and $\text{Re} \ \epsilon = (1.62 \pm 0.09) \times 10^{-3}$ [7]. All experimental results are compatible with $\epsilon = 2.27 \times 10^{-3} \exp (i \ 43.7^\circ)$ and the Superweak Model [8] in which state mixing is the only source of CP violation and $\epsilon' = 0.$

In the theory of six weakly interacting quarks [9], direct CP violation as well as state mixing are introduced by transitions via heavy-quark intermediate states. Based on this, a small but non-zero value of $\epsilon'$ is predicted [10]. From $\pi\pi$ scattering, its phase is determined to be $61 \pm 3^\circ$ [11]. This angle is close to the phase of $\epsilon$, so that to a good approximation $\text{Re} \ \epsilon'/\epsilon = 1/6 (1 - |\eta_{00}/\eta_{+ -}|^2)$.

This relation is used to determine $\epsilon'/\epsilon$ from the double ratio of $K_S$ and $K_L$ decay rates into charged and neutral pions:

$$R = |\eta_{00}/\eta_{+ -}|^2 = \frac{\Gamma(K_L \to 2\pi^0)/\Gamma(K_L \to \pi^+\pi^-)}{\Gamma(K_S \to 2\pi^0)/\Gamma(K_S \to \pi^+\pi^-)}.$$

This experiment has been performed at the CERN Super Proton Synchrotron. It is based on the concurrent detection of $2\pi^0$ and $\pi^+\pi^-$ decays. Collinear $K_S$ and $K_L$ beams are employed alternately, changing frequently from one to the other to reduce time-dependent effects. Details of the apparatus and beams have been given elsewhere [12]. Kaons with energies around 100 GeV are produced by 450 GeV protons incident upon one of two targets at an angle of 3.6 mrad with respect to the kaon beam line. The $K_L$ are derived from $\sim 10^{11}$ protons per pulse and are selected by two-stage collimation at distances of 48 m and 120 m, respectively, from the first production target.

*) We disregard here the two-standard-deviation discrepancy in $\Phi_{00}$. A considerably more sensitive measurement of $\Phi_{00} - \Phi_{+ -}$ is being carried out by this group.
Alternatively, \( \sim 10^7 \) protons per pulse are brought onto the second target, from which the \( K_S \) are selected by collimation after 7 m. The retractable \( K_S \) target station, sweeping magnet and collimator system are mounted on a train which can be moved through 48 m of the \( K_L \) decay region. The \( K_S \) data are taken with the beam train displaced in 1.2 m steps so that both the \( K_S \) and \( K_L \) decay distributions become effectively uniform in the fiducial region (the average \( K_S \) decay length is 6 m).

The detector is based on calorimetry and is designed for good stability and high efficiency, large acceptance and fast data-aquisition. A schematic layout of the apparatus is shown in Fig. 1. The principal features are summarized as follows:

- both \( K_S \) and \( K_L \) beams are transported in vacuum;
- an anticounter in the \( K_S \) beam, preceded by a 7 mm lead converter, vetos decays in the collimator, defines the upstream edge of the decay region, and permits the relative calibration of the \( 2\pi^0 \) and \( \pi^+\pi^- \) energy scales to a precision better than \( \pm 10^{-3} \);
- four ring-shaped anticounters surrounding the decay region detect large-angle photons and thus reduce unwanted three-body decays;
- two wire chambers spaced 25 m apart, with \( \pm 0.5 \) mm resolution in each projection, track charged pions;
- a hodoscope of scintillation counters triggers on \( \pi^+\pi^- \) decays by a coincidence of hits in opposite quadrants;
- a liquid-argon/lead sandwich calorimeter with strip readout measures photons with \( \pm 0.5 \) mm position and \( \pm 7.5\%/\sqrt{E(\text{GeV})} \) energy resolution;
- a plane of scintillation counters, installed in the liquid argon after 13 radiation lengths of material, triggers on \( 2\pi^0 \) decays;
- an iron/scintillator sandwich calorimeter measures, in conjunction with the liquid-argon calorimeter, the energy of charged pions with \( \pm 65\%/\sqrt{E(\text{GeV})} \) resolution;
- two planes of scintillators, after a total of 3 m of iron equivalent, reject \( K^0 \to \pi\mu\nu \) decays.

The decay region is evacuated and the volume between the chambers is filled with helium. A thin composite Kevlar window of \( 3 \times 10^{-3} \) radiation length separates the decay region from the wire chamber section. A tube of 20 cm diameter, through the centre of the window and the detectors, allows the neutral beam to continue in vacuum as far as the final beam dump.

Single counting rates are typically \( 10^5 \) Hz, originating predominantly from \( K^0 \) decays and beam-associated muons. The trigger on two-body \( K^0 \) decays is done in three steps. A pretrigger signal is generated from a coincidence of hits in opposite quadrants of the scintillator hodoscope, or from a left-right coincidence of the liquid-argon scintillators, with a veto from the ring and muon anticounters. A trigger signal is accepted, subject to further conditions on calorimeter energies, the number of hits in the first chamber, and the number of peaks in the liquid-argon calorimeter. After digitization of pulse heights and chamber information, three-body decays are rejected using on-line processors. The pretrigger rate is about 10 kHz, and typically 1000 events are recorded per burst in the \( K_L \) beam.

The \( K^0 \to 2\pi^0 \to 4\gamma \) decays are reconstructed from the measured positions and energies of the photons. Details of the reconstruction method may be found in Ref. [13]. Events with extra photons of more than 2.5 GeV are rejected. For accepted events, the photon energies have to be above 5 GeV with at least 5 cm separation between shower centres, and the centre of gravity of the energies of all photons has to lie within the beam region. The \( K^0 \) energy is measured with typically 1% accuracy. The distance of the decay vertex from the calorimeter is calculated, using the \( K^0 \) mass as a constraint, with similar precision. Constraints on the masses of two photon pairs are used to reduce the background, which is primarily due to \( K_L \to 3\pi^0 \to 6\gamma \) decays with undetected photons. This background is uniformly distributed in a two-dimensional scatter plot of photon-pair masses. The \( \pi^0 \) mass resolution is \( \sim 2 \) MeV. Signal and background events are counted in equal-area \( \chi^2 \) contours.
around the region defined for accepted events (see Fig. 2). The signal region is taken as \(\chi^2 < 9\). Background is subtracted by linear extrapolation into the signal region. It is about 4% in the \(K_L\) beam but depends strongly on the longitudinal vertex position because of the apparent vertex shift due to the missing energy in \(3\pi^0\) decays with undetected photons. It is negligible in the \(K_S\) beam.

The \(K^0 \to \pi^+\pi^-\) decays are reconstructed from space points defined by at least three hits out of the four planes in each of the two wire chambers. Events with extra space points in the first chamber are rejected for both charged and neutral decays. The longitudinal vertex resolution is better than 1 m. The \(K^0\) energy is calculated with 1% precision from the kaon mass, the opening angle between the two tracks, and the ratio of track energies as measured in the calorimeter. This ratio is limited to a maximum of 2.5, in order to achieve this resolution and also to reduce the contribution of \(\Lambda \to p\pi\) decays to a negligible level. Events with isolated photons, such as \(K^0 \to \pi^+\pi^-\pi^0\) decays and events with accidental photons, are rejected. The \(K^0 \to \pi\nu\) events are identified and rejected by comparing, for each track, the energy deposited in the front half of the photon calorimeter with the energy deposited in the hadron calorimeter. About half of the detected \(\pi^+\pi^-\) events are lost equally from \(K_S\) and \(K_L\) because of all these requirements. Possible variations of the rejection rate due to systematic changes in detector response are monitored by the observed \(\pi^+\pi^-\) mass. The response of the hadron calorimeter is evaluated to be constant within \(\pm 0.5\%\), leading to an uncertainty \(< 0.1\%\) in the measured ratio of \(K_S \to \pi^+\pi^-\) and \(K_L \to \pi^+\pi^-\) event rates. After cuts on the \(\pi^+\pi^-\) mass and on the reconstructed centre of gravity with respect to the beam axis, a residual background of the three-body decays must be subtracted.

In a two-body decay the decay plane should contain the production target, but because of measurement errors and multiple scattering, a certain distribution of the perpendicular distance \(d_T\) of this plane to the target is expected, and can be measured with \(K_S \to \pi^+\pi^-\) decays. In the three-body decays of \(K_L\), because of the non-coplanarity of the decay, a much broader \(d_T\) distribution is expected. This is illustrated in Fig. 3, where the \(d_T\) distributions of accepted two-track events in the \(K_S\) and \(K_L\) beams are shown separately. The \(d_T\) distribution in \(K_S\) decays is scaled geometrically in order to compare directly with \(K_L\).

The signal region is taken to be \(d_T < 5\) cm, and the control region for the background extrapolation is taken as \(7\) cm \(< d_T < 12\) cm. The fraction of events in the background region is \((3.6 \pm 0.1) \times 10^{-3}\) of the signal. This background consists mainly of \(K_L \to \pi\pi\nu\) decays and has contributions from \(K \to \pi\mu\nu\) where the muon loses its energy by bremsstrahlung in the hadron calorimeter, from \(K \to \pi^+\pi^-\pi^0\) where one photon overlaps the shower of one of the charged pions, and a small amount of \(K_S\) production in the final \(K_L\) collimator. The \(K^0 \to \pi^+\pi^-\pi^0\) background is subtracted directly by counting events with identified photons as a function of the distance between the photon and the nearest track. The remaining \(K^0 \to \pi\pi\nu\) candidates are identified by the well-defined electron shower width in the photon calorimeter and longitudinal energy deposition, and the \(K^0 \to \pi\mu\nu\) candidates by the shower width in the hadron calorimeter for events in which both charged particles deposit less than 5 GeV in the photon calorimeter. The shape of the \(d_T\) distributions for the background events is determined from data samples for \(K^0 \to \pi\pi\nu\) and residual \(K^0 \to \pi^+\pi^-\pi^0\) decays, and by Monte Carlo for \(K^0 \to \pi\mu\nu\) decays. The inelastic \(K_S\) regeneration on the \(K_L\) beam collimator has been determined from events with the vertex close to the collimator. The average background subtracted by extrapolation in \(d_T\) is \((6.5 \pm 2.0) \times 10^{-3}\), including systematic uncertainties (see Table 1). In the case of \(K_S\) the background is negligible.

The total available statistics is \(\sim 10^6\) \(K_L\) and \(\sim 10^7\) \(K_S\) two-pion decays. The energy spectra of accepted \(2\pi^0\) and \(\pi^+\pi^-\) events are shown in Fig. 4. After reconstruction, the relative energy scales of neutral and charged decays are adjusted to be the same within \(\pm 10^{-3}\) by fits of the vertex distributions to the position of the anticounter in the \(K_S\) beam (see Fig. 5). In this analysis, the data were selected in the energy range 70–170 GeV and with vertices between 10.5 and 48.9 m from the
position of the final $K_L$ beam collimator. A breakdown of event statistics is given in Table 2a. The
double ratio is evaluated in $10 \times 32$ bins in energy and vertex position, for each of 16 self-contained
data sets of $K_S$ and $K_L$. The weighted average, corrected for acceptance and resolution, is $R = 0.977$
$\pm 0.004$ (statistical error). In principle, the detection efficiencies for the two decay modes cancel. A
Monte Carlo calculation has been used to determine the acceptance ratio. It includes the effect of the
known difference in $K_S$ and $K_L$ beam divergences (0.7%) and the scattering of the $K_S$ beam in the
anticounter and collimator (0.3%, as measured from events without centre-of-gravity and $\Delta r$ cuts,
see Table 2c), and the effects due to finite bin size and to energy and vertex resolution. The net total
Monte Carlo correction amounts to 0.3% on $R$ for the weighted average of all bins.

The trigger system and analysis procedures are designed such that no significant bias should
result in the events retained for analysis. Event losses due to inefficiencies of the pretrigger
hodoscope counters and of the trigger system itself are measured using a sample of events with
relaxed trigger conditions. Since those results are consistent with the expectation of no bias (see
Table 2d,e), no correction has been applied. Gains and losses of good events due to accidentals are
measured by overlaying a sample of events with events taken with a random trigger, at a rate
proportional to the neutral beam intensity. These are primarily due to the cuts on extra space points
in the first wire chamber and on the number of photons. An asymmetry between charged and neutral
decays is observed (Table 2f), and a correction is applied (0.34 ± 0.1%). This asymmetry is mainly
due to a loss of charged decays in the $K_S$ beam caused by additional background in the first chamber.
Another correction of 0.06% accounts for the difference in efficiency, for charged and neutral
decays, of the anticounter in the $K_S$ beam.

The various systematic uncertainties are listed in Table 3. Of these, the dominant ones are due to
a possible energy scale difference between charged and neutral decays, the subtraction of
backgrounds in the $K_L$ beam, and the net losses of good events by accidentals. After all corrections
we obtain the final result, $R = 0.980 ± 0.004 ± 0.005$, with statistical and systematic uncertainties
given separately. With combined errors this corresponds to $R \epsilon' / \epsilon = (3.3 ± 1.1) \times 10^{-3}$. This is the
first time that evidence of CP-violating effects is seen in the decay of the CP-odd $K_L$ into two pions,
as implied by a non-zero value of $\epsilon'$. It is at the level predicted recently by several evaluations of the
Standard Model for a $t$-quark mass in the range 50–100 GeV [14] and does not agree with the
Superweak Model [8].

Acknowledgements

We are indebted to our colleagues L. Bertanza, F. Eisele and P. Steffen for their participation in
the early stages of the experiment. We wish to thank the technical staff of the participating
laboratories and universities for their dedicated effort in establishing the beam, the detectors, and the
data-acquisition system for the experiment. We are indebted, in particular, to: H.W. Atherton,
C. Bizeau, F. Blin, M. Clément, G. Di Tore, G. Dubail, G. Dubois, G.P. Ferri, G. Fersuella,
D. Guyon, R. Harfield, D. Jacobs, G. Juban, Ch. Lasseur, G. Laverrière, P. Le Cossec,
K.D. Lohmann, A. Lovell, R. Maleyran, M. Marin, M.L. Mathieu, R. McLaren, L. Pregernig,
and K. Wydinski (Institute of Physics, University of Dortmund); P. McInnes and A. Main (Physics Dept., University of Edinburgh); the UK Science and Engineering Research Council, and the Rutherford Appleton Laboratory; C. Arnauld, A. Bellemain, R. Bernier, A. Bozzone, J.P. Coulon, J.C. Druhot, J.P. Marolleau, E. Plaige, J.P. Richer and A. Roudier (Linear Accelerator Laboratory, Orsay); the IN2P3 Computing Centre at Lyons; C. Avanzini, R. Fantechi, S. Galeotti, G. Gennaro, F. Morsani, G. Pagani, D. Passuello, R. Ruberti, P. Salvadori and L. Zaccarelli (Department of Physics and INFN, University of Pisa); G. Ikosal, M. Roschangar and R. Seibert (Physics Department, University of Siegen).

REFERENCES


Table 1
Background composition for $K_L \rightarrow \pi^+ \pi^-$ decays

<table>
<thead>
<tr>
<th>Background</th>
<th>Control region</th>
<th>Signal region</th>
</tr>
</thead>
<tbody>
<tr>
<td>$K^0 \rightarrow \pi^+ \pi^- \pi^0$</td>
<td>$(0.1 \pm 0.1) \times 10^{-3}$</td>
<td>$(1.0 \pm 1.0) \times 10^{-3}$</td>
</tr>
<tr>
<td>$K^0 \rightarrow \pi^+ \pi^-\mu\nu$</td>
<td>$(2.8 \pm 0.2) \times 10^{-3}$</td>
<td>$(4.4 \pm 0.3) \times 10^{-3}$</td>
</tr>
<tr>
<td>$K^0 \rightarrow \pi^+ \pi^-\mu\nu$</td>
<td>$(0.5 \pm 0.2) \times 10^{-3}$</td>
<td>$(0.7 \pm 0.3) \times 10^{-3}$</td>
</tr>
<tr>
<td>Regenerated $K_S$</td>
<td>$(0.2 \pm 0.1) \times 10^{-3}$</td>
<td>$(0.4 \pm 0.2) \times 10^{-3}$</td>
</tr>
<tr>
<td>Total</td>
<td>$(3.6 \pm 0.1) \times 10^{-3}$</td>
<td>$(6.5 \pm 2.0) \times 10^{-3}$</td>
</tr>
</tbody>
</table>

Table 2
Event statistics and corrections

<table>
<thead>
<tr>
<th>(a)</th>
<th>(b)</th>
<th>(c)</th>
<th>(d)</th>
<th>(e)</th>
<th>(f)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Signal events ($\times 1000$)</td>
<td>Background (%</td>
<td>Scattering (%)</td>
<td>Inefficiencies</td>
<td>Trigger (%)</td>
<td>Accidental losses (%)</td>
</tr>
<tr>
<td>$K_L \rightarrow 2\pi^0$</td>
<td>109</td>
<td>4.0</td>
<td>&lt; 0.1</td>
<td>0.06 ± 0.06</td>
<td>0.20 ± 0.10</td>
</tr>
<tr>
<td>$K_L \rightarrow \pi^+\pi^-$</td>
<td>295</td>
<td>0.6</td>
<td>0.67</td>
<td>0.37 ± 0.07</td>
<td>0.05 ± 0.06</td>
</tr>
<tr>
<td>$K_S \rightarrow 2\pi^0$</td>
<td>932</td>
<td>&lt; 0.1</td>
<td>0.67</td>
<td>0.04 ± 0.02</td>
<td>0.12 ± 0.03</td>
</tr>
<tr>
<td>$K_S \rightarrow \pi^+\pi^-$</td>
<td>2300</td>
<td>&lt; 0.1</td>
<td>0.03</td>
<td>0.48 ± 0.03</td>
<td>0.01 ± 0.01</td>
</tr>
<tr>
<td>Effect on R</td>
<td>0.3</td>
<td>−0.12 ± 0.10</td>
<td>−0.03 ± 0.12</td>
<td>−0.34 ± 0.10</td>
<td></td>
</tr>
</tbody>
</table>

Table 3
Systematic uncertainties on the double ratio R
(in percent)

<table>
<thead>
<tr>
<th>Source of uncertainty</th>
<th>Uncertainty (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Background subtraction for $K_L \rightarrow 2\pi^0$</td>
<td>0.2</td>
</tr>
<tr>
<td>Background subtraction for $K_L \rightarrow \pi^+\pi^-$</td>
<td>0.2</td>
</tr>
<tr>
<td>$2\pi^0/\pi^+\pi^-$ difference in energy scale</td>
<td>0.3</td>
</tr>
<tr>
<td>Regeneration in the $K_L$ beam</td>
<td>&lt; 0.1</td>
</tr>
<tr>
<td>Scattering in the $K_S$ beam</td>
<td>0.1</td>
</tr>
<tr>
<td>$K_S$ anticounter inefficiency</td>
<td>&lt; 0.1</td>
</tr>
<tr>
<td>Difference in $K_S$/$K_L$ beam divergence</td>
<td>0.1</td>
</tr>
<tr>
<td>Calorimeter instability</td>
<td>&lt; 0.1</td>
</tr>
<tr>
<td>Monte Carlo acceptance</td>
<td>0.1</td>
</tr>
<tr>
<td>Gains and losses by accidentals</td>
<td>0.2</td>
</tr>
<tr>
<td>Pretrigger and trigger inefficiency</td>
<td>0.1</td>
</tr>
<tr>
<td>Total systematic uncertainty</td>
<td>± 0.5%</td>
</tr>
</tbody>
</table>
Fig. 1: Schematic layout of apparatus and beams.
Fig. 2: Number of accepted 4γ events as a function of $\chi^2$, for $K_S \rightarrow 2\pi^0$ and $K_L \rightarrow 2\pi^0$ data, and a Monte Carlo calculation for background originating from $K_L \rightarrow 3\pi^0$ decays. The signal region is taken as $\chi^2 < 9$.

Fig. 3: Event distribution for charged decays as a function of distance $d_T$ between the decay plane and the production target, for $K_S$ and $K_L$ decays and for various background components.
Fig. 4: Energy spectra for $K_S$ and $K_L$ decays into two pions.

Fig. 5: $K_S \rightarrow 2\pi^0$ and $K_S \rightarrow \pi^+\pi^-$ event distributions as a function of distance from the anticounter in the $K_S$ beam. The continuous lines show the best fits to the data.