ENERGY MEASUREMENT OF ELEMENTARY PARTICLES

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ABSTRACT

We review the techniques used to measure the energy of elementary particles. The methods discussed span more than 20 orders of magnitude in energy, ranging from a small fraction of an electronvolt, where relic remainders of the Big Bang are being looked for, to the $10^{-20}$ eV domain, where the highest-energy cosmic rays can be found. The emphasis is, however, on techniques employed in particle physics for studying collision processes at accelerators in the GeV–TeV range.

(Submitted to Reports on Progress in Physics)
Experimental particle physicists study the fundamental structure of matter with a variety of approaches, which may be subdivided in two classes: accelerator and non-accelerator experiments. Accelerator experiments have the advantage of well-controlled experimental circumstances, non-accelerator experiments offer the possibility of studying processes that are not accessible to the available accelerator technology.

Accurate energy measurements are a prime tool for increasing the knowledge of the constituents of matter, and the forces by which they interact. Three examples may illustrate this. The fundamental nature of the cosmic background radiation emerged when it was realized that the energy spectrum corresponded to that of a black body radiating at a temperature of 3K. On the high-energy side of the scale, the elementary particles are unstable; without exception, the known ones were discovered by a kinematical reconstruction from their decay products, the quality of which is closely linked to the accuracy of the particle energy measurement. And finally, the crucial question whether the neutrino rest mass is different from zero needs an extremely accurate comparison between energy and momentum in order to be answered.

The energy of elementary particles is measured with instruments that are generally called calorimeters. There is a wide variety of them. The principle is simple. Basically, a calorimeter is a block of matter in which the particle to be measured interacts and transforms (part of) its energy into a measurable quantity. The resulting signal may be electrical, optical, thermal or acoustical. It is of course important that the signal be proportional to the energy that one wants to measure, which is not always easy to achieve.

In this review, we will mainly concentrate on the calorimeters that are used in high-energy physics, i.e. on the detectors used for measuring particle energies in the GeV range and above. However, a short description will be given of emerging techniques employed in searching for low-energy fundamental particles, such as neutrinos and hypothetical species.

In high-energy physics, we have seen in the last 15 years a clear trend by which experiments changed from electronic bubble chambers, aiming for a precise measurement of the 4-vectors of all individual reaction products with spectrometric
methods, to configurations with increasing emphasis on calorimetric particle detection. Some major discoveries, e.g. the existence of the intermediate vector bosons $W$ and $Z$, became possible as a result of this development.

The reasons why calorimeters have emerged as the key detectors in almost any experiment in particle physics, can be divided into two classes. Firstly, there are reasons related to the calorimeter properties:

a) Calorimeters are sensitive to both charged and neutral particles.

b) Owing to differences in the characteristic shower patterns, some crucial particle identification is possible.

c) Since calorimetry is based on statistical processes, the measurement accuracy improves with increasing energy, in contrast to what happens for other detectors.

d) The calorimeter dimensions needed to contain showers increase only logarithmically with the energy, so that even at the highest energies envisaged it is possible to work with rather compact instruments (cost!).

e) Calorimeters do not need a magnetic field for energy measurements.

f) They can be segmented to a high degree, which allows accurate measurements of the direction of the incoming particles.

g) They can be fast-response times better than 100 ns are achievable-which is important in a high-rate environment.

h) The energy information can be used to trigger on interesting events with very high selectivity.

Secondly, there are reasons related to the physics to be studied. Here, the emphasis has clearly shifted from track spectroscopy to measuring more global event characteristics, indicative for interesting processes at the constituent level. These characteristics include missing (transverse) energy, total transverse energy, jet production, multijet spectroscopy, etc. Calorimeters are extremely well suited for this purpose.

In this review, we have decided to discuss in considerable detail developments that took place during the last five years and to complement in this way earlier reviews\textsuperscript{[1,2]}. In Section 2 we describe the various processes by which particles lose their energy when traversing dense matter and by which they eventually
get absorbed. We discuss shower-development phenomena, the effects of the electromagnetic and strong interactions, and the consequences of differences between these interactions for the calorimetric energy measurement of electrons and hadrons, respectively.

In Section 3, the performance of calorimeter systems is described. The section starts with a discussion of the so-called compensation mechanism, its relevance for the performance of hadron calorimeters, and the methods to achieve compensation in calorimeters. In a following subsection, the factors that determine and limit the energy resolution of different calorimetric detectors are discussed. The rest of the section describes in some detail the performance of existing and planned devices in terms of energy and position resolution, particle identification, and signal processing. The section is concluded with an overview of the most important calorimetric detectors currently, or about to be, employed.

Section 4 gives conclusions, and an outlook to further developments of this important experimental technique.

2. ABSORPTION MECHANISMS OF PARTICLES

When a particle traverses matter, it will generally interact and lose (a fraction of) its energy in doing so. The medium is excited in this process, or heated up, hence the word calorimeter. The interaction processes that play a role depend on the energy and the nature of the particle. They are the result of the electromagnetic, the strong and, more rarely, the weak forces reigning between the particle and the medium constituents. In this section, we will describe the various mechanisms by which particles may lose their energy and eventually be absorbed.

2.1 ELECTROMAGNETIC ABSORPTION

The best known energy-loss mechanism contributing to the absorption process is the electromagnetic (e.m.) interaction experienced by charged particles that traverse matter. The charged particles ionize the medium, if their energy is at least sufficient for releasing the atomic electrons from the e.m. nuclear field. This process forms also the principle on which many detectors are based, since the liberated electrons may be collected by means of an electric field, and yield an electric signal.
The e.m. interaction may manifest itself, however, in many other ways. Charged particles may excite atoms or molecules without ionizing them. The de-excitation from these metastable states may yield (scintillation) light, which is also fruitfully used as a source of calorimeter signals. Charged particles travelling faster than the speed of light characteristic for the traversed medium lose energy by emitting Čerenkov light. At high energies, knock-on electrons (δ-rays) and bremsstrahlung are produced, and even nuclear reactions induced by the e.m. interaction may occur.

The e.m. field quantum, the photon, is affected by three different processes. First, there is the photoelectric effect, in which the photon transfers all its energy to an atomic electron. In the Compton process, only part of the energy is transferred in this way. At energies larger than twice the electron rest mass, the photon may convert into an electron-positron pair. The relative importance of these three processes depends strongly on the photon energy and the electron density (∼ Z) of the medium.

Except at the lowest energies, the absorption of electrons and photons is a multistep process, in which particle multiplication may occur (shower development). This phenomenon, which leads to the absorption of high-energy particles in relatively small volumes, is extensively discussed in the next subsections. The other particles subject to only the e.m. interaction, the muons, do not show such behaviour up to very high energies (100 GeV). They lose their energy primarily through ionization and δ-rays. These mechanisms account for an energy loss of typically 1 – 2 MeV/g.cm\(^{-2}\) and, therefore, it takes very substantial amounts of material to absorb high-energy muons (1 TeV muons may penetrate several kilometres of the Earth's crust).

2.1.1 The 0 to 10 MeV range

Already at fairly low energies, relatively simple showers may develop. Let us consider as an example the γ's of a few MeV characteristic of nuclear de-excitation. The sequence of processes through which γ's of a particular energy are absorbed may be very different from event to event. An example of such a sequence is given in fig. 1. A 3370 keV γ enters the detector and converts into an electron- positron pair. Both particles get a kinetic energy of 1174 keV (point A), the remaining energy is needed for the mass of the e\(^+\) and e\(^-\). The electron
loses its kinetic energy through ionization of the detector material and so does the positron. When the positron is stopped, it annihilates with an electron, thus releasing the energy $E = M_e^+e^-$ in the form of two $\gamma$'s of 511 keV each (B). These $\gamma$'s undergo Compton scattering (C,D), in which part of the energy is transferred to an electron and part to a new $\gamma$. The electrons lose their energy as described; the $\gamma$'s may undergo either another Compton scattering (F), or photoelectric effect in which their full energy is transferred to an electron (E,G).

In this example, which is only one out of an infinite number of different possibilities, the energy of the original $\gamma$ is absorbed through ionization of the detector medium by one positron and six different electrons. Events for which the whole sequence has taken place inside the sensitive volume of the detector will yield a signal peak at 3370 keV. In small detectors, leakage phenomena may occur (fig. 1). Either one or both 511 keV $\gamma$'s may escape from the detector. This leads to peaks at energies lower by 511 and 1022 keV, respectively. And if they do not escape, some of the tertiary or higher-order $\gamma$'s might, leading to a continuous background.

At these low energies, a modest role may also be played by photonuclear reactions, e.g. $\gamma n$, $\gamma p$ or photo-induced nuclear fission. However, the cross-sections for these processes usually do not exceed 1% of the cross-sections for the processes mentioned before and may therefore, in general, be neglected.

2.1.2 From 10 MeV to 100 GeV

Most of the energy-loss mechanisms relevant to high-energy shower development were already mentioned in the previous subsection: Ionization for electrons and positrons, pair production, Compton scattering, and the photoelectric effect for photons. There is one more, be it crucial mechanism that contributes at higher energies: bremsstrahlung.

In their passage through matter, electrons and positrons may radiate photons as a result of the Coulomb interaction with the nuclear electric field. These photons have an exponentially falling energy spectrum that, in principle, extends to the electron energy, but in general the emitted photon carries only a small fraction of this energy. In this process, the electron itself undergoes a (usually small) change in direction (multiple or Coulomb scattering). The deviation depends on the angle and the energy of the emitted photon, which in turn depend on the
strength of the Coulomb field, i.e. on the Z of the absorber medium.

Bremsstrahlung is by far the principal source of energy loss by electrons and positrons at high energies. As a consequence, high-energy e.m. showers are quite different from the ones discussed in the previous subsection, since an important multiplication of shower particles occurs. A primary GeV-type electron may radiate on its way through the detector thousands of photons. The ones faster than 5-10 MeV will create $e^+e^-$ pairs. The fast electrons and positrons from this process may in turn lose their energy by radiation as well, etc, etc. The result is a shower that may consist of thousands of different particles, electrons, positrons, and photons. The overwhelming majority of these particles is very soft. The average energy of the shower particles is obviously a function of the age of the shower, or the depth inside the detector: the further the shower has developed, the softer the spectrum of its constituents becomes.

The energy-loss mechanisms are governed by the laws of quantum electrodynamics (QED)\(^3\). They primarily depend on the electron density of the medium in which the shower develops. This density is roughly proportional to the (average) Z of the medium, since the number of atoms per unit volume is within a factor of \(\sim 2\) the same for all materials in the solid state.

The results of calculations on the energy-loss mechanisms for photons and electrons are shown in fig. 2, as a function of energy, in three materials with very different Z-values: carbon (Z = 6), iron (Z = 26), and uranium (Z = 92)\(^{4,5}\). At high energies, above \(\sim 100\) MeV, pair production by photons and energy loss by radiation dominate in all cases, but at low energies the differences between the various materials are considerable. Both the energy at which Compton scattering starts dominating pair production, and the energy at which ionization losses become more important than bremsstrahlung, are strongly material-dependent and are roughly inversely proportional to Z.

These conditions determine the so-called critical energy ($\epsilon_c$), i.e. the point where no further particle multiplication occurs in the shower. Above this energy, $\gamma$'s produce on average more than one charged particle (pair production), and electrons lose their energy predominantly by creating new $\gamma$'s. Below $\epsilon_c$, $\gamma$'s produce only one electron each, and these electrons do not produce new $\gamma$'s themselves.
Figure 2 also shows that the contribution of the photoelectric effect is extremely $Z$-dependent ($\sigma \sim Z^5$). In carbon, it plays a role only at energies below a few keV, while in uranium it is the dominating process below 0.7 MeV.

The approximate shape of the longitudinal shower profile can be deduced from figure 2. If the number of $e^+$ and $e^-$ were to be measured as a function of depth in the detector, one would first find a rather steep rise due to the multiplication. This continues up to the depth at which the average particle energy equals $\epsilon_c$. Beyond that point no further multiplication will take place and, since more and more electrons are stopped, the total number of remaining particles slowly decreases.

The positrons will predominantly be found in the early shower part, i.e. before the maximum is reached. Showers in high-$Z$ materials will contain more positrons than in low-$Z$ materials, because positron production continues until lower energies. The average energy of the shower particles is also lower in high-$Z$ materials, since radiation losses dominate until lower energies. These effects will turn out to have interesting consequences.

Owing to the fact that the underlying physics is well understood and simple, e.m. shower development can be simulated in great detail by Monte Carlo techniques. One program, EGS4\[^6\] has emerged as the world-wide standard for this purpose. It is extremely reliable, and in the following sections several results of it will be shown.

2.1.3 Above 100 GeV

At very high energies new effects will influence the absorption of electrons and photons in a block of matter. In the TeV region, the cross-sections for the e.m. and weak interactions become comparable and, therefore, processes involving hadron and/or neutrino production are no longer negligible.

Another, purely e.m. effect was first pointed out by Landau and Pomeranchuk\[^7\] and treated quantitatively by Migdal\[^8\]. They showed that at energies beyond 10 TeV, multiple scattering of the participating particles may lead to a significant decrease of the cross-sections for bremsstrahlung and pair production. Such effects will obviously change the gross behaviour of the shower development. The experimental information on these phenomena is scarce and, because of their limited practical relevance at present, we will not discuss them further.
2.1.4 Electromagnetic shower characteristics

Since the e.m. shower development is primarily determined by the electron density in the absorber medium, it is to some extent possible, and in any case convenient to describe the shower characteristics in a material-independent way. The units that are frequently used to describe the characteristic shower dimensions are the radiation length ($X_0$) for the longitudinal development and the Molière radius ($\rho_M$) for the transverse development.

The radiation length is defined as the distance over which a high-energy (> 1 GeV) electron loses on average 63.2% ($1 - 1/e$) of its energy to Bremsstrahlung. The average distance that very high energy photons travel before converting into an $e^+e^-$ pair equals $9/7 \ X_0$. The Molière radius is defined by the ratio of $X_0$ and $\epsilon_e$, where $\epsilon_e$ is the electron energy at which the losses through radiation and ionization are the same. For approximate calculations, the following relations hold:

$$X_0 \approx 180A/Z^2 \ (g/cm^2) \ \text{and} \ \rho_M \approx 7A/Z \ (g/cm^2).$$

Expressed in these quantities, the shower development is approximately material-independent. Figure 3 shows the longitudinal development of a 10 GeV electron shower in Al, Fe, and Pb, as obtained with EGS4 simulations. The profile is as expected from the discussion in section 2.1.2. Globally, it scales indeed with $X_0$. The differences between the various materials can be understood as well. The radiation length is defined for GeV-type particles and, therefore, does not take into account the peculiarities occurring in the MeV region. The shift of the shower maximum to greater depth for high-$Z$ absorbers is a consequence of the fact that particle multiplication continues until lower energies; the slower decay beyond this maximum is due to the fact that lower-energy electrons still radiate.

The figure shows that it takes $\sim 25X_0$ to absorb at least 99% of the shower energy. This corresponds to 14 cm Pb, 44 cm Fe, or 220 cm Al. If the energy is increased, only very little extra material is needed to achieve the same containment. A 20 GeV photon will travel on average $9/7$ radiation length before converting into an $e^+e^-$ pair of 10 GeV each. It therefore takes only an extra $1.3X_0$ to contain twice as much energy.

The radiation length is, strictly speaking, defined for infinite energy and has no meaning in the MeV energy range. We just showed that $\sim 15$ cm lead absorb
20 GeV photon showers for more than 99%, whereas it takes more than that to make a proper shielding for a strong $^{60}$Co source that emits 1.3 MeV γ's. The reason for this is clear from fig. 2. The total cross-section around the region where Compton scattering takes over from pair production is considerably lower than at very high energies, particularly in high-Z materials. As a consequence, the mean free path in lead of photons of a few MeV is $\sim 3$ cm, or $\sim 5X_0$!

The lateral spread of an e.m. shower is caused by two effects:

a) Electrons move away from the axis by multiple scattering.

b) In the energy region where the total cross section is minimal, bremsstrahlung photons may travel quite far from the shower axis, in particular if they are emitted by electrons that themselves travel under a considerable angle with this axis.

The first process dominates in the early stages of the shower development, while the second process is predominant beyond the shower maximum, particularly in high-Z media. Figure 4 shows the lateral distribution of the energy deposited by an e.m. shower in lead, at various depths$^{[9]}$. The two components can be clearly distinguished (note the logarithmic ordinate). The radial profile shows a pronounced central core surrounded by a halo. The central core disappears beyond the shower maximum. Similar calculations in aluminium showed that the radial profile, expressed in $\rho_M$ units, is indeed narrower than in lead. Like the radiation length, also the Molière radius does not take into account the peculiarities occurring in the MeV region.

Figure 4 shows that e.m. showers are very narrow, especially in the first few radiation lengths. The Molière radius of lead is $\sim 1.7$ cm. With a sufficiently fine-grained calorimeter, the showering particle can therefore be localized with a precision of $\sim 1$ mm (see section 3.3).

2.1.5 Energy loss by muons

Muons passing through matter lose their energy also through e.m. processes. Compared to electrons, however, the cross-sections for higher-order QED processes, such as bremsstrahlung or $e^+e^-$ pair production are suppressed by a factor of $(m_\mu/m_e)^2 \approx 40000$. The critical energy is, for example, at least 200 GeV. At energies below 100 GeV, the energy loss by muons will, therefore, be dominated by ionization processes.
The mean energy loss per unit path length for these processes, \(< dE/dx >\), is given by the well-known Bethe-Bloch formula\(^\text{[10]}\). For relativistic muons, \(< dE/dx >\) falls rapidly with increasing \(\beta\), reaches a minimum value near \(\beta = 0.96\) (minimum-ionizing particles), then undergoes what is called the relativistic rise, to level off at values of 2 - 3 MeV/g.cm\(^{-2}\) in most materials.

In practical calorimeters, the total energy loss \(\Delta E/\Delta x\) may differ quite a bit from the value calculated from \(< dE/dx >\). This is because of the relatively small number of collisions with atomic electrons, and of the very large fluctuations in energy transfer that may occur in such collisions. Therefore, the energy loss distribution will in general be peaked at values below the ones calculated from \(< dE/dx >\) and have a long tail toward large energy losses, the so-called Landau tail\(^\text{[11]}\). Only for very substantial amounts of matter, at least 100 m of water equivalent, will the energy-loss distribution become approximately Gaussian.

Figure 5 shows some recent experimental results on muon energy loss, measured in the HELIOS calorimeter\(^\text{[12]}\), which consists essentially of \(\sim 1\) m of uranium. The figure clearly shows the asymmetric distribution of energy losses. It also shows that at increasing energies, and in particular at 200 GeV, higher-order QED processes such as bremsstrahlung start dominating over ionization losses, since the distribution of energy losses is shifted by a considerable amount to higher values.

### 2.2 STRONG-INTERACTION PROCESSES

The absorption of particles subject to the strong interaction (hadrons) in a block of matter proceeds in a way that is very similar, in many respects, to the one described for electromagnetically interacting particles, although in detail the particle-production mechanisms are substantially more complicated. When a high-energy hadron penetrates a block of matter, it will at some point interact with one of its nuclei. In this process, mesons are usually produced (\(\pi, K\), etc.). Some other fraction of the initial particle energy is transferred to the nucleus. The excited nucleus will release this energy by emitting a certain number of nucleons and, at a later stage, low-energy \(\gamma\)'s, and lose its kinetic (recoil) energy by ionization. The particles produced in this reaction (mesons, nucleons, \(\gamma\)'s) may in turn lose their kinetic energy by ionization and/or induce new reactions, thus causing a shower to develop.
Some of the particles produced in this cascading process interact exclusively electromagnetically (e.g. $\pi^0, \eta$). Therefore, hadron showers contain in general a component that propagates electromagnetically. The fraction of the initial hadron energy converted into $\pi^0$'s and $\eta$'s may strongly vary from event to event, depending on the detailed processes occurring in the early phase of the shower development, i.e. the phase where production of these particles is energetically possible.

On average, approximately one third of the mesons produced in the first interaction will be $\pi^0$'s. In the second generation of interactions, the remaining $\pi^+, \pi^-$, etc. may produce $\pi^0$'s as well, if they are sufficiently energetic, and so on. And since production of $\pi^0$'s by hadronically interacting mesons is an irreversible process, the average fraction of the initial hadron energy converted into $\pi^0$'s increases (logarithmically) with the energy.

Although the shower development by hadrons and electrons shows many similarities, there exist some characteristic differences which turn out to have crucial consequences.

2.2.1 Shower dimensions

Firstly, the hadronic shower development is (for an important part) based on nuclear interactions and, therefore, the shower dimensions are governed by the nuclear interaction length $\lambda_{\text{int}}$. The nuclear interaction probability is determined by the fraction of a two-dimensional plane occupied by atomic nuclei; since the number of atoms per unit volume is to first order material-independent, $\lambda_{\text{int}}$ will scale with the nuclear radius, i.e. as $A^{1/3}$.

Existing experimental data indicates that the longitudinal and lateral profiles of hadronic showers scale roughly with $\lambda_{\text{int}}$. Figure 6 shows the results of measurements that give a good impression of the longitudinal and lateral development of 300 GeV showers in uranium$^{[13]}$. The profiles look very similar to e.m. showers (figs. 3,4), albeit on a very different scale. It takes about 80 cm of uranium to contain the 300 GeV $\pi^-$ showers at the 95% level, while 10 cm would be sufficient for electrons at the same energy.

The leakage as a function of the detector depth is shown in fig. 7, for hadron energies ranging from 5 to 210 GeV. It turns out that the detector size needed
to contain, for instance, more than 99% of the shower energy, increases only very slightly with the energy, from $6\lambda_{\text{int}}$ at 5 GeV to $9\lambda_{\text{int}}$ at 210 GeV\(^{114}\).

One may use the differences in characteristic energy deposit for particle identification. Since $\lambda_{\text{int}}$ scales with $A^{1/3}$ and $X_0$ with $A/Z^2$, the separation between electromagnetically interacting particles ($\epsilon, \gamma, \pi^0$) and hadrons works best for high-$Z$ materials, where the ratio $\lambda_{\text{int}}/X_0$ may reach values larger than 30 (see section 3.4).

2.2.2 Invisible energy

A second crucial difference between the shower development by high-energy electrons and by hadrons concerns the fact that, in the latter case, a certain fraction of the energy is dissipated in undetectable (invisible) form. Apart from neutrinos and high-energy muons, which may be generated in the hadronic shower-development process and which will generally escape the detector, we refer mainly to the energy needed to release nucleons from the nuclear field that keeps them together. Some fraction of this nuclear binding energy loss may be recuperated when neutrons get captured by other nuclei. The protons, $\alpha$'s, and heavier nucleon aggregates released in nuclear reactions will, however, only lose their kinetic energy, by ionization.

The fraction of invisible energy can be quite substantial, up to 40% of the energy dissipated in non-e.m. form\(^{115}\).

At low energies ($< 2$ GeV) the probability that charged hadrons lose their kinetic energy without causing nuclear interactions, i.e. by ionization alone, increases rapidly. In this case, as for muons and e.m. showers, there are no invisible-energy losses. As a consequence, hadron calorimeters suffer in general from signal non-linearities at low energy\(^{116}\) (see section 3.2).

2.2.3 Non-relativistic shower particles

A third difference, which has important consequences for the calorimetric energy measurement of elementary particles, results from the fact that a large fraction of the energy deposited in hadronic showers is carried by (extremely) non-relativistic particles, i.e. protons and neutrons. We mention three consequences:
i) Many protons produced in the shower-development process have a specific ionization \(< dE/dx >\) that is 10 to 100 times the minimum-ionizing value, depending on the Z of the traversed medium. As a consequence, the fraction of the energy of such particles detected by sampling calorimeters consisting of alternating layers of absorber and active material that usually have very different Z-values, may be considerably different from the fraction detected for minimum-ionizing particles. This is illustrated in fig. 8.

ii) Some frequently used active calorimeter media show a strongly non-linear behaviour in their response to densely ionizing particles. They suffer from saturation (scintillator)\(^{11}\) or recombination effects (liquid argon\(^{12}\), room-temperature liquids\(^{13}\)). Such effects may suppress the response, i.e. the signal per unit deposited energy, by as much as a factor 5 for this shower component\(^{14}\). These effects are much smaller, or absent, when gases or silicon are used as the active calorimeter medium.

iii) Neutrons, which lose their kinetic energy exclusively through strong interactions may travel quite long distances before being finally absorbed. In calorimeters where the neutrons contribute significantly to the signal, this may lead to a considerable prolongation of the pulse duration for hadronic signals, compared with e.m. ones. Typical time constants for the neutron contribution to the calorimeter signal amount to 10 ns for the release of kinetic energy, and 0.5 \(\mu s\) for the \(\gamma\)'s created in the thermal-neutron capture process. These phenomena may be exploited for particle identification, and in particular for \(e/\pi\) separation (see section 3.4.1).

2.2.4 The role of neutrons

Regarding calorimetric applications, perhaps the most crucial difference between e.m. and hadronic shower development comes from the fact that a considerable fraction of the energy is carried by non-ionizing particles, i.e. the soft (few MeV) neutrons from the nuclear evaporation processes.

Since these neutrons lose their kinetic energy exclusively through collisions with atomic nuclei, their contribution to the signal of sampling calorimeters is completely dependent on the nuclear peculiarities of the materials composing the calorimeter. It is well-known that in particular hydrogen is very efficient in slowing down neutrons.
It was shown both experimentally\textsuperscript{[13]} and theoretically\textsuperscript{[10,21,22]} that in calorimeters with hydrogenous active material, the neutrons generated in the shower development may deposit a large fraction of their kinetic energy in the active layers, while charged particles are only sampled at the few per cent level. This effect is an important tool for making so-called compensating calorimeters.

3. PERFORMANCE OF CALORIMETER SYSTEMS

In this section, we will discuss the performance of calorimeters, these instrumented blocks of dense matter in which the particles interact and get absorbed through the processes described in the previous section, yielding signals from which the particle properties (energy, direction, type) can be derived.

Historically, one may distinguish between calorimeters, according to the purpose that they serve, as e.m. and hadronic shower detectors. Nowadays, there is a growing tendency to combine both functions in one instrument.

Another distinction that may be made concerns their composition: homogeneous, fully sensitive devices as opposed to sampling calorimeters. The latter consist of a passive absorber with active material embedded into it, most frequently in the form of a sandwiched layer structure. In this way only a small fraction of the initial particle energy, ranging from $10^{-5}$ for gas calorimeters to a few percent for solid or liquid readout media, is deposited in the active layers.

Although additional fluctuations, affecting the energy resolution, are caused by the fact that only a fraction of the energy is deposited in the active material, the sampling technique is becoming more and more popular, particularly in accelerator-based experiments, for the following reasons:

\textit{i)} Since very dense absorber materials can be used, calorimeters can be made extremely compact. Even at the highest energies envisaged today, 2 m of lead or uranium is sufficient to contain all showers at the 99\% level (see fig. 7).

\textit{ii)} At increasing energies, the energy resolution tends to be dominated by \textit{systematic} effects; therefore, the effects of sampling fluctuations become less important.

\textit{iii)} Contrary to fully sensitive devices, sampling calorimeters can be made \textit{compensating}.
Before discussing in detail actual devices, we will first elaborate on the latter point, which is crucial for the performance of hadron calorimeters.

3.1 COMPENSATION

3.1.1 The role of the e/h signal ratio

In a given calorimeter, hadron showers are detected with an energy resolution that is worse than for e.m. ones. This is mainly because, in hadronic showers, fluctuations occur in the fraction of the initial energy carried by ionizing particles. Losses in nuclear binding energy (see section 2.2.2) may consume up to 40% of the incident energy, with large fluctuations about this average.

As a consequence, the signal distribution for monoenergetic pions is wider than for electrons at the same energy, and has in general a smaller mean value ($e/\pi > 1$). The calorimeter response to the e.m. ($e$) and non-e.m. ($h$) components of hadron showers shows a similar difference ($e/h > 1$). Since the event-to-event fluctuations in the fraction of the energy spent on $\pi^0$ production ($f_{em}$) are large and non-Gaussian, and since $\langle f_{em} \rangle$ increases (logarithmically) with energy, the following effects have to be expected if $e/h \neq 1$:

i) The signal distribution for monoenergetic hadrons is non-Gaussian.

ii) The fluctuations in $f_{em}$ give an additional contribution to the energy resolution.

iii) The energy resolution $\sigma/E$ does not improve as $E^{-1/2}$ with increasing energy.

iv) The calorimeter signal is not proportional to the hadron energy (non-linearity).

v) The measured $e/\pi$ signal ratio is energy dependent.

Because of the latter effect, we prefer to use the energy-independent quantity $e/h$. In practice, the difference between $e/h$ and $e/\pi$ is small, and it vanishes at low energies and for $e/h$ close to 1. All these effects have been experimentally observed\textsuperscript{[12,24,26]} (fig. 9) and can be reproduced with a simple Monte Carlo.

At increasing energies, deviations from $e/h = 1$ (the compensation condition) rapidly become a dominating factor for the (lack of) calorimeter performance, e.g. for the energy resolution $\sigma/E$ (fig. 9a). Signal non-linearities of $\sim 20\%$ over
one order of magnitude in energy have been observed, both in overcompensating \((e/h < 1)\) and undercompensating \((e/h > 1)\) calorimeters (fig. 9b). But perhaps the most disturbing drawback of a non-compensating calorimeter, especially in an environment where high trigger selectivity is required, is the non-Gaussian response (fig. 9c), which may cause severe problems if one wants for example to trigger on (missing) transverse energy: it will be very difficult to unfold a steeply falling \(E_T\) distribution and a non-Gaussian response function. Moreover, severe trigger biases are likely to occur: if \(e/h < 1 \,(>1)\) one will predominantly select events that contain little (a lot of) c.m. energy from \(\pi^0\)s.

There is general agreement that hadron calorimeters for future applications at high energy should be compensating. It should be emphasized that other sources of experimental uncertainty, such as calibration errors, will produce effects similar to the ones caused by deviations from \(e/h = 1\). Therefore, it is not necessary that \(e/h\) be exactly 1. It has been estimated\(^{[14]}\) that \(e/h = 1 \pm 0.05\) is adequate to achieve energy resolutions at the 1% level.

3.1.2 Methods to achieve compensation

Because of the invisible-energy phenomenon, i.e. the nuclear binding energy losses typical for (the non-c.m. part of) hadronic showers, one might naively expect the \(e/h\) signal ratio to be larger than 1 for all calorimeters. This is, however a tremendous oversimplification. Based on our present understanding of hadron calorimetry\(^{[15,21,22]}\), it may be expected that a large variety of very different structures can actually be made compensating. A wealth of available experimental data supports the framework of this understanding, and explicit predictions were experimentally confirmed.

The response of a sampling calorimeter to a showering particle is a complicated issue that depends on many details. This is particularly true for hadronic showers. It has become clear that showers can by no means be considered as a collection of minimum ionizing particles that distribute their energy to absorber and active layers according to \(<dE/dx>\). The calorimeter signal is, to a very large extent, determined by very soft particles from the last stages of the shower development, simply because these particles are so numerous. Many observations support this statement.

Simulations of high-energy e.m. showers in lead or uranium sampling calorimeters show that about 40% of the energy is deposited through ionization by
electrons softer than 1 MeV\textsuperscript{[16]}. Measurements of pion signals in fine-sampling lead/plastic-scintillator calorimeters revealed that there is almost no correlation between the particles contributing to the signal of consecutive active layers\textsuperscript{[26,27]} This proves that the particles that dominate the signal travel on average only a very small fraction of a nuclear interaction length indeed.

For a correct evaluation of the \( e/h \) signal ratio of a given calorimeter, the last stages of the shower development must therefore be understood in detail, \textit{i.e.} the processes at the nuclear and even the atomic level must be analysed. The particles that decisively determine the calorimeter response are \textit{soft photons} in the case of e.m. showers, and \textit{soft protons and neutrons} from nuclear reactions in non-e.m. showers. Since most of the protons contributing to the signal are highly non-relativistic, the saturation properties of the active material for densely ionizing particles are of crucial importance (see section 2.2.3).

There are many other factors that affect the signals from these shower components, and thus \( e/h \). Among these, there are \textit{material} properties, such as the \( Z \) values of the active and passive components, the hydrogen content of the active media (see section 2.2.4), the nuclear-level structure and the cross-section for thermal-neutron capture by the absorber; and there are the \textit{detector} properties, such as the size, the signal integration time, the thickness of the active and passive layers, and the ratio of these thicknesses.

In order to achieve compensation, three different phenomena may be exploited:

\textit{i)} The non-e.m. response may be selectively boosted by using depleted uranium (\( ^{238}\text{U} \)) absorber plates. The fission processes induced in the non-e.m. part of the shower development yield extra energy, mainly in the form of soft \( \gamma \)'s and neutrons\textsuperscript{[24]} . This phenomenon also leads to the commonly used terminology, since the extra energy released in \( ^{238}\text{U} \) fission compensates for the nuclear binding energy losses.

\textit{ii)} One may selectively suppress the e.m. response by making use of the peculiarities of the energy deposit by the soft-photon component of e.m. showers. Below 1 MeV, the photoelectric effect is an important energy loss mechanism. Since the cross-section is proportional to \( Z^5 \), soft photons will interact almost exclusively in the absorber layers of high-\( Z \) sampling calorimeters. They will only contribute to the signal if the interaction takes place sufficiently close to the boundary layer, so that the photoelectron can
escape into the active material. This effect may lead to a considerable sup-
pression of the em response\textsuperscript{[15]} . It may be enhanced by shielding the active
layers by thin sheets of passive low-Z material\textsuperscript{[20,22,28,29]} .

iii) The most important handle on $e/h$ is provided by the neutron response,
in particular for calorimeters with hydrogenous active material (see section
2.2.4). In this case, the fraction of the neutron's kinetic energy transferred
to recoil protons in the active layers varies much more slowly with the
relative amounts of passive and active material than does the fraction of the
energy deposited by charged particles. Therefore, the relative contribution
of neutrons to the calorimeter signal, and hence $e/h$, can be varied by
changing the sampling fraction\textsuperscript{[15,24]} . A small sampling fraction enhances
the relative contribution of neutrons. It is estimated that in compensated
lead- or uranium-scintillator calorimeters, neutrons make up $\sim 40\%$ of the
non-e.m. signal, on average\textsuperscript{[22,23]} . The lever arm on $e/h$ provided by this
mechanism may be considerable. It depends on the energy fraction carried
by soft neutrons (favouring high-Z absorbers), on the hydrogen fraction
in the active medium, and on the signal saturation for densely ionizing
particles.

Apart from these methods, which aim at achieving $e/h = 1$ as an intrinsic
detector property, a completely different approach has been applied, in order to
reduce the mentioned disadvantages of an intrinsically non-compensating detec-
tor by means of off-line corrections to the measured data\textsuperscript{[24,30]} . In this approach,
which requires a very fine-grained detector, one tries to determine the $\pi^0$ content
on a shower-by-shower basis, and a weighting scheme is used to correct for the
different calorimeter responses to the $\pi^0$ and non-$\pi^0$ shower components.

An example of the results of calculations on $e/h$ for uranium calorimeters
is shown in fig. 10\textsuperscript{[15]} . For hydrogenous readout materials (plastic scintillator,
warm liquids) the $e/h$ value sensitively depends on the relative amount of active
material, and in any case configurations can be found with $e/h = 1$.

Experimental results clearly confirm the tendency predicted for plastic scin-
tillator readout\textsuperscript{[12,28,31]} . For non-hydrogenous readout, mechanism iii) does not
apply. Here the neutron response, and hence the $e/h$ ratio, can be affected
through the signal integration time, taking more or less advantage of the con-
siderable energy released in the form of $\gamma$'s when thermal neutrons are captured
by nuclei, a process that occurs at a time scale of 1 μs. Experimental results obtained so far seem to confirm the prediction that it will be hard to achieve full compensation with liquid-argon (LAr) readout\textsuperscript{[32,33,34]} . In U/Si detectors, a full exploitation of mechanisms i) and ii) might yield a compensating calorimeter, since there are no saturation effects\textsuperscript{[26,28,29]} . Detectors with gaseous readout media offer a convenient way to tune $e/h$ to the desired value, i.e. through the hydrogen content of the gas mixture. This has been demonstrated experimentally by the L3 Collaboration\textsuperscript{[30]} .

The curves for TMP calorimeters given in fig. 10 are based on the assumption that the signal saturation in this liquid is equal either to LAr or to PMMA plastic scintillator. Preliminary experimental data indicate that the signal suppression in warm liquids is considerably larger, and that it depends, perhaps, on the electric-field strength and on the particle's angle with the field vector\textsuperscript{[36]} . Figure 11 shows how sensitively the $e/h$ signal ratio depends on the saturation properties. The UA1 Collaboration recently reported having measured an $e/h$ value smaller than 1.1 with their first uranium-TMP calorimeter module\textsuperscript{[37]} .

In summary, compensation is not a phenomenon restricted to uranium calorimeters, nor is the use of uranium absorber a guarantee for achieving compensation. It has become clear that both the readout medium and the absorber material determine the $e/h$ value. Compensation is easier to achieve with high-$Z$ absorbers because of the large neutron production and the correspondingly large leverage on $e/h$. But even materials as light as iron allow compensation, if used in combination with, for instance, plastic scintillator, albeit with impractically thick absorber plates\textsuperscript{[15]} .

The neutron production in lead is considerably smaller than in uranium. In order to bring $e/h$ to 1.0 for lead/scintillator detectors, the neutron signal has therefore to be more enhanced relative to charged particles than for uranium/scintillator calorimeters. As a consequence, the optimal sampling fraction is smaller for lead. The calculations\textsuperscript{[15]} predicted $e/h$ to become 1.0 for lead plates about 4 times as thick as the scintillator, while for uranium plates a thickness ratio of 1:1 is optimal. This prediction was experimentally confirmed by the ZEUS Collaboration\textsuperscript{[34]} . They found $e/h = 1.05 \pm 0.04$, a hadronic energy resolution scaling with $E^{-1/2}$ over the energy range 3 - 75 GeV, and no deviations from a Gaussian line shape.
The mechanisms described above, which make compensating calorimeters possible, only apply to sampling calorimeters. They are based on the fact that only a small fraction of the shower energy is deposited in the active part of the calorimeter; thus, by carefully choosing the parameter values, one may equalize the response to the e.m. and non-e.m. shower components. This does not work for homogeneous devices, where, in the non-e.m. shower part, losses will inevitably occur that cannot be compensated for. Measurements performed so far with homogeneous hadron detectors support this conclusion, for what concerns the \( e/h \) ratio\[^{[39]} \], as well as the resulting non-linearity, the non-Gaussian response, and the poor energy resolution\[^{[40]} \].

### 3.2 ENERGY RESPONSE AND RESOLUTION

#### 3.2.1 Fluctuations in the energy measurement

The detection of particle showers with calorimeters is based on statistical processes: the production of ionization charge, scintillation or Čerenkov photons, phonons, or electron-hole pairs in semiconductors. The energy resolution for particle detection is therefore determined, among other factors, by fluctuations in the number of primary, uncorrelated processes \( n \). The width of the signal distribution \( \sigma_S \) for detection of monoenergetic particles with energy \( E \) will therefore relate to \( n \) as \( \sigma_S/S \sim \sqrt{n}/n \), which leads for linear calorimeters to the familiar relation \( \sigma_E/E = c/\sqrt{E} \).

It has become customary to give a value of \( c \) for expressing calorimetric energy resolutions, where \( E \) is given in units of GeV. Because of the statistical nature of calorimetry, the relative energy accuracy \( \sigma_E/E \) improves with increasing energy. This very attractive feature is one of the reasons why these instruments have become so popular.

Fluctuations in the number of primary processes constituting the calorimeter signal form the ultimate limit for the energy resolution. In most detectors, the energy resolution is dominated by other factors. We mention two exceptions. Firstly, there are the semiconductor nuclear-\( \gamma \) detectors, such as Ge, Ge(Li), and Si(Li) crystals. It takes very little energy to create one electron-hole pair in these crystals, only 2.9 eV in Ge. The signal of a 1 MeV \( \gamma \) fully absorbed in the detector will therefore consist of some 350,000 electrons. The fluctuations in this number lead to an energy resolution of \( \sigma_E/E = 0.17\% \) (at 1 MeV!).
Owing to correlations in the production of consecutive electron-hole pairs (the so-called Fano factor), the limit of the energy resolution given by fluctuations in the number of primary processes will be somewhat larger. In practice, resolutions of $\sim 2.0$ keV at 1 MeV are indeed achieved with such detectors.

A second example are lead-glass e.m. shower counters. They are based on the detection of the Čerenkov light produced by the electrons and positrons from the shower. Particles travelling at a velocity lower than the velocity of light in the absorber will not emit this light, and therefore the lead-glass is only sensitive to electrons with a kinetic energy larger than $\sim 0.7$ MeV. This means that at maximum only $1000/0.7 \sim 1400$ particles can produce Čerenkov light, per GeV of shower energy, and that the resolution $\sigma_E/E$ cannot become better than $\sim 3\%$ at 1 GeV because of fluctuations in this number. The best lead-glass detector systems have reached $\sigma_E/E \approx 5\%$ for e.m. showers in the 1 - 20 GeV energy range.

More frequently, the energy resolution is determined by factors other than the fluctuations in the number of primary processes. These factors may concern statistical processes with a Gaussian probability distribution, or be of a different nature. In the latter case, their contribution to the energy resolution will cause deviations from the $E^{-1/2}$ scaling law. Such deviations are of course most apparent at high energies.

As an example, we mention homogeneous scintillation counters(e.g. NaI(Tl), CsI, BGO). Compared to what happens with the semiconductor crystals discussed before, the following complications arise:

i) The scintillation photons are not monoenergetic.

ii) Only a fraction of the photons reach the light-detecting element. The rest is either absorbed or refracted. These effects strongly depend on the detector geometry and on the position where the light is produced.

iii) The sensitivity of photocathodes or photodiodes depends on the wavelength.

Measurements with NaI(Tl) crystals on 8 keV X-rays yielded $\sigma_E/E \approx 15\%$. If we assume that this result is dominated by fluctuations in the primary processes, this means that on average $\sim 40$ photoelectrons are observed. Based on this result, one would then expect resolutions of $\sigma_E/E \approx 1.5\%$ at 1 MeV. Yet, the best
resolutions obtained at this energy are only about 5%. For e.m. shower detection one finds resolutions \( \sigma_E / E \approx 1\% \) at 1 GeV, while a factor 30 improvement should be expected when extrapolating the 1 MeV results with the \( E^{-1/2} \) scaling law. For this reason, it is incorrect to express resolutions as \( c / \sqrt{E} \) for such detectors.

Other factors which will cause deviations from \( E^{-1/2} \) scaling are instrumental: noise and pedestal contributions to the signal, uncertainties coming from calibration and non-uniformities, or incomplete shower containment.

The energy resolution of sampling calorimeters is frequently dominated by the very fact that the shower is sampled\(^{42} \). The nature of these sampling fluctuations is purely statistical and, therefore, they contribute as \( c / \sqrt{E} \) to the final energy resolution. A major contribution comes from fluctuations in the number of different shower particles contributing to the calorimeter signal. In some devices (e.g. gas or Si readout), also the fluctuations in the energy that the individual shower particles deposit in the active calorimeter layers have to be taken into account. In calorimeters with dense active material (plastic scintillator, LAr), the contribution of sampling fluctuations to the energy resolution tends to scale as \( \sigma_{\text{samp}} / E = \sqrt{t_{\text{abs}} / E} \), for a particular combination of passive and active material, a fixed thickness of the active planes and a thickness \( t_{\text{abs}} \) of the passive planes. The sampling fluctuations depend also on the thickness \( t_{\text{act}} \) of the active planes. Photon conversions in these planes contribute a term which scales like \( c \sqrt{1 / t_{\text{act}}} \), for fixed \( t_{\text{abs}} \).\(^{141} \) The relative contribution of this term depends on the \( Z \) values of the active and passive calorimeter layers. For Fe/LAr, one finds that \( \sigma_{\text{samp}} / E \) scales approximately like \( t_{\text{act}}^{-1/4} \), for fixed \( t_{\text{abs}} \).

When detecting electrons and hadrons with the same calorimeter, sampling fluctuations for the latter particles are considerably larger. First of all, the number of different shower particles contributing to the hadronic signal is smaller, because

i) Individual shower particles may traverse many planes.

ii) The average energy deposited by individual particles in the active layers is larger (soft protons!)

Moreover, the spread in the \( dE/dx \) loss of individual shower particles in the active layers is much larger.
The contribution of sampling fluctuations to the energy resolution can be measured in a straightforward way, by comparing energy resolutions measured with different fractions of the active calorimeter channels\textsuperscript{[16,27]}.

In hadronic shower detection, two additional sources of fluctuation play a role, which have no equivalent for e.m. calorimeters, and which tend to dominate the energy resolution of practically all hadron calorimeters constructed up to now. Firstly, there are the effects of the non-Gaussian fluctuations in the π\(^0\) shower component (section 3.1.1); these contribute a constant term to the energy resolution, which only vanishes for compensating detector structures.

Secondly, there are intrinsic fluctuations, in the fraction of the initial energy that is transformed into ionizing shower particles (the visible energy, see section 2.2.2). These form the ultimate limit for the energy resolution achievable with hadron calorimeters. In general one may therefore write (ignoring instrumental contributions such as shower leakage, calibration, etc.)

\[
\frac{\sigma_{\text{had}}}{E} = \sqrt{\frac{c_{\text{int}}^2 + c_{\text{samp}}^2}{E}} + a
\]

This formula shows that at high energy one will want to have \(a\) as small as possible (compensation); moreover, it is useless to make the sampling much finer than the limit set by the intrinsic fluctuations.

It turns out that calorimeters with hydrogenous readout are not only advantageous for achieving compensation: they may also yield considerably lower values for \(c_{\text{int}}\) than other detectors\textsuperscript{[15]}. The intrinsic resolution is largely dominated by fluctuations in the nuclear binding energy losses. Since most of the released nucleons are neutrons in the case of high-\(Z\) target material, there is a correlation between this invisible energy and the kinetic energy carried away by neutrons. Efficient neutron detection therefore reduces the effect of the intrinsic fluctuations on the energy resolution.

Recently, the ZEUS Collaboration measured the intrinsic-resolution limit for compensating uranium- and lead-scintillator calorimeters to be 19\%/\(\sqrt{E}\) and 11\%/\(\sqrt{E}\), respectively\textsuperscript{[77]}. This difference, which means that in principle better energy resolutions can be achieved with lead calorimeters than with uranium ones, can be explained as follows\textsuperscript{[42]}. The extent to which the mechanism described above works depends on the degree of correlation between the nuclear
binding energy losses and the kinetic neutron energy. This correlation is expected to be better in lead than in uranium, since in the latter case many of the neutrons come from fission processes. These fission neutrons are less strongly correlated to the nuclear binding energy losses.

3.2.2 Performance of electromagnetic calorimeters

The best energy resolutions for e.m. shower detection are obtained with homogeneously sensitive detectors and they remain the method of choice when ultimate performance is needed. While detectors based on NaI(Tl) have been in use for decades, delivering consistently energy resolutions of $\sigma/E \sim 0.02 E^{-1/4}$ there are several recent developments providing alternative, sometimes even superior, performance characteristics. Particularly noteworthy are

i) The use of CsI(Tl), which offers similar performance but better mechanical properties compared with NaI(Tl)\textsuperscript{[45]}.

ii) The use of BGO, which allows the construction of very compact detectors due to its short radiation length\textsuperscript{[46]}.

iii) The use of BaF$_2$ crystals, which have a very fast (rise-time $\approx 500$ ps) ultraviolet scintillation light component, and promise very high rate capability and good radiation resistance\textsuperscript{[47,48,49,50]}.

iv) Studies on homogeneously sensitive noble-liquid (Ar, Kr, Xe) e.m. calorimeters\textsuperscript{[51,52,53,54,55]}, which are evaluated to provide energy resolution in the NaI-range combined with ultimate radiation hardness.

When $\sigma/E$ drops below 1%, the resolution tends to become dominated by systematic effects such as calibration uncertainties. This is generally true for all calorimeters.

The energy resolution reported for lead-glass e.m. shower counters varies between $\sqrt{E}$\textsuperscript{[41]} and $12%/\sqrt{E}$, depending among others on the shower containment.

Achieving a sufficient degree of shower containment is usually no problem for the much cheaper sampling calorimeters. With calorimeters based on plastic-scintillator or LAr readout, energy resolutions are usually found to be in the range from $7%/\sqrt{E}$\textsuperscript{[46]} to $\sim 20%/\sqrt{E}$. With gaseous readout media the energy resolution is usually worse, because of the additional effects of fluctuations in the
energy that individual shower particles deposit in the active layers (path length, Landau fluctuations).

A very fine shower sampling can be obtained when scintillating plastic fibres are used as the active material. Energy resolutions as low as $8\%/\sqrt{E}$ (for 0.5 mm thick fibres) have been achieved with this technique[^7].

Signal linearity is usually no problem for e.m. shower detection. Only calorimeters with gas gain readout operating in a digital mode (streamer, Geiger) may suffer from non-linearities at high energy, because of the increased density of particles in the core of the shower, leading to a saturation in the gas gain.

3.2.3 Performance of hadron calorimeters

As pointed out in section 3.1.1, the energy resolution $\sigma/E$ does in general not scale as $E^{-1/2}$ for hadron calorimeters. Only for devices with $e/h$ sufficiently close to 1.0 is such scaling observed down to values of $\sigma/E \sim 1\%-2\%$, where instrumental effects start dominating the results.

The energy resolution of homogeneous detectors is dominated by their non-compensating nature. The value of $\sigma/E$ does not improve below $\sim 10\%$, even at energies as high as 150 GeV[^22,40].

Most sampling calorimeters currently employed as hadron detectors use iron as the absorber material, with active layers consisting of plastic scintillator, LAr, or wire chambers. None of these detectors has achieved energy resolutions better than $55\%/\sqrt{E}$ (at 10 GeV), while rapid deviations of $E^{-1/2}$ scaling occur at higher energies.

Efforts to determine the $\pi^0$ content on a shower-by-shower basis and to correct the signal by means of a weighting scheme[^24] did result in a restoration of the $E^{-1/2}$ scaling for detection of single pions of known energy; these weighing algorithms may, however, introduce signal non-linearities, and doubts remain about the applicability of such a scheme for detecting jets of unknown composition and energy[^22,20].

With compensating calorimeters, considerably better energy resolutions have been obtained. For uranium/plastic-scintillator detectors, values of $\sim 35\%/\sqrt{E}$ were reported by the HELIOS[^12] and ZEUS Collaborations[^31], scaling with $E^{-1/2}$ up to $\sim 200$ GeV. ZEUS also measured $44\%/\sqrt{E}$ for a compensating Pb/plastic-scintillator sandwich detector (10 mm Pb/2.5 mm scintillator)^[34]. Because of the dominating contribution of sampling fluctuations to the latter result, val-
ues of 30%/√E or better may be expected for the fine-sampling compensating Pb/scintillating-fibre detector that is being developed at CERN[13].

The overcompensating U/scintillator calorimeter built by WA78 showed an energy resolution behaviour similar to the one measured for the undercompensating iron calorimeters mentioned before: \( \sigma/E \sim 52%/\sqrt{E} \) at 10 GeV, rapidly degrading at higher energies\(^{[24]} \).

The deviations from the \( E^{-1/2} \) scaling are less dramatic in U/LAr calorimeters, which have \( e/h \) values closer to 1. The energy resolution obtained by D0 amounts to about 60%/\( \sqrt{E} \) at 10 GeV\(^{[23]} \); SLD found a similar value in their initial prototype studies\(^{[33]} \). HELIOS have recently found resolutions around 45%/\( \sqrt{E} \)\(^{[34]} \).

First results obtained with the new UA1 uranium-TMP calorimeter modules show an energy resolution for pion detection of 45.7%/\( \sqrt{E} \) - 7%\(^{[27]} \).

The best absolute values for \( \sigma/E \) were reported by HELIOS, 1.9% for 3.2 TeV \( ^{16} \)O ions\(^{[12]} \), 1.0% for 6.4 TeV \( ^{32} \)S ions\(^{[34]} \). Figure 12 shows the results of calorimetric measurements on the 3.2 TeV \( ^{16} \)O beam from the CERN SPS, dumped in their U/plastic-scintillator calorimeter. The good energy resolution allows a detailed study of the spectrum of the contaminating lower-mass ions.

The effects of non-compensation on the signal linearity were already discussed in section 3.1.1 and experimental results were shown in fig. 9b. Signal non-linearities of \( \sim 20\% \) over one order of magnitude in hadron energy are commonplace in non-compensating calorimeters like the WA1 and WA78 ones shown in this figure.

The weighting procedure mentioned before did not eliminate these non-linearities, particularly below \( \sim 30 \) GeV. Therefore, a jet composed of 10 particles of 10 GeV will yield a signal that is considerably different from a 100 GeV pion signal and the resolution improvement is likely to be considerably smaller for jet detection.

At low energies, below \( \sim 2 \) GeV, a different kind of non-linearity occurs, also for compensating calorimeters. At these low energies, charged hadrons may lose their energy without undergoing strong interactions and the corresponding nuclear binding energy losses. In that case, they deposit their energy through ionization alone, like muons. The hadronic response \( h \) will go up, and the \( e/h \) ratio down. The response to hadrons thus increases at low energies. This is
clearly confirmed by experimental data. Figure 13 shows the measured $e/\pi$ signal ratio as a function of energy, for various calorimeter configurations. A clear decrease in this ratio, i.e., an increase in the hadronic response, is observed below $\sim 2$ GeV.

3.3 POSITION AND ANGULAR RESOLUTION

The position and the angle of incidence of particles can be obtained with calorimeters, using measurements of the transverse and longitudinal shower distribution.

The localization of e.m. ($\sigma_z^e$) and hadronic ($\sigma_z^h$) showers is derived from the center of gravity of the transverse distributions, which are narrowest in the early part, before the shower maximum. Given adequate transverse granularity, the resolution $\sigma_z^e$ or $\sigma_z^h$ is determined by the signal/noise ratio and, therefore, improves with increasing particle energy $E$, approximately as $E^{-1/2}$.

In the narrow early part, more than 90% of an e.m. shower is contained in a cylinder of radius $r \approx 0.5X_0$ and hence millimetre accuracies for $\sigma_z^e$ are readily obtained, even with rather coarse (i.e., few $X_0 \times$ few $X_0$) granularity. As an example, mm-resolution is quoted for few-GeV showers in a lead-glass array of $3.5 \times 3.5$ cm$^2$ granularity$^{48}$, reaching submillimeter accuracy for 100 GeV showers$^{59,60}$. Even higher spatial resolutions are obtained if a high-resolution detector, such as a Multiwire Proportional Chamber$^{61}$ or a Si-strip array$^{62}$, is inserted into the calorimeter at a depth of $\sim 5X_0$. With such techniques, the position of a 100 GeV e.m. shower may be measured with an accuracy of $\sim 100$ μm!

Similar considerations apply to the localization of hadronic showers, which consist of a very narrow core surrounded by a halo of particles extending to several times the core diameter$^{43,63,64}$ (fig. 6). Measurements of the spatial resolution of the impact point$^{12,31,45,60}$ may be parameterized in the form

$$\sigma_z^h [\text{cm}] \leq 0.2 \lambda_{\text{eff}} [\text{cm}] / \sqrt{E [\text{GeV}]}$$

In compact calorimeters, where the effective nuclear interaction length $\lambda_{\text{eff}}$ may be as low as 20 cm, spatial resolutions in the range of a few cm at 1 GeV are
achievable, reaching a few mm for $E \sim 100$ GeV. The resolution $\sigma^h_\theta$ as a function of the transverse segment length $d(\lambda)$ has been evaluated\textsuperscript{[69]} and a dependence of $\sigma^h_\theta \sim \exp(2d)$ may be derived, suggesting a limit on the useful transverse segmentation of $d \approx 0.1\lambda$.

The measurement of the angular resolution for e.m. ($\sigma^e_\theta$) and hadronic showers ($\sigma^h_\theta$) has been carefully studied for several calorimeters used to investigate neutrino scattering\textsuperscript{[65,68,69,70]} and, more recently, for $4\pi$ calorimeter facilities at future hadron colliders\textsuperscript{[62]}.

While the parametrization of the observed performance shows typically a $1/\sqrt{E}$ improvement of the angular resolution, the achieved values depend critically on the design of the apparatus. Typical results are quoted:

$$\sigma^e_\theta [\text{mrad}] \leq 20/\sqrt{E [\text{GeV}]} \quad (\text{refs. 69,70}),$$

$$\sigma^h_\theta [\text{mrad}] \approx 3.5 + 53/E [\text{GeV}] \quad (\text{ref. 68}).$$

For carefully optimized hadronic angular resolution (achieved by choosing a material in which e.m. and hadronic showers have approximately the same spatial dimensions, i.e. $\lambda \approx 3X_0$), a value $\sigma^h_\theta [\text{mrad}] \approx 160/\sqrt{E [\text{GeV}]} + 560/E [\text{GeV}]$ was reported\textsuperscript{[65,68,71]}.

### 3.4 PARTICLE IDENTIFICATION

Hadronic calorimeters provide identification of a class of particles that are not readily identified by other methods and that are studied more and more often in very topical experiments (see Table I). In the following, we discuss in some detail the identification of electrons, muons, and neutrinos.

#### 3.4.1 Discrimination between electrons (photons) and hadrons

Most frequently, discrimination is based on the spatial differences in the shower profiles, accentuated in absorber materials with very different radiation and absorption lengths, i.e. at high $Z$ (see fig. 14). High-$Z$ materials (lead, tungsten, uranium) are most frequently used to optimize the electron-hadron discrimination.

The principal physics limitation to this technique is the charge-exchange reaction $\pi^- p \rightarrow \pi^0 n$ (or $\pi^+ n \rightarrow \pi^0 p$), which may simulate an e.m. shower. For
few-GeV pions the cross-section for this reaction is at the 1% level of the total inelastic cross-section, and it decreases logarithmically with increasing energy\textsuperscript{[72]}.
Consequently, typical values for $e/\pi$ discrimination are of the order of $10^{-2}$ in the $1 - 10$ GeV range and $10^{-3}$ beyond 100 GeV\textsuperscript{[73,74,75,76,77]}. A further improvement by a factor of 3 to 5 can be obtained if information on the transverse shower profile is available\textsuperscript{[78]}.

The quoted rejection factors are based solely on the use of shower profile analysis. With additional momentum information, e.g. from magnetic momentum analysis, a further improvement in rejection of typically an order of magnitude is obtained.

A novel method, based on the differences in the time development of e.m. and hadronic showers, was recently tested successfully\textsuperscript{[79]} (fig. 15). Using this technique, an $e/\pi$ discrimination of $10^{-2}$ could be achieved for particles at 150 GeV, without using any information on the shower profile.

One of the most challenging detection problems, and of increasing importance for modern particle-physics experimentation, is the identification of electrons close to the core of high-momentum jets. One proposed solution\textsuperscript{[82]} is based on a detailed three-dimensional measurement of energy deposit, through which e.m. showers appear as relatively energetic deposits, concentrated in a very small volume compared with the extension of the hadronic showers from the majority of the jet particles.

A related technique will be used by the ZEUS Collaboration, who will embed in their hadron calorimeter at a depth of $4X_0$ and $7X_0$ a layer of 40000 silicon detectors, each one having an active area of several cm\(^2\). Pulse-height measurements in these Si elements will allow them to discriminate between high-particle-density e.m. showers and the relatively wide hadron showers, permitting electron identification in the presence of hadrons\textsuperscript{[80,81]}.

3.4.2 Muon identification

Several calorimetric methods exist for discriminating between muons and hadrons, all based on the very large differences of energy deposit:

i) Calorimeters with fine longitudinal segmentation: energetic muons are clearly recognized as isolated, minimum-ionizing tracks, possibly ranging far beyond the tracks from hadronic showers. This is the technique used
in experiments on incident neutrinos, but also some of the highly granular collider detectors are expected to offer this identification potential.

ii) Muon penetration through active or passive absorbers: hadrons are adequately absorbed, so that the 'punch-through' probability of pions \( P \sim \exp\left(-d/\lambda\right) \) is sufficiently small. The absorber thickness \( d \) measured in detectable absorption lengths \( \lambda \), was found to agree closely with tabulated values for relatively thin absorbers\(^{[92,93,94]} \) \( d \leq 10\lambda \), but shows significant deviations for absorber thicknesses \( d > 10 - 15\lambda^{[91,96]} \).

The detailed rejection power against hadrons depends critically on the experimental precautions taken; it may be improved by

\( a) \) reducing the background from \( \pi \) and \( K \) decay in front of the calorimeter,

\( b) \) measuring the muon momentum after the calorimeter, for instance in magnetized iron\(^{[97,98]} \) or a precision spectrometer\(^{[99]} \),

\( c) \) correlating the direction or the momentum of muon candidates before and after the absorber.

Very good muon identification will continue to be emphasized when considering experiments for future hadron colliders. In these experiments, accurate muon-momentum measurements will be mandatory because they will exploit missing-energy signatures in the search for new physics phenomena.

3.4.3 Neutrino identification

Apparent missing energy or missing momentum has become a powerful technique to infer the presence of neutrinos among the collision products:

\( a) \) Missing energy relies on a measurement of the total energy using 4\( \pi \) calorimetric coverage for all particles (charged, neutral, muons). This can in practice be achieved for collisions at \( e^+e^- \) storage rings or in fixed-target experiments. Neutrino production is inferred whenever the measured energy is lower than the total available energy and incompatible with the resolution function of the detector. A total-energy measurement is not practical at hadron colliders, because a considerable fraction of the total energy is produced at angles too close to the colliding beams, and hence inaccessible for calorimetric measurements. In this case it is advantageous to implement
b) A **missing-transverse-momentum** measurement, where neutrino production is signalled by $\Sigma p_{\perp,i} \neq 0$, incommensurate with detector resolution. The intrinsic quality of such measurements was estimated to be $\sigma(p_{\perp,\text{miss}}/P_{\text{total}}) \approx 0.3/\sqrt{P_{\text{total}}}$\textsuperscript{[90]}, considerably better than the values achieved up to now: $\sigma(p_{\perp,\text{miss}}/P_{\text{total}}) \approx 0.7/\sqrt{P_{\text{total}}}$\textsuperscript{[91,92,93]} or $\sigma(p_{\perp,\text{miss}}) \approx 0.6p_{\perp}^{0.43}[\text{GeV}]$\textsuperscript{[94]}.

### 3.5 **Calorimetric Spectroscopy of Multi-Jet Systems**

During the last decade, physics emphasis has been shifting from measurements of single particles to the analysis of jets of hadrons, which are the experimental manifestation of high-energy quarks and gluons. At future colliders, the spectroscopy of particles in the 0.1 - 1 TeV mass range will be pursued and will rely on the invariant-mass determination of multi-jet systems\textsuperscript{[90,96]}.

Two distinct contributions affect this invariant-mass distribution. Firstly, unlike single particles, jets are not unambiguously defined objects, but have to be reconstructed with some algorithm\textsuperscript{[97]} (fig. 16). Secondly, the calorimeter performance, and in particular the momentum response to different particles, will contribute to the mass resolution (fig. 17). This is also shown conceptually in fig. 18 for two different calorimeters. At high energies, $E \geq 50$ GeV, the jet resolution is dominated by the relative electron/hadron response. But even for ideal devices the jet definition based on a jet algorithm will introduce a measurement error. At very high energies, according to ref. 62, this will contribute to the total energy (and mass) resolution at the level of $2 - 4\%$.

### 3.6 **Signal Processing**

#### 3.6.1 Readout systems for sampling calorimeters

A great number of different readout systems have been developed, reflecting the desire to tailor the systems performance to a physics application\textsuperscript{[1,2]}.

Light-collecting techniques based on coupling scintillators to a photon detector have been used for two decades\textsuperscript{[38]} . In recent years, the elegant technique of coupling the individual scintillator slabs through a wavelength shifter to the photon detector has permitted the compact, highly subdivided construction of rather uniformly sensitive calorimeters\textsuperscript{[39]}.
Many modern detectors for storage ring experiments have built on this principle. The relative ease of the technique has to be weighted against some of the operational difficulties characteristic of the optical readout. The light collection is inherently non-uniform and deviations from uniform response at a level of $\sim 5\%$ are typical for a well-constructed device. The optical system is also prone to significant long-term changes in the light-detection efficiency, limiting the systematic accuracy of the energy measurement (see section 3.6.2).

Charge-collection readout is the second widely used method, measuring the ionization charge liberated in gases, liquids and solids. Typical of these schemes is the easy segmentation, and the capability of operating in a magnetic field.

Charge collection in gases, usually followed by some degree of internal amplification, forms the basis for many rather diverse systems. The internal amplification facilitates the electronic signal processing, but is at the same time the source of an important systematic error, caused by non-uniformities in the gas gain of such detectors$^{[109]}$.

Better control of systematic effects in the readout is usually found in the ion-chamber calorimeters, collecting the charge in a dielectric liquid (noble liquids, in particular liquid argon, room-temperature liquids such as tetramethylsilane and similar ones). These readout techniques may offer uniformity of response at the fractional per cent level, ease in fine-grained segmentation, good long-term stability, and high radiation resistance. Recent interest has focused on room-temperature liquids$^{[37]}$, because these don’t need the cryogenics which may introduce considerable insensitive areas in a $4\pi$ detector.

Another recent development concerns the use of silicon detectors as active elements. This technique has the attraction of the ion-chamber readout, without the need of a cryogenic system, nor the severe purity requirements characteristic for room-temperature liquids.

3.6.2 Calibration of the calorimeter response

In the previous chapters we argued that modern understanding of calorimeter performance permits energy measurements with few per cent precision for high-energy ($> 100$ GeV) particles. This intrinsic excellent performance is, however, only achieved in large experimental facilities - frequently comprising several tens
of thousands of independent signal channels— if extraordinary care is taken to calibrate the absolute and relative energy scale, and to monitor all components of such a detector with a precision approaching or exceeding the 1% accuracy level. The success of existing or planned facilities depends on extensive, frequently redundant, sometimes ingenious monitoring systems, which need to be designed into the detector system from the very start and become an integral part of it. These monitor systems differ considerably depending on the type of calorimeter (photon- or charge-collection) and are particularly complex for scintillator-based devices.

In general, the following steps must be taken to establish and maintain the absolute and relative energy scale:

i) A number of calorimeter modules have to be exposed to muons, electrons, pions, and protons at different momenta. This procedure establishes the absolute energy scale, the relative response to hadrons and electrons, the energy resolution, and the linearity. Some groups have chosen not to expose all calorimeter cells to such a test-beam procedure \(^{64,101,102}\), but rather to rely on adequately tight construction tolerances (thickness of scintillator and absorber plates, uniformity of optical components), combined with a cosmic-ray muon calibration of all the detector cells to set the absolute energy scale. Other groups have chosen to expose all units to a test-beam calibration \(^{103,104}\).

ii) A monitoring system has to provide a reference signal for the transfer of the energy scale from the test-beam measurements to the experimental facilities and to maintain the long-term stability. For calorimeters with photon-collecting readout, the signal transfer standard is conceptually a light source whose stability is guaranteed by design (e.g. a 241Am radioactive source embedded in a NaI scintillator) or whose light output is controlled with an adequate instrument. Such a stable light source is automatically provided in scintillator calorimeters using 238U as their passive absorber. By a suitable choice of the signal integration time (ADC gate width), the number of photons induced by the radioactive 238U decay can be made equivalent to the light generated by hadrons of 5 to 10 GeV \(^{102,103,104}\). Instead of or in addition to such light sources, many modern calorimeter facilities are using a complex system of light flashers, distributed from a light source (e.g. a N2 laser) to the individual photomultipliers via a fibre-optics system \(^{101,103,105-106}\).
In addition, remotely controlled, small radioactive sources scan the active calorimeter components (scintillator, wavelength shifters) and provide information on (possibly non-uniform) long-term changes\(^{[101,107]}\). Another alternative, frequently proposed, is the use of very stable particle accelerators providing low-energy particle beams of precisely known energy\(^{[108,109]}\).

An example of a system used in practice is shown in fig. 19, combining the use of U radioactivity, external radioactive sources, and a light-pulsing system.

The success of such attention to detail is demonstrated by the results shown in fig. 20: it is possible to maintain long-term stability at the \(1 - 2\%\) level\(^{[93]}\).

Calibration systems for calorimeters based on proportional-gain wire-chamber readout have to cope with both the inherent, comparatively large, gain variations between different wires, and the long-term global variations (changes in gas composition, pressure or temperature).

Adequate uniformity in gas-gain calorimetry can be achieved by controlling the mechanical tolerances. Such a dependence is minimized by using a rectangular tube geometry, a solution adopted for the majority of modern detectors. In very carefully constructed devices, gain variations of \(\sigma \sim 5\%\)^{[110,111]} to \(10\%\)^{[112]} are reported. Averaging of non-uniformities over the dimensions of the shower will reduce these gain variations to a level that should in most cases not affect the performance of these devices. The global gain variations due to gas composition, temperature and pressure are conveniently monitored with a suitable number of reference chambers^{[113,114]}; these calibration signals are sometimes used in a feedback circuit, adjusting the chamber HV to maintain constant global gain^{[115]}.

For charge-collecting calorimeters of the ion-chamber type (room-temperature liquids or LAr) excellent uniformity of response is ensured by controlling mechanical tolerances, and long-term stability is monitored by controlling the quality of the liquid medium. It is therefore sufficient to establish the absolute energy scale for a fraction of the modules of a detector and to transfer and maintain this scale with a precision charge measurement. This is conveniently done by injecting, with a precision pulse generator, a calibration charge into a precision calibration capacity of adequate stability (see also section 3.6.2).

3.6.3 Signal electronics

With increasing demands on the performance of calorimeters, the associated
electronics has developed into the most advanced and complex analog signal processing circuitry in instrumentation for particle physics. The electronics has to process the signal charge - delivered from a photomultiplier, a proportional wire chamber or an ionization chamber - and should therefore fulfil the following specifications:

a) A very large dynamic range: it should span the signals originating from minimum-ionizing particles (muons) to TeV-energy deposits of hadrons or relativistic ions. A dynamic range larger than $10^4$ with 15- to 16-bit effective ADC resolution is required.

b) Low-level precision measurements of calibration signals (e.g. radioactive sources) must be possible.

c) Frequently, timing information is required.

d) An adequate time response (96 ns bunch crossing at HERA, 16 ns or faster at the SSC or LHC) imposes sometimes stringent constraints.

e) Information for the first-level trigger must be provided within $\approx 1\mu s$ after a collision.

f) It must be adapted to system organization for $10^4$ to $10^5$ signal channels.

We illustrate the state-of-the-art in calorimetry front-end electronics with two examples. The functional analog readout for a scintillator-based calorimeter is shown in fig. 21 for the case of the ZEUS calorimeter, comprising $\sim 13000$ photomultiplier (PM) channels$^{116}$ . Each PM output is resistively split into low- and high-gain shapers (to cover the required dynamic range), to a trigger sum, to a circuit for measuring the noise from the depleted uranium, and to a termination. The low- and high-gain channels are sampled individually every 96 ns, permitting both an amplitude and a timing measurement of the PM signal. The analog sample and pipeline is a custom VLSI chip based on switched-capacitor techniques. A 5 $\mu$s analog delay provides adequate time for trigger decisions before signal processing is continued.

Signal processing from ion-chamber calorimeters has to cope with two additional specific problems:

i) The detector capacitance $C_D$ for practical devices is substantial ($\sim 1$ to $\sim 100$ nF), while the amplifier input capacitance $C_A$ of typical low-noise FETs is $\sim 10$ pF. If it is connected directly, the preamplifier 'sees' only a fraction of the produced charge in the ratio $C_A/C_D$. 

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ii) The detector capacitance $C_D$ and the cable inductance $L_C$ connecting the detector to the preamplifier limit the charge-transfer time $t_c \sim 3.5 \sqrt{L_C C_D}$ and hence the speed of the detection process and detector.

In the classical approach\textsuperscript{[114]}, in order to solve problem i) and to optimize the signal/noise ratio ($S/N$), a transformer is used to match $C_D$ to $C_A$, as is shown in fig. 22. Coupling with such a ($n : 1$) transformer reduces the source capacitance by $n^2$, while the charge is reduced only by $n$, resulting in an $S/N$ improvement of the factor $n$. The detailed analysis, using optimal bipolar pulse shaping of length $\lambda$, gives for the equivalent noise charge $ENC$ due to the series-noise\textsuperscript{[116,117]} $ENC \sim \sqrt{C_D/\lambda}$.

While the use of transformer matching results in optimal noise performance, it has two considerable practical drawbacks:

i) Transformers are quite bulky.

ii) Transformers use ferrite cores, which do not tolerate magnetic fields in access of $\sim 0.01$ T without external shielding.

These reasons, combined with the modern trend towards very high granularity and hence smaller detector capacitance, have led groups to circumvent the transformer matching problem by making the individual channel capacitance rather small ($C_D \approx 1$ nF) and accepting a certain degradation in $S/N$\textsuperscript{[114,115]}. A typical block diagram of a single channel of ion-chamber electronics is shown in fig. 23\textsuperscript{[114]}.

3.6.4 High-rate operation

In recent years the physics discovery potential of very high energy hadron colliders ($\sqrt{s} = 20 - 40$ TeV) was extensively discussed\textsuperscript{[120]}. Such machines permit the study of physics approaching the 1 TeV mass scale, provided operation of the collider and of the associated experiments is performed at luminosities $L \approx 10^{23} - 10^{24}$ cm$^{-2}$s$^{-1}$, to compensate for the extremely small production cross-sections of the interesting reactions.

Precision calorimetry is expected to be the instrument of choice at these machines, prompting several studies on the feasibility of calorimeter operation at rates of $10^4 - 10^9$ collisions per second\textsuperscript{[131,132]}. The average time between interactions will therefore be considerably shorter than the integration time for a hadronic shower measurement, which is typically $\approx 50$ ns or longer. There are,
however, two reasons why calorimetry still performs well:

i) A collision may produce $\sim 100$ secondary particles, depositing energy in perhaps 10% of the solid angle of a $4\pi$ detector. Measurement times on a particular readout channel may therefore extend over several collisions.

ii) At these very high luminosities, rare phenomena, revealed by very energetic jets of particles are searched for. The typical average inelastic collision deposits over an order of magnitude less energy, and may therefore be considered as physics noise affecting, but not necessarily masking, the measurement of the energetic events under study.

Several readout techniques can be considered for potential devices $^{[28]}$:

a) Scintillator calorimeters are in principle the fastest detectors, particularly if the light is measured directly, without conversion in wavelength shifters $^{[79]}$.

b) Ionization-chamber calorimetry, although intrinsically slower, may also offer adequate time response. Certain dielectric liquids, such as tetramethyl silane, are particularly interesting in this respect, since the drift time in small gaps may approach values as low as 20-30 ns $^{[123]}$.

The performance of ion-chamber calorimeters in a high-rate environment has been the subject of several studies. Crucial to such operation is the choice of bipolar-pulse shaping $^{[124]}$, so that the pile-up of several events within the sensitive time of the detector does not on average produce a net shift in the measurement of a large signal. For such signal shaping (with total length $\lambda$ of the bipolar weighting function), it can be shown that the pile-up of minimum-bias events with average energy $E_b$ occurring at a rate of $n$ per second will result in a pile-up noise contribution of $\sigma_{\text{pileup}} \approx E_b \sqrt{n\lambda/3}$.

The range of acceptable values of the product $n\lambda$ will therefore depend on the ratio of the energy $E_s$ of interesting signals compared to the background $E_b$. More detailed estimates were done $^{[121,122]}$, on which fig. 24 is based.

Consider, as an example, high-$p_T$ jet spectroscopy, for which an acceptance of $\Delta \Omega \approx 1$ sr is required. With state-of-the-art LAr calorimetry ($\lambda \approx 200$ ns) and interaction rates of $n \approx 10^8$ s$^{-1}$, the pile-up noise is estimated to be as small as $\sigma_{\text{pileup}} \approx 1.5$ GeV, surely acceptable for jet physics at the multi-hundred GeV scale.
Such studies have indicated that there appears to be no fundamental limitation to adequate calorimeter spectroscopy, even at the very high luminosities considered. However, a long list of formidable technical challenges, such as construction problems, trigger bias, radiation damage, etc., will obviously require the most careful attention.

The dependence of the electronic noise on the signal shaping time, as achieved in practical devices, is also shown in fig. 24. Again, for jet spectroscopy requiring 1 sr acceptance, and for rather short shaping times ($\lambda \approx 100$ ns), an electronics noise contribution of $2.5 - 5$ GeV is measured, depending on the drift velocity in the liquid medium, which is comparable to the noise contribution from pile-up. These relatively short response times are achievable, provided attention is given to two overriding engineering considerations:

i) The drift velocity of the ionization charge, which determines the induced current, must be adequately fast ($v_D \geq 1$ cm/$\mu$s).

ii) The time $t_c$ to transfer the charge from the electrodes to the amplifier, which ultimately limits the response of the ionization chamber, must be adapted to the system.

An analysis has shown that it may be $t_c$ which imposes the most stringent requirements on the calorimeter construction: $t_c \approx 3.5(L_c C_{det})^{1/2}$ and $\lambda \geq 5t_c$, where $L_c$ is the cable inductance and $C_{det}$ the detector capacitance. This very stringent limit on the cable inductance implies that the cable length $l$ should be shorter than 1 m to achieve the required value of $t_c$.

Compared with the relatively long shaping times required for accurate energy measurement, the achievable timing resolution on a high-energy event is much smaller. Timing resolutions of $\sigma \approx 3 - 4$ ns have been measured for energy deposits of a few GeV, improving as $E^{-1/2}$, and $\sigma \approx 1$ ns on 100 GeV energy deposits should be achievable with such calorimeters.

3.6.5 Trigger processors

The energy information from calorimeters is usually available in a rather short time interval, typically 50 to 500 ns after the particle impact. This important feature is, therefore, extensively used to select or trigger on interesting collisions, based on the pattern of the energy deposit.
The required selectivity depends on the type of collision under study. At today's hadron colliders, with collision rates of $\sim 1$ MHz, the typical trigger selectivity approaches 1:10$^5$ or better. Considerably larger rejection factors (1:10$^6$) will be required at future colliders, where collision rates will approach or exceed 100 MHz.

The choice of the trigger scheme is probably the most delicate and critical ingredient for successful experimentation at hadron colliders. While very high selectivity is required, novel or unexpected event topologies must obviously not be rejected in this selection process. It is thus not surprising that triggering at the future colliders is emerging as one of the main concerns in the preparation of experiments$^{[123,126,137,139]}$.

The selection of events usually proceeds through a sequence of trigger levels of increasing restrictivity and refinement. As an example we describe the decision flow of the trigger processor development for the UA1 calorimeter, representative of the many modern trigger systems$^{[129]}$. The flow-diagram is shown in fig. 25.

For the fast, first-level decision, signals from the very finely segmented calorimeter are summed to a certain degree, reducing the total number of 20000 channels to 1066 (548) trigger channels carrying e.m. (hadronic) energy information. These signals are encoded with Flash ADCs. The digital information is presented to memory look-up tables, from which the transverse energy $E_T$, the total energy $E$, and $E_T\sin\phi$ and $E_T\cos\phi$ are extracted.

At the first stage, information about e.m. clustering (for electron identification) is obtained. If any of the mentioned quantities exceeds a preset threshold, the event is presented to the second-level trigger for more refined analysis. The rejection of the first level typically exceeds 1 : 10$^3$ and is executed in less than 4 $\mu$s.

At the second stage, selectivity is increased by searching for two-dimensional patterns in e.m. energy deposit (localizing electrons) and improving the jet definition. Such information is the basis of the final trigger criteria.

The range of selection criteria is further enlarged with signals from detectors external to the calorimeter, such as the momentum of muon candidates from the muon detector, or the momentum of electrons from the central tracking detector. Typical decision times at the second level amount to $\sim 1$ ms and a rejection of 1:10 is achieved.
In the final, third level, a farm of several fast processors allows detailed event verification in $\sim 10$ ms, with a further reduction of a factor of 10.

3.7 MONTE CARLO STUDIES OF CALORIMETRY.

The development of calorimeters from crudely-instrumented hadron absorbers to finely-tuned precision instruments owes much to a number of cascade simulation codes.

The relative simplicity of the physics governing the electromagnetic showers has facilitated early Monte Carlo simulation. The present-day world-wide de facto standard, EGS, has undergone a series of revisions and refinements. The current version, EGS4\cite{123}, allows to track the shower electrons to zero kinetic energy and photons down to $\sim 10$ keV. It has successfully passed many detailed tests\cite{124} including one that may well be the ultimate, that of evaluating the absolute energy response to electrons within a few per cent in sampling calorimeters.

The physics, and consequently its simulation, is considerably more complex for hadronic showers. Over the last decade several programs have been developed, with the aim of simulating in all relevant detail the processes taking place in a hadronic cascade\cite{125,126,127}. As an example, the flow-chart of one of these detailed codes is shown in fig. 26\cite{128}.

These programmes continue to provide guidance to modern calorimetry development\cite{129,130}. A recent example of a simulation summarizes results on the possible compensation in U-calorimeters read out with Si diodes (fig. 27).

Besides these very detailed codes, which probe the fundamental properties of particle cascades and detectors, there is need of a second category of codes, involving fast shower simulation for studies requiring a large number of particles, such as trigger efficiencies, acceptance calculations, etc. These approaches are usually based on global parametrizations\cite{131}, parametric representation of hadronic interactions, evaluating individual $\pi^0$'s, energetic charged $\pi$'s and the low-energy nuclear cascades\cite{132}, or other fast sampling techniques\cite{133}.

3.8 CALORIMETER SYSTEMS

In the following discussion of calorimeter systems, we aim to show the great diversity of solutions adopted in the search of the 'best' solution adapted to a
specific physics application. Besides experimental considerations, the operating conditions of accelerators will influence the instrumental choices. We will explain these criteria, indicate strong points and weaknesses, and evaluate the trend in calorimetric approaches. Examples are selected of facilities in operation, in construction, or under preliminary evaluation.

3.8.1 Calorimeter facilities for fixed-target programmes

Among the largest facilities (considering the instrumented volume), we find detectors for neutrino studies, of which a recent version\textsuperscript{[139]} is shown in fig. 28. The design choices for this detector were driven by the need to achieve the best possible angular resolution for electrons (see section 3.3), a readout system allowing very good electron/hadron separation and muon-momentum measurement.

New high-granularity devices have also been constructed for experiments studying the hadronic production of jets\textsuperscript{[24,140-141,142]} and high-resolution missing energy\textsuperscript{[143]}. Choice of LAr readout allowed very-high-granularity detectors without any dead space, thus permitting a very good total-energy measurement. In one case uranium was chosen for best energy resolution up to very high energies. The studies of very rare events implied excellent measurement capabilities in the presence of rather high particle fluxes\textsuperscript{[24]} (see section 3.6).

Interesting and novel techniques are being applied in the very low-energy physics programme at LEAR. The kinematics of \(\bar{p}\)-nucleus collisions produces events which are best detected by a 4\(\pi\) geometry reminiscent of storage ring devices. One such detector uses CsI crystals as a high-quality photon detector\textsuperscript{[143]} These crystals have a very high light output, permitting detection with photodiodes, which can operate in strong magnetic fields\textsuperscript{[107]}. Compared with NaI, the choice of CsI was suggested by the shorter radiation length, allowing a more compact spectrometer construction and better mechanical properties, without incurring higher costs (per \(X_0\)).

The parameters of these facilities are summarized in Table II.

3.8.2 Calorimeter facilities at colliders

The calorimeter facilities devised during the last decade to be used in colliders, demonstrate the increasing importance of calorimetry and reflect a constant adaptation of techniques to the collider and physics environment\textsuperscript{[102,144]}.
The original calorimeter facilities at the CERN $p\bar{p}$ Collider have undergone major improvement programmes. The UA1 Collaboration are at present preparing an extremely advanced device, based on the use of the room-temperature liquid TMP in an ion-chamber mode\cite{143}. The group aims at good hermeticity, high granularity, good and uniform energy resolution, and good long-term stability.

Similar goals, but using conventional scintillator techniques, are pursued by the UA2 Collaboration\cite{144}. The CDF Collaboration, at the FNAL Tevatron collider, have chosen scintillator readout for the central coverage and proportional-gas-gain technology for the end-caps\cite{112,145}.

The D0 Collaboration are constructing a U/LAr calorimeter facility to be operated at the FNAL collider. It aims at good energy resolution ($e/h \leq 1.1$) for electrons and hadrons, and good granularity. The detector is housed in three independent cryostats, which introduces cracks in the $4\pi$ coverage and results in some loss of hermeticity\cite{146,147}.

For the new generation of $\epe$ facilities (see Table II) a number of hadron-calorimeter facilities have been constructed, although most of these do not emphasize state-of-the-art performance. Emphasis is rather given to e.m. shower measurements with good granularity. The very low collision rates allow technically simpler, slow readout systems.

The CLEO Collaboration has adopted an innovative solution to precision e.m. calorimetry, using an array of $\sim 7000$ CsI crystals, which permits an energy resolution of $\sim 2\%$ at 1 GeV\cite{148}.

The TRISTAN $\epe$ collider, now operating at $\sqrt{s} \leq 55$ GeV, will ultimately reach $\sqrt{s} \approx 65$ GeV if it is equipped with superconducting cavities. Three major experiments are operational. AMY is a very compact detector, which has pioneered very-high-field ($B \sim 3$ $T$) tracking\cite{149}. The TOPAZ detector\cite{150,151} also has e.m. calorimetry based on gas-readout in the end-caps, and uses a cylindrical lead-glass array in the $30^\circ < \theta < 150^\circ$ region, while the VENUS calorimeter uses both LAr and lead-glass e.m. calorimetry\cite{152,153}.

At Stanford, the linear accelerator has been ingeniously transformed into the Stanford Linear Collider (SLC), providing $\epe$ collisions at $\sqrt{s} \leq 100$ GeV. The MARK II detector\cite{144} has been upgraded and is at present installed at the SLC.
A very ambitious detector, SLD\textsuperscript{[185]}, is being completed and could move into the collision hall by the end of 1989.

All four LEP experiments have chosen proportional-wire-chamber readout techniques for their hadron calorimetry and have pushed the performance of this technique to new heights\textsuperscript{[189]}, particularly the ALEPH Collaboration\textsuperscript{[186]}. The solutions chosen for the e.m. calorimetry are mechanically and electrically different from those for the hadron detector. DELPHI\textsuperscript{[187]}, L3\textsuperscript{[184]}, and OPAL\textsuperscript{[44]} have adopted particularly performant technologies for their e.m. calorimetry.

We conclude from this short discussion on calorimeter facilities at existing $e^+e^-$ colliders that state-of-the-art hadron calorimetry has not been vigorously implemented. High-precision jet-physics needing the best possible resolution was not considered a high-priority topic. Recent successes using the missing-energy technique will probably call for a revision of this attitude. It is not surprising that SLD, which is the most recently designed experiment, is the first one to aim at high-quality hadron calorimetry.

To date, the most stringent requirements on hadron calorimetry have to be met by the experiments being prepared for HERA. The physics programme relies to a large extent on the precision measurements of the jet momenta, i.e. their energy and direction.

The two experimental groups\textsuperscript{[181,185]} at HERA have chosen very different calorimetry techniques, reflecting the sometimes subjective evaluation of the strengths and weaknesses of different techniques. In previous sections, we have already described the (expected) performance of these detectors. Figure 29 gives an impression of the very advanced design of the H1 calorimeter.

Looking beyond HERA towards the planned high-luminosity hadron colliders, we are witnessing an even stronger reliance on calorimetry as the principal spectroscopic tool. Conceptual experiments have been evaluated\textsuperscript{[186]}, from which a consensus emerged that the known detection principles are adequate to conceive the necessary experiments. The technical difficulties are, however, stupendous, which is summarized aptly as: "We know how to build the accelerator, but we don’t know yet how to build the experiments"\textsuperscript{[126,142]}.

The technical challenge lies in the development of techniques that offer the required radiation resistance\textsuperscript{[142]}, fast response in the environment of $10^9$ to $10^{10}$
collisions per second, signal processing from $10^6$ channels with accuracies of 16 - 18 bits, and trigger capabilities approaching a selectivity of $10^9$. Current thinking is summarized in the proceedings of the recent relevant workshops\textsuperscript{[160]}. 

3.8.3 Non-accelerator-based instruments

During the last ten years, a number of facilities have been constructed, mostly deep underground, to study some of the most fundamental questions in particle physics, such as the search for nucleon decay predicted by the Grand Unified Theories of the strong and electroweak interactions.

In the minimal SU(5) unification scheme, the proton lifetime is predicted to be in the range of $10^{30}$ years, with the dominant decay mode $p \rightarrow e^+ + \pi^0$. If this were true, a detector containing $10^{32}$ to $10^{33}$ protons (500 - 5000 tonnes of water) would in principle observe a few hundred to a few thousand proton decays per year\textsuperscript{[162]}.

The best experimental technique is to instrument several thousand tonnes of material sensitively enough to detect a fair fraction of the expected proton decay modes: a calorimeter! One important complication is the presence of an overwhelming background due to muons produced in the atmosphere, whence the need for all these experiments to be installed deeply underground, shielded by more than a kilometer of rock.

Present nucleon-decay experiments are of two different types:

i) Calorimeters using most frequently iron as the decay mass, finely subdivided and interleaved with active elements, mostly based on wire-chamber technologies.

ii) Instruments using ultra-pure water as the decay mass, with photomultipliers detecting the Čerenkov light produced by the decay products of a possibly disintegrating nucleon.

A summary of the nucleon-decay detectors now in operation is given in Table III\textsuperscript{[164]}.

Although the search for nucleon decay has been negative up to now, there are a number of very ambitious and advanced underground facilities in preparation. They address, besides more sensitive searches for nucleon decay, a wide range of topics: high-energy $\nu$ astronomy, very low-energy solar $\nu$ studies, search for magnetic monopoles, high-energy $\mu$ spectroscopy, etc.
A major new underground laboratory providing facilities for these experiments is in preparation under the Gran Sasso mountain in Italy. We mention two experiments that will use very novel detection techniques. The ICARUS detector is a 5000 t, continuously sensitive and homogeneous calorimeter, using liquid argon as the active material. Given the low event rates, ionization signals will be drifted over very large distances (typically 1 m) to reduce the overall number of readout channels.

Another experiment aims specifically at the study of very low-energy solar neutrinos. The target calorimeter is made from 30 t of GaCl₃, and the detection of solar neutrinos proceeds through the reaction $^{71}\text{Ga} + \nu_e \rightarrow ^{71}\text{Ge} + e^-$, with a threshold of $E_\nu > 233$ keV.

The ultimate calorimeter in size uses more than 1000 km$^3$ of the earth’s atmosphere. Very energetic cosmic-ray particles, incident on the upper layers of the atmosphere, will interact and initiate a hadronic cascade. The cascade particles excite the atmosphere (Čerenkov or fluorescent light), which is detected with an array of 67 light detectors (Fly's Eye)\cite{146}.

Results obtained to date are a measurement of the total cross-section for $pp$ scattering up to $\sqrt{s} = 15$ TeV and information on the shape of the cosmic-ray spectrum beyond $10^{19}$ eV\cite{146}.

3.8.4 Cryogenic detectors

There is a growing interest in calorimetric methods characterized by a cryogenic operating temperature, in the few mK to $\sim 1$ K range. Such detectors exploit either some specific properties of the superconductive phase of matter or the reduction in the thermal noise of the detecting medium (and the associated electronics). These methods promise energy measurements of considerably improved accuracy for the detection of energy deposits in the meV-eV range.

The development of these techniques is pursued because they may offer an experimental tool to answer some of the most fundamental questions in particle physics, such as

– the rest mass of neutrinos,

– the existence of weakly interacting massive particles (WIMP's), which may be a component of the dark matter in the Universe,
– the existence of magnetic monopoles,
– the solar neutrino flux at low threshold,
– the nuclear double $\beta$-decay.

Following earlier suggestions$^{[167,168,169,170]}$, a great variety of detectors have been considered$^{[171,172]}$, all of which are based on the following properties of matter at low temperatures:

i) Elementary excitations have very low energy. For example, Cooper pairs in superconductors have binding energies in the $10^{-6} - 10^{-3}$ eV range and may be broken by phonon absorption.

ii) The specific heat $C$ for dielectric crystals ($C_{lattice} \approx a[T/\Theta_D]^3$) and superconductors ($C \approx b \exp(-1/kT)$) decreases to very low values at cryogenic temperatures.

iii) Thermal noise in the detector and the associated electronics decreases.

iv) Several cryogenic-temperature phenomena provide specific signals (e.g. change in magnetization, latent heat release, quasi-particle multiplication) which may be the basis of detectors.

In the following, we select among the many ingenious proposals three categories of detectors which are widely studied$^{[171,172]}$.

**Bolometers.** These are the true 'calorimeters', where the energy deposition of particles in an insulating crystal at very low temperature may be measured with a resistive thermometer. The ultimate energy resolution (neglecting noise in the readout electronics) depends on the temperature $T$ and the mass $M$ of the crystal as $\Delta E \propto T^{5/2}M^{1/2}$, whence a sizeable increase in detector mass may be balanced by a modest decrease in temperature.

The rise-time of the signals from such devices is relatively fast (1 to 100 $\mu$s range). Energy resolutions as low as $\sigma \sim 7$ eV have been reported for 6 keV X-rays, approaching the range of interest for a measurement of the $\nu_e$ rest mass from $^3$H decay. Relatively large devices (close to 1 g Ge as absorber) have been developed$^{[174]}$; background suppression has been achieved by measuring, in addition to the temperature rise, a complementary signal such as scintillation light. This procedure allows particle identification, i.e. differentiation between recoil nuclei and minimum-ionizing particles based on the temperature/light ratio.

The principle thrust of present-day bolometry is directed toward large devices
(100 - 1000 g) for the search of neutrinoless double $\beta$-decay, where good energy resolution is crucial for background suppression, and for dark-matter searches through the detection of nuclear recoil, where sensitivity to energy deposits below 1 keV is required.

**Superconducting Tunnel Junctions (STJ).** The very low excitation energy of current carriers in superconductors ($\lesssim 10^{-3}$ eV) has led to the development of STJs, in which the quasi-particles and holes excited by incident radiation tunnel through a thin superconducting layer separating the two superconducting materials. For the detection of X-rays of a few keV, the energy resolutions observed to date are close to 0.1%.

Applications for $\nu$-mass measurements and solar-$\nu$-flux measurements might be contemplated. Such devices might also prove interesting as detectors of phonons produced in crystals, where ballistic phonons would be converted into quasi-particles.

**Superheated Superconducting Granules (SSG).** Type I superconductors can exhibit metastable states owing to a positive normal-superconducting interface energy. Type I samples may therefore remain superconducting in external magnetic fields in excess of the critical field $H_c$. This has been observed for metallic spheres with diameters in the 1 - 400 $\mu$m range.

SSG detectors are usually prepared as a colloid of metallic granules suspended in a dielectric matrix (e.g. paraffin). Heat deposited by a particle interaction would drive one or several granules normal, entailing a change of magnetic flux (disappearance of Meissner effect), which would be sensed by a macroscopic pickup coil.

Applications to the detection of solar neutrinos, based on the neutral-current process of elastic neutrino-nucleus scattering, appear attractive. Dark-matter searches, where the nuclear recoil flips only one sphere at best, require increased sensitivity, which might be achieved through a micro-avalanche mechanism$^{[172]}$.

Development of cryogenic detectors is actively pursued in a number of laboratories. They promise to open a new era in astro-particle physics. For the time being, studies of principles are being pursued, often involving fundamental research in solid-state physics and materials science. The feasibility of practical detectors of adequate size has yet to be shown, and their signal-processing requirements are at present far beyond the scope of the most advanced particle-physics instrumentation.
4. CONCLUSIONS AND OUTLOOK

The use of calorimetric detection methods in high-energy physics has rapidly evolved from a technique employed for some rather specialized applications (neutrino scattering) to the prime experimental tool in modern experiments.

This evolution, inspired by the physics goals of the experiments concerned, has gone hand in hand with crucial developments in the calorimeter technology itself. The sophistication of the instrumentation, the understanding of the basic principles of operation and of the limitations of the technique have all reached a very mature level, guaranteeing optimal exploitation possibilities.

Nevertheless, in view of the strongly increasing demands on calorimeter performance for future experiments, particularly at the proposed multi-TeV pp Colliders, further R&D is needed, which will have to focus on those calorimeter features which are likely to be essential in the next decade:

- hermeticity,
- energy resolution,
- rate capability,
- radiation resistance,
- electron/pion discrimination.

It is unlikely that one single instrument will emerge as the ultimate solution, best performing in all aspects listed above. Choosing a calorimeter technique for a particular experiment will remain a matter of evaluating (dis)advantages of different approaches.

We see two trends that are likely to shape detectors for future experiments. Firstly, compensating calorimeters will become the standard. As we pointed out in section 3.1, the compensation requirement does not necessarily imply the use of uranium absorber. When hydrogenous readout material is used (plastic scintillator, room-temperature liquids, gas) it can be achieved with a variety of absorber materials of which lead is probably the most attractive one.

Secondly, we expect a development towards integrated calorimetry, i.e. combining in one instrument the functions of e.m. and hadronic shower measurement, electron and muon identification; the traditional subdivision in an e.m. calorimeter and a hadron calorimeter will disappear.
Research and development and prototype studies will be an even more essential part of the experimental programme than in the present generation of experiments. The time scales involved, the size and the cost of the calorimeters simply do not permit design errors.

We hope that the information provided in this review may serve as guidance and encouragement for a continued perfecting of this very powerful and elegant experimental technique.

Acknowledgements

We are grateful to the many colleagues who have helped us in preparing this review by making their results available and discussing them with us.
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<table>
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<tr>
<th>Particle produced</th>
<th>Calorimeter technique</th>
<th>Comment</th>
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<tr>
<td>Electron, e</td>
<td>Charged particle initiating electromagnetic shower</td>
<td>Background from charge exchange $\pi^+ N \rightarrow \pi^0 + X$ in calorimeter; $\pi$ discrimination of $\sim 10$-$1000$ possible</td>
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<tr>
<td>Photon, $\gamma$</td>
<td>Neutral particle initiating electromagnetic shower</td>
<td>Background from photons from meson decays</td>
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<tr>
<td>$\pi^0, \eta, \ldots \rightarrow \gamma \gamma$</td>
<td>Invariant mass obtained from measurement of energy and angle</td>
<td>Classical application for electromagnetic calorimeters;</td>
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<tr>
<td>$\varphi, \phi, J/\psi, T, \ldots$ $\rightarrow e^+ e^-$</td>
<td>Visible energy $E_{vis}$ in calorimeter compared with momentum of particle</td>
<td>$E_{vis}^{\pi^0} = (\vec{p}<em>e^2 + m_e^2)^{1/2} - (+)m</em>\pi$ Protons (antiprotons) identified up to $4(5)$ GeV/c; deuterons (antideuterons) correspondingly higher</td>
</tr>
<tr>
<td>Protons, deuterons, tritons ..., and their antiparticles</td>
<td>Visible energy $E_{vis}$ in calorimeter compared with missing momentum</td>
<td>Important tool for $e^+ e^- \rightarrow \nu(\bar{\nu}) + X$ and at CERN Collider (FNAL p$\bar{p}$ collider), pp(p$\bar{p}$) $\rightarrow \nu(\bar{\nu}) + X$</td>
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<tr>
<td>(Anti)neutrino</td>
<td>Visible energy $E_{vis}$ in calorimeter compared with missing momentum</td>
<td>Background from non-interacting pions or $\pi$ and $K$ decays</td>
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<tr>
<td>Muon</td>
<td>Particle interacting only electromagnetically (range). $E_{vis}$ compared to $\vec{p}$.</td>
<td>Some discrimination perhaps possible based on detailed (longitudinal) shower information</td>
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<td>Neutron or $K^0_L(\bar{\nu}, \bar{K}^0_L)$</td>
<td>Neutral particle initiating hadronic shower</td>
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<td>Accelerator</td>
<td>Facility</td>
<td>Principal physics goals</td>
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<td>Top-quark search; mW, mZ; physics beyond SM; QCD tests.</td>
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<td>VENUS</td>
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<td>CERN LEP $\sqrt{s} \leq 200$ GeV (reached in several improvement programmes)</td>
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<td>Precision tests of SM; t-quark and Higgs search</td>
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<td>High-lumin. hadron colliders</td>
<td>Physics of the 1 TeV scale [e.g. massive Higgs, SUSY particles]</td>
<td>Need for compensation at $e/\pi \leq 1.1$ level. Different techniques may be viable</td>
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### Table III
Properties of the nucleon decay detectors

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<th>Experiment</th>
<th>Total mass (t)</th>
<th>Detector granularity</th>
<th>Depth (mwc)</th>
<th>Detector elements</th>
<th>Lifetime sensitivity (years)</th>
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<td>KGF</td>
<td>140</td>
<td>Iron 3 mm</td>
<td>7600</td>
<td>1700 proport.</td>
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<tr>
<td>Soudean I</td>
<td>30</td>
<td>Taconite 2 cm</td>
<td>1800</td>
<td>3456 proport.</td>
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<td>NUSEX</td>
<td>150</td>
<td>Iron 1 cm</td>
<td>5000</td>
<td>47000 streamer</td>
<td>$10^{31}$</td>
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<tr>
<td>Frejus</td>
<td>900</td>
<td>Iron 3 mm</td>
<td>4200</td>
<td>$10^6$ flash tubes</td>
<td>$10^{32}$</td>
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<tr>
<td>HPW</td>
<td>800</td>
<td>Water</td>
<td>1600</td>
<td>704 PMTs</td>
<td>$10^{33}$</td>
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<td>Kamioka</td>
<td>3000</td>
<td>Water</td>
<td>2700</td>
<td>1044 PMTs</td>
<td>$10^{33}$</td>
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<td>IMB</td>
<td>8000</td>
<td>Water</td>
<td>1600</td>
<td>2048 PMTs</td>
<td>$10^{33}$</td>
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FIGURE CAPTIONS

1. Shower development induced by few-MeV nuclear $\gamma$'s. In diagramme a), one possible sequence of absorption processes is shown, with the energies of the $e^+$, the $e^-$'s, and the $\gamma$'s given in keV. The $\gamma$-spectrum measured with a Ge(Li) crystal that only partly contains the showers initiated by (among others) the 3370 keV $\gamma$ is shown in diagrammes b). The total-containment peak (3369.9 keV), the single-(2858.9 keV) and double-escape peak (2347.8 keV), and the continuum background reflect the different degrees of absorption that may occur in this crystal (see text).

2. The cross-sections for pair production, Compton scattering and photoelectric effect, as a function of the photon energy in carbon (a), iron (b), and uranium (c). The fractional energy loss by radiation and ionization, as a function of the electron energy in carbon (d), iron (e), and uranium (f).

3. The energy deposit as a function of depth, for a 10 GeV electron shower developing in aluminium, iron, and lead, showing approximate scaling of the longitudinal shower profile, when expressed in units of radiation length, $X_0$. Results of EGS4 calculations.

4. The lateral distribution of the energy deposited by a 1 GeV e.m. shower in lead, at various depths. Results of EGS4 calculations.

5. The energy loss distributions, $\Delta E_\mu$, for 8 - 200 GeV muons, measured in a 8.5 nuclear interaction lengths deep uranium/plastic-scintillator calorimeter. The dashed line, drawn to guide the eye, corresponds to the most probable energy loss, measured for 200 GeV muons. Data from ref. 12.

6. Longitudinal (top diagramme) and lateral (lower diagramme) shower profiles for 300 GeV $\pi^-$ interactions in a block of uranium, measured from the induced radioactivity. The ordinates indicate the number of radioactive decays of a particular nuclide, produced in the absorption process of the high-energy pion. Since the different nuclides are produced by different types of shower particles, such experimental data may yield valuable information on details of the shower development process (from ref. 13).

7. The leakage as a function of the detector depth, for pions of 5 - 210 GeV, measured in a uranium/plastic-scintillator calorimeter. Data from ref. 25.
8. The fraction of the ionization energy deposited in the active layers by non-interacting protons, in various calorimeter configurations. From ref. 16.

9. Experimental observation of the consequences of $e/h \neq 1$. Results of measurements on pion absorption in undercompensating$^{24}$, compensating$^{22}$, and overcompensating$^{26}$ calorimeters. In diagramme a), the energy resolution $\sigma/E \cdot \sqrt{E}$ is given as a function of the pion energy, showing deviations from scaling for non-compensating devices. In diagramme b), the signal per GeV is plotted as a function of the pion energy, showing signal non-linearity for non-compensating detectors. The signal distribution for monoenergetic pions (the line shape, diagramme c) is only Gaussian for the compensating calorimeter.

10. The signal ratio $e/h$ for uranium calorimeters employing different readout materials, as a function of the ratio of the thicknesses of absorber and readout layers. Results of experimental measurements are included. From ref. 15.

11. The $e/h$ signal ratio as a function of Birk's constant $k_B$, for TMP calorimeters with uranium (a) and lead (b) absorber. The liquid gaps are 2.5 mm wide. From ref. 20.

12. The HELIOS calorimeter as a high-resolution spectrometer. Total energy measured in the calorimeter for minimum-bias events, showing the composition of the CERN heavy-ion beam. Data taken from ref. 12.

13. The ratio of the e.m. to hadronic response as a function of energy, for various calorimeter configurations, showing the non-linearity for hadron detection at low energy.

14. The ratio of the nuclear interaction length and the radiation length as a function of $Z$.

15. Time distribution of the full width at half maximum for 150 GeV electron and pion pulses from a lead/scintillation-fibre calorimeter. Data from ref. 79.

16. Two-jet mass resolution as a function of the two-jet mass and for various assumptions on the detector performance. See ref. 97 for more details.
17. Two-jet invariant-mass distribution from UA2. The smooth curves are the results of the best fits to the QCD background alone (curve a) or including two Gaussians describing W and Z decays (curve b). The measured width is 8 GeV, of which 5 GeV can be attributed to non-ideal calorimeter performance\[93\].

18. Jet resolution for an infinitely thick 4π calorimeter, assuming a Feynman-Field-like fragmentation function. The advantage of a (nearly) compensated calorimeter is particularly evident at very large jet energies. From ref. 97.

19. Schematic arrangement of the light flasher calibration system being built for the ZEUS calorimeter facility. One N₂ laser is the source of light, which is distributed in two stages to all of the approximately 13000 photomultipliers. Provision is made for linearity measurements, using remotely controlled neutral-density filters, absolute light level monitoring [with vacuum photodiodes, NaI(²⁴¹Am) light sources and Si photodiodes] and pulsing with LEDs for timing and triggering purposes (from ref. 80).

20. Long-term stability of a number of UA2 calorimeter modules. After several years of operation, remeasurement in a test beam demonstrated the validity of the energy scale within σ ~ 2%.

21. Analog readout architecture for the photomultiplier signals of the ZEUS calorimeter. The signals are split, shaped, sampled and delayed in a custom VLSI chip, and subsequently multiplexed[110].

22. Transformer matching of an ion-chamber calorimeter with capacitance C_D to the input of a preamplifier.

23. Block diagram of a single channel for a liquid-argon calorimeter, showing the preamplifier, the shaper, and the data-acquisition section.

24. Estimates (solid lines) of pile-up noise (left ordinate) as a function of the product of the shaping time \( \lambda \) and the collision rate \( n \) (bottom abscissa) for two different sensitive areas. It is compared with the typical electronic noise, as realized in the HELIOS U/LAr calorimeter (dashed lines), as a function of the signal shaping time \( \lambda \) (right-hand ordinate and top abscissa).

25. Decision flow in the UA1 trigger processor.
26. Flow-chart of one of the hadronic cascade codes\textsuperscript{[134]}.

27. The calculated variation of $\epsilon/h$ and $\sigma/\sqrt{E}$ with the thickness of a fibreglass sheet placed between the 2 mm uranium plates in a U-Si calorimeter and the silicon detectors. Without Si a slight overcompensation is expected, which can be tuned by changing the thickness of G10\textsuperscript{[135]}.

28. Overview of the CHARM II detector. One of the inserts shows the use of several techniques (scintillator counters, streamer tubes, cathode pick-up strips) for the energy and direction measurement of the showers. The detector is combined with modules of the CDHS $\nu$-detector (no longer operational), which are used for muon momentum analysis.

29. Partial cross-section through the H1 liquid-argon calorimeter, which has rotational symmetry about the beam axis. Shown is the transverse and longitudinal segmentation, which permits a quasi-projective tower geometry, pointing to the interaction point IP.
Fig. 2

LONGITUDINAL DEVELOPMENT
EM SHOWERS (EGS4, 10 GeV e⁻)

Fig. 3
Fig. 4

Fig. 5
PLATE 139 (4λ)

- $^{237}\text{U}$
- fission products
- $^{239}\text{Np}$

Fig. 6
Fig. 9
Fig. 10
Fig. 11

Fig. 12
Fig. 13

Fig. 14
Fig. 15

Two-jet mass resolution

- a Ideal detector
- b Cell level
- c Cluster level
- d Cluster level without vertex

Fig. 16
Fig. 17

 UA2
 W, Z → q̅q

\[ \frac{dN}{dm} \text{ (GeV}^4) \]

\[ m \text{ (GeV)} \]

(a) (b)

W Z

Fig. 18

\[ \frac{\sigma(E)}{\langle E \rangle} \]

\[ E_{\text{jet}} \text{ (GeV)} \]

Cu: \[ \sigma(E)/E = 0.48/\sqrt{E}; \] e/π = 1.48

U: \[ \sigma(E)/E = 0.37/\sqrt{E}; \] e/π = 1.11
Fig. 19

mean 0.993
rms 0.021
recalibration after 5 years

UA2

Fig. 20
Fig. 21

Fig. 22
Fig. 23

Fig. 24
Calorimeter Trigger

≈1700 bytes ADCs

Convert to $E_t$, $E$, $E_t \sin \phi$, $E_t \cos \phi$

Electrons

- Compare to local $E_t$ thresholds
  - Find 2-d e.m. clusters
  - Count clusters

Jets

- Compare to local $E_t$ thresholds
  - Find 2-d jet clusters
  - Count clusters

Global sums

- Energy adding tree
  - Compare to global energy thresholds

External signals

Final decision: combinations of conditions

1 bit trigger

Fig. 25
CALOR

HETC
HIGH ENERGY HADRONIC
TRANSPORT CODE

$\pi^+, \gamma, e^\pm$

SPECT
HADRONIC ANALYSIS
CODE

$\nu < 20$ MeV

MORSE
LOW ENERGY NEUTRON
TRANSPORT CODE

EGS
ELECTRON-POSITRON
AND GAMMA-RAY
TRANSPORT CODE

$\gamma$

FINAL
COMBINE AND ANALYSE
RESULTS FROM
TRANSPORT CODES

Fig. 26

![Plot of HETC/EGS/MORSE Calculations](image)

- 2 mm U/0.4 mm Si
- $e/\pi$
- 10 GeV $\pi^-$
- $\sigma/\sqrt{E}$

Fig. 27