Performance of the first prototype of the CALICE scintillator strip electromagnetic calorimeter


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A future high energy lepton collider [1,2], running up to TeV-scale energies, will play a crucial role in unravelling the nature of the Higgs sector and potential physics beyond the Standard Model (SM), as well as providing high precision measurements of SM processes involving W, Z bosons, and the top quark. Since these latter particles will decay largely into multi-jet final states, precise jet energy measurement is a critical issue. A jet energy resolution of 3% over a wide range of jet energies, significantly better than what has been achieved in past and present collider detectors, will allow hadronic decays of W and Z bosons to be effectively distinguished. Event reconstruction by Particle Flow Algorithms (PFA) [3,4] has the potential to achieve this level of jet energy resolution. A number of detector designs, optimised for the use of PFA, are being developed [5,6]. These designs require calorimeters of very fine granularity, which allow the identification of single particles inside jets within the calorimeter, an essential requirement for PFA. The electromagnetic (EM) calorimeter (ECAL) for such an approach requires a lateral granularity of $5 \times 10^{-16}$ mm$^2$ [7], typically giving $10^7$–$10^8$ readout channels. The single particle energy resolution of the calorimeters is less critical in the PFA approach: an ECAL energy resolution of $15\% / \sqrt{E (\text{GeV})}$ gives a rather small contribution to the jet energy resolution [4]. The large number of channels in such a detector requires a design with rather simple and robust construction methods to enable the detector to be built within reasonable time and manpower resources.

The CALICE scintillator strip-based ECAL (ScECAL) achieves the required granularity with a scintillator strip structure. Each strip is individually read out by a Multi Pixel Photon Counter (MPPC), a silicon photon detector produced by Hamamatsu Photonics K.K. [8]. Although plastic scintillators have been widely used in calorimeters, this is the first time that a highly granular...
calorimeter has been made using scintillator strips. Such an ECAL has a smaller cost than alternative technologies using silicon sensors (e.g. [9]). The MPPC has promising properties for the ScECAL: a small size (active area of 1 × 1 mm² in a package of 4.2 × 3.2 × 1.3 mm³), excellent photon counting ability, low cost and low operation voltage (~80 V), with disadvantages of temperature-dependent gain, saturation at high light levels, and a relatively high dark noise rate. The use of tungsten absorber material minimises the Molière radius of the calorimeter, an important aspect for the effective separation of particle showers required by PFA reconstruction. The chosen strip geometry allows a reduction in the number of readout channels, while maintaining an effective granularity given by the strip width, by the use of appropriate reconstruction algorithms. One such algorithm, known as the Strip Splitting Algorithm [10], has been developed and demonstrated to perform well in jets expected at ILC.

A first ScECAL prototype consisting of 468 channels was constructed and then tested in February and March 2007 using positron beams provided by the DESY-II electron synchrotron [11]. The aim of this experiment was to demonstrate the feasibility of a scintillator strip ECAL with MPPC readout for a future detector, with sufficiently good energy resolution for PFA-based jet energy reconstruction. Large-scale tests of Hamamatsu MPPCs in a real detector had not yet been performed before the present tests.

In this paper we present an analysis of the energy resolution and linearity of the first ScECAL prototype, using data collected with 1–6 GeV/c positron beams. In Section 2, the ScECAL prototype is described. Section 3 presents the measurement and correction of the non-linearity of the MPPC response, and in Section 4 we describe the instrumentation on the DESY beam line and present the data analysis and its results. A Monte Carlo simulation of the prototype is presented in Section 5. The results are discussed and summarised in Section 6.

2. ScECAL prototype

The ScECAL prototype is shown in Fig. 1. It consisted of 26 pairs of 3 mm thick scintillator and 3.5 mm thick absorber layers, placed in an acrylic support structure. The absorber material was composed of 82% tungsten, 13% cobalt and about 5% carbon, with an estimated radiation length of 5.3 mm. The effective Molière radius of the prototype was 22 mm.

Each scintillator layer consisted of two 45 × 90 mm² “mega-strip” structures consisting of nine 45 × 10 mm² strips. Compared to a design based on individual strips, a mega-strip design allows simpler alignment and construction techniques to be used when producing a large-scale detector with tens of millions of channels; on the other hand it has the disadvantage of optical cross-talk between strips, which complicates the interpretation of collected data. The mega-strips were produced by machining holes and grooves in a 3 mm-thick Kuraray SCSN38 plastic scintillator plate, as shown in Fig. 2. White polyethylene terephthalate (PET) film (thickness ~ 130 μm) was placed (not glued) into the grooves to optically isolate adjacent strips. Test bench studies measured an optical cross-talk between strips of around 10%. Within each layer, two mega-strips were placed side-by-side separated by a strip of the same PET film. The two sides of each layer were covered first by a sheet of 3 M radiant mirror reflector film to increase the amount of light collected by the MPPCs, and then a black vinyl sheet to block external light. Two types of detection layers were produced: “type-F (ibre)” with a 1 mm diameter Kuraray Y-11 wavelength shifting optical fibre (WLSF) running along the length of the strip, and “type-D (irect)” without the WLSF or its associated hole. The WLSF was held in place by its natural curvature within the straight hole, without the use of any glue. The presence of the WLSF improves the response uniformity along the strip length (from a non-uniformity of around 30% for type-D to 15% for type-F), but increases the complexity of scintillator strip manufacture and assembly.

Each mega-strip was read out by nine, 1600 pixel MPPCs soldered onto a custom-made flat readout cable and mounted in holes at the end of each strip. The alignment of the strips to the MPPCs was controlled at the level of ± 100 μm. To simplify the construction procedure, no special optical coupling (glue or grease) was used between the fibre and MPPC. The distribution of the MPPCs’ break-down voltage had a mean of around 74 V and a variation (RMS) of around 0.5%. The variation of the MPPC pixel capacitance was around 5%. A uniform operating over-voltage (difference between the operation and break-down voltage) could therefore be used within each module without introducing large gain fluctuations.

Two 13-layer modules were constructed, each using a single mega-strip type. These two modules were tested in two configurations: in the “F–D configuration”, the type-F module was placed directly upstream of the type-D module, while in the “D–F configuration” the type-D module was placed directly upstream of the type-F module, with the type-D module placed downstream of the type-F module.
configuration”, their order was reversed. Since most of the EM shower energy (88–75% for 1–6 GeV/c electrons) is contained in the first half of the ScECAL prototype, the characteristics of each configuration were dominated by the upstream module. Scintillator layers were placed in two alternating orientations, with horizontally and vertically aligned strips, giving an effective granularity of 10 × 10 mm². The total active volume was about 90 × 90 × 200 mm³, with a thickness of around 17 radiation lengths, and was read out by 468 MPPCs. After assembly, five channels were found not to provide signals, probably due to problems with signal line connections. Since these correspond to only around 1% of all channels, and were located mostly at the edge of the detector, their effect on the overall calorimeter performance is expected to be negligible.

Signals from the MPPCs were read by the front-end (FE) electronics developed for the CALICE analogue hadron calorimeter (AHCAL) prototype [12], consisting of the pre-amplifier, shaper and sample-and-hold circuit within the ILC-SiPM ASIC [13], followed by a 16 bit ADC in the CALICE readout cards. The digitised data from the ADCs were transmitted to and further processed by the CALICE data acquisition system. The FE also provided an adjustable bias voltage to the MPPCs.

Two gain modes of the CALICE FE were used: a high-gain mode (with a gain of ~90 mV/pC) giving sufficient sensitivity to measure single photo-electron signals but a small dynamic range (linear up to around 11.5 pC), and a low-gain mode (~8 mV/pC) with lower sensitivity but a sufficiently large dynamic range (linear up to 190 pC) to measure large calorimeter signals [14]. All beam data were collected in the low-gain mode, while the high-gain mode was used to make calibration measurements using MPPC single pixel signals, as described in Section 3.

The applied MPPC over-voltage was chosen to give a large enough gain to clearly resolve single photon peaks when using the high gain readout mode. While satisfying this requirement, essential for the gain calibration, as low as possible an over-voltage is preferred to maximise the dynamic range when running in low-gain mode with electron showers, and to minimise the MPPC inter-pixel cross-talk and dark noise rate. Neither of these undesirable MPPC features had a significant adverse effect on this prototype’s performance. An over-voltage of 2.9 V (3.2 V) was applied to MPPCs in type-F (type-D) layers. The higher over-voltage used in type-D results in an improved MPPC light detection efficiency, partially compensating for the lower scintillation light collection efficiency of this strip type.

The detector was equipped with an LED calibration system used to perform in situ measurements of the MPPC gain. Each layer was equipped with one blue SMD LED (package size 1.6 × 0.8 × 0.4 mm², from the SEIWA electric company), connected via a 0.3 mm-thick flexible flat cable. The LED was placed just off the centre of one of the two mega-strips, over the boundary between two strips. The light was transmitted to the scintillator by a small hole in the black vinyl sheet and reflector film, and propagated to adjacent strips due to the non-perfect optical isolation between strips. Around 25% of strips could be calibrated using this system.

3. MPPC saturation correction

The MPPC response is intrinsically non-linear due to its finite number of pixels, which leads to a saturation of its response at high light levels. If an input light pulse is shorter than the MPPC recovery time (measured to be ~4 ns for the MPPCs used in this experiment), the MPPC response can be parameterised by

\[
N_{\text{fired}}(N_{\text{p.e.}}) = N_{\text{pix}}(1 - e^{-N_{\text{p.e.}}/N_{\text{pix}}}),
\]

where \(N_{\text{fired}}\) denotes the number of fired pixels, \(N_{\text{pix}}\) the total number of MPPC pixels, and \(N_{\text{p.e.}}\) the number of photo-electrons created (the product of the number of incoming photons and the MPPC photon detection efficiency). This function is approximately linear for \(N_{\text{p.e.}} < N_{\text{pix}}\), however for larger signals the MPPC output begins to saturate, with a maximum response of \(N_{\text{fired}} = N_{\text{pix}}\) as the number of photo-electrons approaches infinity. The MPPCs used in this experiment have \(N_{\text{pix}} = 1600\).

If the input light pulse is longer than the typical MPPC recovery time, the effective dynamic range is increased due to the possibility of a single pixel firing several times within the same light pulse. This effect occurs particularly in type-F strips due to the relatively slow decay time of the WLSF (measured to be ~8 ns). The decay time of the scintillator itself was measured to be ~2 ns, significantly shorter than the MPPC recovery time, so type-D strips are not expected to show a strong enhancement of the dynamic range. To take this enhancement into account, we replace \(N_{\text{pix}}\) with an effective number of pixels \(N_{\text{pix}}^{\text{eff}}\) in the MPPC response function (1), and measure this effective pixel number in both strip types.

In the following we discuss the procedure used to correct for this saturation effect: measurement of the single pixel signal, the MPPC response curve, and the formulation of the saturation correction.

3.1. Single pixel signal

The signal \(d\) produced by a single fired pixel is related to the MPPC gain \(G\) by \(d = k \cdot q = k \cdot G \cdot e\), where \(k\) is the conversion factor from signal charge to ADC counts. It was measured (in terms of ADC counts) in the 25% of strips accessible to the LED calibration system. Using a low power LED signal, and with the FE electronics in high-gain mode, characteristic signal distributions were observed, consisting of a pedestal and a few fired-pixel peaks. An example is shown in Fig. 3 (left). These spectra were fitted by a function of the form

\[
f(x) = \sum_{i=0}^{3} A_i e^{-\alpha_i - (x - d - \mu_i)^2/2\sigma_i^2},
\]
in which the Gaussian with index \( i \) corresponds to the \( i \)th fired-pixel peak. The parameter \( \mu_0 \) is the central value of the first, zero fired pixel peak, which corresponds to the pedestal. The distance between peak pixels, \( d \), corresponds to the signal due to a single fired pixel. It is taken to be constant, assuming linear MPPC response in this low-signal region. \( A_i \) and \( \sigma \) are, respectively, the normalisations and width of the Gaussian peaks. The width of each peak is dominated by electronics noise rather than variations in pixel gain, so a common width was assumed for all peaks. \( A_i, d, \mu_0 \) and \( \sigma \) were treated as free parameters in the fit. The result of such a fit is also shown in Fig. 3 (left).

Fig. 3 (right) shows the distribution of the single pixel signals measured in the \( \sim 25\% \) of accessible channels in the type-F module using an over-voltage \( \Delta V \) of 2.9 V. A second measurement of a similar number of MPPCs was made at an over-voltage of 3.7 V. The single pixel signal at \( \Delta V = 3.2 \) V, as used in the type-D module, was taken to be an interpolation between these two measurements, assuming a linear dependence of the single pixel signal on the over-voltage. The averages and variations (RMS) of the single pixel signal distributions at the two chosen over-voltages were determined to be

\[
\begin{align*}
  d_{\text{high-gain}}^{\text{type-F}} &= 144.9 \pm 6.4 \text{ (RMS) ADC counts at } \Delta V^{\text{type-F}} = 2.9 \text{ V} \\
  d_{\text{high-gain}}^{\text{type-D}} &= 151.6 \pm 8.3 \text{ (RMS) ADC counts at } \Delta V^{\text{type-D}} = 3.2 \text{ V}.
\end{align*}
\]

To apply the single pixel signals measured in high gain mode to the test beam data collected in low gain mode, the single pixel signal must be translated from high to low gain mode using the ratio of the two gains. This gain ratio \( R_{\text{high/low}} \) was measured by comparing the MPPC signals produced by a medium-strength LED signal of around 150 photo-electrons using both high and low gain modes. This ratio was measured in 30 channels, shown in Fig. 4, yielding a mean value and RMS of

\[
R_{\text{high/low}} = \frac{\langle \text{ADC}_{\text{high-gain}} \rangle}{\langle \text{ADC}_{\text{low-gain}} \rangle} = 10.08 \pm 0.95 \text{ (RMS)}.
\]

This average gain ratio was applied to both module types to calculate the low gain single pixel signals shown in Table 1. The uncertainty on \( d_{\text{low-gain}} \) takes into account the variation of the measurements of \( d_{\text{high-gain}} \) and of the gain ratio.

3.2. MPPC response curve

The response of the scintillator strip – MPPC system was measured using the dedicated apparatus shown in Fig. 5. An ultraviolet LED was used to inject a light pulse with a length of a few ns into the centre of a scintillator strip. The generated scintillation light was measured at both ends of the strip, at one end by a photomultiplier tube (PMT) from Hamamatsu Photonics and at the other by a MPPC of the same type as used in the prototype. The scintillator strip had dimensions of \( 45 \times 10 \times 3 \) mm\(^2\), and was made of the same material as the megastrips used in the prototype. Two types of strips were tested, with and without a WLSF. The signals from the PMT and MPPC were read out using the CALICE FE electronics in low-gain mode. The signal from the PMT, which does not suffer from saturation at high light levels, is proportional to the light produced in the scintillator, and therefore also to the light input to the MPPC. The comparison of the PMT and MPPC responses at different light intensities allows the extraction of the MPPC response curve.

The MPPC signal (in ADC counts) was converted to the number of fired pixels \( N_{\text{fired}} \) using the single pixel signal \( d_{\text{low-gain}} \) obtained as described in Section 3.1:

\[
N_{\text{fired}} = \text{ADC}_{\text{MPPC}} / d_{\text{low-gain}}.
\]

The number of effective pixels \( N_{\text{eff}}^{\text{pix}} \) was then obtained by measuring the dependence of the number of fired MPPC pixels on the PMT signal. To extract the number of pixels \( N_{\text{eff}}^{\text{pix}} \), this dependence was fitted by a function of the form

\[
N_{\text{fired}} = N_{\text{eff}}^{\text{pix}} (1 - e^{-p \text{ADC}_{\text{PMT}} / N_{\text{eff}}^{\text{pix}}}),
\]

where \( \text{ADC}_{\text{PMT}} \) is the photomultiplier response (in ADC counts). The multiplicative factor \( p \), calculated separately for each measured response curve, is used to convert the PMT signal in ADC counts to the number of photo-electrons, compensating for the different gains and efficiencies of the two devices.
which was then converted back to a corrected ADC signal. The type-F strip shows a larger enhancement of the MPPC dynamic range. The average of the saturation correction, the imperfect knowledge of the MPPC response curves when using the two types of scintillator strips at different MPPC over-voltages $\Delta V$. The dashed line shows a linear response. Typical effective pixel numbers for the two types are given in Table 1.

Fig. 5 shows the response curves of the two scintillator types at different bias voltages. The type-F strip shows a larger enhancement of $N_{\text{pix}}^\text{eff}$ than the type-D strip, due to the slow decay time of the WLSF emission. No strong dependence on the applied bias voltage was observed with either scintillator type. This is expected, since only the time structure of the input light determines the enhancement of the MPPC dynamic range. The average of $N_{\text{pix}}^\text{eff}$ values measured at different bias voltages was used in the saturation correction. These averages for the two strip types are shown in Table 1. The statistical uncertainty on $N_{\text{pix}}^\text{eff}$ estimated by the fit procedure is at most a few pixels in all cases. The fact that only a rather small enhancement is observed in the type-D strip demonstrates that the length of the input light pulse is somewhat shorter than the MPPC recovery time, and that the present results can be applied to test beam data, in which the energy deposition is essentially instantaneous.

3.3. Saturation correction

The effects of MPPC saturation in beam data were corrected using the results outlined above. The signal from each MPPC, $\text{ADC}_{\text{raw}}$, was converted to the corresponding number of fired pixels by using the appropriate single pixel signal (d): $N_{\text{fired}} = \text{ADC}_{\text{raw}}/d_{\text{low-gain}}$. The saturation-corrected number of photo-electrons $N_{\text{p.e.}}$ was estimated as

$$N_{\text{p.e.}} = -N_{\text{pix}}^\text{eff} \ln \left( 1 - \frac{N_{\text{fired}}}{N_{\text{pix}}^\text{eff}} \right),$$

which was then converted back to a corrected ADC signal

$$\text{ADC}_{\text{corrected}} = N_{\text{p.e.}} \cdot d_{\text{low-gain}}.$$  

3.4. Estimation of systematic effects

There are two possible sources of uncertainty in the application of the saturation correction, the imperfect knowledge of $d_{\text{low-gain}}$ and $N_{\text{pix}}^\text{eff}$. Effects due to $d_{\text{low-gain}}$ depend only on the MPPC and FE electronics, and are therefore expected to have similar behaviour in different detector configurations and regions. A single uncertainty was therefore used for these effects. Measurements of $d_{\text{high-gain}}$ were made in around 25% of all channels, and the gain ratio was measured in thirty ($\sim 6\%$) channels. The means of these two sets of measurements were used to calculate an average value for $d_{\text{low-gain}}$ in the two strip types. The uncertainty on these average values (reflected in Table 1) is dominated by the $\sim 10\%$ variation in the measurements of $R_{\text{high-low}}$. The uncertainty was estimated by comparing the results obtained when varying $d_{\text{low-gain}}$ above and below its nominal value by its uncertainty with the results obtained when using the nominal value.

Effects due to $N_{\text{pix}}^\text{eff}$ are expected to depend also on the strip type, since the two types produce a different number of photo-electrons per MIP, giving rise to different saturation characteristics as a function of MIPs. Different uncertainties were therefore used for the two detector configurations. The nominal value of $N_{\text{pix}}^\text{eff}$ was taken from the measurement of only a single strip of each type. The relative uncertainty on the fitted $N_{\text{pix}}^\text{eff}$ is small $\lesssim 10^{-3}$. Although the MPPCs used in this experiment were measured to have rather similar properties, some residual variations can be expected, due to non-uniform properties of the MPPC, scintillator strip, WLSF, and the couplings between them. The scale of the effect of these variations on $N_{\text{pix}}^\text{eff}$ is not very precisely known. The length of the light pulse used to measure $N_{\text{pix}}^\text{eff}$ is also not very well known, which can affect the precision on the effective pixel number. To estimate the uncertainty due to these effects, a comparison was made of the detector performances estimated when assuming different values of $N_{\text{pix}}^\text{eff}$, uniformly applied to all detector channels. $N_{\text{pix}}^\text{eff} = 1600, 1077$, and 2073 were considered, corresponding respectively to the physical number of pixels, and the measured effective pixel numbers for type-D and type-F strips. Half of the larger difference seen when comparing $N_{\text{pix}}^\text{eff} = 1600$ and 2073, and $N_{\text{pix}}^\text{eff} = 1600$ and 1077, was taken as a conservative estimate of the systematic uncertainty due to imprecise estimation of the effective pixel number.

4. Test beam at DESY

This test beam experiment was performed at the DESY-II electron synchrontron (at DESY, Hamburg, Germany) using positron beams with momenta of 1, 2, 3, 4, 5, and 6 GeV/c. A sketch of the beam line instrumentation is shown in Fig. 6. The trigger (T1-3) and veto (V1, 2) counters are scintillator detectors of size $3 \times 3$ cm$^2$ and 20 × 20 cm$^2$, respectively. The veto counters have a $2 \times 2$ cm$^2$ hole at their centre. These counters were each read out by two photomultipliers (PMT). Two trigger and one veto counter were placed upstream of the prototype, and one trigger and one veto counter were placed downstream of the ScECAL. The beam line was also instrumented with four pairs of drift chambers (DC1-4). Each DC has an active area of $\sim 72 \times 72$ mm$^2$ and measures either the x or y coordinate. Each pair of DCS measures both the x and y position of beam particles. The ScECAL was placed on a movable stage, allowing it to be moved with 0.1 mm precision in the plane normal to the beam. The readout electronics were housed in a crate placed next to the prototype. The temperature was monitored by a number of temperature sensors placed on and around the detector.

During beam data taking, the acquisition was triggered by a coincidence of signals from one PMT of trigger counter T1 and one PMT of T2. The pedestal distribution of all ScECAL channels was
monitored regularly during data taking by recording 1000 randomly triggered events every 10000 beam events. In each readout channel, the mean signal recorded in these randomly triggered events was subtracted from the following set of beam trigger events.

4.1. Calibration

The absorber plates were removed from the detector to collect data used for calibration. Calibration runs were performed several times during the test beam period, using a 3 GeV/c positron beam. The detector was moved during calibration runs to ensure that all strips were exposed to a sufficient number of particles. An event pre-selection required that the signals from all trigger and veto counters, both up- and down-stream of the ScECAL, were consistent with a single, non-showering particle passing through the ScECAL.

Each strip was then individually calibrated with data for which the drift chamber track reconstruction showed that a particle passed through the strip. Events satisfying this requirement are in the following referred to as DC-selected. An additional event selection was applied to these events, using the data in other ECAL layers, as illustrated in Fig. 7. The signals on the two preceding and two succeeding ECAL layers with the same orientation as the target strip layer were considered. If such a layer was not available, the requirement was ignored. Within these layers, the signals on the “same-position” strips (the strips in the same x, y position as the target strip) were required to measure a signal at least 80 ADC counts above pedestal, and the strips in other positions on these same layers were required to have a signal no larger than 80 ADC counts above pedestal. Events satisfying these criteria are referred to as ECAL-selected.

The signal distributions of a representative type-F channel after these two event selections are shown in Fig. 8. The mean values of the final ECAL-selected distributions were used as the channel-by-channel calibration constants translating the signal in ADC counts to Minimum Ionizing Particle equivalent units (MIPs). The mean MIP signals measured in all strips are plotted in Fig. 8. Two distributions are seen, due to the two scintillator types. Type-F strips give, on average, a larger signal than type-D (this depends on differences in light collection efficiency and MPPC gain between the two types), and also a significantly larger dispersion (23% for type-F, compared to 11% for type-D). The dispersion for type-F is consistent with our expectation of effects due to the ±100 μm variations in the relative positioning of the WLSF and MPPC, in particular variations in the distance between the end of the WLSF and the MPPC package.

4.1.1. Estimation of systematic effects

A pseudo-experiment method was used to estimate the uncertainties arising from the statistical uncertainty of the measured MIP calibration constants. In each pseudo-experiment the calibration constant of each channel was randomly varied according to a Gaussian distribution whose standard deviation was the measured statistical uncertainty of the channel's calibration. The variation seen within an ensemble of one hundred pseudo-experiments was taken as the systematic uncertainty due to this effect.

4.2. Temperature dependence

Since the MPPC gain G depends strongly on the temperature T (δG/δT = −2%/°C at 20 °C [8]), correction of this effect is essential. Calibration runs were taken several times during the test beam period, covering the temperature range encountered during EM shower data taking. The mean MIP response was measured individually in each calibration run, and used to extract its dependence on the temperature. Fig. 9 shows this variation for a representative channel. The dependence of each channel's response on temperature T = c(T) was fitted with a linear function

\[ c(T) = c(T_0) \cdot (1 + f_{\text{temp}} \cdot (T - T_0)) \]

where the reference temperature T_0 was chosen to be 20 °C. The distributions of the fitted temperature coefficients, f_{\text{temp}}, for the two strip types are shown in Fig. 9. The MIP response decreases with increasing temperature in a similar way for type-F and type-D strips, as expected. In the analysis of EM shower events described in Section 4.4, the response of each strip was calibrated using a temperature-dependent calibration function determined by these fitted functions.

To demonstrate the efficacy of this correction, in Fig. 10 we show the reconstructed energy distributions of central EM shower events collected by the F-D configuration detector at a beam momentum of 4 GeV/c. The data were collected during two data-taking periods, each of around 20 min, separated by around 14 h. The mean temperatures of the prototype during the two runs were 20.3 and 21.5 °C. The application of the temperature correction reduces the relative difference between the mean energy response in the two data-taking periods from \( (4.51 \pm 0.06)\% \) to \( (0.17 \pm 0.06)\% \).

4.2.1. Estimation of systematic effects

A pseudo-experiment method was used to estimate the uncertainties arising from the statistical uncertainty of the measured temperature dependence. In each pseudo-experiment the temperature correction factor f_{\text{temp}} of each channel was randomly varied according to a Gaussian distribution whose standard deviation was the measured statistical uncertainty of f_{\text{temp}}. The variation seen within an ensemble of one hundred such pseudo-experiments was taken as the systematic uncertainty due to this effect.
4.3. Optical cross-talk

Adjacent strips in the same mega-strip were not perfectly optically isolated by the PET film inserted into the pairs of grooves (shown in Fig. 2). The resulting optical cross-talk was measured using the calibration data by comparing the signals in a given strip when the positron passed through the strip itself, an adjacent strip, or a more distant strip in the same mega-strip. It was measured separately across each strip boundary. Fig. 11 shows an example of these signals in a particular strip, and the distribution of the cross-talk measured between all pairs of strips within the same mega-strip. The cross-talk between neighbouring strips within a given layer can be expressed as 

\[ \{ \text{MPPC signal} \} \times \{ \text{cross-talk} \} = \{ \text{measured strip energy} \} \]

where the cross-talk term is a matrix 

\[ M_{\text{calibration}} \] 

which transforms the light produced in the strips into the signal measured in each strip. The cross-talk contribution from the signal measured in each strip. The cross-talk correction procedure was developed to subtract the estimated cross-talk contribution from the signal measured in each strip. The cross-talk between strips is not uniform in the detector, energy deposited in strips with larger cross-talk would get a larger weight in the sum. This is in effect a miscalibration, and would introduce an additional constant term into the energy resolution. A cross-talk correction procedure was developed to subtract the estimated cross-talk contribution from the signal measured in each strip. The cross-talk between strips within a given layer can be expressed as 

\[ \{ \text{MPPC signal} \} \times \{ \text{cross-talk} \} = \{ \text{measured strip energy} \} \]

Since the MIP calibration was defined without accounting for cross-talk, a simple sum over measured strip energies would give an overestimate of the deposited energy in terms of MIPs. If the cross-talk between strips is not uniform in the detector, energy deposited in strips with larger cross-talk would get a larger weight in the sum. This is in effect a miscalibration, and would introduce an additional constant term into the energy resolution. A cross-talk correction procedure was developed to subtract the estimated cross-talk contribution from the signal measured in each strip. The cross-talk between strips within a given layer can be expressed as 

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\[ \{ \text{MPPC signal} \} \times \{ \text{cross-talk} \} = \{ \text{measured strip energy} \} \]
4.4. Energy linearity and resolution

EM shower data, taken with absorber plates installed between the scintillator layers, were collected using beam momenta of 1–6 GeV/c. Events were pre-selected by requiring that the signals in the upstream trigger and veto counters were consistent with the passage of a single positron: the signals in the two trigger counters were required to be consistent with a single MIP signal, while in the veto counter a pedestal-only signal was required. The corrections described in previous sections were then applied to the data: correction of the MPPC response non-linearity, conversion to MIP equivalent units using the measured temperature-dependent calibration constants, and the correction of optical cross-talk. The measured event energy, in MIPs, was calculated as the sum of all strip energies.

The detector response was measured in the two configurations and in two detector regions. The “central region”, selected by requiring that the beam axis was centred within 1.5 mm of the detector centre $x,y=0$, is the least affected by transverse shower leakage, however most energy is deposited near the ends of the scintillator strips (near the boundary between megastrips), making it the most susceptible to effects of any non-uniformity of the response along the strip length. In the “uniform region”, events in which the DCs reconstruct an impact on the front face of the ECAL within the four $10 \times 10 \text{ mm}^2$ areas centred at $x,y = \pm 22.5 \text{ mm}$, particles pass near the strips’ centres in both layer orientations, minimising the effects of non-uniform strip response.

The distributions of the measured event energy for central events recorded by the F–D configuration at each beam momentum are shown in Fig. 13. Such distributions were made for both regions of both detector configurations, and were fitted with Gaussian functions. The dependence of the mean of the Gaussian on the beam momentum, in the case of the uniform region of the D–F configuration, is shown in the same figure. These measurements were then fitted by a linear function. The $\chi^2$ of the fit, in which systematic uncertainties were not considered, is rather high. If, as an illustrative exercise, an uncertainty of 0.22% is assigned to the average beam momentum, the $\chi^2$ per degree of freedom becomes exactly unity, and the constant and slope terms of the function change to $3.8 \pm 0.3 \text{ MIP}$ and $95.7 \pm 0.2 \text{ MIP/(GeV/c)}$, respectively.

The deviations from linear behaviour $(E – E_{\text{fit}})/E_{\text{fit}}$, where $E_{\text{fit}}$ is the prediction of the linearity fit, are shown in Fig. 14. Deviations from linearity are within 1% for all measured energies, configurations and detector regions.

The relative width of the Gaussian (its width $\sigma_E$ divided by its mean $E$) was used to estimate the energy resolution. Fig. 15 shows this relative width as a function of the beam momentum in the two regions of the two detector configurations. These points were fitted by a function of the form

$$\frac{\sigma_E}{E} = \sqrt{\frac{\sigma_{\text{stochastic}}^2}{E_{\text{beam}}^2} + \sigma_{\text{constant}}^2},$$

where $\sigma_{\text{stochastic}}$ and $\sigma_{\text{constant}}$ are the stochastic and constant terms of the energy resolution, and $E_{\text{beam}}$ is the beam energy in GeV. The results of these fits are shown in the same figure, and are presented in Table 2. When a term describing detector noise was included in the above expression, its fitted value was always consistent with zero.

4.5. Summary of the systematic uncertainties

The approach taken to the systematic uncertainties arising from the MIP calibration, saturation, temperature and cross-talk corrections are described in previous sections. The observed shifts in the stochastic and constant terms of the energy resolution when these procedures were applied were used as systematic uncertainties. Where uniform systematic uncertainties were assumed (for example, in the cross-talk correction), the average of the shifts in different configurations and regions was used. The resulting uncertainties on the stochastic and constant terms of the energy resolution are shown in Table 3.

The systematic uncertainties are dominated by uncertainties in the MPPC saturation correction, from the effective number of pixels which characterises the MPPC response enhancement and the signal corresponding to a single fired pixel. The uncertainty on the effective number of pixels stems from the fact that only a single strip–MPPC unit was tested, necessitating a conservative estimate of the systematic uncertainty. The uncertainty on the single pixel signal is dominated by the small fraction (~6%) of electronics channels in which the ratio between the high and low gain modes was measured.
Any spread in the beam momentum will contribute to the width of the reconstructed energy distributions shown in Fig. 13 (left). If this beam momentum spread is well understood, it can be subtracted from the measured widths to give the intrinsic calorimeter energy resolution. However, the momentum spread of the test beam at DESY is not very well understood at present. An estimated upper limit on the momentum spread is given as 5% [11], but the true spread is likely to be smaller, and may depend on energy. Due to this uncertainty, we have chosen not to subtract a beam momentum spread for the nominal measurement, but assign a systematic uncertainty due to this effect. We estimate this uncertainty by subtracting, in quadrature, 5% from the energy resolution measured at each beam momentum. This has a large effect on the measured energy resolutions, reducing

![CALICE ScECAL F-D config. central](image1.png)

![CALICE ScECAL D-F config. uniform](image2.png)

<table>
<thead>
<tr>
<th>Configuration</th>
<th>Region</th>
<th>Contribution (%)</th>
<th>Statistical</th>
<th>Systematic</th>
</tr>
</thead>
<tbody>
<tr>
<td>F-D</td>
<td>Central</td>
<td>Stochastic</td>
<td>13.2 ± 0.05</td>
<td>± 0.20 ± 0.16</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Constant</td>
<td>3.65 ± 0.05</td>
<td>± 0.47 ± 0.16</td>
</tr>
<tr>
<td>Uniform</td>
<td>Stochastic</td>
<td>13.76 ± 0.07</td>
<td>± 0.21 ± 0.16</td>
<td></td>
</tr>
<tr>
<td></td>
<td>Constant</td>
<td>3.52 ± 0.07</td>
<td>± 0.47 ± 0.16</td>
<td></td>
</tr>
<tr>
<td>D-F</td>
<td>Central</td>
<td>Stochastic</td>
<td>13.43 ± 0.06</td>
<td>± 0.07 ± 0.08</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Constant</td>
<td>4.45 ± 0.04</td>
<td>± 0.22 ± 0.46</td>
</tr>
<tr>
<td>Uniform</td>
<td>Stochastic</td>
<td>13.73 ± 0.08</td>
<td>± 0.07 ± 0.23</td>
<td></td>
</tr>
<tr>
<td></td>
<td>Constant</td>
<td>3.35 ± 0.07</td>
<td>± 0.22 ± 0.52</td>
<td></td>
</tr>
</tbody>
</table>

Norbert Meyners (DESY), personal communication (2013).
The energy response of the model to single positrons in the range 1 to 6 GeV was estimated for a number of different scenarios, to identify impacts of the detector characteristics on the response:

(a) large detector size (no energy leakage), no insensitive MPPC volume, and uniform strip response;
(b) same as (a), but with insensitive MPPC volume;
(c) same as (b), but with same size as prototype;
(d) same as (c), but with non-uniform strip response (F–D configuration);
(e) same as (c), but with non-uniform strip response (D–F configuration).

The energy resolution was simulated in the “central” and “uniform” regions of each of these scenarios. These simulations were used to estimate the contributions to the constant term from the MPPC volume, limited prototype size, and strip non-uniformity, as shown in Table 4. The contribution due to the non-uniformity is the largest in the “central” region, while the energy leakage is the most significant contribution in the “uniform” region.

The predicted and measured energy resolutions in the different regions and configurations are compared in Fig. 16. The stochastic term of the energy resolution measured in data is consistent with the Monte Carlo prediction in all detector configurations and regions. The constant term measured in the uniform region is around 1% larger than the predicted one in both detector configurations, possibly due to the beam momentum spread, which is not accounted for in the simulation. The size of the discrepancy suggests that the true beam momentum spread is significantly smaller than the conservative bound of 5% quoted by the test beam operators. In the central region, the measured constant term is consistently smaller than the simulated one, however this difference is similar in size to the systematic uncertainty due to the scintillator strip attenuation length.

The energy measurement of this calorimeter prototype was measured to be linear to within 1% in the energy range between 1 and 6 GeV. The residual non-linearities do not depend strongly on the detector configuration or the region of the detector (central or uniform).

6. Summary

During this test beam campaign, several hundred MPPCs were successfully operated in a prototype scintillator strip-based ECAL. This demonstrates that such a technique is feasible and represents an important milestone in the development of a ScECAL for future high energy lepton collider. The applied temperature-based corrections to the MPPC response successfully stabilised the prototype’s response.

The energy measurement of this calorimeter prototype was measured to be linear to within 1% in the energy range between 1 and 6 GeV. The residual non-linearities do not depend strongly on the detector configuration or the region of the detector (central or uniform).

The stochastic terms in the various configurations and regions are measured to be between 13 and 14%, sufficient for the use of Particle Flow Algorithms at future lepton collider detectors. The constant term was measured to be between 3 and 4.5%. The energy resolution measured in the F–D configuration (whose performance is dominated by the type-Fibre module), is very similar in the two detector regions. In the D–F configuration, the constant term is significantly larger in the central region. This difference is attributed to the effect of non-uniform response along the strip length, and the effect of the dead volume due to the MPPC package. A simulation study supports these conclusions, and has shown that major contributions to the constant term of the energy resolution are the non-uniformity of the strip response, the limited size of the prototype, and the insensitive volume due to the MPPC package.

the fitted constant term to zero in each case, and also leading to significant reductions of the stochastic terms.

5. Simulation

A GEANT4 simulation of the prototype was developed using the Mokka package [15]. Active scintillator layers were segmented into strips, with an insensitive region corresponding to the MPPC package at one end of each strip. The simulated module was significantly larger than the prototype in both the transverse and longitudinal dimensions, eliminating the effects of energy leakage; to estimate the effect of leakage, only energy deposited within a volume corresponding to the prototype was considered. Type-D (-F) strips were modeled as having a non-uniform response along their length, characterised by an exponential function with an attenuation length of 115 mm (280 mm), the average of several measurements of strip uniformity made using data collected in detailed position scans performed during the beam test. The root mean square variation of the measured attenuation lengths was used to set a systematic uncertainty on the simulated results.

<table>
<thead>
<tr>
<th>Source</th>
<th>Configuration</th>
<th>Region</th>
<th>$\delta_{\text{statistic}}$</th>
<th>$\delta_{\text{constant}}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>MIP calibration</td>
<td>F–D</td>
<td>Central</td>
<td>± 0.01</td>
<td>± 0.02</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Uniform</td>
<td>± 0.02</td>
<td>± 0.02</td>
</tr>
<tr>
<td></td>
<td>D–F</td>
<td>Central</td>
<td>± 0.01</td>
<td>± 0.02</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Uniform</td>
<td>± 0.02</td>
<td>± 0.02</td>
</tr>
<tr>
<td>Temperature correction</td>
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<td>± 0.02</td>
<td>± 0.01</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Uniform</td>
<td>± 0.04</td>
<td>± 0.02</td>
</tr>
<tr>
<td></td>
<td>D–F</td>
<td>Central</td>
<td>± 0.01</td>
<td>± 0.02</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Uniform</td>
<td>± 0.02</td>
<td>± 0.02</td>
</tr>
<tr>
<td>Cross-talk correction</td>
<td>Both</td>
<td>Both</td>
<td>± 0.03</td>
<td>± 0.12</td>
</tr>
<tr>
<td>Single pixel signal</td>
<td>Both</td>
<td>Both</td>
<td>± 0.06</td>
<td>± 0.17</td>
</tr>
<tr>
<td>Effective pixel number</td>
<td>F–D</td>
<td>Both</td>
<td>± 0.19</td>
<td>± 0.42</td>
</tr>
<tr>
<td></td>
<td>D–F</td>
<td>Both</td>
<td>± 0.01</td>
<td>± 0.07</td>
</tr>
<tr>
<td>Total (not including)</td>
<td>F–D</td>
<td>Central</td>
<td>± 0.20</td>
<td>± 0.47</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Uniform</td>
<td>± 0.21</td>
<td>± 0.47</td>
</tr>
<tr>
<td>beam energy spread</td>
<td>D–F</td>
<td>Central</td>
<td>± 0.07</td>
<td>± 0.22</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Uniform</td>
<td>± 0.07</td>
<td>± 0.22</td>
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<tr>
<td>Beam energy spread</td>
<td>F–D</td>
<td>Central</td>
<td>± 0.16</td>
<td>± 0.65</td>
</tr>
<tr>
<td>(assumed to be 5%)</td>
<td></td>
<td>Uniform</td>
<td>± 0.16</td>
<td>± 0.65</td>
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<td></td>
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<tr>
<td></td>
<td></td>
<td>Uniform</td>
<td>± 2.34</td>
<td>± 3.16</td>
</tr>
</tbody>
</table>

Table 3
Summary of the systematic uncertainties on the stochastic and constant terms of the energy resolution measurement. The quoted figures are the absolute uncertainties on the stochastic and constant terms (in %).

Table 4
Contributions to the constant term of the energy resolution in the two detector regions, estimated by Monte Carlo simulations. In the case of the non-uniformity ("non-un") the first uncertainty is statistical, the second due to variations of the strip attenuation length.

<table>
<thead>
<tr>
<th>Configuration</th>
<th>Region</th>
<th>Central (%)</th>
<th>Uniform (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>MPPC volume</td>
<td>2.0 ± 0.2</td>
<td>0.9 ± 0.4</td>
<td></td>
</tr>
<tr>
<td>Leakage</td>
<td>2.1 ± 0.2</td>
<td>1.6 ± 0.2</td>
<td></td>
</tr>
<tr>
<td>Non-un (F–D)</td>
<td>3.3 ± 0.2 ± 0.9</td>
<td>1.4 ± 0.3 ± 0.1</td>
<td></td>
</tr>
<tr>
<td>Non-un (D–F)</td>
<td>4.9 ± 0.1 ± 1.1</td>
<td>1.4 ± 0.3 ± 0.2</td>
<td></td>
</tr>
</tbody>
</table>
The present study has highlighted various aspects of the ScECAL design which must be addressed before building a full detector: improved uniformity of the scintillator strip response, and reduced dead volume due to the MPPC package (to reduce the constant term of the energy resolution); development of an improved LED-based MPPC monitoring system able to monitor the gain of all channels; tests of a prototype with larger volume, to measure the constant term without leakage effects; tests of this larger detector using electron and other particle beams with a larger energy range; and the use of embedded front-end electronics, to realise the high channel density and small number of external cables required for integration into a future collider experiment. The results of tests of a larger ScECAL prototype, which address a number of these issues, will be reported in a later paper.

Acknowledgements

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