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A MEASUREMENT OF THE PROMPT $e^{\pm}$ PRODUCTION CROSS-SECTION
IN PROTON-PROTON COLLISIONS AT $\sqrt{s} = 62.2$ GeV

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ABSTRACT

A measurement of prompt $e^{\pm}$ production in proton-proton collisions at the CERN ISR, for a centre-of-mass energy $\sqrt{s} = 62.2$ GeV, in an angular range $\Delta\theta = 35^\circ$ around 90° , and over a transverse momentum range $1.0 \text{ GeV}/c \leq p_T^* \leq 3.0 \text{ GeV}/c$, is reported.

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1. INTRODUCTION

The invariant cross-sections for prompt electrons and positrons ($e^\pm$), produced in proton-proton interactions, in an angular range $\Delta\theta = 35^\circ$, around 90° c.m. polar angle, and at $\sqrt{s} = 62.2$ GeV, has been measured, in a transverse momentum range of $e^\pm$ from 1.0 to 3.0 GeV/c. The value of the $e^\pm$ fractional longitudinal momentum was $|x_F| = |2p_L/\sqrt{s}| \leq 0.03$.

The measurements reported in the present study were particularly relevant for our programme of heavy flavour search at the ISR. In fact the electron-to-pion (e/π) ratio, especially in the high p_T range, is strictly correlated with the semi-leptonic decay of the heavy flavours produced at the ISR.

The interest of these measurements is, however, more general than our own experimental research programme, where a detailed understanding of the ratio (e/π) was essential. In fact, at $\sqrt{s} = 62$ GeV and at 90° only one experiment¹⁾ had been performed; at a lower energy, $\sqrt{s} = 53$ GeV, again only one experiment²⁾ had been done, not in the 90° region, but at $\sim 30^\circ$ c.m. polar angle, and for lower transverse momenta $p_T \lesssim 1$ GeV/c.

2. EXPERIMENTAL APPARATUS

The experiment was performed at the CERN ISR using the upgraded Split-Field Magnet (SFM) detector, which has almost full solid angle coverage for unidentified charged-particle detection. A system of auxiliary detectors placed around the SFM was used for trigger and particle identification purposes. As shown in Fig. 1, the experimental set-up consisted of:

- i) a system of multiwire proportional chambers (MWPCs)³⁾, located inside the SFM poles' gap, to provide the momentum measurement for charged secondaries;
- ii) a small multiwire proportional chamber with analogue read-out ("dE/dx" chamber)⁴⁾, placed near the vacuum chamber, to detect Dalitz and external-conversion e^+e^- pairs;
- iii) six atmospheric pressure Čerenkov counters (C0, C1, C2, C3, C4, C5) consisting of four cells each, to reject charged particles heavier than $e^\pm$;

- iv) four electromagnetic shower detectors (EMSDs)⁵⁾ of the lead/scintillator sandwich type (SW2, SW3, SW4, SW5) to complement the Čerenkov selection and the SFM momentum measurement;
- v) two electromagnetic shower detectors (EMSDs) of the lead-glass total absorption Čerenkov type (LG3, LG4) to cover the almost-zero-field region ($\theta_{\text{cm}} \approx 90^\circ \pm 5^\circ$) of the SFM, on the trigger side;
- vi) extra multiwire chambers, in front of and behind the Čerenkov counters, to allow the reconstruction of charged-particle trajectories up to the electromagnetic shower detectors;
- vii) a time-of-flight system (TOF)⁶⁾ for the identification of charged-particles up to ~ 2 GeV/c momenta.

The results presented in this paper refer to a set of data where the prompt $e^\pm$ trigger was required in an interval of about $\pm 17.5^\circ$ around $\theta_{\text{cm}} = 90^\circ$, externally to the ISR ring (see Fig. 2).

Notice that, since the proton-proton centre-of-mass system moved away from the trigger region with a velocity $\beta \approx 0.152$, the transverse momenta of the $e^\pm$ in the centre-of-mass system were $\sim 12\%$ to 16.5% (depending on the polar angle) larger than the momenta measured in the laboratory system.

A detailed description of the design and performances of the various elements of the set-up can be found elsewhere³⁻⁷⁾; in the following only a summary of the main characteristics of the detectors relevant to the prompt $e^\pm$ trigger will be given.

2.1 Lead/scintillator sandwiches (SW3, SW4)

Each of these telescopes consisted of six 200×20 cm² modules. Their sandwich structure was provided by a 1 cm thick lead plate followed by 10 layers of 1 cm thick scintillator interleaved with 9 plates of 0.4 cm thick lead. The total thickness of 8.2 radiation lengths was chosen such as to obtain an 80% shower containment at 4 GeV $e^\pm$ energy. In the $e^\pm$ energy range 0.5 to 4.0 GeV, the

pulse-height response was linear with the energy within less than 5% and, at 1 GeV, it corresponded to eight times the minimum ionizing charged-particle level; the uniformity of each module over its full surface was better than 3% and the r.m.s. energy resolution was fitted by the formula

$$\frac{\sigma(E)}{E} = a + \frac{b}{\sqrt{E(\text{GeV})}},$$

with the average parameter values: $\langle a \rangle = 0.03$, $\langle b \rangle = 0.14$. For $e^\pm$ energies above 1 GeV a r.m.s. time resolution better than 0.32 ns and a r.m.s. space resolution, along the counter, better than 3 cm were obtained.

Concerning the π/e discrimination power of these counters, at 1 GeV and with an $e^\pm$ detection efficiency of 95%, the pion contamination was 4%.

During data taking, the stability of the energy calibration was monitored by triggering on penetrating particles across the central part of the modules. For this purpose, two scintillator counters (15 cm wide) were mounted on the back of each telescope at half height and matched its full horizontal width.

2.2 Lead-glass Čerenkov counters (LG3, LG4)

The lead-glass array LG3 consisted of 60 hexagonal counters, each of inner diameter 13.6 cm and thickness 32.5 cm. LG4 consisted of 70 square counters ($10 \times 10 \text{ cm}^2$) plus 26 rectangular counters ($15 \times 7.4 \text{ cm}^2$) all of thickness 35 cm; see Fig. 3. Each array covered an area of $\sim 1 \text{ m}^2$ and was about 15 radiation lengths thick. The r.m.s. energy resolution for the two types of counters was fitted by the formula:

$$\frac{\sigma(E)}{E} = a + \frac{b}{\sqrt{E(\text{GeV})}},$$

with the following average parameter values:

$$\langle a \rangle = 0.030, \langle b \rangle = 0.040 \quad \text{for LG3}$$

$$\langle a \rangle = 0.015, \langle b \rangle = 0.048 \quad \text{for LG4.}$$

In the $e^\pm$ energy range 0.5 to 3.0 GeV, the pulse-height response of the counters was expressed by a parabolic behaviour with the quadratic term coefficient smaller than 5% of the linear term coefficient.

During data taking, the stability of the gain of each counter was monitored by three methods:

- i) measurement of the spectrum produced by a radioactive source in a small scintillator installed in the centre of the front face of the counter;
- ii) measurement of the spectrum produced by particles penetrating the lead-glass block and triggering one element (punch-through counter) of a scintillator hodoscope located behind each lead-glass array; a hodoscope of five scintillator counters placed just in front of the array was used in coincidence with the punch-through one;
- iii) study of the invariant mass spectrum of photon pairs of more than 0.7 GeV energy; the constancy of the peak value and of the full width of the observed π^0 mass spectrum (see Fig. 4) was used as a monitor.

2.3 Gas Čerenkov counters (C0, C3, C4)

The Čerenkov counters C0, C3, C4 were filled with nitrogen and operated at atmospheric pressure; the pion momentum threshold was ~ 5.7 GeV/c.

Each of these counters was divided into four optical cells, each viewed by one photomultiplier (PM) whose window was treated with a wavelength shifter to increase the efficiency in the ultraviolet region. The light was collected by spherical mirrors and focused (after reflection on a second plane mirror for C0) on the photocathode of the relative PM (see Figs. 5a and b). The optical system was designed bearing in mind the necessity to focus, on a relatively small surface (5 in. tube), the light coming from a rather large source (interaction region + magnetic field); conical light catchers were used to increase the light-collection efficiency.

As the SFM field could affect the efficiency of CO phototubes, each of them was equipped with a set of three coils, inside the mu-metal shield, producing a magnetic field opposite to the one found in the photocathode region. A reference signal was provided by a light-emitting diode placed in the centre of the front end of the counter.

A typical Čerenkov pulse-height response for an equal number of $e^\pm$ and pions of 2 GeV/c momentum obtained in a test beam is shown in Fig. 5c; a Poisson fit to the $e^\pm$ spectrum gives (4.4 ± 0.1) as the average number of photoelectrons; to an $e^\pm$ efficiency $\geq 99\%$ corresponds a pion efficiency of about 0.8%.

2.4 dE/dx chamber

This was a small ($57 \times 27 \text{ cm}^2$ sensitive area) proportional chamber with three vertical and one horizontal wire planes with 4 mm spacing; each of the 493 wires had an independent analogic read-out channel (ADC). This chamber was located just outside the vacuum pipe (see Fig. 1: chamber labelled "209") and covered a solid angle of about 2 sr.

For each reconstructed track crossing the dE/dx chamber (Fig. 2), the four energy-loss samplings, corrected for impact angle and saturation effects, were used and an average loss was computed from the three lower pulse-height values. In Fig. 6 the average pulse-height ($\overline{\text{PH}}$) distribution obtained with a "pion" trigger for momenta larger than 0.5 GeV/c is shown; the energy-loss resolution is about 50% FWHM. [The "pion" trigger was defined, as in the $e^\pm$ case (see Section 3), by a coincidence of MWPC and EMSD signals. To the latter, a "low threshold" condition, fully efficient for minimum ionizing charged particles, was applied. No Čerenkov requirement was used at the on-line level.]

During the experiment, the gain stability of each channel was periodically monitored by injection of a fixed current pulse in the wire preamplifier. At the off-line level, corrections for small gain variations (a few per cent) were applied to the pulse-height value of each wire.

2.5 The ISR vacuum chamber

It is finally worth mentioning the ISR vacuum chamber used in the pp interaction region where this experiment was mounted. In fact, a major design and engineering effort was needed to reach a compromise between mechanical strength and wall thickness, the latter being an obvious requirement for an $e^\pm$ detection experiment.

The resulting chamber was a corrugated stainless-steel cylindrical pipe, 50 cm long, 24 cm in diameter, and 0.2 mm thick.

When compared with the previous existing vacuum chamber, it represented an improvement by a factor of eight in the effective thickness traversed by $e^\pm$ and by a factor of two in the minimum distance of the first MWPC from the interaction region.

3. $e^\pm$ TRIGGER

The single electron (SEL) trigger consisted of the electronic OR of four possible triggers (SEL/SW3, SEL/SW4, SEL/LG3, SEL/LG4), each corresponding to an $e^\pm$ candidate in one of the four EMSDs of Fig. 2.

The standard trigger condition was defined by the following simultaneous requirements:

- i) a signal from Čerenkov counter C0;
- ii) a signal from Čerenkov counter C3 (for SEL/SW3 and SEL/LG3) or C4 (for SEL/SW4 and SEL/LG4);
- iii) a fast signal from the wire planes of MWPCs "200" and "203" (see Fig. 2);
- iv) a fast signal from the wire planes of MWPCs "230" or "231" (for SEL/SW3), "230" (for SEL/LG3), "240" (for SEL/LG4), "240" or "241" (for SEL/SW4);
- v) an energy deposition exceeding a given threshold in any module of a sandwich telescope or in any two adjacent columns of a lead-glass array; the nominal threshold values were 0.5 GeV for SW3, SW4 and 0.8 GeV for LG3, LG4.

More details about the electronic trigger logic can be found elsewhere⁷⁾.

4. DATA TAKING

The measurements reported in this paper refer to a sample of 2.9×10^6 SEL triggers, corresponding to a total luminosity $\mathcal{L} = 4.39 \times 10^{36} \text{ cm}^{-2}$. At the beginning of each running period the luminosity was measured by using the SFM monitoring counter system and the Van der Meer method.

As already mentioned, during data taking special calibration runs were periodically intercalated in order to monitor the stability of all the electronic channels connected to the various detectors (EMSDs, Čerenkovs, dE/dx chamber, MWPCs) and to check the energy calibration reference points of the EMSDs. Single and coincidence rates, together with pulse-height and time-of-flight spectra for each detector element, were continuously monitored.

With an average instantaneous luminosity $\langle L \rangle \approx 0.9 \times 10^{31} \text{ cm}^{-2} \text{ s}^{-1}$, the SEL trigger rate was about 6 s^{-1} , while the "pion" trigger rate was about $1.5 \times 10^4 \text{ s}^{-1}$; a rejection factor against charged hadrons of about 2.5×10^3 was hence achieved on line by means of the "electron" requirements on the Čerenkov counters and the EMSDs.

5. DATA ANALYSIS

The 2.9×10^6 collected events went through a fast off-line filtering process for a refinement of the trigger conditions and for a further rejection of the background caused by neutral and charged hadrons. The filter was based on the following requirements:

- i) the reconstruction of the trigger particle track in the MWPC telescopes of Fig. 2, with a laboratory momentum larger than $0.5 \text{ GeV}/c$;
- ii) the geometrical match of this track with:
 - a) the Čerenkov counter cells;
 - b) the EMSD elements which had caused the trigger;
 - c) a set of four wire clusters, having a cluster size compatible with the crossing angle of the track, in the dE/dx chamber.

Only 15% of the input events survived the above off-line trigger criteria.

Since the main residual background sources for the prompt $e^\pm$ signal were Dalitz decays of high-momentum π^0 and η mesons, and conversions of high-momentum photons in the vacuum chamber wall or in the external foam frame of the dE/dx chamber, a search for the companion $e^\pm$ of the triggering one was made in the dE/dx chamber. In fact, the average pulse-height ($\overline{PH}$) distribution associated with the trigger track clearly showed (see Fig. 7) a two-peak structure, corresponding to a single- and double-particle (unresolved pairs) ionization losses. Dalitz and external-conversion e^+e^- pairs were therefore rejected by requiring a $\overline{PH}$ value smaller than 1.4 times the most probably ionization loss of the prompt $e^\pm$.

The shape of the $\overline{PH}$ distribution of the single particle (Fig. 6) was used to evaluate the efficiency of this cut for prompt $e^\pm$ detection (see Table 1) and the contamination level of narrow unresolved pairs in the surviving sample of events.

By inspection of the $\overline{PH}$ distributions for both the "pion" and the "electron" triggers, an approximate 25% increase of the most probably ionization loss was observed for $e^\pm$ (at the Fermi plateau) with respect to minimum ionizing particles. A fit to the lower end of Fig. 7 using variable fractions of the "pion" and "electron" spectra showed that, once the above $\overline{PH}$ cut was applied, the pion contamination was less than 2%.

After having rejected the narrow unresolved e^+e^- pairs, a search was made in the dE/dx chamber for narrow resolved pairs. Owing to the Dalitz decay and external-conversion kinematics and to the high transverse-momentum trigger condition, a very small opening angle or a largely asymmetric energy sharing were expected for the e^+e^- pair. In both cases, the reconstruction (i.e. identification) of the two $e^\pm$ trajectories in the rapidly varying and largely inhomogeneous SFM magnetic field at $\sim 90^\circ$ was very unlikely.

In fact, an excess of wire clusters in the dE/dx chamber, associated with a very low momentum track accompanying the trigger track, was found in the "electron" data when compared with the "pion" data (see Fig. 8a). A correlation of the minimum distance between the clusters associated with the $e^\pm$ trigger track and any

other cluster in the same dE/dx chamber plane, for any two planes, was observed (see Fig. 8b).

Narrow but resolved e^+e^- pairs were then rejected by requiring, in each dE/dx chamber plane, no wire hit inside a correlation region of approximately 7° opening angle around the trigger track. From the "pion" trigger data the random vetoing effect of this cut was estimated to be 9.5%.

The events satisfying all these cuts (1.7% of the input events) were then fully reconstructed by using the whole system information of the SFM MWPCs. A very high charged multiplicity associated with the SEL trigger was found, its average value being 16.

The filtering process described above was then repeated on the trigger particle track found by the full reconstruction program; in fact, in a fraction of events ($\sim 10\%$), this track did not coincide with that previously reconstructed by the faster but less accurate track-finding algorithm. Finally, this trigger track was required to originate from the interaction vertex, determined by all the reconstructed tracks of the event.

A further reduction of the charged hadron background was achieved by comparing the behaviour of the momentum p (determined by the reconstruction program) with the energy E (measured by the EMSDs) of those trigger particles traversing the "good" magnetic field region ($\sim 80\%$ of the total). The quantity $T = (p - E)/\sqrt{p^2 + E^2}$ was used. Its distribution for the $e^\pm$ candidates (Fig. 9a), while well centred on zero as expected for true $e^\pm$, showed long tails both for positive and negative*) values, the former being more populated than the latter.

The T distribution of the selected $e^\pm$ sample was compared with that of the "pion" trigger sample (Fig. 9b) and with that of the rejected sample of high $\overline{PH}$ tracks in the dE/dx chamber (Fig. 9c). Notice that in Fig. 9c the excess of events for $T > 0.8$ was due to slow particles below the minimum of ionization, releasing a large pulse height in the dE/dx chamber.

*) The background contribution to the negative T region mainly came from antiproton annihilation in the EMSDs; by comparing the T distributions of positive and negative particles (Fig. 9a) an antiproton contamination of about 0.8% was evaluated.

From the study of these three T distributions a maximum charged hadron contamination of 2% was estimated; this value was in excellent agreement with that derived from the $\overline{\text{PH}}$ spectrum analysis.

$e^\pm$ candidates in the "good" magnetic field region were therefore required to have a T value compatible with zero within three standard deviations ($\sigma_T = 0.13$); for those in the almost-zero-field region an equal amount of charged hadron background was assumed and hence subtracted before computing the cross-section. After this T distribution cut, the charged hadron contamination was reduced to less than 1.5%.

A final sample of 45,819 events was thus selected.

6. BACKGROUND DETERMINATION

In order to estimate the number of genuine prompt $e^\pm$ in the final sample of events, the background escaping the cuts of the filter (Section 5) had to be determined.

The main sources of this residual background were:

- i) Dalitz decays of π^0 and η mesons producing either very energy-asymmetrical e^+e^- pairs with the lower-momentum $e^\pm$ escaping detection in the dE/dx chamber or unresolved pairs giving a pulse height smaller than 1.4 times the most probable ionization loss of the prompt $e^\pm$;
- ii) external conversions of photons in the vacuum chamber wall and in the external foam frame of the dE/dx chamber, producing e^+e^- pairs with the same characteristics as those from Dalitz decays;
- iii) three-body semileptonic decays of charged and neutral kaons (K_{e3}) producing genuine but uninteresting (because of known origin) prompt $e^\pm$;
- iv) prompt e^- from Compton scattering of high-momentum photons in the vacuum chamber wall or in the external foam frame of the dE/dx chamber.

The absolute number of background events, from each of the above sources, in each bin of centre-of-mass transverse momentum (p_T^*) was computed via a Monte Carlo program whose input data were:

- a) the British-Scandinavian Collaboration two-component function⁸⁾ to parametrize the p_T^* production spectra, at the ISR, of π^0 [taken as half the sum⁸⁾ of π^+ and π^- spectra], $K^\pm$, and K_L^0 [taken as half the sum⁹⁾ of K^+ and K^- spectra];
- b) the η/π^0 production ratio measured at the ISR by the CCRS¹⁰⁾ and ABCS¹¹⁾ Collaborations for p_T^* larger than 3 GeV/c and assumed to hold true also in the lower p_T^* range of this experiment ($1 \leq p_T^* \leq 3$ GeV/c);
- c) the known¹²⁾ branching ratios for the following decay processes: $\pi^0 \rightarrow \gamma\gamma$, $\eta \rightarrow \gamma\gamma$, $\pi^0 \rightarrow \gamma e^+ e^-$, $\eta \rightarrow \gamma e^+ e^-$, $K^\pm \rightarrow e^\pm \nu \pi^0$, $K_L^0 \rightarrow \pi^\pm e^\mp \nu$.

The contribution to the $e^\pm$ signal of the various background sources was then computed with the procedure described below.

6.1 $e^\pm$ from Dalitz decays

The generation of π^0 and η mesons was done according to the parametrization and the relative rate mentioned above, in the centre-of-mass kinematical region corresponding to the SEL trigger:

- a) (azimuthal angle) $\Delta\phi^* = \pm 18^\circ$, in the $\hat{x}$ - $\hat{z}$ plane, around the $\hat{x}$ axis of the SFM reference system (see Figs. 1 and 2);
- b) (rapidity) $|y^*| < 0.7$, with $y^* = \frac{1}{2} \ln [(E^* + p_L)/(E^* - p_L)]$;
- c) (transverse momentum) $p_T^* > 0.5$ GeV/c.

The normalization of the simulated background of $\pi^0(\eta)$ was derived from the total $\pi^0(\eta)$ production cross-section in that kinematical region [obtained by integration of the inclusive $\pi^0(\eta)$ invariant cross-section] and from the total integrated luminosity of the experiment. A vertex distribution reproducing the experimental diamond-shaped one was used. The e^+e^- Dalitz pairs were generated according to the known¹³⁾ invariant mass and angular distributions of the $\pi^0(\eta)$ decay.

For those events where at least one electron of the pair had a momentum larger than 0.5 GeV/c, the $e^\pm$ trajectories in the trigger region (Fig. 2) were tracked

up to the EMSDs, and the hit positions on the MWPC planes (dE/dx chamber included) were digitized. The pulse heights of the dE/dx chamber hit wires were also generated according to the experimental single-particle reference spectrum. After track reconstruction (with multiple scattering and energy loss taken into account), the Monte Carlo events went through a filtering analysis identical with the one applied to the data.

The p_T^* distribution of the surviving Dalitz $e^\pm$ was then parametrized according to the following formula:

$$\frac{dN}{dp_T^*} = A p_T^* e^{-B p_T^*} + \frac{C}{(p_T^{*2} + D)^E}.$$

The best fit parameters (A, B, C, D, E) had different values for π^0 and η and furthermore A and C differed for positrons and electrons and for the four EMSD telescopes.

6.2 $e^\pm$ from external conversions of photons

Experimental measurements on "direct" photon production at the ISR¹⁴⁾ show that at the centre-of-mass energy of this experiment no "direct" photon contribution is present below $p_T^* \approx 3$ GeV/c. Only π^0 and η mesons decaying into two gammas were then considered as a source of conversion background.

The isotropic decay of these neutral mesons, generated with the same distribution and in the same kinematical region as for the Dalitz case, produced two photons, one of which, at least, was required to have an energy larger than 0.5 GeV. The probability of photon conversion into an e^+e^- pair, occurring either in the ISR vacuum chamber wall (0.2 mm thick) or in the foam frame (1 cm thick) of the dE/dx chamber, was computed by using known¹⁵⁾ e^+e^- pair energy-sharing and angular distributions. The effective thickness of material along the photon trajectory, and in particular the corrugation of the vacuum chamber wall, was carefully simulated in the Monte Carlo calculation.

For each electron of the pair the same tracking and filtering procedure as for the Dalitz case was applied. The p_T^* distribution of the accepted conversion $e^\pm$ was parametrized according to the same kind of formula as for the Dalitz $e^\pm$.

An independent evaluation of the absolute level of the residual conversion background in the final $e^\pm$ sample was derived from the same experimental data; a good agreement with the results of the Monte Carlo calculations was obtained (see Appendix A).

6.3 $e^\pm$ from K_{e3} decays

Charged and neutral (K_L^0) kaons were also generated with the above-mentioned distributions and kinematical cuts and allowed to decay semileptonically via the standard matrix element. The decay probability was constrained by the on-line and off-line requirements that the decay occurred before the first Čerenkov counter (C0) (for $K^\pm$) or the first dE/dx chamber plane (for K_L^0).

After the parent kaon and its decay $e^\pm$ were tracked through the detector telescopes of Fig. 2, they were required to be reconstructed as a unique track.

The p_T^* distribution of such $e^\pm$ surviving the filtering analysis was parameterized by the following formula:

$$\frac{dN}{dp_T^*} = A_1 e^{-Bp_T^*} + A_2 \frac{\left(1 - p_T^*/p_{\text{beam}}\right)^m}{\left(p_T^{*2} + M^2\right)^n},$$

where $p_{\text{beam}} = 31.11 \text{ GeV/c}$, $B = 8.24 (\text{GeV/c})^{-1}$, $M = 1.0 \text{ GeV/c}$, and $n = 4.0$; the other parameters were assigned different values for positrons and electrons and for the four EMSD telescopes.

6.4 Electrons from Compton scattering

The contribution from π^0 and η decay into two photons to the prompt (negative-charge) electron signal, due to Compton scattering of the photons in the vacuum chamber wall or in the foam frame of the dE/dx chamber, was evaluated by using the Sternheimer¹⁶⁾ and the Klein-Nishina¹⁷⁾ formulae to integrate over the $\pi^0(\eta)$ and the photon energy spectra in the $e^\pm$ trigger region. The absolute invariant cross-section as a function of p_T^* relative to this type of background is given in Table 2.

The fractional contribution of the studied background sources to the experimentally observed $e^\pm$ signal is shown in Fig. 10, as a function of p_T^* .

7. ACCEPTANCE AND EFFICIENCY

The $e^\pm$ acceptance of the apparatus was studied by tracking Monte Carlo simulated particles in the SFM magnetic field and by requiring each track to hit all the detectors (dE/dx chamber, Čerenkov counters, MWPCs, EMSDs) involved in the on-line $e^\pm$ trigger (see Fig. 2). The $e^\pm$ were generated with a flat rapidity distribution and with an azimuthal angle and a transverse momentum within the allowed kinematical region of the trigger. Multiple scattering and energy loss in the various materials along the $e^\pm$ trajectory were duly taken into account.

The prompt $e^\pm$ effective acceptance, integrated over transverse momenta and averaged over the two electric charge states, turned out to be 1.06×10^{-2} , while the purely geometrical acceptance, due to the solid angle subtended by the detector, was 1.5×10^{-2} . The shape of this acceptance for positive and negative electrons in the two types of EMSDs is given in Fig. 11 as a function of p_T^* . The efficiency of the analysis was then evaluated step by step.

The efficiency of track-finding and reconstruction in the trigger region was computed by simulation, and its behaviour as a function of p_T^* was determined; its value varied from 0.95 to 0.98, increasing with p_T^* , for $p_T^* \geq 1.0$ GeV/c.

The Čerenkov efficiency was evaluated by using the final sample of SEL triggered events. A Poissonian fit to the spectrum of each Čerenkov PM provided the mean number of observed photoelectrons. From these numbers, the efficiency to detect $e^\pm$ producing a pulse height larger than the hardware threshold (which corresponded to about 1/10 of the one photoelectron peak) was determined. The results are summarized in Table 1.

The efficiency of the geometrical-match requirement between the trigger track and the energy cluster in the EMSDs was estimated as follows. Firstly, it was checked that the distance between the track impact point (determined by extrapolation from the last chamber in front of the EMSD) and the nearest energy cluster

showed a Gaussian distribution where the noise, coming from random hits, was negligible. Then, the efficiency was computed by looking at how many tracks did not have an associated energy cluster. The results, for sandwich (SW) and lead-glass (LG) EMSDs are summarized separately in Table 1.

The efficiency of the geometrical-match requirement between the trigger track and the four hit wire clusters on the planes of the dE/dx chamber was derived from the rate of intermediate missing planes, using for cleanness the sample of "pion" triggers. Only the configurations with the 2nd, the 3rd or the 4th plane missing were taken into account. The resulting efficiency was 0.944.

As already mentioned, the "pion" trigger $\overline{\text{PH}}$ distribution in the dE/dx chamber was used to evaluate the efficiency of the pulse-height cut for $e^\pm$. The charged hadron $\overline{\text{PH}}$ spectrum was normalized and shifted so as to reproduce the prompt $e^\pm$ spectrum (lower peak in Fig. 7). The efficiency of the cut was in this was determined to be 0.78.

By using the same charged-hadron triggered events, the random vetoing introduced by the rejection criteria against narrow resolved e^+e^- pairs was computed. The efficiency of this cut for the $e^\pm$ trigger events was found to be 0.905.

When applying the filtering process to the trigger track, as found by the full reconstruction program, 10.4% of the events were rejected because the match of the track either with the energy cluster in the EMSDs or with the four hit wire clusters on the dE/dx chamber planes was missing.

Other small inefficiencies, due to a bad tape-writing format or to an excess of hit wires in the MWPCs (not handled by the full reconstruction program), occurred during data taking and contributed with a factor equal to 0.934 to the total analysis efficiency.

A summary of all efficiencies is given in Table 1; the over-all efficiency varied from 0.40 to 0.45 (± 0.01) depending on the p_T^* value and the type of EMSD involved (sandwich or lead-glass).

8. THE INVARIANT CROSS-SECTION

To evaluate the prompt $e^\pm$ invariant cross-section, the centre-of-mass transverse momentum p_T^* was derived from the energy measured in the EMSDs, since no reliable momentum measurement was, in fact, expected in the almost-zero magnetic field region covered by the lead-glass arrays.

The effect of the EMSDs' energy resolution on the $e^\pm p_T^*$ spectrum was taken into account by an unfolding procedure based on the known energy dependence of the energy resolution for each EMSD element, and on a parametrization of the $e^\pm p_T^*$ spectrum derived from the charge-averaged pion spectrum shape^{8)*}). The total background contamination, which was obtained by introducing the same inefficiencies as for real data in the Monte Carlo results of Section 6, was then subtracted from the unfolded p_T^* spectrum. Finally, after correction for the total $e^\pm$ detection efficiency, the invariant cross-section as a function of p_T^* was computed separately for positive and negative electrons: for the latter, the Compton background contribution was subtracted.

No data below $p_T^* = 1.0$ GeV/c were used, since only above this value was the efficiency of the EMSDs' hardware threshold at a maximum and the confidence level of the background evaluation satisfactory. In order to investigate a possible charge asymmetry effect, the difference in invariant cross-section between positrons and electrons was studied as a function of p_T^* (Fig. 12). No evidence of charge asymmetry was found, the weighted average of the above difference in the p_T^* range from 1.0 to 3.0 GeV/c being (0.035 ± 0.038) .

The charge-averaged invariant cross-section for prompt $e^\pm$ was then computed (Table 3); in Fig. 13 its dependence on p_T^* is shown together with the results of a previous experiment¹⁾ performed in the same kinematical region at the ISR. The behaviour of the charge-averaged pion cross-section⁸⁾ multiplied by 10^{-4} is also shown. This allows us to derive the (e/π) ratio versus p_T^* .

*) This unfolding procedure introduces into the experimental data a point-to-point correlation whose range, determined by the experimental energy resolution, varies slowly with energy. This effect can clearly be observed in Figs. 12 to 14, where the point-to-point fluctuations are obviously smaller than those expected from statistics.

9. CONCLUSIONS

The (e/π) ratio, as a function of p_T^* , is presented in Fig. 14 and Table 4; the weighted average in the p_T^* range from 1.0 to 3.0 GeV/c is $(1.58 \pm 0.06) \times 10^{-4}$.

Statistical errors and systematic errors on the detection efficiency and the background subtraction were taken into account in computing the $e^\pm$ cross-section (Figs. 12 to 14). Other systematic errors originating from uncertainty in the luminosity measurement ($\pm 5\%$) and the accuracy of the absolute EMSD energy calibration ($\pm 5\%$) would result in a total normalization uncertainty of about $\pm 30\%$.

In order to compare our results with previous ISR experiments^{1,2)}, at similar centre-of-mass energies, the following remarks are needed:

- i) the ACHMNR data²⁾ are not corrected for a systematic effect which goes up to about +33%; this means that the (e/π) ratio measured by this group is smaller than the true value;
- ii) the CCRS data¹⁾ are affected by an over-all systematic error of $\pm 28\%$ on the inclusive $e^\pm$ measurement (Fig. 13) and of $\pm 7.3\%$ on the (e/π) ratio (Fig. 14).

As mentioned in the Introduction, the quantity (e/π) is strictly correlated, especially in the high p_T range, with the semileptonic decay of the heavy flavours produced in high-energy (pp) interactions. In the present study this quantity has been measured using the same hardware and software set-up which is used to study the heavy flavour production at the ISR. Our results are consistent with previous measurements, and, besides providing a new contribution to the further knowledge of this basic quantity in high-energy hadron physics, they represent an important over-all consistency check of the hardware and software systems used.

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Table 1

Summary of prompt $e^\pm$ detection efficiencies

Selection applied	Efficiency
Track finding and reconstruction (the efficiency, varying with p_T^* from 1 to 3 GeV/c is averaged over positive and negative electrons)	0.95 to 0.98 $\pm$ 0.01 (SW) 0.96 to 0.99 $\pm$ 0.01 (LG)
Cerenkov pulse-height cut (the effi- ciency is averaged over C0•C3 and C0•C4 PM combinations)	0.833 $\pm$ 0.004
Track-energy cluster geometrical match	0.908 $\pm$ 0.01 (SW) 0.970 $\pm$ 0.01 (LG)
Track-wire clusters (dE/dx chamber) geometrical match	0.944 $\pm$ 0.002
$\overline{PH} < 1.4 \times$ (prompt $e^\pm$ $\overline{PH}$ peak) cut in the dE/dx chamber	0.780 $\pm$ 0.009
Angular cut of narrow resolved pairs	0.905 $\pm$ 0.002
Geometrical match of energy and wire clusters after full recon- struction	0.896 $\pm$ 0.005
Bad event format and full recon- struction event loss	0.934 $\pm$ 0.005
TOTAL	0.40 to 0.41 $\pm$ 0.01 (SW) 0.43 to 0.45 $\pm$ 0.01 (LG)

Table 2

The invariant cross-section for
Compton e^- production
as a function of p_T^*

p_T^* (GeV/c)	$E d^3\sigma/dp^3$ (cm ² /GeV ²)
1.022	1.360×10^{-32}
1.072	0.996
1.122	0.736
1.172	0.548
1.222	0.411
1.272	0.310
1.322	0.236
1.372	0.180
1.422	0.139
1.472	0.107
1.522	0.830×10^{-33}
1.572	0.648
1.623	0.506
1.673	0.399
1.723	0.316
1.773	0.252
1.823	0.200
1.873	0.161
1.923	0.129
1.973	0.104
2.041	0.784×10^{-34}
2.142	0.519
2.242	0.350
2.342	0.238
2.442	0.164
2.542	0.114
2.642	0.799×10^{-35}
2.743	0.564
2.843	0.404
2.943	0.291
3.043	0.212
3.143	0.155
3.294	0.979×10^{-36}
3.597	0.408
3.900	0.178
4.202	0.821×10^{-37}
4.504	0.392
4.806	0.194

Table 3

The charge-averaged invariant cross-section
for inclusive $e^\pm$ production
at $\sqrt{s} = 62.2$ GeV as a function of p_T^*

p_T^* (GeV/c)	$Ed^3\sigma/dp^3$ (cm^2/GeV^2)
1.022	$(6.83 \pm 0.88) \times 10^{-32}$
1.072	(5.86 ± 0.74)
1.122	(4.70 ± 0.60)
1.172	(3.64 ± 0.49)
1.222	(2.81 ± 0.40)
1.272	(2.23 ± 0.34)
1.322	(1.75 ± 0.28)
1.372	(1.41 ± 0.24)
1.422	(1.13 ± 0.20)
1.472	$(9.18 \pm 1.74) \times 10^{-33}$
1.522	(7.55 ± 1.50)
1.572	(6.18 ± 1.30)
1.623	(5.17 ± 1.14)
1.673	(4.28 ± 1.00)
1.723	(3.56 ± 0.88)
1.773	(2.99 ± 0.78)
1.823	(2.50 ± 0.69)
1.873	(2.12 ± 0.62)
1.923	(1.79 ± 0.55)
1.973	(1.50 ± 0.49)
2.041	(1.16 ± 0.30)
2.142	$(8.05 \pm 2.36) \times 10^{-34}$
2.242	(5.51 ± 1.88)
2.342	(3.77 ± 1.50)
2.442	(2.60 ± 1.21)
2.542	(1.87 ± 0.99)
2.642	(1.37 ± 0.82)
2.743	(1.01 ± 0.68)
2.843	$(7.38 \pm 5.71) \times 10^{-35}$
2.943	(5.08 ± 4.68)
3.043	(3.34 ± 3.78)
3.143	(2.14 ± 3.06)
3.294	(1.06 ± 1.24)
3.597	$(7.44 \pm 8.89) \times 10^{-36}$
3.900	(6.14 ± 7.03)
4.202	(3.41 ± 4.92)
4.504	(0.93 ± 2.65)
4.806	(2.05 ± 4.57)

Table 4

The charge-averaged ratio
 $[(e^+ + e^-)/(\pi^+ + \pi^-)] \times 10^4$
as a function of p_T^* , at $\sqrt{s} = 62.2$ GeV

p_T^* (GeV/c)	$(e/\pi) \times 10^4$
1.022	1.49 ± 0.19
1.072	1.63 ± 0.20
1.122	1.66 ± 0.21
1.172	1.62 ± 0.22
1.222	1.57 ± 0.23
1.272	1.56 ± 0.23
1.322	1.53 ± 0.25
1.372	1.54 ± 0.26
1.422	1.53 ± 0.27
1.472	1.53 ± 0.29
1.522	1.55 ± 0.31
1.572	1.56 ± 0.33
1.623	1.60 ± 0.35
1.673	1.62 ± 0.38
1.723	1.63 ± 0.40
1.773	1.66 ± 0.43
1.823	1.68 ± 0.46
1.873	1.72 ± 0.50
1.923	1.74 ± 0.53
1.973	1.75 ± 0.57
2.041	1.72 ± 0.44
2.142	1.70 ± 0.50
2.242	1.64 ± 0.56
2.342	1.56 ± 0.62
2.442	1.48 ± 0.69
2.542	1.46 ± 0.77
2.642	1.46 ± 0.87
2.943	1.30 ± 0.52

Figure captions

- Fig. 1 : TOP view of the SFM detector, showing the MWPCs and the external apparatus for particle identification:
- i) C0 to C5 are gas threshold Čerenkov counters;
 - ii) SW2 to SW5 are lead/scintillator sandwiches;
 - iii) LG3 and LG4 are lead-glass arrays;
 - iv) TOF is the time-of-flight system;
 - v) Chamber labelled "209" is the dE/dx chamber.
- Fig. 2 : The detector region where the single-electron (SEL) trigger was required.
- Fig. 3 : Front view of the two lead-glass arrays and details of the three types of lead-glass blocks.
- Fig. 4 : Invariant mass spectrum of photon pairs with more than 0.7 GeV energy, obtained with the lead-glass arrays. The r.m.s. mass resolution at the π^0 peak is 14%.
- Fig. 5 : a) Side view of the Čerenkov counter C0 showing the mechanical structure and the optical system.
b) Same as in a) for Čerenkov counters C3 and C4.
c) Pulse-height spectrum of one of these Čerenkov counters, obtained in a test beam with equal numbers of electrons (full-line histogram) and pions (dashed-line histogram) of 2 GeV/c momentum.
- Fig. 6 : Average pulse-height ($\overline{\text{PH}}$) distribution of the dE/dx chamber obtained with the "pion" trigger for charged particles with momenta larger than 0.5 GeV/c. The arrow points to the most probable energy-loss channel value. The FWHM resolution is about 50%.

Fig. 7 : Average pulse-height ($\overline{PH}$) distribution of the dE/dx chamber obtained with the SEL trigger for tracks surviving the fast off-line filtering process (Section 5). The two peaks correspond to single- and double-particle (unresolved pairs) energy losses. The arrow points to the most probably energy-loss channel value for the single-particle case.

Fig. 8 : a) Distribution of the minimum distance between the cluster associated with the $e^\pm$ trigger track and any other cluster in the same dE/dx plane for the SEL trigger (full-line histogram) and "pion" trigger (dashed-line histogram) events.
b) Scatter plot of the minimum distance between clusters associated with the $e^\pm$ trigger track and any other cluster in the same dE/dx plane, for the first and the second plane of this chamber. Only events surviving the $\overline{PH}$ cut entered the plot. The same type of correlation was found for any two planes of the chamber.

Fig. 9 : a) $T = (p - E)/\sqrt{p^2 + E^2}$ distribution for a sample of $e^\pm$ candidates surviving the off-line filtering process;
b) same as in a) for a sample of "pion" trigger events;
c) same as in a) for a sample of SEL trigger events which were rejected by the $\overline{PH}$ cut.

Fig. 10 : Ratio of the Monte Carlo $e^\pm$ background to the experimentally observed $e^\pm$ signal, after the off-line filtering process, as a function of p_T^* .

Fig. 11 : Prompt $e^\pm$ acceptance (in terms of the effective rapidity times the azimuthal angle acceptance) as a function of p_T^* , for the two charge states and the two types of EMSDs; SW stands for SW3 + SW4, LG for LG3 + LG4.

Fig. 12 : Charge asymmetry as a function of p_T^* for the final $e^\pm$ sample.

Fig. 13 : Prompt $e^\pm$ charge-averaged invariant cross-section as a function of p_T^* obtained in this experiment (black circles) and in a previous ISR experiment¹⁾ (CCRS Collaboration: open circles) at $\sqrt{s} = 62.4$ GeV in the same kinematical region. The full line represents the fit⁸⁾ to the charge-averaged inclusive pion cross-section at 90° multiplied by 10^{-4} . Notice that only statistical errors are shown for the CCRS data points.

Fig. 14 : Charge-averaged (e/π) ratio measured in this experiment (black circles) as a function of p_T^* . The same fit⁸⁾ to the inclusive pion cross-section as that of Fig. 13 was used to compute this ratio. Also shown are the results of two previous ISR experiments: one²⁾ at 30° and $\sqrt{s} = 53$ GeV (ACHMNR Collaboration: black triangles), and the other¹⁾ at 90° and $\sqrt{s} = 62.4$ GeV (CCRS Collaboration: open circles). For the latter, the ratio of the electron to the π^0 rate, which was measured in the same experiment, is presented.

Fig. 15 : Final $e^\pm$ rate as a function of the crossing-point position (y coordinate) along the vacuum chamber, showing the modulation effect of the external-conversion pairs caused by the pipe corrugations.

APPENDIX A

EXPERIMENTAL ESTIMATE OF THE BACKGROUND OF e^+e^- PAIRS

Owing to the corrugated shape of the ISR vacuum chamber, the mean thickness of stainless steel traversed by photons varied from point to point in a periodic way. The minimum thickness was 0.2 mm, but the mean thickness, integrated over the source length and crossing angles, was 0.32 mm.

A Monte Carlo simulation of the vacuum pipe showed a periodic variation of the effective thickness which could be fitted by a simple sinusoidal function superimposed on a continuum. The period was 2.5 cm (the input period of the corrugation was deduced from the design figures of the vacuum chamber) and the amplitude of the modulation $(32 \pm 5)\%$ of the mean value.

e^+e^- pairs originating from external conversions in the pipe wall must have the same modulation; this effect was, in fact, found in the experimental data. The e^+ rate (of the final sample of events) as a function of the crossing-point position along the vacuum pipe is shown in Fig. 15. The distribution could be fitted by a smooth function (continuum) plus a sinusoid.

A fit of this kind was applied to two sets of data: a) a sample of unresolved e^+e^- pairs, selected by means of their average pulse-height ($\overline{PH}$) in the dE/dx chamber; b) the sample of finally selected prompt e^+ events. The results of these fits can be summarized as in Table A1. A confirmation that a real effect was observed came from the stability of the period T and the zero coordinate y_0 in the two fits, implying that the "same" vacuum chamber was observed in the two samples of events.

The interpretation of these results is the following. In the first case (sample a) true unresolved e^+e^- pairs from external and internal (Dalitz) conversions were detected; internal conversion e^+ cannot be affected by the modulation

effect, therefore the fit to sample a allowed the evaluation of the upper limit of the ratio of external to external-plus-internal conversion, i.e.

$$\frac{\text{Ext. conv.}}{(\text{Ext.} + \text{int.}) \text{ conv.}} \leq \frac{12.3 \pm 2.7}{32 \pm 5} = (38 \pm 10)\%$$

In the second case (sample b) the amplitude of the modulation effect was a measurement of the residual external conversion background in the final $e^\pm$ sample, i.e.

$$\frac{\text{Ext. conv.}}{\text{Total } e^\pm \text{ signal}} = \frac{4.41 \pm 0.65}{32 \pm 5} = (14 \pm 3)\%.$$

This experimental estimate compares well with the results of the Monte Carlo calculations (see Section 6) on the residual background from external conversions.

Table A1

Fit parameter	Sample a	Sample b
Period T (cm)	2.39 ± 0.03	2.42 ± 0.02
Zero coordinate y_0 (cm)	0.91 ± 0.08	0.83 ± 0.06
Amplitude (% of the mean)	12.3 ± 2.7	4.41 ± 0.65
$\chi^2/\text{d.o.f.}$	60/77	90/77

Fig. 1

Fig. 2

Fig. 3

Fig. 4

Fig. 5a

Fig. 5b

Fig. 5c

Fig. 6

Fig. 7

Fig. 8a

Fig. 9a

Fig. 9b

Fig. 9c

Fig. 10

Fig. 11

Fig. 12

Fig. 13

Fig. 14

Fig. 15