KAON PRODUCTION IN \( \bar{p}p \)-REACTIONS
AT A CENTRE OF MASS ENERGY OF 540 GeV

UA5 Collaboration

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ABSTRACT
Using the UA5 detector, the inclusive central production of \( K_S^0 \) and \( K^+ \) mesons has been measured in non single-diffractive interactions at the CERN SPS \( \bar{p}p \) Collider at a c.m. energy of 540 GeV. The average transverse momentum is found to be \( \langle p_T \rangle = 0.57 \pm 0.03 \) GeV/c in the rapidity range \( |y| < 2.5 \), which is an increase of about 30% over the top ISR energy. The K/\( \pi \) ratio has increased from about 8% at ISR energies to 9.5 ± 0.9 ± 0.7% (the last error is systematic) at 540 GeV. The average number of \( K_S^0 \) per non single-diffractive event is 1.1 ± 0.1 and the inclusive inelastic cross-section is estimated at 49 ± 5 mb.

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1. INTRODUCTION

With the start of the CERN SPS pp Collider a new energy region (centre of mass energy $\sqrt{s} = 540$ GeV*) has been opened for studying hadronic interactions. In a general survey of hadronic interactions at this new energy regime we have observed non-scaling behaviour in multiplicity and rapidity distributions [2, 3]. Observation of non-scaling behaviour often points to either changing composition of produced particles or to changes in the production mechanism. In the past ten years there have been several suggestions to explain these observations and even suggestions for the existence of new phenomena [4].

The study of strange particle production provides a useful tool in understanding the production mechanisms. Observations up to ISR energies ($\sqrt{s} = 63$ GeV) show that the $K/\pi$ ratio increases very slowly with energy to about 8% at ISR [5-46]. Naïvely, it may be believed that at sufficiently high energy the production of strange quarks relative to lighter quarks is not suppressed, but in reality the observed strange particles may be the result of mechanisms for which the suppression is governed by factors other than the centre of mass energy. For example, for the strange particles coming from the decay of non-strange resonances the suppression is governed more by the mass of the resonance than by the centre of mass energy. Furthermore, the above ratio for the associated production of strange particles in the fragmentation region may be different from that of centrally produced pairs of strange particles. A study of rapidity and $p_T$ distributions of strange particles could provide information on the production mechanisms or on the non-scaling behaviour mentioned above, perhaps through the existence of a threshold (e.g. charm production).

The average transverse momentum, $<p_T>$, is known to increase slowly with energy up to ISR energies, the value for kaons being some 30% larger than that for pions [24]. At the Collider the UA1 experiment has shown [47] that for charged particles the average transverse momentum has increased substantially, to $<p_T> = 0.424$ GeV/c from $<p_T> = 0.37$ GeV/c [24] at the ISR. Furthermore, in the

* The nominal beam momentum was 270 GeV/c, but measurements give 273.0±1.4 GeV/c [1].
UA1 experiment the \( <p_T> \) has been shown to increase with event multiplicity up to a point and then to level off at higher multiplicities, the levelling-off being interpreted as a sign of a possible phase transition of hadronic matter [48-50].

Detailed measurements of kaon production exist at c.m. energies up to 63 GeV for pp [5-29] and up to 14 GeV for \( \bar{p}p \) reactions [30-42]. The first results on kaons in the \( p_T \)-range 0.2-1.8 GeV/c at the Collider energy based on 2100 minimum bias events were published from this experiment [51]. Also the UA2-experiment has published results on the inclusive \( K^\pm \) production in the \( p_T \)-range 0.4-1.1 GeV/c and for pseudorapidity \( |\eta|<0.7 \) [52] (\( \eta = -\ln \tan \theta/2 \), where \( \theta \) is the centre of mass angle between the particle direction and the beam axis).

This paper gives the results from the UA5 experiment on the production of neutral and charged kaons at the Collider, based on a study of the decays \( K_S^0 \rightarrow \pi^+\pi^- \) and \( K^\pm \rightarrow \pi^\pm\pi^0\pi^- \) (\( K_{13} \)) from about 8000 minimum bias events observed in the UA5 streamer chambers. The increased statistics permit a more detailed study of kaon production in the rapidity region \( |y| \leq 3.5 \) and the \( p_T \)-range 0-3.5 GeV/c, where \( y = 0.5 \ln \left( (E+p_L)/(E-p_L) \right) \) is the rapidity in the c.m. system (\( E \) is the energy and \( p_L \) is the longitudinal momentum of a particle). We present results on inclusive \( p_T \) and rapidity distributions and kaon yields. Studies of dependence on charged multiplicity as well as comparisons with results at lower energies are presented.

The outline of the paper is as follows. In section 2 we describe the UA5-detector and the data analysis procedures used to obtain a clean kaon sample. In section 3 the results are presented and discussed and comparisons with other data are made. Conclusions are drawn in section 4.

2. EXPERIMENTAL PROCEDURES

2.1 Detector and data taking

For a detailed description of the detector the reader is referred to ref. [53]. Fig. 1 shows a schematic layout of the UA5 detector. It consists of two large streamer chambers, 6 m by 1.25 m by 0.5 m, placed 4.5 cm above and below the
SPS beam axis respectively, giving a geometrical acceptance for charged particles of about 95% for the pseudorapidity range $|\eta| \leq 3$, falling to zero at about $|\eta| = 5$. Each chamber is viewed by three cameras, which are equipped with mirror systems to give stereoscopic pairs of views. The two main cameras each view slightly more than half the chamber at a demagnification of 50 and the central supplementary camera views the whole chamber at a demagnification of 80. The system is triggered by large scintillation counter hodoscopes at each end covering a pseudorapidity interval of $2.0 < |\eta| < 5.6$. The minimum bias trigger, requiring at least one detected particle at each end of the detector, accepted (95±2)% of the inelastic, non single-diffractive events as determined by Monte Carlo simulations.

There is no magnetic field in the chambers and thus no direct momentum measurements of the charged primary particles are possible. However, the kinematics of the $K^0_S$ and the $K_{S3}$ decays allow determination of the kaon momentum once the directions of the charged decay products are seen in the chambers. The three-body decay of $K^0_L$ with one unseen neutral outgoing particle does not allow momentum calculation. Fig. 2 depicts schematically an event and indicates the different features that we are able to measure.

Data were obtained during two different runs, the first in October—November 1981 with a Collider luminosity of about $10^{25}$ cm$^{-2}$s$^{-1}$ and the second in September 1982 when the luminosity reached about $2 \times 10^{26}$ cm$^{-2}$s$^{-1}$. An important improvement to the detector was the change of the 0.4 mm corrugated steel beam pipe used in the first run to a 2 mm beryllium pipe for the 1982 run, giving far fewer electro-magnetic showers. Our published results on strange particles [51] are based on data from the first run while the data presented here were obtained during the second run and thus analysed under much cleaner conditions. The $K^0_S$ data are based on 7120 minimum bias events and the event sample underlying the $K_{S3}$ data includes 1133 additional events photographed with only the two central supplementary cameras.

2.2 Scanning and measurements

Two independent methods were used to find candidates for the strange particle decays $K^0_S \to \pi^+\pi^-$ and $K^+ \to \pi^+\pi^+\pi^- \pi^-$: namely a special visual scan of the events
on film, and software cuts applied to measured events.

2.2.1 Visual scan

A special scan of the minimum bias events for decays seen in the chamber volumes was carried out. The signature looked for was either a V, i.e. two charged tracks starting at the same point without an associated incoming track, or a C3, i.e. a charged track branching into three charged tracks. To reduce the background, mainly from photon conversions in the chamber gas characterized by small opening angles, a V had to have a projected opening angle larger than 2° on the scanning table to be accepted. A photograph of an event with a V and a C3 is shown in fig. 3.

2.2.2 Software search

After the events had passed the UA5 analysis procedure [3] where all observed tracks were digitized, reconstructed in space and associated with primary or secondary vertices, special software cuts were applied to the measured data in order to find neutral two-prong or charged three-prong decays. The aim was to find tracks close to each other with their point of closest approach inside the chamber volumes. The spatial resolution did not allow an unambiguous identification of decay vertices outside the chamber volumes.

2.2.3 Check scan

All V and C3 candidates found by either method were reconstructed in space, if necessary remeasured and finally checked visually using the film and a graphics display of the measurements. To be finally accepted as a $K_S^0$ or $K_{τ3}$ the candidate had to pass strict cuts further described in the next section.

The efficiency for finding a decay appearing in the final sample was calculated assuming the two methods described above to be independent. The overall finding efficiency was found to be 96% for the neutral and 84% for the charged decays. No significant variation of the finding efficiency with $η$, $y$ or $p_T$ was found.
2.3 Data reduction

2.3.1 Monte Carlo techniques

Most kaons decay before they reach the chambers ($K^0_S$, ct=2.7 cm [54]) or after they have passed the chambers ($K_{\pi3}$, ct=371 cm [54]). Thus the acceptance correction is large and in order to get high statistics and an estimate of systematic errors we used a simple Monte Carlo technique (MC1) to make this correction. We generated single kaons and simulated their decay in the detector. The geometrical limits of the chambers were taken into account, but interactions and measurement errors were neglected. The $p_T$ and rapidity distributions were assumed to factorize (see section 3.1.2 below). They were generated with the same shape as the fits to the experimental results described in section 3 below and the parameters were tuned to fit the data.

To reduce background and to extract a clean kaon sample the event candidates were subject to a number of cuts. To determine most of these and to correct for remaining background the UA5 Monte Carlo program (MC2) [55, 58] was used. This program generates complete events with particle ratios and inclusive distributions tuned to fit the data. All particles are followed through the detector allowing for decays, hadronic and electromagnetic interactions as well as simulating measurement errors on the tracks.

2.3.2 The $K^0_S$ sample

The sample of $V$'s included decays of $K^0_S$, $K^0_L$, $\Lambda$, $\bar{\Lambda}$, photons converting in the chamber gas and other background reactions. Since the detector has no magnetic field we cannot distinguish $\Lambda$ from $\bar{\Lambda}$ and from now on $\Lambda$ or $\bar{\Lambda}$ is denoted with only $\Lambda$.

In order to get tracks of good quality the track length was required to be greater than 15 cm in space and the track fit root mean square less than 30 $\mu$m on the film. The two tracks of a $V$-candidate were fitted to a common vertex using a general least squares method taking into account the measurement errors and correlations of the track parameters [56].
The background from photon conversions was reduced by requiring the opening angle of the V to be greater than $3^\circ$ in space. The opening angle distributions for Monte Carlo (MC2) generated photon conversions in the chamber gas and Monte Carlo (MC2) generated $K_S^0$S are shown in fig. 4 where 80% of the photons are seen to be excluded by this cut alone. After all cuts are applied we estimate a 0.2% remaining contamination of photons in the final $K_S^0$ sample.

The two-body decays of $K_S^0$ and $\Lambda$ give $V$'s that are coplanar with the primary vertex, i.e. the plane formed by the two outgoing tracks contains the primary vertex. The coplanarity cut to separate $K_S^0$ or $\Lambda$ from $K_L^0$ was defined by $d$, the perpendicular distance between the V plane and the primary vertex, and $\delta$, the angle between the V plane and the line connecting the primary and the V vertices. In fig. 5 a geometrical picture of the parameters is given. Fig. 6a-c show scatter-plots of $d$ versus $\delta$ for $V$'s decaying in the chambers. Fig. 6a and b contain $K_S^0$ and $K_L^0$ decays, respectively, extracted from 30000 Monte Carlo (MC2) generated events and fig. 6c contains the data sample of $V$'s based on about 7100 events. The area of each circle is proportional to the number of events in the cell. The straight line in fig. 6a-c is the adopted cut, $d$(cm) $\leq 4 - \delta$(°). According to the Monte Carlo (MC2) studies only 1.9% of the true coplanar $K_S^0$'s were lost while 72% of the acoplanar $K_L^0$ sample was excluded. The final contamination of $K_L^0$ in the $K_S^0$ sample was estimated at 3.1%.

For V candidates passing the coplanarity cut a new least squares fit to a V-vertex was performed with the constraint of the V being coplanar with the primary vertex [56]. This fit produced improved track parameters of the V tracks which were used for further calculations. The z-coordinate (the z-axis is perpendicular to the chamber bases with its origin between the two chambers) of the V-vertex was required to be $|z| \geq 5.5$ cm to make sure that the V was produced inside one of the chambers.

To fulfill momentum conservation of a neutral two-body decay the V had to straddle the line between the primary and the V vertices. Once masses are assigned to the tracks of a coplanar V it is possible to compute the momenta of the incoming neutral particle and the charged decay products from the measured angles in the laboratory frame of reference. In principle it is a constrained fit with one degree of freedom (3 momenta to be determined from 4
constraint equations) but since we have already demanded coplanarity one of the momentum equations is automatically fulfilled and it is a straightforward matter to solve the equations. We get one solution for the \( K_S^0 \)-hypothesis assigning \( \pi \)-masses to the outgoing tracks, and two solutions for the two possible \( \Lambda \)-hypotheses, assigning proton mass to one and \( \pi \)-mass to the other outgoing track and vice versa. Considering errors on the tracks from measurements we estimate the relative error in the momentum determination to be typically \( \pm 2\% \) for \( K_S^0 \).

To reduce further the background from \( K_L^0 \) the \( V \)-vertex was restricted to the volume of a cylinder around the beam axis with a radius of 40 cm. Also the proper lifetime of the neutral strange particle was restricted to be less than \( 10 \tau \) where \( \tau = 89 \) ps is the mean lifetime of \( K_S^0 \) [54].

A quite clean \( K_S^0 \) sample can be derived from the mixed \( K_S^0 \)-\( \Lambda \) sample by exploiting their different decay kinematics. Due to the low Q-value and to the proton being much heavier than the pion, the \( \Lambda \)-decay tends to be very asymmetric in the laboratory frame of reference with the proton emitted forwards in the \( \Lambda \)-direction. Consequently interpreting all \( V \)'s as \( K_S^0 \), boosting to the \( K_S^0 \) rest frame will give most true \( \Lambda \)'s rather high values of \( |\cos \theta_K^*| \), whereas true \( K_S^0 \)'s will populate the \( \cos \theta_K^* \) distribution uniformly (\( \theta_K^* \) is the angle between the incoming \( K_S^0 \) and the direction of the decay products in the \( K_S^0 \) rest frame). This is illustrated in fig. 7 which shows our coplanar data sample together with Monte Carlo (MC2) generated \( K_S^0 \)'s and \( \Lambda \)'s. The proportion and normalization of the generated \( K_S^0 \)'s and \( \Lambda \)'s are chosen according to data assuming that the left hand part of the data plot contains clean \( K_S^0 \)'s. The dashed line corresponds to \( K_S^0 \) (MC2) and the solid line to the sum of \( K_S^0 \) and \( \Lambda \) (MC2). It turns out that almost all \( \Lambda \)'s will have \( |\cos \theta_K^*| > 0.5 \) and consequently the \( K_S^0 \) sample is defined as having \( |\cos \theta_K^*| \leq 0.5 \).

The geometrical efficiency for detecting a \( K_S^0 \) in the chambers is very small for large rapidities and for small proper lifetimes (fig. 8b and 8c). Furthermore, remaining contamination from \( \Lambda \)'s tend to simulate \( K_S^0 \) with small values of proper lifetime. The \( K_S^0 \) sample was therefore restricted to \( |y| \leq 3.5 \) and to proper lifetimes \( t > 0.75\tau \).
The remaining contamination from Λ's in the final $K_S^0$ sample was estimated to 2.1% and corrected for using the UA5 Monte Carlo program (MC2).

The probability density function for the proper lifetime of a $K_S^0$ observed in our detector is a truncated exponential distribution

$$f(t) = \frac{e^{-t/\tau}}{e^{-t_{min}/\tau} - e^{-t_{max}/\tau}}$$

where $t_{min}$ and $t_{max}$ are the minimum and maximum lifetimes respectively for the detection of each $K_S^0$ in the fiducial volume of our detector. Since $e^{-t_{max}/\tau}$ is negligible compared to $e^{-t_{min}/\tau}$ the variable $t-t_{min}$ is expected to be exponentially distributed with the slope $1/\tau$. Fig. 9 shows the distribution of $(t-t_{min})/\tau$ for our final $K_S^0$ sample. The data show the expected exponential behaviour with a slope of one (the straight line), thus providing a valuable check of the purity of the $K_S^0$ sample.

Using Monte Carlo (MC1) generated decays $K_S^0 \rightarrow \pi^+\pi^-$ in the region $|y|<3.5$, and applying all cuts the resulting geometrical efficiency was 3.9%. Using instead the region $|y|<2.5$ we found 4.1%. Fig. 8 shows the geometrical efficiency to detect such a decay in the chambers as a function of $p_T$ (in the region $|y|<2.5$) (a), rapidity (b) and number of proper lifetimes (in the region $|y|<2.5$) (c). The detection efficiency is found to be fairly uniform over the rapidity region considered. As expected the efficiency versus $p_T$ is low for $K_S^0$ in the region $p_T<0.3$ GeV/c. The overall efficiency was found to be quite sensitive to the $<p_T>$ used in MC1, e.g. varying $<p_T>$ for $K_S^0$ from 0.5 to 0.6 GeV/c increased the acceptance in the region $|y|<3.5$ from 3.2% to 4.1%. Using different shapes of the y-distribution did not change the acceptance appreciably, e.g. changing from a y-distribution with a flat plateau up to $|y|<2.5$ and a gaussian tail of width 0.5 to a flat distribution in the whole region changed the acceptance for $|y|<3.5$ from 3.9% to 3.7%.

The trigger inefficiency caused a loss of 5% of the minimum bias events but since the lost events had low multiplicities we estimate the loss of kaons to be 1.5%. After correcting for this loss and for the branching ratio of 68.61% [54] fig. 10 shows the fully corrected proper lifetime distribution for $K_S^0$. The
data are seen to be consistent with the line which has the expected slope of one thus constituting a check of the adopted correction procedures.

A summary of the cuts applied to the V sample is given in table 1a. Table 2a gives the observed numbers of $K_S^0$ in the considered rapidity ranges after the cuts were applied.

2.3.3 The $K_{X3}$-sample

To get good quality of the measurements the track lengths were required to be at least 10 cm for both incoming and outgoing tracks and the track fit root mean square should be less than 30 μm on the film. The four tracks were fitted to a common vertex using a general least squares method with the constraint of the incoming track emerging from the primary vertex [56]. The scanning efficiency was low for candidates in which the angle between the outgoing tracks was small and therefore candidates for which the opening angle between any pair of outgoing tracks was less than 2° were rejected from the sample.

The main source of background to the $K_{X3}$-decays is hadronic interactions of charged particles in the chamber gas. Generally the average opening angle between any pair of outgoing tracks, $<\alpha>$, of such an interaction is bigger than that of a $K_{X3}$-decay. Fig. 11a-c show distributions of $<\alpha>$ of Monte Carlo (MC2) generated hadronic interactions and Monte Carlo (MC2) generated $K_{X3}$-decays in the ranges $|\eta|<1$, $1\le|\eta|<2$ and $|\eta|\ge 2$ respectively. The dashed lines indicate the different cuts applied in the three regions. The cuts of $<\alpha>$ < 90°, 70° and 60° exclude 61%, 81% and 85% of the interactions in the respective region.

Also for this decay it is possible to solve for the momenta of the incoming and outgoing tracks. Assigning K-mass to the incoming and π-masses to the outgoing tracks one obtains four equations from 4-momentum conservation and can thus solve for the 4 unknown momenta. The relative precision of the kaon momentum determination is estimated to be typically ±6% for $K_{X3}$. If the momentum solution of one or several tracks was negative the decay candidate was rejected. Indeed Monte Carlo (MC2) studies showed that this was the case for about 67% of the hadronic three-prong interactions in the gas. The remaining contamination of hadronic interactions in the final sample was
estimated to be about 2%. A further correction of the order of 6% was applied to the \( K_{\pi 3} \) sample to take into account measurement errors causing a negative solution of the momentum.

As for the \( K_S^0 \) the geometrical efficiency depends on \( y \) (fig. 8b). For \( K_{\pi 3} \) we restricted ourselves to the region \( |y| \leq 2.5 \).

Monte Carlo (MC1) generation of the decay \( K^+ \to \pi^+\pi^+\pi^- \) showed that applying the cuts mentioned above results in an overall geometrical efficiency of 9.2%.

Fig. 8 shows the efficiency of detecting a \( K_{\pi 3} \) decay as a function of \( p_T \) (a), rapidity (b) and number of proper lifetimes (c). As can be seen from fig. 8a the \( K_{\pi 3} \) sample is a complement to the \( K_S^0 \) sample in the low \( p_T \)-region. For \( K_{\pi 3} \) the overall efficiency was found to be less sensitive to \( \langle p_T \rangle \) used in MC1 than in the case of \( K_S^0 \) e.g. an increase of \( \langle p_T \rangle \) in MC1 from 0.5 to 0.6 GeV/c implied a decrease in the acceptance from 9.9% to 9.2%.

The cuts applied to the sample are summarized in table 1b and the observed number of \( K_{\pi 3} \)-decays used for the analysis is given in table 2a.

3. RESULTS AND DISCUSSION

3.1 Inclusive \( p_T \)-distributions

3.1.1 Production ratio of \( K^\pm \) and \( K_S^0 \)

The fully corrected \( p_T \)-distribution for \( K_S^0 \) and \( (K^+K^-)/2 \) in the range \( |y| \leq 2.5 \) is shown in fig. 12 and given in table 3. The branching ratios used were taken from ref. [54]. The invariant cross-section is computed assuming a non single-diffractive cross-section of 43.2±1.8 mb [57, 58]. This distribution is found to be consistent with our earlier published data [51].* In the \( p_T \) region 0.35 to 1.4 GeV/c the \( K_S^0 \) and \( K_{\pi 3} \) data overlap and there is good agreement. Integrating the

* One should note that our earlier data [51] refer to the range \( |\eta| \leq 3 \), compared to the range \( |y| \leq 2.5 \) used here. A direct comparison between the sets of data is therefore not possible.
(K⁺K⁻)/2 and the K⁺ data points separately in this p_T range gives the value 0.96±0.22 for the production ratio (K⁺K⁻)/(2K⁺). This value is consistent with one as expected. From now on we combine our data points from K⁺ and (K⁺K⁻)/2 and refer to them as the K-data.

3.1.2 p_T-distributions in different rapidity intervals

In order to study the factorization between y and p_T in the kinematic region considered, we show in fig. 13a-c the p_T-distributions for the K-data in the rapidity intervals 0≤y<0.8 (a), 0.8≤y<1.6 (b) and 1.6≤y<2.5 (c) and in fig. 13d the p_T-distribution for K⁺ in the interval 2.5<y<3.5.

The lines in the figures represent the fit found for the inclusive K data (table 4a) in the region |y|≤2.5 normalized to these sets of data. The form of this fit, a combination of an exponential in transverse mass and a power law, is discussed in detail in section 3.1.3. The curves are seen to well represent the data which is also born out by a χ² test giving the following values of χ²/NDF for fig. 13 a-d respectively: 9.9/11, 3.1/10, 9.5/9 and 2.7/5. We draw the conclusion that y and p_T factorize.

In order to get better statistics we therefore use the K⁺ data in the region |y|≤3.5 (p_T-distribution given in table 3) and rescale them to the region |y|≤2.5 to combine them with the K⁺ data. The scaling factor, 0.80±0.03, is calculated integrating the data points of the fully corrected K⁺ rapidity distribution discussed in section 3.2 below.

Fig. 14 shows the invariant cross-section as a function of p_T for our K-data in the region |y|≤2.5 (the K⁺ points are rescaled from |y|≤3.5) compared to the published UA2 data on K⁺ (|η|≤0.7) [52] rescaled to account for the value of the inelastic cross-section [59]. There is good agreement between the two sets of data.

3.1.3 The form of the inclusive p_T-distribution and calculation of <p_T>

The decreasing invariant cross-section for inclusive particle production is usually parametrized according to an exponential in p_T for p_T< 1.5 GeV/c. At ISR energies parametrizations like exp(Αp_T + Βp_T^2) were often used [25] to take
into account that the distributions are flatter for larger \( p_T \). At the Collider the inclusive spectra of charged hadrons \([47, 59]\), and of pions \([52, 59]\) have been measured up to very high transverse momenta and the invariant cross-sections follow nicely a QCD inspired power law form:

\[
E \frac{d^3\sigma}{d^3p} = C \left( \frac{p_T}{p_0 + p_T} \right)^n.
\]  

(1)

a formula which for small values of \( p_T \) approaches \( C \exp(-np_T/p_0) \).

There are few data available from high energy colliding beam experiments on the low part of the \( p_T \)-spectrum, say below 0.3 GeV/c. This region was studied in detail by one experiment at the ISR \([26]\) where it was found that the form best fitting the data was an exponential in transverse mass \( m_T^2 = m^2 + p_T^2 \), \( m \) being the mass of the particle:

\[
E \frac{d^3\sigma}{d^3p} = A \exp(-b m_T).
\]  

(2)

It has also been pointed out by Hagedorn \([49]\) that from a statistical point of view form \( (2) \) is more likely than a simple exponential for low \( p_T \), being closer to a thermal Boltzmann distribution. Since our data extend right down to \( p_T = 0 \) we are in a good position to study the form of the \( p_T \)-spectrum over a large range.

The \( p_T \) distribution of our \( K \) data is shown in fig. 15. The straight line is a fit to an exponential in \( p_T \) and the curve a fit with a combination of the forms \( (1) \) and \( (2) \), the changeover point between the forms being \( p_T = 0.4 \) GeV/c. The results of the fits are given in table 4a. It is clear that the power law shape \( (1) \) is preferred over the exponential at the high \( p_T \) part of the spectrum. At the low \( p_T \) part we cannot distinguish between an exponential in \( p_T \) and an exponential in \( m_T \) on grounds of \( \chi^2 \) but for reasons given above we choose a combination of the forms \( (1) \) and \( (2) \) to fit the data.

In fig. 16 we compare our \( K \) data to data on charged kaon production in the central region \( (y=0) \) from the ISR \((\sqrt{s} = 53 \) GeV \([25]\)) and to the inclusive charged particle data for \(|y| < 2.5 \) at the Collider obtained by the UA1 experiment \([47]\).

Our \( K \) distribution falls less steeply than that from the ISR, indicating an
increased average $p_T$ with increasing energy. It is also less steep than the charged particle distribution from UA1 showing that also at Collider energy the $\langle p_T \rangle$ increases with increasing mass of the produced particle.

The average transverse momentum $\langle p_T \rangle$ is estimated from the fit to the combined forms (1) and (2), and has the value $0.57\pm0.03$ GeV/c (see table 4a for details). If one varies the changeover point between forms (1) and (2) from 0 to 0.8 GeV/c the change in the resulting $\langle p_T \rangle$ is within the statistical error of $\pm 0.03$ GeV/c. A similar fit to the ISR $K^\pm$-data gives $\langle p_T \rangle = 0.457\pm0.002$. For comparison the UA1 experiment quotes the value $\langle p_T \rangle = 0.424\pm0.001$ [47] for charged hadrons, assuming the power law form (1) to be valid for all $p_T$, which very likely underestimates $\langle p_T \rangle$ by some 50 MeV/c [49].

Fig. 17a shows a compilation of $\langle p_T \rangle$ for data on inclusive production of $K_S^0$ and $K^\pm$ in pp interactions [5-29] together with data points at 540 GeV from this experiment and from the UA2 experiment [52]*. One should note that the errors given are statistical only and do not take into account systematic errors varying from experiment to experiment. The $\langle p_T \rangle$ is seen to increase slowly with energy.

Fig. 17b shows the energy variation of the average transverse momentum for pions, kaon and protons. The data below 540 GeV are obtained from a compilation [24], where data from different experiments are treated in a coherent way. The straight lines are fits to the form $\langle p_T \rangle = a + b \ln s$ in the c.m. energy range 23-83 GeV. Extrapolating these fits to the Collider and comparing with the measured values shows an increase over the extrapolated value for pions [52], kaons (this experiment) and protons [52] of $14\pm13$ %, $21\pm17$ % and $29\pm19$ % respectively*. In calculating the error of the overshoot at 540 GeV we took into account the systematic error of 10% in the compiled values.

* To calculate $\langle p_T \rangle$ for the UA2 data [52] the following fits to the $p_T$-spectra were used. For pions we used the UA2 fit to the charged and neutral pion data [52] combined with an exponential in transverse mass for $p_T<0.4$ GeV/c. For kaons and protons the UA2 data cover only a limited range in $p_T$ and exponential fits were used.
There is a suggestion of an average transverse momentum larger than a
Ans extrapolation from lower energies.

3.1.4 $p_T$-distributions in bands of charged multiplicity

A correlation between $\langle p_T \rangle$ and multiplicity has been found in cosmic ray data [4] and in the UA1 data on charged particles [47]. Fig. 18 shows corrected $p_T$-distributions for our K sample in the region $|y| \leq 2.5$ (the $K_S^0$ data are scaled from $|y| \leq 3.5$) divided into three bands of observed charged multiplicities in the region $|\eta| \leq 3.5$, $0 \leq n_{ch} \leq 18$ (a), $19 \leq n_{ch} \leq 38$ (b) and $n_{ch} \geq 39$ (c). Results of fits to the combined forms (1) and (2) (the solid lines) are given in table 4b. The average $p_T$ derived from the fit is shown in fig. 19a as a function of rapidity density. The data are consistent with an $\langle p_T \rangle$ - multiplicity correlation of similar magnitude as observed by the UA1 experiment for charged hadrons [47], also shown in the figure. The correlation is not significantly changed if instead of correlating $\langle p_T \rangle$ with the total charged multiplicity in $|\eta| \leq 3.5$ we correlate $\langle p_T \rangle$ with the local track density in a pseudorapidity region, $\Delta \eta$, centered on the kaon pseudorapidity, which can be seen from fig. 19b.

3.2 Inclusive rapidity and pseudorapidity distributions

The corrected $K_S^0$ and $K^\pm$ rapidity distributions folded around zero and averaged are shown in fig. 20a. The height of the plateau of the $K_S^0$ distribution is found to be consistent with the one of the $K^\pm$ distribution. This is a consistency check of the value of $\langle p_T \rangle$, $0.57 \pm 0.03$ GeV/c, found for the combined kaon sample and used as input to the Monte Carlo (MC1) program to compute geometrical efficiencies. An increase of $\langle p_T \rangle$ in MC1 increases the geometrical efficiency for $K_S^0$ and decreases it for $K^\pm$ (most $K_S^0$ decay before reaching the chambers whereas most $K^\pm$ decay after leaving the chambers).

The distributions have a central plateau with a half width at half maximum of

* The central region for the charged multiplicity, $|\eta| \leq 3.5$, was chosen to be able to compute central rapidity densities comparable to the ones measured by the UA1 experiment [47] in the range $|y| < 2.5$. 
approximately 3 units in rapidity. The central rapidity density is $0.16 \pm 0.02$ for non single-diffractive events. Comparing the height of the charged particle pseudorapidity distribution of our non single-diffractive data to the one of our inelastic data [58], we estimate the central rapidity density for $K_S^0$ in inelastic events to be $0.15 \pm 0.02$. In fig. 21 is shown the energy dependence of the central rapidity density for $K_S^0$ production. Shown are data from lower energy pp reactions [5-29] and our measurement at 540 GeV. The rapidity density is seen to increase smoothly with energy. The line is a fit of the form $a + b \times n$ to lower energy pp data and our inclusive data point at 540 GeV. The result of the fit is given in table 6.

Fig. 20b displays the $K_S^0$ and $K^+$ pseudorapidity distributions folded around zero and averaged. The charged and neutral kaon distributions are found to be consistent. The dashed line in fig. 20a and b represents the UA5 charged particle pseudorapidity distribution rescaled by 0.04, which is the ratio of the central pseudorapidity densities for the kaon data and the charged particle data [58]. The shape of the kaon distributions are similar to that of the charged particle distribution.

In fig. 20c are shown the $K_S^0$ rapidity distributions in three bands of observed charged multiplicity in the region $|\eta| \leq 3.5$, $0 \leq n_{ch} \leq 21$, $22 \leq n_{ch} \leq 35$ and $n_{ch} \geq 36$. They are all consistent with having the same shape as the full distribution.

3.3 Rates and cross-sections

In table 2b are given the corrected numbers of $K_S^0$ per event. In the range $|y| \leq 2.5$ the value $\langle n_{K_S^0} \rangle = 0.72 \pm 0.06$ was calculated by integrating the fit of the combined forms (1) and (2) to the corrected $p_T$-distribution of the $K$ data shown in fig. 15. For the calculation in the range $|y| \leq 3.5$ only $K_S^0$ data were used. In this range the yield was additionally calculated from the corrected lifetime distribution in fig. 10. The two values are consistent and in table 2b their average, $\langle n_{K_S^0} \rangle = 0.92 \pm 0.07$, is given. These results are consistent with the published 1981 data [51] if proper allowance is made for the different rapidity or pseudorapidity ranges used.

In table 5 we give the corrected number of $K_S^0$ in $|y| \leq 2.5$ per observed charged
track in $|\eta|<3.5$ for three bands of observed charged multiplicity in this $\eta$-range. The numbers of $K_S^0$ are obtained from integrating the fits to the combined forms (1) and (2) shown in fig. 18. The ratio is consistent with being constant, i.e. the production of kaons is proportional to the production of charged particles.

In order to extrapolate the yield of $K_S^0$ from the measured region $|y|<3.5$ to the full phase space we have used three different methods. We have tried various types of parametrizations to fit the $K_S^0$ rapidity distribution shown in fig. 20a: a gaussian, a flat distribution with gaussian wings and a Fermi-distribution, $\left[1+\exp((y-y_0)/\sigma)\right]^{-1}$. The fits to the rapidity distribution turn out to be somewhat unstable, since the shape of the tail is heavily dependent on the last data point. However, from the fits we estimate a $K_S^0$ yield per event of 1.02±0.10 in the full phase space. The error includes the systematic uncertainty.

An independent estimate of the $K_S^0$ yield in the full rapidity range was made assuming the shape of the charged particle pseudorapidity distribution, which is measured in the region $|\eta|<5$, (fig. 20a,b) to be valid also for the $K_S^0$ distribution. Using the UA5 event generator (MC2) to correct for the differences between rapidity and pseudorapidity and to extrapolate from $|\eta|<5$ to full phase space (an extrapolation of the order of 4%), we estimate the $K_S^0$ yield per event to be 1.08±0.08.

We have made a third estimate of the yield in full phase space using the UA5 event generator (MC2) to scale the yield in $|y|<3.5$. In the event generator, which is tuned to fit the measured distributions, the production characteristics of pions and kaons are assumed to be the same apart from kinematic effects. Using this method gives a number of 1.11±0.08 $K_S^0$ per event in the full rapidity region.

The three methods give compatible results for the yield in the full phase space and our best estimate, given in table 2b, is the average value of 1.1±0.1 $K_S^0$ per non single-diffractive event. The error includes systematic uncertainties. Using the value 48.6±1.6 mb for the inelastic cross-section [57] and the value 5.4±1.1 mb for the single-diffractive cross-section [58] and assuming the same ratio of kaons to charged particles in non single-diffractive and single-diffractive events, we estimate a value of 1.0±0.1 $K_S^0$ per inelastic event. The
dependence on energy of the inclusive $K^0_S$ production in $pp$ [5-29] and $\bar{p}p$ [30-42] reactions is shown in fig 22a. Lower energy $\bar{p}p$ data are dominated by the annihilation component which is negligible at 540 GeV. We have therefore used $pp$ data in the energy range 3.6 to 53 GeV and our inclusive data point at 540 GeV to make a fit of the form $a + b \ln s + c (\ln s)^2$. The line in fig. 22a shows the result of the fit and the parameters are given in table 6.

Using a value for the inelastic non single-diffractive cross-section of $\sigma_{\text{NDS}} = 43.2 \pm 1.8$ mb [57, 58] we get a non single-diffractive cross-section for $K^0_S$ of 48\pm 5 mb at $s=540$ GeV. Using our estimate of the single-diffractive cross-section, 5.4\pm 1.1 mb [58], and again assuming the same ratio of kaons to charged particles in non single-diffractive and single-diffractive events, we get a single-diffractive contribution to the $K^0_S$ cross-section of 1.3\pm 0.5 mb and an inelastic cross-section of 49\pm 5 mb. This is compared to lower energy data [5-42, 60] in fig. 22b. The line is again a fit to the lower energy $pp$ data including our inclusive data point at 540 GeV to the form used in fig. 22a and the parameters are given in table 6.

3.4 $K/\pi$ ratio and strangeness suppression

The $K/\pi$ ratio was calculated separately in the two regions $|y|\leq 3.5$ and $|y|\leq 2.5$. The pion yields were obtained from the measured charged particle yields in $|\eta|\leq 3.5$ and $|\eta|\leq 2.5$ [61]. The measured rates of $K^\pm$ (this work) and $\Xi^-$ [62] and the estimated rates of $p\bar{p}$ and $\Sigma^+$ were subtracted* and a correction for Dalitz pairs was made. The difference between pseudorapidity and rapidity was corrected for using the UA5 Monte Carlo program (MC2). The $K/\pi$ ratio was found to be consistent in the two regions with an average value of 0.095\pm 0.009\pm 0.007 (the last error is systematic). The energy variation of this ratio is shown in fig. 23 (only statistical errors are shown) where it is compared to results at lower energies [5-29, 55, 63]. The $K/\pi$ ratio is seen to increase with energy.

* The $p\bar{p}$ rate was estimated using a $K/p$ ratio of 1.48\pm 0.11 calculated from exponential fits to $p_T$-distributions of kaons and protons as measured by the UA2 experiment [52]. In estimating the $\Sigma^\pm$ rate we used our previously measured $\Lambda$ rate [51] and the assumption $\sigma(\Lambda) = \sigma(\Sigma^+ + \Sigma^- + \Sigma^0)$. 
Fig. 24 shows the variation of the K/π ratio, R, with the transverse momentum. We used the K$^0_S$ and K$^+$ data from this experiment and the charged pion data from the UA2 experiment [52, 59]. Also shown are the UA2 values of the ratio K$^+$/π$^+$ [52]. The full line represents central (y=0) ISR data at $\sqrt{s}=53$ GeV [25, 26]. The Collider data at $\sqrt{s}=540$ GeV are consistent with the transverse momentum variation of R seen at the ISR at $\sqrt{s}=53$ GeV. Indeed, all central ISR data on the K$^+$/π$^+$ ratio [25] in the c.m. energy range 23-63 GeV are consistent with the same transverse momentum dependence. Also bubble chamber data on K$^0_S$ production in the c.m. energy range 11-27 GeV [13, 16, 19, 21, 23], although in a more limited transverse momentum range, show the same p$_T$-dependence of R.

Although the errors are large the data are consistent with an energy independent variation of R with p$_T$. The observed energy variation of the inclusive K/π ratio, see fig. 23, reflects therefore merely the change of the slope of the p$_T$-distribution, becoming less steep with increasing energy.

It is interesting to note, that in a recently reported measurement for η=0.8 at the ISR [64], the K$^+$/π$^+$ ratio was found to stay constant at 0.46 for p$_T$>3 GeV/c. In this case the constant value of R was interpreted [64] as being due to the fragmentation of quark-quark scattered jets. The available data on kaon production at the Collider do not allow a quantitative comparison for large values of p$_T$.

Finally we have estimated the strangeness suppression factor λ, defined as the ratio of the numbers of produced s̅ to u̅ or d̅ pairs. We have used the formula by Anisovich and Kobrinski [65] derived from a statistical quark model which takes into account the additional suppression from resonance decays. From the K/π ratio of 0.095±0.009±0.007 we get a value of 0.30±0.03±0.03 for λ (last errors are systematic), consistent with the result of Malhotra and Orava [66] who from an analysis of experimental data get an energy independent value of λ.

* For p$_T$>0.4 GeV/c we used the published UA2 π fit [52] renormalized with +15.5% according to [59]. For p$_T$<0.4 GeV/c we extrapolated using an exponential in m$_T$. 
\( \lambda \approx 0.29 \pm 0.02 \). In a recent review by Wroblewski [67] various estimates of \( \lambda \) are shown to be consistent with a slow increase with energy. The energy dependence of \( \lambda \) is further discussed in references [68, 69].

4. CONCLUSIONS

We have presented results on the inclusive production of \( K_S^0 \) and \( K^\pm \) mesons in non single-diffractive \( pp \) interactions at a c.m. energy of \( \sqrt{s} = 540 \) GeV. The measurements were made in the central region with a c.m. rapidity \( |y| \leq 3.5 \). We have reached the following conclusions:

(i) In overlapping kinematical regions the production cross-section for \( K_S^0 \) equals that of \( (K^+K^-)/2 \). The average number of \( K_S^0 \) is \( 1.1 \pm 0.1 \) per non single-diffractive event and \( 1.0 \pm 0.1 \) per inelastic event. The inclusive non single-diffractive cross-section for \( K_S^0 \) is \( 48 \pm 5 \) mb, and the corresponding inelastic cross-section is \( 49 \pm 5 \) mb.

(ii) Rapidity and transverse momentum are found to factorize. The inclusive \( p_T \)-distribution is well described by an exponential in transverse mass for \( p_T < 0.4 \) GeV/c and a power law dependence for \( p_T > 0.4 \) GeV/c. The average transverse momentum is found to be \( 0.57 \pm 0.03 \) GeV/c.

(iii) The rapidity distribution shows a central rapidity density of \( 0.16 \pm 0.02 \) and a half width at half maximum of approximately 3 units for non single-diffractive events. The central rapidity density for all inelastic events is estimated at \( 0.15 \pm 0.02 \).

(iv) The \( K/\pi \) ratio is found to be consistent with an energy independent variation with \( p_T \). The inclusive \( K/\pi \) ratio, however, is seen to have increased from about 8% at ISR energies to \( 9.5 \pm 0.9 \pm 0.7\% \) (last error is systematic) at the Collider, where the \( p_T \)-distributions are less steep. From the
inclusive K/π ratio at the Collider we deduce a strangeness
suppression factor of $\lambda = 0.30 \pm 0.03 \pm 0.03$ (last error is
systematic).

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the Stockholm group by the Swedish Natural Science Research Council. Last,
but not least, we acknowledge the contribution of the engineers, scanning
and measuring staff of all our laboratories.
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        24 GeV/c).
        (pp, \(p_{lab}\) = 100 GeV/c).
        (pp, \(p_{lab}\) = 360 GeV/c).
        pp, \(\sqrt{s}\) = 3-53 GeV).
[38] B.V. Batyunya et al., Univ. of Helsinki, Report Series in Physics, HU-P-229 (1983) (pp. $p_{\text{lab}}=22.4$ GeV/c).
[59] UA2 Collab., M. Banner et al., "Inclusive Particle Production in the Transverse Momentum Range between 0.25 and 40 GeV/c at the CERN SpS Collider", DPhPE 84-07.


TABLE CAPTIONS

Table 1 Criteria to be fulfilled to be accepted as a kaon, for \( K^0_S \) (a) and \( K_{\pi 3} \) (b).

Table 2 Kaon yields, observed numbers (a) and corrected numbers (b). The quoted errors are statistical only.

Table 3 The invariant cross-section for neutral (a) and charged (b) kaons as a function of \( p_T \). The errors given are statistical only. We estimate a systematic scale error of about 5%.

Table 4 Results of fits to \( p_T \) distributions (\( f = 1/\sigma \, d\sigma/dp_T^2 \)). Forms used:

\[
\begin{align*}
(1) \quad f & \propto C \frac{p_0^n}{(p_0 + p_T)^{\eta}} & \text{if} \, p_T > 0.4 \, \text{GeV/c} \\
(2) \quad f & \propto A \exp(-b \, m_T) & \text{if} \, p_T < 0.4 \, \text{GeV/c} \\
(3) \quad f & \propto A \exp(-b \, p_T).
\end{align*}
\]

When combining forms (1) and (2) the parameters \( A, p_0 \) and \( n \) are fitted. The parameters \( C \) and \( b \) are given by requiring continuity of the curve and its slope and take the values \( C = 9.87 \) and \( b = 7.43 \) for the case of UA5 K data in \( |y| < 2.5 \) with rescaled \( K^0_S \) data.

Data sets used: (a) UA5 kaon data in accessible \( y \)-ranges and ISR data [25] and (b) UA5 data in bands of observed charged multiplicity in the range \( |\eta| < 3.5 \).

Table 5 Kaon yields in \( |y| < 2.5 \) per observed charged track in the region \( |\eta| < 3.5 \) in bands of observed charged multiplicity in this region.

Table 6 Results of fits of the form \( a + b \, \ln s + c \, (\ln s)^2 \) to the energy dependence of experimental values of \( 1/\sigma_{\text{inel}} \, d\sigma/dy \) \( y = 0 \) (c kept fixed at zero), \( <n_{\pi 0}> \) and \( \sigma(\pi^0) \) from pp data in the energy range 3.6 to 53 GeV and our inclusive result at 540 GeV.
<table>
<thead>
<tr>
<th>Requirement</th>
<th>Value</th>
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</thead>
<tbody>
<tr>
<td>Length of each track</td>
<td>( \geq 15 \text{ cm} )</td>
</tr>
<tr>
<td>Track fit RMS</td>
<td>( \leq 30 \text{ (\mu)m} )</td>
</tr>
<tr>
<td>Opening angle</td>
<td>( \geq 3 \text{ degrees} )</td>
</tr>
<tr>
<td>Coplanarity cut (fig. 6)</td>
<td>( d(\text{cm}) \leq 4 - 8(\text{degrees}) )</td>
</tr>
<tr>
<td>Absolute value of z-coordinate</td>
<td>( \geq 5.5 \text{ cm} )</td>
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<tr>
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<tr>
<td>Distance between decay vertex and beam axis</td>
<td>( \leq 40 \text{ cm} )</td>
</tr>
<tr>
<td>Proper lifetime</td>
<td>( \geq 0.75 \tau )  ( \leq 10 \tau )</td>
</tr>
<tr>
<td>(</td>
<td>\cos \theta_K^*</td>
</tr>
<tr>
<td>Absolute value of rapidity</td>
<td>( \leq 3.5 )</td>
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<td>Condition</td>
<td>Value</td>
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<tr>
<td>------------------------------------------------</td>
<td>----------</td>
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<td>track fit RMS</td>
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<td>opening angle for each</td>
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<td>pair of outgoing tracks</td>
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<td>average opening angle</td>
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<tr>
<td>for</td>
<td>η</td>
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<td>for 1≤</td>
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<tr>
<td>for</td>
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</tr>
<tr>
<td>momentum of incoming and outgoing particles</td>
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<tr>
<td>abs. value of rapidity</td>
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**Table 2**

(a) observed numbers

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<th>$K_S^0$</th>
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<th>$K^\pm$</th>
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<tbody>
<tr>
<td>$</td>
<td>y</td>
<td>\leq 2.5$</td>
<td></td>
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<tr>
<td>min. bias events</td>
<td>7120</td>
<td>7120</td>
<td>8253</td>
</tr>
<tr>
<td>no of decays used</td>
<td>171</td>
<td>204</td>
<td>53</td>
</tr>
</tbody>
</table>

(b) corrected numbers *

|        | $|y|\leq 2.5$ | $|y|\leq 3.5$ | full phase space |
|--------|-------------|-------------|-----------------|
| $<n_{\text{KL}}>$ | 0.72 ±0.06 | 0.92±0.07 | 1.1±0.1** |
| $K/\pi$ ratio | 0.095±0.009 |

* By assumption $\sigma(K^0_S) = 0.5 (\sigma(K^+) + \sigma(K^-))$.
** Both statistical and systematic errors are included.
### Table 3

<p>| $p_T$ (GeV/c) | $E \frac{d^2\sigma}{d\phi d^3p}$ (mb GeV$^{-2}$c$^3$) $K_S^0 |y| \leq 2.5$ | $E \frac{d^2\sigma}{d\phi d^3p}$ (mb GeV$^{-2}$c$^3$) $K_S^0 |y| \leq 3.5$ |
|---------------|------------------------------------------------|------------------------------------------------|
| 0.425         | 1.66 ±0.59                                      | 1.78 ±0.52                                      |
| 0.55          | 2.73 ±0.62                                      | 2.69 ±0.53                                      |
| 0.65          | 1.53 ±0.36                                      | 1.36 ±0.29                                      |
| 0.75          | 0.89 ±0.22                                      | 0.82 ±0.18                                      |
| 0.85          | 0.68 ±0.17                                      | 0.52 ±0.12                                      |
| 0.975         | 0.28 ±0.07                                      | 0.26 ±0.06                                      |
| 1.125         | 0.17 ±0.05                                      | 0.17 ±0.04                                      |
| 1.275         | 0.13 ±0.04                                      | 0.11 ±0.03                                      |
| 1.425         | 0.090 ±0.028                                     | 0.066 ±0.020                                     |
| 1.6           | 0.031 ±0.013                                     | 0.032 ±0.012                                     |
| 1.85          | 0.031 ±0.010                                     | 0.024 ±0.007                                     |
| 2.25          | 0.012 ±0.004                                     | 0.010 ±0.003                                     |
| 3.0           | 0.0018±0.0010                                    | 0.0016±0.0009                                    |</p>
<table>
<thead>
<tr>
<th>$p_T$ (GeV/c)</th>
<th>$E \frac{d^2\sigma}{dp}$ (mb GeV$^{-2}$c$^3$)</th>
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<tr>
<td></td>
<td>$(K^+ + K^-)/2 \</td>
</tr>
<tr>
<td>0.1</td>
<td>11.3 ±2.8</td>
</tr>
<tr>
<td>0.3</td>
<td>4.5 ±1.0</td>
</tr>
<tr>
<td>0.5</td>
<td>2.23±0.67</td>
</tr>
<tr>
<td>0.8</td>
<td>0.30±0.17</td>
</tr>
<tr>
<td>1.2</td>
<td>0.22±0.16</td>
</tr>
</tbody>
</table>
Table 4

(a) UA5 data fitted to form (3)

<table>
<thead>
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<th>data</th>
<th>parameters</th>
<th>( \langle p_T \rangle ) (GeV/c)</th>
<th>( &lt;n_{K^0} &gt; )</th>
<th>( X^2/\text{NDF} )</th>
</tr>
</thead>
<tbody>
<tr>
<td>( K^-</td>
<td>y</td>
<td>&lt;2.5, \ K^0_S ) rescaled from (</td>
<td>y</td>
<td>\leq3.5 )</td>
</tr>
</tbody>
</table>

UA5 data fitted to the combined forms (1) and (2)

<table>
<thead>
<tr>
<th>data</th>
<th>parameters</th>
<th>( \langle p_T \rangle ) (GeV/c)</th>
<th>( &lt;n_{K^0} &gt; )</th>
<th>( X^2/\text{NDF} )</th>
</tr>
</thead>
<tbody>
<tr>
<td>( K^-</td>
<td>y</td>
<td>\leq2.5 )</td>
<td>( 127\pm41 ) ( 7.97\pm0.55 ) ( 1.30\pm0.16 )</td>
<td>0.57\pm0.03</td>
</tr>
<tr>
<td>( K^-</td>
<td>y</td>
<td>\leq2.5 \ K^0_S ) rescaled from (</td>
<td>y</td>
<td>\leq3.5 )</td>
</tr>
<tr>
<td>( K^-</td>
<td>y</td>
<td>\leq3.5 )</td>
<td>( 119\pm51 ) ( 10.42\pm0.67 ) ( 1.99\pm0.24 )</td>
<td>0.58\pm0.04</td>
</tr>
</tbody>
</table>

\((K^+K^-)/2 \) at \( \bar{V}=53 \text{ GeV} \) [25] fitted to the combined forms (1) and (2)

<table>
<thead>
<tr>
<th>data</th>
<th>( A ) (GeV(^{-2}) c(^2))</th>
<th>( n )</th>
<th>( P_0 ) (GeV/c)</th>
<th>( \langle p_T \rangle ) (GeV/c)</th>
<th>( &lt;n_{K^0} &gt; )</th>
<th>( X^2/\text{NDF} )</th>
</tr>
</thead>
<tbody>
<tr>
<td>( K^- ) ( y=0 )</td>
<td>( 296\pm12 ) ( 15.17\pm0.14 ) ( 2.52\pm0.03 )</td>
<td>0.457\pm0.002</td>
<td>34.6/17</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
(b) UA5 K data in $|y|\leq 2.5$ ($K_S^0$ rescaled from $|y|\leq 3.5$) fitted to the combined forms (1) and (2)
(the parameter $p_0$ is kept at a fixed value of 1.4 GeV/c)

<p>| $n_{ch}$ | $|\eta|\leq 3.5$ | $n_{ch}/\Delta\eta$ | parameters | $A$ ($GeV^{-2}c^2$) | $n$ | $&lt;p_T&gt;$ (GeV/c) | $&lt;n_{K^0}&gt;<em>S$ | $\chi^2$/NDF |
|---------|-----------------|---------------------|-------------|-------------------|-----|----------------|----------------|-------------|
| 0 - 18  | 1.67±0.01       | 99±42               | 8.90±0.50   | 0.52±0.04         | 0.40±0.04 | 15.1/8         |
| 19 - 38 | 3.81±0.01       | 80±32               | 7.68±0.46   | 0.64±0.06         | 0.70±0.09 | 11.5/9         |
| 39 -    | 6.93±0.04       | 248±107             | 7.98±0.51   | 0.61±0.05         | 1.78±0.26 | 5.9/9          |
| $n</em>{ch}$ in $|\eta|\leq3.5$ | $&lt;n^0_S&gt;/&lt;n_{ch}&gt;$ |
|-----------------------------|-----------------|
| 0  -  18                    | 0.034±0.003     |
| 19  -  38                   | 0.026±0.003     |
| 39  -                        | 0.037±0.005     |
| all                          | 0.034±0.003     |</p>
<table>
<thead>
<tr>
<th>data</th>
<th>parameters</th>
<th></th>
<th></th>
<th>$\chi^2$/NDF</th>
</tr>
</thead>
<tbody>
<tr>
<td>$1/\sigma , d\sigma/dy$ at $y=0$</td>
<td>a: $-0.035\pm0.002$</td>
<td>b: $0.015\pm0.001$</td>
<td>c: $0$ (fixed)</td>
<td>30/12</td>
</tr>
<tr>
<td>$&lt;n_{K^0}\rangle_{K_S}$</td>
<td>a: $0.014\pm0.004$</td>
<td>b: $-0.028\pm0.002$</td>
<td>c: $0.0094\pm0.0003$</td>
<td>95/22</td>
</tr>
<tr>
<td>$\sigma (K^0_S)$</td>
<td>a: $0.93 \pm 0.12$</td>
<td>b: $-1.18 \pm 0.07$</td>
<td>c: $0.34 \pm 0.01$</td>
<td>98/22</td>
</tr>
</tbody>
</table>
FIGURE CAPTIONS

Fig. 1  Schematic lay-out of the UA5-detector.

Fig. 2  Schematic picture of an event as detected in the streamer chambers. The items in parentheses indicate what features we are able to measure for the various particles.

Fig. 3  Photo of an event as seen in one of the streamer chambers. The arrows point to the decays of a $K^0_S$ and a $K^0_{\pi 3}$ respectively.

Fig. 4  Distribution of opening angles for Monte Carlo (MC2) generated photon conversions in the chamber gas (the dashed histogram) and Monte Carlo (MC2) generated $K^0_S$ decays (the solid line histogram). The dashed line indicates the opening angle cut.

Fig. 5  Geometrical picture of the parameters $d$ and $S$ used to define the coplanarity cut.

Fig. 6  Scatter plot of $d$ versus $S$ for Monte Carlo (MC2) generated $K^0_S$ (a), Monte Carlo (MC2) generated $K^0_L$ (b) and the data sample of $V'$s (c). The area of each circle is proportional to the number of events in the cell. Plots (a) and (b) have the same scale, the largest circle corresponding to 1912 events. The largest circle in plot (c) corresponds to 379 events. The lines indicate the coplanarity cut described in the text.

Fig. 7  The histogram shows the distribution of $|\cos \theta_K^*|$ for the data sample of coplanar $V'$s. The dashed line corresponds to Monte Carlo (MC2) generated $K^0_S$'s and the full line to the sum of Monte Carlo generated $K^0_S$'s and $\Lambda$'s, the proportions of which are explained in the text.

Fig. 8  Curves showing the geometrical efficiency, $\varepsilon_G$, for $K^\pm$ and $K^0_S$, after applying all cuts, plotted as a function of
$p_T$ (a), rapidity (b) and number of lifetimes (c).

**Fig. 9** Distribution of the proper time spent inside the fiducial volume for the observed $K^0_S$'s. The line has the expected slope of 1.

**Fig. 10** Fully corrected proper lifetime distribution for the $K^0_S$ sample. The line has the expected slope of 1.

**Fig. 11** Distributions of the average opening angle for Monte Carlo (MC2) generated hadronic threeprong interactions in the streamer chamber gas (the dashed histograms) and Monte Carlo (MC2) generated $K_{R3}$ decays (the solid line histogram) in the regions $|\eta|<1$ (a), $1<|\eta|<2$ (b) and $|\eta|>2$ (c). The dashed lines indicate the adopted cuts in the three regions.

**Fig. 12** Inclusive $p_T$–distribution for $(K^+ + K^-)/2$ and $K^0_S$ in the region $|y|\leq 2.5$.

**Fig. 13** Inclusive $p_T$–distributions for $(K^+ + K^-)/2$ and $K^0_S$ in the regions $|y|<0.8$ (a), $0.8\leq |y|<1.6$ (b), $1.6\leq |y|\leq 2.5$ (c) and $2.5<|y|\leq 3.5$ (d). The curves in (a) to (d) have all the same shape given by the fit to the inclusive $K$ data in $|y|\leq 2.5$, but they are normalized to each set of data.

**Fig. 14** The invariant cross-section plotted as a function of $p_T$ for $(K^+ + K^-)/2$ and $K^0_S$ measured in this experiment in the range $|y|\leq 2.5$ (the neutral kaons are rescaled from the region $|y|\leq 3.5$) and for $(K^+ + K^-)/2$ measured by the UA2 experiment in the range $|\eta|<0.7$ [52, 59].

**Fig. 15** Inclusive $p_T$–distribution for $(K^+ + K^-)/2$ and $K^0_S$ in the region $|y|\leq 2.5$ (the neutral kaons are rescaled from the region $|y|\leq 3.5$). The lines are fits described in the text.

**Fig. 16** The invariant cross-section plotted as a function of $p_T$. The circles represent kaon data measured in this experiment and
the curve through them is a fit described in the text.

(K⁺+K⁻)/2 data from ISR at √s=53 GeV [25] are
represented by a fit to the same shape. The UA1 inclusive
charged hadron data are represented by the fit in ref. [47].

Fig. 17 (a) The dependence of <p_T> on c.m. energy for kaon data. Data below
540 GeV are from references [5-29]. The open triangle at 540
GeV is an estimate of <p_T> from a fit described in the text
to UA2 data [52].
(b) The dependence of <p_T> on c.m. energy for pions,
kaons and protons. Data below 540 GeV are from ref. [24] (the
error in each point is assumed to be 5%). At 540 GeV the pion,
kaon (other than UA5) and proton points are estimated from fits,
described in the text, to UA2 data [52].

Fig. 18 Inclusive p_T distributions for kaons in three bands of observed
charged multiplicities in the region |η|<3.5, n_ch≤18 (a),
19≤n_ch≤38 (b) and n_ch≥39 (c). The curves are
results of fits to the combined forms (1) and (2) (table 4b).

Fig. 19 (a) <p_T> for our K data and UA1 data [47] on charged hadrons
plotted as a function of charged particle rapidity density.
We have estimated the rapidity density as the observed
number of charged particles per unit of pseudorapidity in
the region |η|<3.5. The charged particle data from
ref. [47] are measured in the region |y|<2.5.
(b) <p_T> for our K data plotted versus pseudorapidity
density in the interval |η|<3.5 and in the intervals
Δη=1 and Δη=2 centered on the kaon pseudorapidity.
One should note that the 3 sets of points are correlated.

Fig. 20 Inclusive rapidity (a) and pseudorapidity (b) distributions for kaons.
The dashed lines represent the UA5 charged particle
pseudorapidity distribution rescaled by the K₀/S/charged
ratio of 0.04.
(c) Rapidity distributions for kaons in bands of observed
charged multiplicity in the region $|\eta| \leq 3.5$.

Fig. 21 The c.m. energy dependence of the central rapidity density for inclusive $K^0_S$ data. Also plotted is our non single-diffractive measurement. The data points other than UA5 are estimated from diagrams in references [5-29]. The line is a fit described in the text.

Fig. 22 The c.m. energy dependence of the inclusive $K^0_S$ yield (a) and the inclusive $K^0_S$ cross-section (b). Also plotted is our measurement of the $K^0_S$ yield in non single-diffractive events. Data points other than UA5 are from references [5-42]. The cross-section point covering the range 30.4–62.2 GeV is an average value estimated from ref. [60]. The lines are fits described in the text.

Fig. 23 The c.m. energy dependence of the $K/\pi$ ratio. The data points other than UA5 are estimated from references [5-29, 55, 63].

Fig. 24 The ratio of the invariant cross-sections of kaons to that of pions as a function of $p_T$. At 540 GeV the kaon data are from UA5 and UA2 [52] and the pion data are from UA2 [52]. The curve represents ISR data at $\sqrt{s}=53$ GeV estimated from references [25, 26].
Fig. 4
Fig. 7
Fig. 11
\[ \frac{1}{\sigma_{\text{NSD}}} \frac{d\sigma}{dp_T^2} \text{ (GeV}^2 \text{c}^{-2}) \]

\[ \text{p}_T \text{ (GeV/c)} \]

Fig. 12
Fig. 13
Fig. 14
$\frac{1}{\sigma_{\text{NSD}}} \frac{d\sigma}{dp_T^2}$ (GeV$^2$/c$^2$)

$\circ (K^+ + K)/2$

$\bullet K_S^0$

$p_T$ (GeV/c)

Fig. 15
Figure 17
$\frac{1}{\sigma_{\text{NSD}}} \frac{d\sigma}{dp_T^2}$ (GeV$^2$/c$^2$)

- $o(K^+ + K^-)/2$
- $\bullet K^0_s$

$n_{\text{ch}}$ in $|\eta| \leq 3.5$

- a) $0 - 18$
- b) $19 - 38$
- c) $\geq 39$

Fig. 18
Fig. 24