Searches for New Physics at the Compact Muon Solenoid Experiment and Precision Timing Calorimetry

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To my parents, brother, wife, and son
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ABSTRACT

In this thesis, we present several searches for beyond the standard model physics in proton-proton collisions recorded by the Compact Muon Solenoid Experiment at center-of-mass energy of 8 and 13 TeV. We search for particle dark matter in events with two or more jets and missing transverse momentum at $\sqrt{s} = 8$ TeV. In this search we use the razor variables to discriminate signal from background events and thus improve the overall sensitivity of the analysis. We observe agreement between the observation and the background estimation. The interpretation of the results is carried out in the context of an effective field theory that couples the standard model quarks to the dark matter candidate. A search for anomalous production of Higgs bosons using 15.3 fb$^{-1}$ of proton-proton collisions at $\sqrt{s} = 13$ TeV is also presented; this search selects events with a Higgs boson in association with jets, where the Higgs candidate decays into two photons. We also employ the razor variables ($M_R, R^2$) to discriminate signal from background. We observe an excess of events in one of the search bins with relatively high values of $M_R$ and $R^2$. The interpretation of this analysis is pair production of bottom squarks in the context of supersymmetry, this model is also presented in one of the appendices of this thesis. In the other appendix of this thesis, we present a search for new phenomena in high-mass diphoton events using 12.9 fb$^{-1}$ of proton-proton collisions at $\sqrt{s} = 13$ TeV. This search observed a significant excess (3.4 standard deviations, local) with 2015 data at a diphoton invariant mass of 750 GeV, equivalent to $\approx 20\%$ of the current dataset. By repeating the search with the larger dataset collected in 2016, we found that the aforementioned excess has been greatly disfavored. Additionally, in order to confirm the robustness and correctness of the data analysis techniques used in this search, we have carried out a second – completely independent – analysis, which confirms the absence of an excess at a diphoton invariant mass of 750 GeV.

We also present detector research and developments studies of electromagnetic calorimeters equipped with precision timing capabilities. We present several calorimeter prototypes that were tested at the Fermilab Test Beam Facility. These prototypes include LYSO-based calorimeters, tungsten-LYSO “shashlik” sampling calorimeters, micro-channel-plate sampling calorimeters, and silicon-based sampling calorimeters. The results of these studies indicate that time resolutions of the order of $\approx 30$ ps are readily available when measuring electromagnetic showers. A discussion about the applications of precision timing in high energy physics experi-
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8.11 The non-resonant background yields, SM Higgs background yields, best fit signal yields, and observed local significance are shown for the signal plus background fit in each search region bin. The uncertainties include both statistical and systematic components. The non-resonant background yields shown correspond to the yield within the window between 122 GeV and 129 GeV and is intended to better reflect the background under the signal peak. The observed significance for the bins in HighRes and LowRes categories are identical because they are the result of a simultaneous fit. The significance is computed using the profile likelihood, where the sign reflects whether an excess (positive sign) or deficit (negative sign) is observed.

9.1 Tabulated values for $L_{rad}$ and $L'_{rad}$ from Y. S Tsai.

B.1 Photon isolation requirements, as in Ref [178]. The photon isolation variables, $I_y$, $I_n$, and $I_\pi$, are computed by summing the transverse momenta of photons, neutral hadrons, and charged hadrons, respectively, inside an isolation cone of radius $\Delta R = 0.3$ around the selected photon.

B.2 HighRes bin numbering scheme as in Ref. [237].
Part I

Preliminaries, the Standard Model, and Dark Matter
Chapter 1

INTRODUCTION

Particle physics is perhaps facing one of the biggest crossroads since the discovery of the electron in 1897. The subject evolved from having just one particle to have a catalog of particles and their possible interactions, and even explain the origin of the particles masses. This knowledge is encoded in what we know today as the Standard Model (SM) of particle physics, the most precise and perhaps the most successful theory that humankind has formulated. The SM is a quantum field theory that sets the rules by which the fundamental particles that we have observed interact with each other. These interactions compose three of the four fundamental force we know: the strong, weak, and electromagnetic interactions, leaving gravity aside. Since its formulation in the 1960s, many of the SM predictions have been experimentally confirmed: at hadron colliders, we have produced the W and Z bosons, the top quark, and recently the last piece of the puzzle, the Higgs boson, has been observed by the ATLAS and CMS collaborations [94, 17]. Precise measurements of the Z boson properties have been matched by accurate calculations to the level of one part in a million. The mechanism by which the SM accounts for C, P, and CP violation were experimentally confirmed with dedicated low-energy experiments, without giving any sign of CPT violation. However, despite the success and completeness of the SM, we are now faced with fundamental questions, both experimentally and theoretically motivated:

- Why is the Higgs boson mass close to the weak-force energy scale while its value is sensitive to the ultraviolet completion of the theory through radiative corrections (the fine tuning problem)?
- Is there a unification of the gauge couplings closer to the Planck scale?
- What is the nature of dark matter, whose existence has only been inferred by gravitational anomalies in astrophysical observations?
- What is the nature of the matter/anti-matter asymmetry observed in the universe?
• What is the nature of dark energy, whose existence provides an explanation for the expansion of the universe?

• Is there a quantum theory of gravity?

This thesis is more concerned with the first three bullets, which can actually be answered with a single theory: supersymmetry, a quantum field theory that relates fermions, and bosons [218, 143, 252, 131, 201, 109, 150]. Supersymmetry tackles these questions by adding a dark matter candidate to the particle spectrum, unifying the gauge couplings at about the Planck scale, and alleviating the fine tuning of the Higgs mass.

Although supersymmetry is a very compelling theoretical framework, it is not needed for having a suitable dark matter candidate. In fact, in order to match the observed dark matter relic density, there are just two conditions that need to be satisfied. These are the strength of the interaction of the dark matter (DM) candidate – here it is assumed that the DM candidate is a fundamental particle – with the SM particles is at the level of the weak interaction, and the mass of the DM candidate is about 100 GeV. This realization is called the weakly interacting massive particle (wimp) miracle. This led to the idea that DM candidates can be produced at particle colliders by just inverting the direction of interaction (see Figure 3.6), i.e. two SM particles annihilating into two DM candidates. Unfortunately, this event topology will leave no trace on the particle detectors due to the weakly interacting nature of the DM candidate, and therefore another particle must be produced in the event; the latter is easily resolved by the production of additional particles via initial-state radiation (ISR) off the incoming SM particles. All of the above led to collider searches in events with one highly-energetic jet or photon and substantial momentum imbalance. These searches became known as monojet [24, 95] and monophoton [180, 23], respectively.

Another line of thought, driven by experimental considerations, is the fact that there has to be new phenomena, since the SM falls short on explaining some of the current experimental observations. This realization gives ground to what is called model-independent searches, in which the events are selected based on interesting topologies rather than a particular theoretical model. Examples of such data analyses are dijet and diphoton resonance searches. Another way to probe new physics is to search for anomalous production of Higgs bosons, where new phenomena could enhance the SM Higgs production or decay rates. In this case one can just measure
the Higgs production rate inclusively or in specific phase spaces (e.g., vector-boson production). The comparison between the measured cross sections and the predicted SM values allows to probe new physics. These searches have recently been enabled by the measurements of the Higgs boson properties.

The broad experimental programs established by the ATLAS and CMS collaborations rely on the good performance of the particle detectors, reconstruction algorithms, as well as the large datasets provided by the Large Hadron Collider (LHC). The High-Luminosity upgrade of the LHC will significantly boost the sensitivity to rare processes but at the cost of increasing the pileup interactions to about 200. This high pileup environment will deteriorate particle reconstruction and identification due to the large occupancy in the detector. One solution to alleviate this detrimental effect is to have a calorimetric device capable of delivering a time stamp for particle detection with a resolution of about 30 ps (approximately 1 cm in the z-axis). Detector research and development (R&D) is crucial in order to make precision timing calorimetry a reality that could enhance the potential discovery and characterization of new physics. First results along this research path are presented in this thesis.

This thesis is organized in five parts: the first part gives a brief introduction to the main theoretical and phenomenological considerations covered by the experimental searches in the following parts; the second part provides an introduction to the LHC and the Compact Muon Solenoid Experiment where the searches presented in this thesis are carried out; the third part covers in detail two searches for beyond the SM (BSM) physics with razor variables using data collected by the CMS experiment at a center-of-mass energy of 8 TeV and 13 TeV; the fourth part presents the research and development on precision timing calorimetry that we carried out at Fermilab and CERN; the fifth part – the appendices – presents another search for new resonances in high-mass diphotons using 13 TeV data collected by the CMS experiment as well as a reinterpretation of the excess observed by CMS in events with SM Higgs produced in association with jets at 8 TeV.
2.1 The Standard Model of Particle Physics

The Standard Model (SM) of particle physics is a renormalizable quantum field theory based on symmetries and the gauge principle \([155, 251]\). The SM explains the electromagnetic, weak, and strong interactions, as well as having a complete catalog of all subatomic particles known. The interactions between the fermions (spin 1/2 particles) are realized by the exchange of force carriers (spin-1 particle).

The SM is represented by the symmetry group \( \text{SU}(3)_C \times \text{SU}(2)_L \times \text{U}(1)_Y \), where each of the fundamental forces, represented by gauge fields, corresponds to one of symmetry groups. This is better understood by the following diagrammatic representation:

\[
\begin{array}{ccc}
\text{SU}(3)_C & \times & \text{SU}(2)_L & \times & \text{U}(1)_Y \\
\downarrow & & \downarrow & & \downarrow \\
G^\alpha_\mu & & W^a_\mu & & B_\mu \\
\alpha = 1, \cdots, 8 & & a = 1, 2, 3
\end{array}
\]

where \( G^\alpha_\mu \) represents the eight boson, the gluons, that take part in the strong interaction and are associated with the \( \text{SU}(3)_C \) term; \( W^a_\mu \) represents the three bosons that take part in the weak interaction and are associated with the \( \text{SU}(2)_L \); while \( B_\mu \) represents the boson associated with the hyper-charge \( \text{U}(1)_Y \) term. The latter four bosons mix to form the most commonly known \( W^\pm \) and \( Z \) bosons of the weak interaction, and the photon (\( \gamma \)) of the electromagnetic interaction.

The particles that make up matter are represented by fermion fields in the form of left- and right-handed Weyl spinors. These fermions are divided into two categories: quarks (u, d, c, s, t, and b), and leptons (e, \( \mu \), \( \tau \), \( \nu_e \), \( \nu_\mu \), and \( \nu_\tau \)). Quarks are the only fermions that experience the strong interaction. Both are further categorized into three generations of matter – where (e, \( \nu_e \)) and (u,d) are in the first generation and (\( \tau \), \( \nu_\tau \)) and (t,b) are in the third generation – with particles masses increasing in the same order as the generations. Figure 2.1 shows the whole catalog of particles and interactions in the standard model, including their categorization, and the Higgs boson, which will be discussed in the following section.
The dynamics and kinematics of the SM are controlled by the Lagrangian density, which in conjunction with the particle content and force carriers completes the theory. The Lagrangian density is presented below in its compact expression:

\[
\mathcal{L}_{\text{SM}} = -\frac{1}{4} B^{\mu\nu} B_{\mu\nu} - \frac{1}{4} W^{\alpha}_{\mu\nu} W_{\mu\nu}^{\alpha} - \frac{1}{4} G^{\mu\nu}_{\mu\nu} G^{\mu\nu}_{\mu\nu} \quad \text{(gauge terms)}
\]

\[
+ \bar{\ell} L \tilde{\sigma}^{\mu i} D_{\mu} \ell_{L} + \bar{e}_{R} \sigma^{\mu i} D_{\mu} e_{L} + \bar{\nu}_{R} \sigma^{\mu i} D_{\mu} \nu_{L} \quad \text{(lepton kinetic terms)}
\]

\[
+ \bar{q}_{L} \tilde{\sigma}^{\mu i} D_{\mu} q_{L} + \bar{u}_{R} \sigma^{\mu i} D_{\mu} u_{L} + \bar{d}_{R} \sigma^{\mu i} D_{\mu} d_{L} \quad \text{(quark kinetic terms)}
\]

\[
+ \mathcal{L}_{\text{Higgs}} + \mathcal{L}_{\text{Yukawa}} \quad \text{(Higgs and Yukawa terms)},
\]

(2.1)

where \( \ell_{L} = \begin{pmatrix} e_{L} \\ \nu_{L} \end{pmatrix} \) is the lepton SU(2) \( L \) doublet, \( q_{L} = \begin{pmatrix} u_{L} \\ d_{L} \end{pmatrix} \) is the quark SU(2) \( L \) doublet, \( D_{\mu} \) is the corresponding covariant derivative, and \( \sigma_{\mu\nu} \) is the identity and the Pauli matrices \( (\sigma_{\mu} = 1, \sigma^{i}) \). The \( \mathcal{L}_{\text{Higgs}} \) and \( \mathcal{L}_{\text{Yukawa}} \) are presented in sections 2.2 and 2.3, respectively. Table 2.1 presents the matter field representation in the SM gauge group.

2.2 The Higgs Boson and Electroweak Symmetry Breaking

In order to maintain the local symmetries, gauge theories prohibit explicit mass terms for the gauge bosons in the SM. Therefore the observed masses of the gauge

\[
\begin{array}{cccc}
\text{Particle} & \text{Mass} & \text{Charge} & \text{Spin} \\
up & >2.3 \text{ GeV} & 2/3 & 1/2 \\
\text{charm} & >1.375 \text{ GeV} & 2/3 & 1/2 \\
t & >173.07 \text{ GeV} & 2/3 & 1/2 \\
gluon & >126 \text{ GeV} & 0 & 1 \\
H & \text{Higgs boson} & \text{Higgs boson} & \text{Higgs boson} \\
\end{array}
\]
Table 2.1: Group representation of the matter fields in the SM.

<table>
<thead>
<tr>
<th>field</th>
<th>SU(3)$_C$</th>
<th>SU(2)$_L$</th>
<th>U(1)$_Y$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$q_L$</td>
<td>3</td>
<td>2</td>
<td>1/6</td>
</tr>
<tr>
<td>$\ell_L$</td>
<td>1</td>
<td>2</td>
<td>-1/2</td>
</tr>
<tr>
<td>$u_R$</td>
<td>$\bar{3}$</td>
<td>1</td>
<td>-2/3</td>
</tr>
<tr>
<td>$d_R$</td>
<td>$\bar{3}$</td>
<td>1</td>
<td>1/3</td>
</tr>
<tr>
<td>$e_R$</td>
<td>1</td>
<td>1</td>
<td>1</td>
</tr>
<tr>
<td>$h$</td>
<td>1</td>
<td>1</td>
<td>1/2</td>
</tr>
</tbody>
</table>

bosons must be attributed to a different mechanism taking place in nature. The gauge boson masses in the SM are realized by the spontaneous breaking of the SU(2)$_L \times U(1)_Y$ symmetry, which is induced by the specific form postulated for the SM Higgs potential [127, 153, 151, 149, 152, 184]. The best way to understand the Higgs mechanism is to closely look at the Lagrangian density:

$$\mathcal{L}_{\text{Higgs}} = (D^\mu \Phi) \dagger (D^\mu \Phi) + V(\Phi); \quad V(\Phi) = -\mu^2 \Phi \dagger \Phi + \lambda (\Phi \dagger \Phi)^2,$$  \hspace{1cm} (2.2)

where $D^\mu$ is the covariant derivative; $\Phi$ is a spin-0 complex field, and a SU(2)$_L$ doublet with weak hyper-charge $Y = 1/2$. The field is more easily represented as a SU(2)$_L$ doublet in the following fashion:

$$\Phi = \begin{pmatrix} \phi^+ \\ \phi^0 \end{pmatrix}.$$  \hspace{1cm} (2.3)

When $\mu^2 > 0$, the potential $V(\Phi)$ exhibits the commonly known “Mexican hat” shape, shown in Figure 2.2, with a minimum which does not preserve the original SU(2)$_L \times U(1)_Y$ symmetry. Therefore the scalar field acquires a non-zero vacuum expectation value (vev):

$$\langle \Phi \rangle \equiv \langle 0 | \Phi | 0 \rangle = \frac{1}{\sqrt{2}} U(x) \begin{pmatrix} 0 \\ v \end{pmatrix}; \quad v = \sqrt{\frac{\mu^2}{\lambda}},$$  \hspace{1cm} (2.4)

where $U(x)$ is a unitary transformation that transforms the field into the degenerate solution. An important consequence is that the vev of field preserves a $U(1)$ symmetry from the original SU(2)$_L \times U(1)_Y$ symmetry of the Lagrangian. Therefore the full electroweak symmetry of the SM, SU(2)$_L \times U(1)_Y$, is spontaneously broken into $U(1)_{\text{EM}}$. 

Figure 2.2: The shape of the Higgs potential (“Mexican hat”). The degeneracy of the potential is observed along the azimuthal angle

This spontaneous breaking of the $\text{SU}(2)_L \times \text{U}(1)_Y$ symmetry is responsible for the appearance of masses to 3 of the four gauge bosons in the electroweak sector. This is called the Higgs mechanism. The masses become apparent when replacing the Higgs kinetic term in the Lagrangian with the vev:

\[
(D^\mu \Phi)^\dagger (D^\mu \Phi) \rightarrow \Delta \mathcal{L} = \frac{1}{2} \begin{pmatrix} 0 & v \end{pmatrix} (gA^a_\mu \tau^a + g'B_\mu)(gA^{b\mu} \tau^b + g'B^b) \begin{pmatrix} 0 \\ v \end{pmatrix}. \tag{2.5}
\]

Evaluating the matrix products, using $\tau^a = \sigma^a/2$ and $\{\tau^a, \tau^b\} = \delta^{ab}/2$, we find

\[
\Delta \mathcal{L} = \frac{v^2}{8} \left[ g^2 (A^1_\mu)^2 + g^2 (A^2_\mu)^2 + (-gA^3_\mu + g'B_\mu)^2 \right]. \tag{2.6}
\]
This forms the mass matrix squared for the gauge boson in the \((A_i^\mu, B_\mu)\) basis

\[
m^2 = \left(\frac{v}{2}\right)^2 \begin{pmatrix}
g^2 & 0 & 0 & 0 \\
0 & g^2 & 0 & 0 \\
0 & 0 & g^2 & -gg' \\
0 & 0 & -gg' & g^2
\end{pmatrix}.
\] (2.7)

By diagonalizing this matrix, it is clearly observed that there are three massive and one massless gauge boson, the linear combination of the gauge fields and their respective masses are the following:

\[
\begin{align*}
W^\pm_\mu &= \frac{1}{\sqrt{2}} (A^1_\mu \mp A^2_\mu) \quad \text{with mass} \quad m_W = g\frac{v}{2} \\
Z^0_\mu &= \frac{1}{\sqrt{g^2 + g'^2}} (g A^3_\mu - g' B_\mu) \quad \text{with mass} \quad m_Z = \sqrt{g^2 + g'^2}\frac{v}{2} \\
A_\mu &= \frac{1}{\sqrt{g^2 + g'^2}} (g' A^3_\mu + g B_\mu) \quad \text{with mass} \quad m_A = 0.
\end{align*}
\] (2.8)

Besides providing the Higgs mechanism, the inclusion of the \(SU(2)_L\) field in the SM predicts the presence of a self-interacting massive spin-0 boson, and this is realized by the fluctuation of the field around the vev, i.e.

\[
\Phi = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v + h(x) \end{pmatrix}.
\] (2.9)

Now, collecting the higgs-related terms in the Lagrangian, we obtain the following:

\[
L_{\text{Higgs}} \supset \frac{1}{2} \left( \partial_\mu h \right)^2 - \lambda v^2 h^2 - \lambda v h^3 - \frac{\lambda}{4} h^4,
\] (2.10)

where the first term is the standard kinetic term, the second term is the mass term \((m_h = \sqrt{2\lambda v})\), and the last two are the higgs self-interaction terms.

### 2.3 Fermion Masses

Fermion masses in the SM arise from the inclusion of interaction terms between the fermions and the \(\Phi\) field [251], when the latter is at the vev. These interactions are called Yukawa terms, and they have different strength depending on the particle type and generation. The corresponding part of the Lagrangian in Eq. 2.1 is

\[
L_{\text{Yukawa}} = -y_e \bar{\ell}_L \Phi e_R - y_u \bar{q}_L \Phi u_R - y_d \bar{q}_L \Phi d_R + (h.c.),
\] (2.11)
where \( y_{e,u,d} \) are the Yukawa couplings to the leptons, up-type quarks, and down-type quarks, respectively; \( \Phi = i\sigma^2\Phi^* \) with weak hyper-charge \( Y = -1/2 \) is used in the third term to generate the down-type quark masses. After the \( \Phi \) field acquires its vev we can identify the fermion mass terms as

\[
\begin{align*}
  m_e &= \frac{yev}{2} \\
  m_u &= \frac{yu v}{2} \\
  m_d &= \frac{yd v}{2} \\
  m_\mu &= \frac{ym \nu}{2} \\
  m_\tau &= \frac{y_\tau v}{2} \\
  m_t &= \frac{yt v}{2} \\
  m_s &= \frac{ys v}{2} \\
\end{align*}
\]  

(2.12)

The Yukawa terms give mass to all the fermions in the SM, provide decay modes of the physical Higgs boson – with \( h \to b\bar{b} \) having the highest branching fraction –, and allow the fermions to modify the observed mass of the Higgs boson through loop corrections – the most important correction comes from the top-quark, which has the largest Yukawa coupling.

2.4 On the Hierarchy Problem and Supersymmetry

A concrete example of the limitations of the SM is the apparent “unnatural” value of the Higgs boson mass \([94, 17] (m_H \approx 125 \text{ GeV})\). This can be understood by looking at the physical Higgs mass value, computed from the theory, after the fermionic quantum corrections are applied. Since the Yukawa coupling of the top quark is the largest, we concentrate on it. The physical mass of the Higgs, \( m_{h^0} \) can be written as

\[
m_{h^0}^2 = m_{h^0(\text{bare})}^2 + \Delta m_{h^0}^2,
\]  

(2.13)

where

\[
\Delta m_{h^0}^2 = \frac{3|y_t|^2\Lambda_{\text{UV}}^2}{8\pi^2} + \cdots.
\]  

(2.14)

In this last equation, \( m_{h^0(\text{bare})} \) is the bare mass of the Higgs boson, before quantum corrections are applied, \( \Delta m_{h^0}^2 \) is the contribution from quantum corrections to the Higgs mass squared, and \( \Lambda_{\text{UV}} \) is the ultra violet cutoff of the theory. If the SM is indeed a complete theory, then we expect \( \Lambda_{\text{UV}} \sim M_{\text{planck}} \sim 10^{19} \text{ GeV} \), where gravity becomes relevant. The later implies that the observed Higgs mass \((\approx 125 \text{ GeV})\) is
obtained by a remarkable cancelation between the two terms in the right-hand side of equation 2.13. This fine tuning has become known as the hierarchy problem or the naturalness problem of the Higgs mass. A possible alleviation of this problem in the introduction of new physics a mass scale in between the weak scale (\(\sim 100 \text{ GeV}\)) and the Planck scale. As mentioned earlier, one appealing theory is supersymmetry, since besides alleviating the naturalness problem, it also provides unification of the gauge coupling at about \(M_{\text{Planck}}\) and a suitable dark matter candidate. In supersymmetric theories there is a new particle for every field degree of freedom in the SM; the new particles have the opposite spin-statistics to those of the SM, i.e. bosons in the SM have fermion partners in supersymmetric models and vice versa. The scalar partners of the SM fermions are commonly known as sfermions (squarks, sleptons, etc.) and they are labeled with as their SM counterparts but adding a tilde (e.g. \(\tilde{t}, \tilde{e}\) for the stop, and selectron, respectively).

Supersymmetry alleviates the naturalness problem by adding new quantum corrections to the Higgs mass. The most relevant contribution comes from the two top partners, which contribute by canceling (at least in part) the corresponding top-quark contribution:

\[
\Delta m^2_{h_0} = m^2 \rightarrow t \rightarrow h^0 + \tilde{t}_i \rightarrow h^0 + \tilde{t}_i \rightarrow h^0 + \cdots
\]

\[
= -\frac{3|y_t|^2}{8\pi^2} \Lambda^2_{\text{UV}} + \frac{3|y_t|^2}{16\pi^2} \Lambda^2_{\text{UV}} - \sum_i \frac{3|y_t|^2 m^2_{\tilde{t}_i}}{8\pi^2} \log \left( \frac{\Lambda_{\text{UV}}}{m_{\tilde{t}_i}} \right) + \cdots
\]

\[
\Delta m^2_{h_0} = -\sum_i \frac{3|y_t|^2 m^2_{\tilde{t}_i}}{8\pi^2} \log \left( \frac{\Lambda_{\text{UV}}}{m_{\tilde{t}_i}} \right) + \cdots,
\]

(2.15)

where \(m_{\tilde{t}_i}\) is the mass of the \(i\)th top squark. As it can be seen in Equation 2.15 the additional quantum corrections due to the inclusion of the top squark loops cancel the quadratic divergence of the top quark contribution, but they add a logarithmic dependence – that is why the naturalness problem is only alleviated. By requiring natural supersymmetric scenario, where the fine tuning is at the 10% level, requires \(m_{\tilde{t}_i} < 400 \text{ GeV}\), which in turn has motivated various LHC searches since stop
production cross-sections at that mass level is high enough to be detected.

The particle spectra of SUSY is rich, and one important component comes from spin-1/2 particles, the partners of the SM vector bosons. These particles are known as gauginos. Similar to the mixing of the $SU(2) \times U(1)$ gauge boson the gauginos, including the higgsinos (the spin-1/2 partners of the Higgs doublet needed to produce an anomalous free theory), mix to form neutral and charged eigenstates, particularly, there are four neutral mass eigenstates (the neutralinos) $\tilde{\chi}^0_{1,2,3,4}$, and two charged mass eigenstates (the charginos) $\tilde{\chi}^{\pm}_{1,2}$. In most models the lightest neutralino ($\chi^0_1$) is the lightest supersymmetric mass state.

In order to explain the observed lifetime of the proton, supersymmetric model usually require an extra symmetry (R-parity) – which is not built in in the theory – that is conserved,

$$R = (-1)^{3(B-L)+2s},$$

where $B$ is the baryon number, $L$ is the lepton number, and $s$ is the spin of the particle. By construction all SM particle are even (+1), and all SUSY particles are odd (-1) under R-parity. This multiplicative quantum number has very interesting experimental consequences: 1) the supersymmetric particles are produced in even numbers (usually) at particle colliders, 2) supersymmetric particles decay to an even number of supersymmetric particles, and 3) the lightest supersymmetric particle is stable – in fact this last point is a consequence of the second. The later consequence in conjunction with the fact that in most SUSY model, the lightest particle in the spectra is neutral, and provides a weakly interacting dark matter candidate, with a mass value expected to be around 100 GeV.

Since SUSY particles couple to the Higgs boson – as they help to alleviate the naturalness problem – it is expected for some of them to produce decays involving Higgs final states, such as $q \rightarrow h^0 \tilde{\chi}^0_1$ and $\tilde{\chi}^0_2 \rightarrow h^0 \tilde{\chi}^0_1$, that could enhance the SM prediction for Higgs production and could be searched for at the LHC (see Chapters 8 and Appendix B). So far, no sign of SUSY particle production has been detected. On the other hand, the searches conducted so far have mainly focused on striking signatures (e.g., high-$p_T$ jets, large missing energy, etc). With more integrated luminosity, it is now time to address the issue of searching for SUSY in difficult corners of the parameter space. In this respect, a large dataset allows the use of rare (but clean) Higgs final states, like 4-leptons and 2-photons, for the first time.
Different observations during the twentieth century indicate that baryonic matter is not the dominant form of matter in the universe. In fact, recent measurements constrain the amount of baryonic matter to be about 5% of the total energy density, while the rest is comprise of dark matter and dark energy, accounting for approximately 27% and 68%, respectively [215]. The existence of dark matter has been inferred by several astronomical and astrophysical measurements since the 1930s, as well as the recent success of the standard model of Big Bang cosmology (commonly known as the \( \Lambda \)CDM). Nowadays, the existence of dark matter is widely accepted but little is known about its nature. Dark energy is perhaps the least understood component of our Universe; currently, we infer its existence based on the missing energy density in conjunction with the measured flatness of the universe, as well as the accelerated rate of the expansion of the universe.

This chapter is intended to briefly summarize the evidence supporting the existence of dark matter and to introduce the concepts needed to understand the basis of the current searches for dark matter in direct detection experiments, indirect detection experiments, and the experiments at the Large Hadron Collider. The rest of this chapter has been based on [145, 139].

### 3.1 The Evidence for Dark Matter

#### Early evidence

Perhaps the first convincing evidence of the existence of dark matter was the measurements carried out in the Coma cluster by F. Zwicky in 1933; J. Oort also had measured earlier inconsistencies between the velocities of stars near the center of our galaxy and its luminous mass. Zwicky measured the velocities of the galaxies in the Coma cluster by observing the doppler shifts in their emission spectra. By employing the virial theorem he was able to calculate the cluster’s total mass [261, 259]. The cluster mass was \( M_{\text{cluster}} = 4.5 \times 10^{13} M_\odot \), since there are approximately 1,000 galaxies in the cluster the average galactic mass is \( M_{\text{galaxy}} = 4.5 \times 10^{10} M_\odot \). The mass of the galaxies was also measured using the standard mass-to-light ratio, which yielded a galactic mass approximately 2% of that measured by Zwicky. Therefore most of the mass in the Coma cluster was missing, or at least did not
interact electromagnetically and was thus dubbed “dark matter”.

In the 1970s, Vera Rubin and others set to measure the rotation curves of about 100 isolated galaxies [229]. What they found was that the rotation velocities reached a plateau at radii of about 10 kpc, which blatantly contradicted the observations from the luminous matter profile in the galaxies. The measured rotation curves measured by Persic and Salucci [213] are shown in Figure 3.1, and a rotation curve from the spiral galaxy M33 is shown in Figure 3.2. The fact that the luminous matter decays exponentially with the radius of the galaxy implies that the velocity of gas and stars in the outskirts of the galaxy should start to decrease at around the optical radius $R_{\text{opt}} = 10$ kpc – the radius such that 83% of the light is contained in it. As observed in Figures 3.1 and 3.2, this is not the case, since the velocities tend to be flat or even increase as a function of the galactic radius. To solve this conundrum one can introduce a dark matter halo with a spherically symmetric profile to account for the apparent missing mass that would explain the observed rotation curves. The most pedagogical way to visualize this effect is by considering the rotation velocity to be constant (at large radius), assuming circular trajectories in the galactic disk, and using a spherically symmetric density profile. Thus one finds

$$\frac{GM(r)}{r^2} = \frac{v_c^2}{r} \quad \text{and} \quad M(r) = \int_0^r 4\pi \rho(r) r^2 dr$$

$$\Rightarrow \quad \frac{v_c^2}{G} = \frac{4\pi}{r} \int_0^r \rho(r) r^2 dr \quad (3.1)$$

$$\Rightarrow \quad \rho(r) = \frac{v_c^2}{4\pi Gr^2},$$

where $\rho(r)$ is the density profile of the dark matter halo, $v_c$ is the constant rotational velocity (about 220 km/s), $G$ is the gravitational constant, and $r$ is the galactic radius. A more accurate density profile, which fits the observed galaxy rotation data, was proposed by Navarro, Frenk, and White [206]

$$\rho(r) = \frac{\rho_0}{r} \left(1 + \frac{r}{R_s}\right)^{-2}, \quad (3.2)$$

where the central density ($\rho_0$) and the scale radius ($R_s$) are parameters that vary from galaxy to galaxy.

**Cosmological evidence**

Cosmological evidence arise later by comparing the measurements of light elements (H, D, He, and Li) – produced at the early stages of the universe in what is called the
SECTION 1.3. EVIDENCE FOR THE EXISTENCE OF DARK MATTER AND ENERGY

Figure 1.1: Average rotation curves for an ensemble of spiral galaxies. Each bin contains galaxies in the luminosity range indicated by the corresponding plot’s title (in absolute magnitudes). The mean luminosities of the lowest and highest bins differ by a factor of $\sim 75$. There are 50–100 galaxies in each bin (except for the highest luminosity bin). The lines indicate the contributions of various components. Solid: combined disk and halo contribution. Dotted: disk contribution. Dashed: halo contribution. The individual rotation curve contributions add in quadrature. Note that these are averages, not 11 separate galaxies, as was implied in Figure 1.1 of [8]. Figure taken from [4].

Figure 3.1: The rotation curves for different galaxies as measured by Persic and Salucci [213].

Figure 3.2: The rotation curve of the M33 galaxy [113, 230].
Figure 1.12: Abundances of light elements relative to H as a function of the present baryon density. The top horizontal scale converts $\rho_b$ to $\Omega_b$, with $h = 0.65$ assumed. The widths of the abundance curves indicate 95% CL confidence intervals for the abundance predictions. Measurements of the abundances in primordial environments are shown as boxes. The vertical shaded band indicates the region allowed by deuterium observations. Figure taken from [36].

Big Bang Nucleosynthesis – abundances with the theoretical calculations of nuclear physics and known reaction rates. The results are shown in Figure 3.3, where the bands represent the predicted abundances and their uncertainties, as a function of the baryonic density, the rectangular boxes represent the experimental measurements, and the vertical band indicates the region allowed by the deuterium observation. R. H Cyburt calculated possible values of the baryon relative density ($\Omega_b$) by using two deuterium measurements [116]

$$\Omega_b h^2 = 0.0229 \pm 0.0013 \quad \text{and} \quad \Omega_b h^2 = 0.0216^{+0.0020}_{-0.0021}, \quad (3.3)$$

where $h$ is the reduced Hubble parameter. Again, the baryon density is found to be very low compared to the energy budget of the universe, thus indicating the presence of dark matter – and later, dark energy.

The Cosmic Microwave Background (CMB) discovered by Penzias and Wilson in 1964 as an excess of background temperature of about 3.5 K at a wavelength of 7.5 cm [117], has undoubtedly revolutionize the realm of precision cosmology. Later the CMB has been measured to be consistent with an almost perfect black-
body spectrum with a temperature of $2.72548 \pm 0.00057$ K, and thus consistent with compatible with the expected relic radiation in the form of photons from the epoch of recombination (380,000 years after the Big Bang). Although the CMB is very much isotropic and uniform, there are fluctuation of about 1 part in $10^5$ in the temperature of the CMB as measured by the COBE satellite. These fluctuations are attributed to two different effects, first: the Sachs-Wolfe effect, where photons with lower energy today came from denser areas at the time of recombination as they lost energy on their way out (these are associated with large angular scales); and second, the acoustic oscillations of the photon-baryon fluid that underwent compression and rarefaction and thus imprinted temperature fluctuations in the photons released when the baryons became electrically neutral and the CMS photons were released (these fluctuation are associated with small angular scales). The Wilkinson Microwave Anisotropy Probe (WMAP) measured the temperature fluctuations in the CMB with unprecedented precision and allowed the measurement of different cosmological parameters, including the density of baryonic dark matter. The spectrum of the CMB anisotropies is shown in Figure 3.4, where a multipole expansion has been performed in order to clearly see the intensity of each mode. The features of CMB anisotropies are directly related to the cosmological parameters such as baryonic matter and dark matter. This is clearly shown in Figure 3.4, where different values of the baryonic density are overlaid with the real data from WMAP; as observed, the incorrect baryonic density clearly mismodels the observations. Finally, a global fit can be performed to the CMB power spectrum and thus obtain the cosmological parameters. The Plank satellite – the current state of the art CMB experiment – has measured the relative densities to be [215]

$$\Omega_b h^2 = 0.02230 \pm 0.00014 \quad \text{and} \quad \Omega_{DM} h^2 = 0.1188 \pm 0.0010$$

$$\Omega_m = 0.6911 \pm 0.0062 \quad \text{and} \quad \Omega_\Lambda = 0.3089 \pm 0.0062,$$

where $\Omega_{DM}$ is the dark matter relative density, $\Omega_m$ is the total matter density (baryonic and dark) – the statistical significance of this observation largely exceeds the customary 5 level for discovery and at the same time its value is consistent with the observations described above. $\Omega_\Lambda$ is the dark energy relative density.

**Recent evidence**

Most recent evidence for dark matter was obtained from the Bullet cluster, formed by the sub-cluster (“the bullet”) colliding with the larger cluster 1E 0657-56. During the collision, the galaxies pass by each other without interacting since the inter-
the anisotropies in the CMB. Located at the Earth-Sun L2 point (about a million miles from Earth), the satellite has taken data continuously (most recently having released an analysis of seven years of operation) and is able to detect temperature variations as small as one millionth of a degree. Due to the increased angular resolution of WMAP (and through the use of computer codes which can calculate the CMB anisotropies given fundamental parameters such as the baryon density) we now know the total and baryonic matter densities from WMAP:

\[ \Omega_m h^2 = 0.1334 \pm 0.0056 \]

\[ \Omega_b h^2 = 0.02260 \pm 0.00053 \]

(5)

where \( \Omega_m h^2 \) is the total matter density, and \( \Omega_b h^2 \) is the baryonic matter density. The first essential observation is that these two numbers are different; baryonic matter is not the only form of matter in the universe. In fact, the dark matter density, \( \Omega_{dm} h^2 = 0.1123 \pm 0.0035 \), is around 83% of the total mass density. Locally, this corresponds to an average density of dark matter \( \rho_{dm} \approx 0.3 \text{ GeV/cm}^3 \approx 10^{28} \text{ kg/m}^3 \) at the Sun’s location (which enhanced by a factor of roughly \( 10^5 \) compared to the overall dark matter density in the universe due to structure formation).

An analysis of the CMB allows for a discrimination between dark matter and ordinary matter precisely because the two components act differently; the dark matter accounts for roughly 85% of the mass, but unlike the baryons, it is not linked to the photons as part of the “photon-baryon fluid.” Fig. (3) demonstrates this point extremely well; small shifts in the baryon density result in a CMB anisotropy power spectrum (a graphical method of depicting the CMB anisotropies) which are wholly inconsistent with WMAP and other CMB experiment data.

Figure 3.4: The CMB anisotropy spectrum measured by WMAP [162]. Different values of the baryonic matter are also shown with different curves. In the multipole expansion of the CMB anisotropies \( l \approx \pi/\theta \), where \( \theta \) is the angular scale in radians.

galaxy distance is about 1 Mpc. Nevertheless, the bulk of the baryonic mass in the cluster is formed by the hot intergalactic gas that did interact during the collision, as a result of the excitations, the gas produced X-rays that were detected by the Chandra X-ray Observatory. This measurement provides an approximate distribution of the baryonic mass in the Bullet cluster that was compared with measurements carried out by using weak gravitational lensing. The comparison revealed that regions from where the detected X-rays originated did not match the regions compatible with gravitational lensing measurements; in fact the majority of the cluster’s mass is non-baryonic in nature [100]. Similar measurements have been recently made with the Hubble Space Telescope [163].

3.2 Weakly Interacting Dark Matter Candidates

There are several dark matter suitable dark matter candidates, such as axions, MA-CHOs, Kaluza-Klein particles, among others. Nevertheless, the most relevant DM candidate for this thesis is what is called a Weakly Interacting Massive Particle (WIMP). WIMPs are perhaps the most widespread non-baryonic DM candidate since they have compelling properties, including the prediction of the correct abun-
dance of dark matter that we observe today as a relic from the early stages of the universe. Besides their gravitational interaction, WIMPs only interact with a strength at the scale of the weak interaction with the known SM particles. It will be shown that these assumptions will provide a suitable DM candidate, predicting the correct relic abundance, with a mass of about 100-1000 GeV. Thus, this beneficial concurrence of events has become known as the WIMP miracle. WIMPs are now being searched for in three different type of experiments (see Figure 3.6), direct detection, where a large mass detector capable of detecting energy deposits from WIMP-nucleus interactions is placed underground to avoid backgrounds; indirect detection, where a satellite equipped with particle detectors looks for annihilation of WIMPs into SM particles; and particle collider experiments, such as ATLAS and CMS, where two SM particles (usually quarks) annihilate to produce two WIMPs, an extra SM particle with large transverse momentum should be produce in order to trigger and record the events since WIMPs will scape detection due to their weakly interacting nature. All these searches are currently underway, and up to now, there has not been any concrete detection, which may indicate that the WIMP miracle is not as miraculous as we once thought.

In order to see why WIMPs are interesting from the astrophysical and experimental point of view we need to first derive their relic density; this is the density that they will obtain by falling out of thermal equilibrium in the early stages of the universe (freeze-out). In here we consider the standard case where WIMPs are non-relativistic at the time of freeze-out. The WIMP decoupling occurs when their annihilation rate drops below the rate of expansion of the universe, i.e

\[ \langle \sigma_A v \rangle_f n_f \sim H_f, \]  

(3.5)

where \( \sigma_A \) is the annihilation cross-section (\( \chi \chi \rightarrow \) anything, where \( \chi \) is the WIMP), \( v \) is the WIMP relative velocity, \( f \) indicates the freeze-out time, \( n_f \) is the WIMP number density, and \( H_f \) is the Hubble rate. The number density at freeze-out can be current relic density by using the freeze-out redshift (\( z_f \)):

\[ \Omega_\chi = \frac{8\pi G}{3H_0^2} \rho_\chi = \frac{8\pi G}{3H_0^2} \frac{n_f M_\chi}{(1+z_f)^3}, \]  

(3.6)

where we have used \( \rho_\chi = \frac{n_f M_{\chi_{	ext{relic}}}}{(1+z_f)^3} \)—coming from the dilution created by the expansion of the universe. Now the redshift at freeze-out can be related to the freeze-out
temperature by using the temperature of the CMB today, and thus

\[
T_f = \left( \frac{1 + 3 \frac{7}{8} \Pi}{g_f} \right)^{1/3} (1 + z_f) T_{\text{CMB}},
\]

(3.7)

where the pre-factors in the numerator arise changes in the contributing degrees of freedom in the entropy, and \( g_f \) is the effective numbers of degrees of freedom. We can now express the number density in terms of the freeze-out temperature and the WIMP parameters by combining Equations 3.6 and 3.7:

\[
n_f = \frac{3}{8\pi G} \frac{\Omega_x H_0^2}{M_X} \left( \frac{g_f}{1 + 3 \frac{7}{8} \Pi} \right) \left( \frac{T_f}{T_{\text{CMB}}} \right)^3.
\]

(3.8)

In order to solve Equation 3.5 for the temperature averaged annihilation rate \((\langle \sigma_A v \rangle)_f\), we first need to find an expression for the expansion rate at the time of freeze-out. The latter is readily available from the Friedmann equations and the fact that the universe was radiation dominated at the epoch of freeze-out:

\[
H_f^2 = \frac{8\pi G}{3} \rho_f^{\text{rad}},
\]

(3.9)

where \(\rho_f^{\text{rad}}\) is the radiation dominated energy density at the time of freeze-out. Using the correct expression for the latter yields

\[
H_f^2 = \frac{8\pi G}{3} \kappa_p g_f \frac{\pi^2}{30} T_f^4,
\]

(3.10)

where \(\kappa_p\) is a numerical value close to unity depending on the nature of the WIMP (boson, fermion). Now combining Equations 3.8 and 3.10 we find:

\[
\langle \sigma_A v \rangle_f = \frac{H_f}{n_f} \sim \frac{10^{-27}}{\sqrt{8\pi G} \Omega_x h^2} \frac{M_X}{T_f} \text{ cm}^3 \text{ s}^{-1}.
\]

(3.11)

Now the only remaining unknown is the WIMP mass to temperature ratio at freeze-out \(\frac{M_X}{T_f}\). This can be approximated by the Boltzmann distribution – in the non-relativistic limit – for \(n_f\) at the freeze-out temperature and combining that with Equation 3.8:
Figure 3.5: Comoving number density for WIMPs as a function of $\frac{M}{T}$ [187].

\[
n_f = \left(\frac{k_B T_f M_X}{2\pi \hbar}\right) \exp\left(\frac{M_X c^2}{k_B T_i}\right) \quad \text{and} \quad n_f = \frac{3}{8\pi G} \frac{\Omega_X H_0^2}{M_X} \left(\frac{g_f}{1 + \frac{3}{8} \frac{4}{11}}\right) \left(\frac{T_f}{T_{CMB}}\right)^3
\]

\[
\Rightarrow \frac{M_X}{T_f} = \frac{3}{2} \log\left(\frac{M_X}{T_f}\right) = 18.9 + \log\left(\frac{M_X}{\Omega_X h^2 g_f}\right).
\]

This last expression is fairly similar for relevant WIMP masse of the order of 1 GeV to 1 TeV, which yields $\frac{M_X}{T_f} \approx 25 - 30$. This mass to temperature ratio at freeze out can be obtained more accurately by solving the appropriate differential equation yielding a result of the same order as obtained in 3.12. Figure 3.5 show the evolution of the WIMP number density as a function of the $\frac{M_X}{T_f}$ ratio – which is a proxy for the time evolution of the universe. Finally, by assuming a relevant relic density today ($\sqrt{g_f}^{-1} \Omega_X h^2 \sim 1$) we find that WIMP annihilation rate $\langle \sigma_A \nu \rangle_f = 10^{-26} \text{ cm}^3 \text{ s}^{-1}$.

Now this annihilation rate can also be obtained from a particle physics prospective by using a weak scale interaction strength. The annihilation rate in this case is given by the following expression (Fermi’s golden rule):

\[
\Gamma = \langle \sigma_A \nu \rangle = \frac{2\pi}{\hbar} |\mathcal{M}|^2 \rho(E) \quad \text{with} \quad \rho(E) = \frac{4\pi}{(2\pi \hbar c)^3} E^2,
\]

where $\mathcal{M}$ is the matrix element for the annihilation channel, and $\rho(E)$ is the density of states, where we have assumed relativistic particles in the final state. When the
WIMPs are not relativistic the final state particle obtain an energy \((E)\) that is equal to the mass of the WIMP. Now, assuming the simplest possible annihilation channel where the matrix element squared \((|M|^2)\) is just given by Fermi’s constant squared \((G_F^2)\) we can compute the annihilation rate:

\[
\langle \sigma_A \rangle = \frac{1}{\pi} \frac{1}{(\hbar c)^3} G_F^2 M_X^2 c^4
\]

\[
= \frac{1}{\pi} \frac{(\hbar c)^3}{\hbar} (1.66 \times 10^{-5} \text{ (GeV)}^{-2})^2 M_X^2 (\text{GeV})^2
\]

\[
\langle \sigma_A \rangle \sim \frac{(\hbar c)^3}{\hbar} 10^{-10} \text{ (GeV)}^{-2} M_X^2
\]

\[
\langle \sigma_A \rangle \sim 10^{-27} M_X \text{ cm}^3 \text{ s}^{-1} M_X^2,
\]

where \(M_X\) is in units of GeV. Now we can readily see that a WIMP mass at the weak scale (1 GeV-1 TeV) gives the correct order of magnitude for the WIMP annihilation. The fact that WIMPS with a weak scale interaction strength produces the necessary annihilation rate for a cold dark matter relic obtained in Equation 3.11 – purely from astrophysical considerations – is what some literature has named the *WIMP miracle*.

### 3.3 Searches for WIMP Dark Matter

Three different type of experiments to search for WIMP dark matter are currently underway. These searches are named, direct detection experiments, indirect detection experiments, and particle collider experiments. Figure 3.6 shows a Feynman diagrams with the possible ways in which WIMP DM can be detected, and the dashed blob represents the interaction of dark matter with the SM (quarks in this case).

**Direct detection**

Direct detection experiments are based on WIMP-nucleus scattering which in turn depend on the WIMP-quark cross-section. Assuming a standard WIMP scenario the WIMP-nucleus cross section is of the order of \(10^{-36} \text{ cm}^2\), which yields a detectable rate of interactions of about 1 event per kilogram per day. This requires a large mass detector and large exposure times in order to increase the possibilities to detect WIMPs. Another consideration in direct detection experiments is the amount of energy transferred to the nucleus by the WIMP and the ability to record that energy. In an elastic collision the energy transfer to the nucleus (recoil energy) is
Figure 3.6: Feynman diagram including the possible manner in which DM can be experimentally detected. The green arrows indicate the orientation in which the diagram should be read to produce a particular detectable signal.

\[
E_{\text{recoil}} = \frac{2 M_N}{M_{DM}^2} E_{DM},
\]

(3.15)

where \(E_{\text{recoil}}\) is the recoil energy, \(M_N\) is the nucleus mass, \(M_{DM}\) is the DM mass (assumed to be around 100 GeV), and \(E_{DM}\) is the DM kinetic energy (assuming a velocity of about 270 km/s yield a kinetic energy of about 50 keV). Assuming an nucleus with an atomic weight of about 72-131 (Germanium and Xenon, respectively), the recoil energy is about 25 keV (note that the maximum kinetic energy is in fact just twice the DM kinetic energy). The experimental techniques used include detection of thermal/phonons fluctuations, ionization detectors, and scintillator detectors. No evidence of a DM detection has been announced and the current DM-nucleon cross-section limits are presented in Figure 3.7.

**Indirect detection**

Assuming WIMP dark matter, the same mechanism by which the observed relic density was obtained at the early stages of the universe, i.e. WIMP-WIMP annihilation, should still be taking place in regions where there are large amounts of dark matter. The annihilation rate is proportional to the WIMP density squared \(\Gamma_{\chi\chi \to X} \propto n_X^2\), where \(\chi\) represents the WIMP), and therefore the detection is increased when looking at regions of high DM density such as the Earth, the sun, and the galactic center. This annihilation signature is looked for in different channels that ultimately will
produce excess of gamma-rays, neutrinos, or anti-particles – particularly positrons. These astrophysical searches are classified as indirect detection [61, 164], since WIMPs are not directly detected.

Gamma-rays could be produce by the $\chi \chi \rightarrow q \bar{q}$ reaction (specially in the galactic center), and subsequently the quarks will hadronize and produce photons that can be detected by a particle detector, but only as a continuum excess, as is the limitation of this mode. Other reactions that could produce an enhancement of gamma-rays are $\chi \chi \rightarrow \gamma \gamma$ and $\chi \chi \rightarrow \gamma Z$, where the excess will be observed by a line in the gamma-ray spectrum. The EGRET collaboration reported an excess of events in their gamma-ray spectrum in 1998[125], indicating a standard WIMP scenario. The EGRET excess remains controversial due to the null observation in the antiproton flux. The Fermi Gamma-ray Space Telescope (Fermi-LAT) launched in 2008 [111] has also observed some excesses coming from the galactic center [122]; though encouraging results, the community awaits more data to be collected to elucidate these hints of DM detection. Figure 3.8 shown the gamma-ray map collected by FERMI-LAT.

Excess of neutrino flux can also indicate the presence if WIMP dark matter. The sun is a good place to look for neutrino flux excesses since the solid angle for annihilation is greatly increased with respect to that of the galactic center. Processes such as $\chi \chi \rightarrow t\bar{t}, b\bar{b}, c\bar{c}, ZZ, W^+W^-$, and $\tau^+\tau^-$ will lead to neutrino final states. Detectors can be located in Earth since neutrinos interact very weakly with matter.
Large detector such as IceCube, and Super-Kamiokande, among other, are already in place trying to detect DM by observing neutrino flux excesses.

Since anti-matter is rare in our universe, search for excesses of anti-particles is an attractive way to observed WIMP annihilation – particularly those producing positrons and antiprotons. Again, positrons can be produced directly or as decay product of other SM particles, while antiprotons can be produced via quark hadronization. The PAMELA satellite[79] has observed an excess of events with positron energies between 1.5-100 GeV [29]. As in the gamma-ray excesses, larger data samples are needed to confirm or disprove the current observations, and such data sets will be provided by FERMI-LAT.

**Searches for dark matter production at the LHC**

Dark matter could be produced at the LHC as a decay product of heavier states in the context of SUSY, and this will result in a signature with a variety of SM particles in the final state along with missing transverse-momentum due to the weakly interacting nature of the DM candidate – the lightest neutralino. A different approach to search for dark matter in particle colliders which involves different couplings between the the relevant SM particles at the LHC and the DM candidate has been adopted by the ATLAS and CMS collaborations. These interactions involve different non-renormalizable effective operators – in the context of quantum field theory – where the mediating force carried field is assumed to be above the LHC energies and therefore integrated out. A list of the possible effective operators is shown in Table 3.1. The most popular operator studied in the 7 and
8 TeV run of the LHC where the vector and axial-vector operators. The upper limits on these operators can be translated to spin-independent and spin-dependent DM-nucleon cross section, and thus be compared to the results obtained by direct detection experiments. This comparison is the result of a series of assumptions in both experiments and therefore they should be interpreted with caution. These event topologies will not be recorded in the particle detectors since they produce two DM candidates in the final state that will completely escape detection. Therefore another high-\(p_T\) particle needs to be produced in order to activate the trigger systems deployed in modern particle detectors. This extra requirement is satisfied by the production of initial-state-radiation off the quarks (see left panel of Figure 7.1). Such events topologies became known as mono-\(X\), where \(X\) denotes the high-\(p_T\) object that could be a jet, photon, lepton, \(Z/W\) bosons, or a Higgs boson, among others. Figure 3.9 shows the spin-independent results from the mono-jet and mono-photon analyses released by the CMS collaboration [24, 95, 180, 23]. The effective field theory approach to obtain the operators in Table 3.1 turned out to be violated in a portion of the events recored at the LHC and therefore their bounds are not completely accurate [69, 70, 71]. Attempts to solve this issue, have now been made, such as including the mediator particle and the coupling strength to be parameters of the model [26]. Chapter 7 presents a search for particle DM in events with two or more jets, providing the LHC searches with a inclusive analysis approach that is at the same time complementary to the existing mono-jet searches by ATLAS and CMS. This search also quantifies the fraction of events that violate the EFT assumption.

<table>
<thead>
<tr>
<th>Name</th>
<th>Initial state</th>
<th>Type</th>
<th>Operator</th>
</tr>
</thead>
<tbody>
<tr>
<td>D1</td>
<td>(q\bar{q})</td>
<td>scalar</td>
<td>(\frac{m_q^2}{M_*^2} \bar{\chi} \chi \bar{q}q)</td>
</tr>
<tr>
<td>D5</td>
<td>(q\bar{q})</td>
<td>vector</td>
<td>(\frac{1}{M_*^2} \bar{\chi} \gamma_\mu \chi \bar{q} \gamma^\mu q)</td>
</tr>
<tr>
<td>D8</td>
<td>(q\bar{q})</td>
<td>axial-vector</td>
<td>(\frac{1}{M_*^2} \bar{\chi} \gamma_\gamma^S \chi \bar{q} \gamma^\mu \gamma^S q)</td>
</tr>
<tr>
<td>D9</td>
<td>(q\bar{q})</td>
<td>tensor</td>
<td>(\frac{1}{M_*^2} \bar{\chi} \sigma_\mu\nu \chi \bar{q} \sigma_\mu\nu q)</td>
</tr>
<tr>
<td>D11</td>
<td>(gg)</td>
<td>scalar</td>
<td>(\frac{1}{M_*^2} \bar{\chi} \chi \alpha_s (G^{\mu\nu}_s)^2)</td>
</tr>
</tbody>
</table>

Table 3.1: A selection of the possible effective operators for DM production at the LHC [147]. \(M_*\) is the cutoff scale of the effective operator (sometimes this quantity is also represented by \(\Lambda\)).
Figure 3.9: The DM-nucleon cross section 90% CL. bounds published by the CMS mono-jet and mono-photon searches.
Part II

The Large Hadron Collider and The Compact Muon Solenoid Experiment
4.1 The Large Hadron Collider

The CERN Large Hadron Collider (LHC) is a two-ring superconducting accelerator and collider with 27 km of circumference, which is located in the tunnel constructed for the CERN Large Electron-Positron Collider (LEP). The tunnel lies between 45 m and 170 m below the surface on an inclined plane (1.41% slope) towards Lake Léman and spans between the French and Swiss border close to Geneva. The layout of the tunnel is such that contains 8 arc sections that spans most of the circumference and 8 straight sections where the experimental halls are located.

The LHC is a particle-particle collider – in its most common configuration it collides protons – with a designed center-of-mass energy of 14 TeV. In order to achieve such high energies, the LHC uses the existing CERN facilities to gradually increase the energy of the protons. Everything starts with a bottle of compressed hydrogen gas, then, hydrogen atoms are fed into the source chamber of the linear accelerator, where an electric field strips off their electrons. The resulting protons are then injected into the linear accelerator, Linac 2, which is the first step in the accelerator chain and boosts the protons energy up to 50 MeV. The accelerated proton beam is then divided into 4 (to increase its intensity) and enters the second stage of acceleration, this occurs in the Proton Synchrotron Booster (PSB), where protons are now accelerated to 1.4 GeV. Subsequently, the proton beam is recombined and sent to the Proton Synchrotron (PS), which increases the energy to 25 GeV, followed by the Super Proton Synchrotron (SPS), which brings the beam energy to 450 GeV.

Finally, the proton beam is transferred to the two beam pipes of the LHC. The beams circulate in opposite directions. The LHC filling time is 4 minutes and 20 seconds, but it takes around 20 minutes for the protons to reach their maximum energy. Figure 4.1 shows the CERN accelerator complex just described. At this point, the two beams are brought to collide at the four interaction points (IP) in the straight sections where the LHC’s experiments are located. There are two main purpose experiments located in diametrical opposite locations, the ATLAS experiment is located at point 1 and the CMS experiment is located at point 1. There are also two specialized experiments: the LHCb experiment, which studies
B-hadron physics, and the ALICE experiment, which specializes in studying heavy ion collisions (another type of collision possible at the LHC). Figure 4.2 shows an schematic layout of the LHC. Due to the small diameter of the tunnel in the arcs (3.7 m), which complicates the installation of two separate proton rings. The LHC uses a twin-bore magnet design, proposed in 1971 by John Blewett at the Brookhaven National Laboratory (BNL) [63] as a cost-saving alternative.

Since the usage of superconducting magnets a the Intersecting Storage Rings at CERN, particle colliders have used them as the default technology for their operation. However, the main difference is that the LHC’s superconducting magnets operate at a temperature lower (below 2 K) than the standard superconducting magnets in other particle colliders (4-5 K). The LHC ring accommodates 1,232 NbTi main dipole magnets, cooled down to 1.9 K by using superfluid helium; they operate at fields above 8 T. The twin-bore design allow for a common nonmagnetic collar and iron yoke, as well as common cryogenic system. The core of the dipole magnet system is enclosed by a cylindrical alloyed low-carbon steel vacuum vessel with an outer diameter of 914 mm and a wall thickness of 12 mm. Figures 4.3 and 4.4 show a cross sectional view and a 3-dimensional visualization of the main dipole magnet.
The goal of the LHC program is to reveal the nature of new physics. The high-energy collision (14 TeV) are a key ingredient to probe new physics, since new physics could just be present at that energy scale. However, it is by no means the only ingredient; new physics will likely have smaller cross sections than that of the known SM processes and therefore a large number of proton-proton collision is needed. The number of events for a particular physics process $N_{exp}$ generated in the LHC is the product of the experimental cross section $\sigma_{exp}$ and the integrated luminosity, i.e.

$$N_{exp} = \sigma_{exp} \int L(t) dt,$$

where $L(t)$ is the instantaneous luminosity, which depends on the LHC beam parameters and can be written as [128]:

$$L(t) = \frac{N_b^2 n_b f_{rev} \gamma_r}{4\pi \epsilon_n \beta^*},$$

where $N_b$ is the number of particles per bunch, $n_b$ is the number of bunches per beam, $f_{rev}$ is the revolution frequency, $\gamma_r$ is the relativistic factor, $\epsilon_n$ is the normalized transverse beam emittance, $\beta^*$ is the transverse size of the beam at the IP, and $F$ is
Figure 4.3: An schematic cross sectional view of the LHC dipole magnet.

Figure 4.4: An 3D visualization of a LHC dipole magnet.
Figure 4.5: Integrated luminosity received by the CMS experiment during the LHC operation.

the geometric luminosity reduction factor due to the crossing angle at the IP:

\[ F = \left( 1 + \left( \frac{\theta_c \sigma_z}{2\sigma^*} \right) \right)^{-1/2}. \]  

(4.3)

In the last expression, \( \theta_c \) is the full crossing angle at the IP, \( \sigma_z \) is the rms. bunch length, and \( \sigma^* \) is the transverse rms. beam size at the IP. The designed peak luminosity to be delivered the ATLAS and CMS is \( \mathcal{L}(t) = 10^{34} \, \text{cm}^{-2} \, \text{s}^{-1} \). Figure 4.5 shows the integrated luminosity received by the CMS experiment from 2007 to 2016.
Chapter 5

THE COMPACT MUON SOLENOID EXPERIMENT

The Compact Muon Solenoid (CMS) detector operates at the LHC at CERN. It was designed to operate in proton-proton (and lead-lead) collisions at a center-of-mass energy of 14 TeV (5.5 TeV) and at luminosities up to $10^{34}\text{cm}^{-2}\text{s}^{-1}$ ($10^{27}\text{cm}^{-2}\text{s}^{-1}$). The CMS has cylindrical geometry and its dimensions are a length of 21.5 m, a diameter of 14.6, and a total weight of 12,500 tons. At the heart of the CMS detector system lies a 4 T magnetic field produced by a large-bore superconducting solenoid which encloses a silicon – pixel and strips – tracker, a homogeneous lead-tungstate crystal electromagnetic calorimeter, and a brass-scintillator sampling hadron calorimeter. Outside the superconducting solenoid lies an steel yoke for magnetic flux-return instrumented with four stations for muon detection. Forward sampling calorimeters extend the rapidity coverage up to $\eta < 5$ and thus ensure good hemeticity. Figure 5.1 shows a schematic representation of the CMS detector and Figure 5.2 shows a cartoon with a cross-sectional-slice view of the CMS detector along with different particle detections.

This chapter presents an introduction to the CMS detector systems and reconstruction algorithms. It is by no means a complete picture of the CMS detector and its mostly based on Ref. [88].

5.1 The Superconducting Solenoid

The superconducting solenoid magnet is at the heart of the CMS detector and the rest of the detector systems are built around it. The superconducting magnet is 6 m in diameter and 12.5 m in length. It is comprised of 4 layer of winding made from reinforced NbTi conductors. Creating a cold mass of about 220 tons. The magnitude of the magnetic field is 3.8 T – produced by a current of 19.1 kA running through the conductors – along the $z$–direction in the barrel sector. The magnetic flux is return by means of a 10,000 tons steel-yoke which is designed in modular fashion: there are 5 wheels in the barrel, each divided in 12 sectors in the transverse plane, and 2 endcaps, each composed of 3 disks along the $z$-axis. Figure 5.3 shows a map of the magnetic field produced by the CMS superconducting solenoid magnet. A view of the steel-yokes in the early stages of assembly is presented in Figure 5.4
Figure 5.1: A perspective view of the CMS detector.

Figure 5.2: A cross-sectional-slice view of the CMS detector. The different components of the detector are clearly labeled and different particle detections are depicted.
Figure 5.3: Map of the magnetic field in the $y - z$ plane of the CMS detector.

Figure 5.4: A photograph of the steel-yoke in the early stages of assembly. The centermost wheel in the barrel support the superconducting coil. One of the endcaps yoke can be seen at the back.
5.2 The Tracker System

The tracker is the innermost system of the CMS detector. It was designed to measure efficiently and precisely the trajectories of charged particles coming from the interaction points, as well as to provide a precise reconstruction of the secondary vertices at each bunch crossing. When running at the LHC designed conditions, every bunch crossing, i.e. 25 ns, the number of proton-proton collision will be about 20 and they will produce an average number of particles of about 1000. These conditions and the above requirements implied a highly granular and fast response design. That being said, this design due to its high power consumption requires an efficient cooling system which in turn is in conflict with the goal of minimizing the material budget and thus reducing unwanted interactions. In addition, the harsh radiation environment that will deteriorate the detector performance posed further challenges in its construction. Therefore, the system – silicon sensors, readout, mechanical structures, granularity, etc – was designed to operate for 10 years and satisfy the considerations listed above. The CMS tracker is composed of three layers of pixels detectors up to a radius of 10.2 cm, a 10-layer silicon strip tracker up to a radius of 1.1 m, 2 endcap disks at each side of the barrel pixel detectors, 3 endcap disks at each side of the inner region of the strips (up to a radius of 55 cm), and finally 9 disks covering the $|z| > 120$ cm regions starting a radius of 55 cm. More details about the tracker layout will be given below and are summarized in Figure 5.5. The tracker covers up to pseudorapidities of $|\eta| < 2.5$ with a about 200 m$^2$ of active silicon area implemented. The material budget of the CMS tracker is shown in Figure 5.6. The most heavily implemented pseudorapidity is found to be at $|\eta| \approx 1.4$.

Pixel Tracker

The inner pixel detector is composed of three 53-cm-long cylindrical layers at a radii of 4.4, 7.3, and 10.2 cm – which is called BPix. It is finalized by two disks of pixel modules at each side extending from approximately 6 to 15 cm in radius – which is called FPix. The barrel is composed of 672 full and 96 half modules, a full (half) module is composed of 16 (8) read-out chips equipped with 52×80 pixels of size 100×150 µm. A completed full-module has the dimensions of 66 mm×26 mm and is provided with readout and power. Figure 5.7 shows a completed full- and half-module as well as a schematic of the different component integrated in the module. The two disks at each side of the pixel barrel (see Figure 5.5) are composed of 24 modules with a trapezoidal geometry. Each disk is composed of two different panel
Figure 5.5: A cross-sectional view of the silicon tracker layout. The different subsystems are clearly labeled.

Figure 5.6: Material budget of the CMS tracker in units of radiation length as a function of pseudorapidity $\eta$ for the (left) different sub-detectors and (right) functional contributions.
Figure 3.13: Exploded view (middle panel) of a barrel pixel detector full module (right panel) and picture of an assembled half module (left panel).

modules will then be connected through the MUSR connector to the optical ribbon cable. These adapters are mounted at the circumference in the first part of the supply tube. The length of each supply tube is 2204 mm. Only a flexible mechanical connection is made between the barrel and the supply tube.

Pixel barrel detector modules

The barrel part of the CMS pixel detector consists of about 800 detector modules. While the majority of the modules (672) are full modules as seen in figure 3.13 on the right, the edges of the six half-shells are equipped with 16 half-modules each (96 in total, see figure 3.13 on the left).

Geometry and components. A module is composed of the following components (figure 3.13).

One or two basestrips made from 250 µm thick silicon nitride provide the support of the module. The front end electronics consists of 8 to 16 read-out chips with 52 x 80 pixels of size 100 x 150 µm each, which are bumpbonded to the sensor. The chips are thinned down to 180 µm. The High Density Interconnect, a flexible low mass 3 layer PCB with a trace thickness of 6 µm equipped with a Token Bit Manager chip that controls the read-out of the ROCs, forms the upper layer of a module and distributes signals and power to the chips. The signals are transferred over an impedance matched 2 layer Kapton/copper compound cable with 21 traces and 300 µm pitch. The module is powered via 6 copper coated aluminium wires of 250 µm diameter.

Figure 5.7: BPix completed modules; (left) half-module, (center) an schematic of the different component forming the a full-module,(right) full-module.

types: the first and closest to the interaction point is formed by a 1×2, 2×3, 2×4, and 1×5 plaquettes amounting to a total of 21 read-out chips; the second and furthest from the interaction point is formed by a 2×3, 2×4, and 2×5 plaquettes amounting to a total of 24 read-out chips. A plaquette is the basic unit of the FPix and consist of a single pixel sensor bump-bonded to the read-out chip and wired-bonded to a very-high-density-interconnect (VHDI) that provides data connections, power, and control. Figure 5.8 show a schematic of these two different panels as well as a photograph of a finalized panel. Finally, a layout of the pixel tracker system is given in Figure 5.9 as well as the a detection efficiency as a function of the pseudorapidity. The total number of pixels in the pixel tracker is about 66 millions and they are equivalent to an area of about 1 m².

Strip Tracker

The silicon tracker is located outside the inner pixel tracker and is composed of three subsystems that extend from 20 cm to 116 cm in the radial direction. The Tracker Inner Barrel and Disks (TIB/TID) are the innermost subsystem extending up to a radius of 55 cm, it includes 4 barrel layers and 3 disks at each side. The TIB/TID with their 320 µm thick silicon micro-strip sensor oriented along the z-axis records up to 4 r-φ measurements on a particle’s trajectory. The strips pitch in the TIB – the distance between each strip – varies between 80 µm and 120 µm in layers 1-2 and
layers the drift of the electrons to the collecting pixel implant is perpendicular to the magnetic design that allows partial depleted operation even at very high particle fluences. For the barrel the full 3 barrel layers and the forward pixel disks on each side gives 3 tracking points over almost 103 cm. The BPix layers will be located at mean radii of 4.4, 7.3 and 10.2 cm. The FPix disks extending from b and τ decays, and forming seed tracks for the outer track reconstruction and high level triggering. It consists of three barrel layers (BPix) with two endcap disks (FPix). The 53-cm-long panels on the side of the cooling channel closest to the IP contain 1

The basic unit of construction for the forward pixel detector is the plaquette. A total of 672 plaquettes are attached to a given sensor. The largest plaquette, the type plaquette with a total of 24 ROCs. The sensors are offset on the upstream and downstream panels so that there are no cracks in the coverage due to the ROC sharing and helps to separate signal and noise hits as well as to identify large hit clusters from overlapping tracks.

The pixel detector covers a pseudorapidity range \(|\eta| < 3.4\). Figure 3.6: Geometrical layout of the pixel detector and hit coverage as a function of pseudorapidity.

3-4, respectively. The resulting single point resolution is therefore 23 \(\mu m\) and 35 \(\mu m\) for the 1-2 and 3-4 layers, respectively. The TID has strip pitches between 100 -140 \(\mu m\) – resulting in single point resolution between 29-41 \(\mu m\). The TIB/TID is completely surrounded by the Tracker Outer Barrel (TOB), which with its 6 barrel layer extends up to a radius of 116 cm. The layers are composed of 500 \(\mu m\) thick micro-strips sensor with pitches of 183 \(\mu m\) and 122 \(\mu m\) for the first 4 and last 2 layer, respectively – recording up to 6 \(r-\phi\) measurements on a particle’s trajectory with single point resolutions of 53 \(\mu m\) and \(\mu m\), respectively. The TIB/TID and the TOB cover the region with \(|z| < 113\ cm\), beyond this point (see Figure 5.5) the Tracker EndCaps (TEC\(\pm\)) – where the sign, obviously, represents the position on the \(z\)-axis – extend from 124 cm \(|z| < 282\ cm\) and 22.5 cm \(|r| < 113.5\ cm\). The TEC consists of 9 disks which contain up to 7 rings of silicon micro-strips; the latter are 320 \(\mu m\) and

Figure 5.8: FPix module; (left) a schematic of the two types of module, (right) a photograph of one of the completed FPix modules.

Figure 5.9: (Left) the layout of the silicon pixel tracker, (right) the pixel tracker detection efficiency as a function of the pseudorapidity.
The tracking efficiency for single muons is measured in 7 TeV data as a function of the muon pseudorapidity $\eta$ and the number of reconstructed vertices using the tag-and-probe technique on muons decaying from Z bosons. The results are shown in Figure 5.10, where the muon efficiency is above 99% within the tracker acceptance and up to 20 reconstructed vertices. The muon transverse momentum and transverse impact parameter resolution as a function of $\eta$ are estimated from the CMS full simulation, the results are shown in left and right panel of Figure 5.11, respectively. The muon transverse momentum resolution is about 1-3% for $|\eta| < 1.5$ for muons of different energies. The transverse impact parameter is estimated to be between $\sim 10-20 \mu m$ for a 100 GeV muon while the for 1 GeV muons the resolution is between $\sim 80-250 \mu m$. 

**Performance of the CMS Tracker**

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isolated muons

Figure 14: Resolution, Resolution in the track parameters

Resolution in \( d \mu m \) (10 radians)

Resolution in \( 10^{-2} \) radians

CMS simulation

Figure 5.11: Resolution as a function of the pseudorapidity \( \eta \) for muons of \( p_T = 1, 10, \) and 100 GeV. The left panel shows the transverse momentum resolution and the right panel the transverse impact parameter resolution. Both quantities are estimated from Simulation.

5.3 The Electromagnetic Calorimeter

The CMS electromagnetic calorimeter (ECAL) is a granular and homogeneous calorimeter built out of 61,200 lead tungstate (PbWO\(_4\)) crystals in the barrel and closed by 7,324 PbWO\(_4\) crystals in each of the two endcaps. Additionally, a preshower detector is place in front of the endcaps – i.e. closer to the interaction point. The scintillating light is collected by silicon avalanche photodiodes (APDs) in the ECAL barrel (EB) and by vacuum phototriodes (VPTs) in the ECAL endcaps (EE). Figure 5.12 shows a projectional schematic layout as well as a geometric view of a quarter of the CMS ECAL. The ECAL excellent performance is one of the keystones of the physics results of the CMS experiment, perhaps best exemplified by the Higgs boson search and characterization in the \( H \rightarrow \gamma \gamma \) and \( H \rightarrow ZZ^* \) decay channels [175, 91].

The PbWO\(_4\) crystals with a density of 8.28 g/cm\(^3\) provided a good candidate because of their small radiation length (\( X_0 = 0.89 \) cm), small molière radius (2.19 cm), and fast response. PbWO\(_4\) crystals have a relatively low light yield of about 10 photoelectrons/MeV and therefore they required to be read out by sensors with internal amplification inside the 3.8 T magnetic field. The crystals in the EB are 23 cm long and have a cross-sectional area of 2.2\( \times \)2.2 cm\(^2\) (equivalent to 0.0174\( \times \)0.0174 in \( \eta, \phi \)), they are located at radius of 1.29 m and arranged in a quasi-projective geometry with 170 crystals – 85 at each side – covering up to a pseudorapidity...
The performance of the calorimeter has been extensively tested with electron beams of the first LHC running period (early 2013). A small fraction (about 1% in EB, 2% in EE, and 3% in ES) of non-operational channels by the end to help with

A sample amplitudes provide information about the timing of the signal with respect to the trigger. These are stored in a buffer until a Level-1 (L1) trigger is received. At 40MHz by a 12-bit analog-to-digital converter (ADC) on the front-end, providing a discrete set of digitization factor of about 10) are used as photodetectors in the EB and EE respectively. The signal from the photodetectors is amplified and shaped by the front-end electronics, and then digitized at 40MHz by a 12-bit analog-to-digital converter (ADC) on the front-end, providing a discrete set of

The EE crystals are located at $z = \pm 315.4$ cm, they have a cross-sectional area of 2.86×2.86 cm$^2$ and 3.0×3.0 cm$^2$ at the front and rear faces, respectively, and a length of 22 cm. They crystals are grouped in mechanical structure of 5×5 crystals and arranged in the traditional $x$-$y$ directions. Each endcap is divided into halves or Dees, holding 3,662 crystals. The EE extends the ECAL coverage up to the range $1.479 < |\eta| < 3.0$. The left and right panels of Figure 5.13 show the EB crystal instrumented with an APD and the EE crystal instrumented with a VPT, respectively. Real photographs of an EB module equipped with crystal is presented in Figure 5.14 while an EE Dee fully instrumented with crystals is shown in Figure 5.15.

**ECAL Performance**

The EB has been extensively tested using electron beams. In this test beam setup – with no magnetic field or material in front – the energy resolution has been measured

![Figure 5.12: The layout of the CMS electromagnetic calorimeter. The left panel shows a projectional schematic layout including all the major parts while the left panel shows a geometric view of a quarter of the ECAL.](image)

![Figure 5.13: The PbWO$_4$ crystal of the CMS ECAL, (left) a EB crystal instrumented with an APD and (right) a EE crystal instrumented with a VPT.](image)
with water at 18°C. The water runs through a thermal screen placed in front of the crystals which thermally decouples them from the silicon tracker, and through pipes embedded in the aluminium grid, connected in parallel. Beyond the grid, a 9 mm thick layer of insulating foam (Armaflex) is placed to minimise the heat flowing from the read-out electronics towards the crystals. Return pipes distribute the water through a manifold to a set of aluminium cooling bars. These bars are in close contact with the very front end electronics (VFE) cards and absorb the heat dissipated by the components mounted on these cards. A thermally conductive paste (gap filler 2000, produced by Bergquist) is used to provide a good contact between the electronic components and a metal plate facing each board. This plate is coupled to the cooling bar by a conductive pad (ultrasoft gap pad, also produced by Bergquist). Both the gap pad and the gap filler have been irradiated with twice the dose expected in the ECAL endcaps after 10 years at the LHC and have shown no change in character or loss of performance.

Extended tests of the cooling system have been performed with good results. Residual effects caused by a possible variation of the power dissipated by the electronics were measured in the extreme case of electronics switched on and off. The conclusion is that contributions to the constant term of the energy resolution due to thermal fluctuations will be negligible, even without temperature corrections.

4.3 Photodetectors

The photodetectors need to be fast, radiation tolerant and be able to operate in the longitudinal 4-T magnetic field. In addition, because of the small light yield of the crystals, they should amplify and be insensitive to particles traversing them (nuclear counter effect). The configuration of the magnetic field and the expected level of radiation led to different choices: avalanche photodiodes in the barrel and vacuum phototriodes in the endcaps. The lower quantum efficiency and internal gain of the vacuum phototriodes, compared to the avalanche photodiodes, is offset by their larger surface coverage on the back face of the crystals.

4.3.1 Barrel: avalanche photodiodes

In the barrel, the photodetectors are Hamamatsu type S8148 reverse structure (i.e., with the bulk n-type silicon behind the p-n junction) avalanche photodiodes (APDs) specially developed for the CMS ECAL. Each APD has an active area of 5×5 mm² and a pair is mounted on each crystal. They are operated at gain 50 and read out in parallel. The main properties of the APDs at gain 50 and 18°C are listed in table 4.1. The sensitivity to the nuclear counter effect is given by the effective thickness of 6 µm, which translates into a signal from a minimum ionizing particle traversing an APD equivalent to about 100 MeV deposited in the PbWO₄.
to be:

$$\frac{\sigma_E}{E} = \frac{2.8\%}{\sqrt{E\text{(GeV)}}} \oplus \frac{12\%}{E\text{(GeV)}} \oplus 0.3\%,$$

(5.1)

where $E$ is the electron beam energy in units of GeV. The terms in the right-hand side of the Eq. 5.1 are the so called stochastic, noise, and constant terms. The first is due to the fluctuations related to the development of the electromagnetic shower inside the calorimeter crystals, the second is due to electronic noise of the readout chain, and the third is related to the instrumental effect such as non-linear response, radiation damage, shower leakage among others.

The test beam ideal conditions clearly differ from those at the CMS experiment and therefore in situ measurements of the performance of the ECAL have been performed during the data-taking period at 7 and 8 TeV. One key measurement is the trigger efficiency for electron/photon ($e/\gamma$) candidates, the Level-1 trigger was operated with a threshold of $E_T = 20$ GeV (provided by $5 \times 5$ crystals) in 2012 and found to be above 99% efficient for $E_T > 40$ GeV, thus enabling a fully efficient $H \rightarrow \gamma \gamma$ search.

The $e/\gamma$ energy measurement depends upon the correct reconstruction of electromagnetic showers in the ECAL. Some $e/\gamma$ candidates interact – by bremsstrahlung or photon conversion – with the silicon tracker prior reaching the ECAL or their trajectories are modified due to the 3.8 T magnetic field causing the showers to spread on the azimuthal direction and thus their energy is shared by multiple crystals. In order to account for these effects and ensure a more accurate $e/\gamma$ reconstruction, a dynamic clustering algorithm is used to merge clusters of energy deposited that belong to the same electromagnetic shower into the so-called _superclusters_ (SCs). Once the SC is formed, the $e/\gamma$ candidate energy ($E_{e/\gamma}$) is reconstructed using the following expression:

$$E_{e/\gamma} = F_{e/\gamma} \cdot (G \cdot \sum S_i(t)C_iA_i + E_{ES})$$

(5.2)

where $F_{e/\gamma}$ is a correction accounting for the imperfect clustering, material, and geometric effect; $G$ is the ADC-to-GeV conversion; $S_i(t)$ is the time-dependent correction to account for the response variations of the $i$-th crystal; $C_i$ is the intercalibration coefficient of the $i$-th crystal; $A_i$ is the amplitude of the $i$-th crystal in ADC counts; and finally, $E_{ES}$ is the pre-shower energy – only relevant for $e/\gamma$s in the EE. Figure 5.16 shows the effect of the clustering process and the application of
Figure 5.16: The reconstructed Z invariant mass from $e^+e^-$ decays. The left and right panels show the reconstructed invariant mass for the EB and EE, respectively, with different algorithms to reconstructed electron energies.

the $F_e/\gamma$ correction by comparing the invariant mass of $e^+e^-$ pairs coming from a Z boson with respect to the usage of the simple fixed 5×5 cluster energy.

The inter-calibration coefficient is responsible for correcting the channel-to-channel variation in response. The main sources for such variations are the crystal light yield variations (up to ~15%) and the spread on the gain of the photodetectors (up to ~25%). An inter-calibration is carried out in situ by methods that exploit the time- and $\phi$-invariance of the energy flow in the crystals at a given $\eta$ in minimum-bias events, as well as the $\pi^0/\eta$ mass constraint to the photons pair from its decay, and the momentum constraint of isolated electrons from W and Z boson decays. The precision of these methods as a function of $\eta$ is shown in Figure 5.17. The invariant mass of diphotons consistent with a $\pi^0$ and $\eta$ used in the inter-calibration is shown in the left and right panels of Figure 5.18, respectively.

Another important ingredient to the precise measurement of the electromagnetic shower energy is the time dependent corrections, at CMS the ECAL crystals undergo changes in transparency due to the radiation received while collisions occur, while during downtime the transparency is recovered. In order to correct for the transparency changes a laser monitoring system is installed and run every ~40 minutes. Laser light ($\lambda = 440$ nm) close to the emission peak of PbWO$_4$ is impinged into all the crystals, thus tracking their response variations. The variations on transparency as a function of time for different $\eta$ ranges is shown in the left panel of Figure 5.19, where it is observed that the transparency variations are more severe at large pseudorapidities. The validity of the laser monitoring (LM) correction is checked using electrons from W decays. The stability of the LM correction is
Figure 5.17: The reconstructed Z invariant mass from $e^+e^-$ decays. The left and right panels show the reconstructed invariant mass for the EB and EE, respectively, with different algorithms to reconstructed electron energies.

Figure 5.18: The reconstructed Z invariant mass from $e^+e^-$ decays. The left and right panels show the reconstructed invariant mass for the EB and EE, respectively, with different algorithms to reconstructed electron energies.
The reconstructed Z invariant mass from $e^+e^-$ decays. The left and right panels show the reconstructed invariant mass for the EB and EE, respectively, with different algorithms to reconstructed electron energies.

estimated by the rms. of the $E/p$ ratio in these events and found to be about 0.1% and 0.3% for the EB and EE, respectively. The right panel of Figure 5.19 shows the LM correction effect on electron from W events in the EE. The effect of the inter-calibration and LM corrections is shown Figure 5.21, where the invariant mass of $e^+e^-$ pairs from Z decays is reconstructed with and without such corrections being applied.

Finally, the overall energy resolution of the CMS ECAL has been measured and compared to simulation, this is shown in the right panel of Figure 5.22. The energy resolution is found to be between 1-2% for $|\eta| < 1$ and between 3-5% in the EE, it is also observed that the simulation and measurement do not agree and that an extra constant term as a function of $\eta$ should be added to the simulation. The performance of the ECAL can also be observed in the width of the invariant mass of the Higgs boson. This is shown in the left panel of Figure 5.22, where $\sigma_{eff} = 1.36$ GeV is observed.
Figure 5.20: The reconstructed Z invariant mass from $e^+e^-$ decays. The left and right panels show the reconstructed invariant mass for the EB and EE, respectively, with different algorithms to reconstructed electron energies.

Figure 5.21: The reconstructed Z invariant mass from $e^+e^-$ decays. The left and right panels show the reconstructed invariant mass for the EB and EE, respectively, with and without the IC and the LM corrections.

5.4 The Hadronic Calorimeter

The CMS Hadron Calorimeter (HCAL) is surrounds the silicon tracker and the electromagnetic calorimeter. It is composed of four different subsystems: the barrel (HB), endcaps (HEs), the outer (HO), and the forward (HF) calorimeters. The HB and HE are located inside the cryostat of the superconducting solenoid and both are sampling calorimeters with brass as the absorber and plastic scintillator as the active medium. The HO is a plastic scintillator calorimeter located outside the superconducting solenoid cryostat and is designed to catch the energy leakage from the HB. The HF is a quartz fiber and steel calorimeter located at $z = \pm 11.15$ m, thus, extending the pseudorapidity coverage up to $|\eta| = 5$. The layout of the HCAL
Figure 5.22: The reconstructed Z invariant mass from $e^+e^-$ decays. The left and right panels show the reconstructed invariant mass for the EB and EE, respectively, with different algorithms to reconstructed electron energies.

Figure 5.23: The CMS HCAL layout.

is presented in Figure 5.23.

The hadronic energy resolution for the barrel HCAL and ECAL combination was measured in beam test using pions and protons and found to be:

$$\frac{\sigma_E}{E} = \frac{0.847 \pm 0.016 \text{ GeV}}{\sqrt{E(\text{GeV})}} \oplus 0.074 \pm 0.008. \quad (5.3)$$

The energy resolution in the endcaps is similar to that of the barrel.

The following passages are aimed to give a more detailed description of the four HCAL subsystems.
The Barrel Hadronic Calorimeter

The HB is a sampling calorimeter made of a brass absorber and plastic scintillator as the active medium. The whole EB is built out of two identical cylindrical structures, each of which is composed of 18 brass wedges. The pseudorapidity coverage of the HB reaches approximately $|\eta| = 1.4$ while the $\phi$ coverage is $360^\circ$. The segmentation of the HB is provided by the plastic scintillator tiles inserted in the layers of the brass wedges; the latter are segmented into four $\phi$ sector, while there are 16 scintillator tiles along the $\eta$ direction, thus providing the HB with an equivalent segmentation of $0.087 \times 0.087$ in $\eta$, $\phi$. Each wedge calorimeter is composed of 16 layers of absorber and 17 layers of plastic scintillator; the intermediate layers are made of brass absorber and 3 mm plastic scintillator while the first and last layers are made of stainless steel and thicker 9 mm plastic scintillator tiles. The very first layer is scintillator in order to detect showers developed in the electromagnetic calorimeter material. Figure 5.24 shows a schematic of a HB wedge. The 16 scintillator tiles of each layer are laid in a tray in order to facilitate their insertion and removal. Each tile’s scintillating light is collected by a green double-cladded wavelength-shifting (WLS) fibers from Kuraray (Y-11) placed in groove in the scintillator. Upon exiting the scintillating tile, each WLS is spliced into a clear fiber which subsequently ends in an optical connector at the back of the tray. At this point, optical cables take the light from the clear fiber into a 19 pixel hybrid photodiode (HPD), which is designed to work inside the 3.8 T magnetic field. The total interaction lengths ($\lambda_I$) of the HB varies with pseudorapidity, there are $5.8 \ \lambda_I$ at $\eta = 0$, increasing up to $10.6 \ \lambda_I$ at $|\eta| = 1.3$. The finalized HB is shown in Figure 5.25.

The Endcap Hadronic Calorimeter

The HE is a brass/plastic-scintillator sampling calorimeter that extend the pseudo-rapidity coverage from $1.3 < |\eta| < 3$. It is composed of 79-mm-thick brass plates with 9 mm gaps to accommodate the scintillator. The total material, including the crystals in the EE, is about $10 \ \lambda_I$. There are 18 layers – along the $z$-direction – of plastic scintillators: the first layer, right after the EE, is 9-mm-thick, while the rest are 3-mm-thick. The scintillators are segmented in the radial direction and their light is collected by embedded WLS fiber. The scintillator tiles and the WLS are laid in trays with a trapezoidal geometry. Figure 5.26 shows a schematic of the trays. The WLS are spliced to clear fibers which are subsequently terminated in an optical connector. Optical cables transport the light from the optical connector the HPDs, which, as mentioned earlier, could operate in the presence of a magnetic field. This
Figure 5.4: Isometric view of the HB wedges, showing the hermetic design of the scintillator sampling.

Figure 5.5: Scintillator trays.

After exiting the scintillator, the wavelength shifting fibres (WLS) are spliced to clear fibres (Kuraray double-clad). The clear fibre goes to an optical connector at the end of the tray. An optical cable takes the light to an optical decoding unit (ODU). The ODU arranges the fibres into read-out towers and brings the light to a hybrid photodiode [109]. An additional fibre enters each

Figure 5.24: A schematic drawn of one of the wedges of the CMS HB.

Figure 5.25: A photograph of the finalized CMS HB.
Figure 5.26: A schematic of the HE geometry in the $\phi$ direction is presented in the left panel. The configuration of two adjacent scintillator trays is presented in the right panel.

design results in a granularity of $0.087 \times 0.087$ ($\eta \times \phi$) for $|\eta| < 1.6$ and $0.17 \times 0.17$ for $|\eta| > 1.6$. Figure 5.27 shows one partially finalized HE, where only some of the scintillator trays have been inserted.

The Outer Hadronic Calorimeter

The space constraints posed by the superconducting solenoid limited the stopping power of the combined EB and HB and therefore their ability to fully contain hadronic showers. In order to overcome this limitation, another calorimeter layer, the HO, is located just outside the cryostat of the superconducting solenoid in the central region ($|\eta| < 1.3$) of the detector. The HO uses the solenoid coil as an additional absorber layer equivalent to $1.4 / \sin(\theta)$ $\lambda_I$. The active layer are 10-cm-thick plastic scintillator. The geometry of the HO is constrained to that of the muons system and therefore is composed of 5 rings along the $z$-direction (each ring is about 2.52 m). The HO rings are labelled with numbers -2, -1, 0, 1, and 2, which are located at $z$-positions of -5.342 m, -2.686 m, 0, +2.686 m, and +5.342 m, respectively. The central ring (ring-0) has two 10 cm thick layers of plastic scintillator at each side of a 19.5 cm iron slab located at $r = 3.82$ m and $r = 4.07$ m. The rest of the rings contain only one 10 cm thick scintillator layer and no extra absorber. This brings the total calorimeter depth to a minimum of about 12 $\lambda_I$ except at the boundary between the HB and the HE. Each ring is divided into 12 identical
Absorber geometry

The design of the absorber is driven by the need to minimize the cracks between HB and HE, rather than single-particle energy resolution, since the resolution of jets in HE will be limited by pileup, magnetic field effects, and parton fragmentation [110, 111]. The plates are bolted together in a staggered geometry resulting in a configuration that contains no projective "dead" material (figure 5.13). The design provides a self-supporting hermetic construction. The brass plates are 79-mm-thick with 9-mm gaps to accommodate the scintillators. The total length of the calorimeter, including electromagnetic crystals, is about 10 interaction lengths ($I$).

The outer layers of HE have a cutout region for installation of the photodetectors and front-end electronics. To compensate for the resulting reduction of material, an extra layer (1) is added to tower 18 [112]. The outer layers are fixed to a 10-cm-thick stainless steel support plate. The optical elements are inserted into the gaps after the absorber is completely assembled; therefore, the optical elements must have a rigid structure to allow insertion from any position.

Scintillator trays

The scintillation light is collected by wavelength shifting (WLS) fibres [113, 114]. The design minimizes dead zones because the absorber can be made as a solid piece without supporting structures while at the same time the light can be easily routed to the photodetectors. Trapezoidal–
Tiles

Scintillator tiles are made from Bicron BC408 scintillator plates of thickness $10 \pm 0.1$ mm. Figure 5.24 shows a typical HO scintillator tile. The WLS fibres are held inside the tile in grooves with a keyhole cross section. Each groove has a circular part (of diameter $1.35$ mm) inside the scintillator and a neck of 0.86 mm width. The grooves are 2.05-mm deep. Each tile has 4 identical grooves, one groove in each quadrant of the tile. The grooves closely follow the quadrant boundary. The corners of the grooves are rounded to prevent damage to the fibre at the bend and to ease fibre insertion. The groove design is slightly different for the tile where the optical connector is placed at the end of the tray. Since the tiles are large, 4 grooves ensure good light collection and less attenuation of light.

The HO has 95 different tile dimensions, 75 for layer 1 and 20 for layer 0. The total number of tiles is 2730 (2154 for layer 1 and 576 for layer 0).

Trays

All tiles in each slice of a sector are grouped together in the form of a tray. Each tray contains 5 tiles in rings $\pm 2$; 6 tiles in rings $\pm 1$ and 8 tiles in ring 0. The edges of the tiles are painted with Bicron reflecting white paint for better light collection as well as isolating the individual tiles of a tray. Further isolation of tiles is achieved by inserting a piece of black tedlar in between the adjacent tiles. The tiles in a tray are covered with a single big piece of white, reflective tyvek paper. Then they are covered with black tedlar paper to prevent light leakage. This package is placed between two black plastic plates for mechanical stability and ease of handling. Figure 5.25 shows a cross section of a tray to illustrate the different components. The plastic covers (top and bottom) have holes matching with the holes in the tiles. Specially designed countersunk screws passing through these holes fix the plastic covers firmly on the tiles. The 2 mm plastic sheet on the top has 1.6 mm deep channels grooved on it (on the outer side) to route the fibres from individual tiles to an optical connector placed in a groove at the edge of the tray. A 1.5-mm-wide straight groove runs along the edge of the top cover to accommodate a stainless steel tube. This is used for the passage of a radioactive source which is employed in calibrating the modules. Each connector has two holes and they are fixed to the scintillator-plastic assembly through matching holes. Each sector in each ring has 6 trays. There are 360 trays for layer 1 and 72 trays for layer 0.

Table 5.6: HO tile dimensions for different rings and layers. The tile sizes, which are constrained by muon ring boundaries, are also given.

<table>
<thead>
<tr>
<th>Tower #</th>
<th>Layer 0</th>
<th>Length (mm)</th>
<th>Tower #</th>
<th>Layer 1</th>
<th>Length (mm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Ring 0</td>
<td>Tower max</td>
<td>0.087</td>
<td>Tower max</td>
<td>0.087</td>
<td></td>
</tr>
<tr>
<td>1</td>
<td>331.5</td>
<td>351.2</td>
<td>1</td>
<td>331.5</td>
<td>351.2</td>
</tr>
<tr>
<td>2</td>
<td>334.0</td>
<td>353.8</td>
<td>2</td>
<td>334.0</td>
<td>353.8</td>
</tr>
<tr>
<td>3</td>
<td>339.0</td>
<td>359.2</td>
<td>3</td>
<td>339.0</td>
<td>359.2</td>
</tr>
<tr>
<td>4</td>
<td>248.8</td>
<td>189.1</td>
<td>4</td>
<td>248.8</td>
<td>189.1</td>
</tr>
<tr>
<td>Ring 1</td>
<td>Tower max</td>
<td>0.436</td>
<td>Tower max</td>
<td>0.960</td>
<td></td>
</tr>
<tr>
<td>5</td>
<td>391.5</td>
<td>420.1</td>
<td>5</td>
<td>391.5</td>
<td>420.1</td>
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</tr>
<tr>
<td>7</td>
<td>411.0</td>
<td>583.3</td>
<td>7</td>
<td>411.0</td>
<td>583.3</td>
</tr>
<tr>
<td>8</td>
<td>430.9</td>
<td>626.0</td>
<td>8</td>
<td>430.9</td>
<td>626.0</td>
</tr>
<tr>
<td>9</td>
<td>454.0</td>
<td>333.5</td>
<td>9</td>
<td>454.0</td>
<td>333.5</td>
</tr>
<tr>
<td>10</td>
<td>426.0</td>
<td></td>
<td>10</td>
<td>426.0</td>
<td></td>
</tr>
<tr>
<td>Ring 2</td>
<td>Tower max</td>
<td>0.960</td>
<td>Tower max</td>
<td>1.920</td>
<td></td>
</tr>
<tr>
<td>11</td>
<td>420.1</td>
<td>452.1</td>
<td>11</td>
<td>420.1</td>
<td>452.1</td>
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<tr>
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</tr>
<tr>
<td>14</td>
<td>626.0</td>
<td>658.0</td>
<td>14</td>
<td>626.0</td>
<td>658.0</td>
</tr>
<tr>
<td>15</td>
<td>333.5</td>
<td>365.5</td>
<td>15</td>
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</tr>
<tr>
<td>16</td>
<td>365.5</td>
<td></td>
<td>16</td>
<td>365.5</td>
<td></td>
</tr>
</tbody>
</table>

Figure 5.29: A schematic drawing presenting the geometry of the HO.

... z-direction. The quartz fibers propagate the Cherenkov light that the secondary particles of a shower produce when traversing through them. In order to separate electromagnetic showers that tend to be produced closer to the front face of the HF, from hadronic showers; two different types of fiber are embedded in the steel, and half of the fibers cover the whole length of the HF (165 cm $\approx 10\lambda_t$ ) while the other half start to run 22 cm from the front face of the HF; these two groups are read out separately by PMTs with a borosilicate glass window. The fibers are grouped in such a way that the effective granularity of the HF is $0.175 \times 0.175$ in $\eta \times \phi$. Figure 5.30 shows a photograph of some of the HF steel wedges equipped with quartz fibers.

5.5 The Muon Chambers

The CMS muon system is designed to trigger, identify, and measure the momenta of muons over a large kinematic range. Good muon momentum resolution is provided...
by the high granularity of the muon system and the relatively high magnetic field provided by the superconducting solenoid and its steel flux-return yoke. The muon system design requirements are the following:

- Trigger on single- and multi-muon event with thresholds from a few to 100 GeV
- Muon momentum (muon system only) resolution of 8-15% at 10 GeV, and 20-40% at 1 TeV
- Muon momentum (muon & tracker system) resolution of 1-1.5% at 10 GeV, and 6-17% at 1 TeV
- Charge miss-assignment < 0.1% at muon $p_T$ of 100 GeV

The muon system detector is based in gas ionization chambers. In order to achieve the physics requirement and comply with the geometry constraints, three different technologies are used: drift tubes (DT) chambers, cathode strip chambers (CSCs), and resistive plate chambers (RPCs). There are 250 DT chambers, 540 CSCs, and 610 RPCs; each chamber operates independently and is assembled into the muon detector system. In order to match the cylindrical geometry of the CMS detector, a barrel region – covering up to $|\eta| = 1.2$ – and 2 endcap regions – covering the $0.9 < |\eta| = 2.4$ region – are used. The barrel is equipped with DT chambers, the endcaps consists of CSCs, while the RPCs are used in both the barrel and endcap.
regions. The muon stations are collections of chambers around fixed $r$ and $z$ in the barrel and endcap regions, respectively. There are 4 stations in the barrel and endcaps, they are labeled MB1-MB4 and ME1-ME4, respectively. The barrel is divided into 5 “wheels” along the $z$-direction, wheel-0 (W0) is centered at $z = 0$, W+1 and W+2 are located in the positive $z$-region, while W-1 and W-2 are located in the negative $z$-region. The endcaps are divided in the $r$-direction, forming rings of CSCs and RPCs. Thus, the former are labeled ME1/n-ME4/n, where n is an index that increments radially outwards. Figure 5.31 show a layout of the muon system with its different detectors as well as the other systems of the CMS detector.

The Drift Tube Chambers

The DTs are composed of standard rectangular cells filled with a gas mixture of 85% Ar and 15% CO$_2$, the latter are called drift cells. Each cell has a transverse size of $42 \times 13$ mm$^2$, they are equipped with a gold-plated stainless-steel anode wire of 50 $\mu$m diameter at the center, and four electrodes – including two cathode strips – at each side of the cell to shape the electric field. The anode wire operates at $+3,600$ V while the top/bottom electrodes and the electrodes on the side are operated at $+1,800$ V and $-1,800$ V, respectively. The gas mixture in the drift cell provide a drift velocity of $55 \mu$m/s and good quenching properties. The maximum drift time was measured to be around 400 ns. Drift cells are grouped in 4 parallel and staggered layers – each layer at different $r$ – to form a super-layer (SL). All DTs chambers – except those in MB4 – are formed by 2 SLs with wires along the $z$-direction, thus measuring
The ability of the muon chambers to provide a fast, well-defined signal is crucial and, because the fundamental readout frequency is 40 MHz, clock times are often quoted in quantity for both the accelerator and the detectors is the bunch crossing (BX) “unit” of 25 ns, between bunch crossings, in which proton–proton collisions occur. Thus, a convenient time separated by one (or more) time steps of 25 ns. This is therefore also the minimum separation.

The LHC is a bunched machine, in which the accelerated protons are distributed in bunches timing discrimination.

Crucial properties of the DT and CSC systems are that they particles to about 5% of all muons reaching the first station and to about 0.2% of all muons absorbing material before the first muon station reduces the contribution of punch-through transition region between the barrel outer wheels and the endcap disks [15]. The amount of 96–99% except in the gaps between the 5 wheels of the yoke (at

The Cathode Strips Chambers

Due to the higher rate of particles and the non-uniformities of the magnetic field in the endcap regions standard DTs are not a good candidate to detect muons in this

Figure 5.32: (Left) a schematic of a barrel chamber with DT and SL clearly labeled. (Right) a schematic of a drift cell.

Figure 5.33: A photograph of the a barrel wheel during construction. The DT chambers are gray while the steel return-yokes are painted in red.

\[ r - \phi \] coordinates, and one SL with wires running perpendicular to the z-axis at fixed distance from the beam pipe, and therefore measuring \( r - z \) coordinates. The MB4 chambers have only an \( r - \phi \) SL. The left and right panels of Figure 5.32 show schematics of a barrel chamber and a DT, respectively. The chambers are 2.5 m long in the z-direction, and their transverse size varies with the station, raging from 1.9 for MB1 and 4.1 for MB4. Figure 5.33 shows a photograph of a barrel wheel during construction.

The Cathode Strips Chambers

Due to the higher rate of particles and the non-uniformities of the magnetic field in the endcap regions standard DTs are not a good candidate to detect muons in this
region. Therefore, the muon endcap system is composed of cathode strip chambers; which have a fast response, can be finely segmented, and can be operated in the presence of a non-uniform magnetic field – Figure 5.3 shows the magnetic field lines and intensity in the CMS detector. Each endcap regions has four disk-shaped stations perpendicular to the z-axis. The endcap stations are formed by different sizes of CSC. The CSC units have 6 layer – again, along the z-axis –, each of which has cathode strips along the r-direction and wires running perpendicular to the strips. Thus, the CSC units provide a 2-dimensional measurement in the $r-\phi$ plane. All CSC are filled with a gas mixture composed of 50% CO$_2$, 40% Ar, and 10% CF$_4$; the ME1/1 chambers are operated at an anode voltage of 2,900 V while the rest of them at of 3,600 V. Each chamber has 80 cathode strips subtending an angle between 2.2 and 4.7 mradian. The ME1/1 anode wires are 30$\mu$m in diameter and placed 2.5 mm apart, while the rest of the chambers wire’s are 50$\mu$m in diameter and placed 3.12 or 3.16 mm apart. Alternative layers are shifted in order to minimize gaps between chambers. A schematic of one the CSC is shown in Figure 5.34 while a photograph of one of the endcaps during construction is shown in Figure 5.35.

The Resistive Plate Chambers
The resistive plate chambers of the muon system are a complementary and dedicated trigger system with excellent time resolution in order to correctly identify the correct bunch crossing when the LHC is operating at high luminosities. The barrel and endcaps of the muon systems are equipped – in addition to the main their main tracking systems, DT chambers and CSCs, respectively – with RPCs, which provide
an independent trigger with lower $p_T$ thresholds up to $|\eta| = 1.6$. The resistive plates are double-gap chambers consisting of two 2-mm-thick resistive Bakelite plates separated by a 2-mm-thick gas gap. The gas mixture is 95.2% Freon, 4.5% isobutane, and 0.3% sulphur hexafluoride. The outer surface of the resistive plates is coated with a conductive graphite layer and operated at 9,600 V. Figure 5.36 shows a schematic layout of a resistive plate. The geometry of the RPCs follows closely that of the DT chambers and the CSCs, thus, there are organize in 4 and and 3 stations in the barrel and each of the endcaps, respectively. In the barrel, there are two RPCs at each side of the DT chambers in the first two stations while there is only one in the front of the DT chamber in stations 3 and 4. In the endcaps, each station is divided into 3 rings at different radial distances. The RPCs are divided into 2 or 3 partitions in $\eta$. Figure 5.31 shows the locations of the RPCs in the muon system, labeled with blue.

5.6 The Trigger System
Due to the large rate of proton-proton collisions, the large amount of data needed to be recorded in order to reconstruct an event, and the constraints posed by the DAQ and computing systems, a selection mechanism that significantly reduces the rate of events needed to be deployed. This task is carried out by the CMS trigger system,
Overview of the muon system

2-mm-thick bakelite plate
2-mm-thick gas gap
Readout strip
Backward roll
Forward roll
GND
V
RPC Up
RPC Down

Figure 7: Schematic view of a generic barrel RPC with 2 "roll" partitions.

cap (RE) the 3 stations are RE1, RE2, and RE3. The innermost barrel stations RB1 and RB2 are instrumented with 2 layers of RPCs facing the innermost (RB1in and RB2in) and outermost (RB1out and RB2out) sides of the DT chambers. Every chamber is then divided from the readout point of view into 2 or 3 partitions called "rolls" (Fig. 7). In the endcaps, each station is divided into 3 rings (identified as rings 1, 2, and 3) at increasing radial distance from the beam line. Ring 1 was not instrumented in 2010; the RPC system therefore covered only the region up to $|\eta| = 1.6$. Each endcap ring is composed of 36 chambers covering the full azimuthal range. From the readout point of view, each endcap chamber is divided into 3 partitions (rolls) identified by the letters A, B, and C. Thus the endcap RPCs are identified in the following way: $\text{RE}n/r/x$ where $n$ is the station ($\pm 1$, $\pm 2$, $\pm 3$), $r$ is the ring (2 or 3), and $x$ is the roll (A, B, or C).

2.3 Muon triggering, tracking, and reconstruction

The triggering scheme of the CMS muon system relies on 2 independent and complementary triggering technologies: one based on the precise tracking detectors in the barrel and endcaps, and the other based on the RPCs. The tracking detectors provide excellent position and time resolution, while the RPC system provides excellent timing with somewhat poorer spatial resolution.

For values of $p_T$ up to 200 GeV/c, the momentum resolution is dominated by the large multiple scattering in the steel, combined in the endcaps with the effect of the complicated magnetic field that is associated with the bending of the field lines returning through the barrel yoke. The detectors designed to meet the required measurement specifications and to operate in this environment are robust, multilayered chambers from which the fine spatial resolution required for good momentum resolution at high muon momenta can be obtained with a modest resolution per layer.

The large number of layers in each tracking chamber is exploited by a trigger hardware process thus starting the event selection process. The CMS trigger is a two stage system, composed of two sequential but independent trigger systems. The first is the Level-1 (L1) trigger, which is largely based in FPGAs and ASICs, and therefore uses coarse and crude information to reduce the rate from 40 MHz to 100 kHz. The second is the High-Level Trigger (HLT), which is a software based system, implemented in computing farm with approximately 16,000 CPU cores, that reduces the L1 trigger rate to a viable level for storage of about 1 kHz.

The L1 trigger has different components. First, the Local Triggers, also called Trigger Primitive Generators (TPG), are based in the calorimeter trigger towers, track segments, and hit patterns in the muon chambers. Second, the Regional Triggers combine the information from the TPGs to rank and sort trigger objects such as electron or muon candidates in limited spatial regions. Ranking is assigned based on the energy/momentum and quality of the parameters measured by the L1 trigger system. Third, The Global Calorimeter and Global Muon Triggers determine the highest-ranked calorimeter and muon object in the entire CMS detector and they transfer this information to the last step in the L1 hierarchy, the Global Trigger. The latter decides whether to reject or accept to event to be further analyze at the HLT. This decision is based on various algorithms and the readiness of the sub-detectors and the DAQ system, which is in turn determined by the Trigger Control System (TCS). The latency of the L1 trigger is about 4 $\mu$s. A schematic of the architecture
Figure 8.1: Architecture of the Level-1 Trigger.

The High-Level Trigger is software based and constructed in a modular fashion. The time of the HLT decision is fundamentally constraint by the computing power of the HLT farm and the L1 output rate, this requires the HLT decisions to be made in about 300 ms; surpassing this limit will result in the inability to efficiently collect data. The HLT modular design is such that it allows logically independent trigger paths, which to a large extent could be run in parallel – thus better using the computing resources. Each trigger path is sequence of software modules and classified based on their function, there are reconstruction modules (producers) and filtering modules (filters). The latter usually accept or reject events based on the properties of physics object or kinematic variables, such as the new physics sensitive $M_R$ and $R^2$, described in Section 6.2. The HLT modules are organized in ascending complexity, such that the faster algorithms are executed first and thus the filters can reject events at an earlier stage. The online HLT reconstruction is kept as similar as possible to that of the offline reconstruction, taking into account the computation and time constraints. A schematic diagram of the HLT is provided in Figure 5.38.

At the LHC the data processing is limited by the bandwidth at which the events are stored on disk, usually resulting in an increment on the trigger thresholds (physics objects $p_T$, missing transverse energy, etc.). In order to overcome this limitation,
The CMS experiment has implemented special trigger paths where the event data-size is kept small, and thus more events – in other words triggers paths with lower thresholds – can be recorded without stressing the allocated bandwidth. The latter solution has been adopted for the alignment and calibration of the detector and to increase the acceptance to certain event topologies interesting to probe new physics. The left and right panels of Figure 5.39 show a summary of the data streams recorded by the CMS experiment during 2012 and 2015, respectively.
The Trigger of the CMS Experiment

While maintaining the largest possible acceptance of interesting physics signal events from the collisions and efficiently rejecting the non-interesting ones, Figure 5.12 presents the design chosen for the trigger of the CMS experiment. It is a two-level system. The Level 1 (L1) trigger is based on FPGA and custom ASIC technology and uses information from the calorimeters and muon spectrometers of the experiment in order to accept or reject an event; it reduces the event rate down to approximately 100 kHz, acceptable by the readout electronics. The High-Level Trigger (HLT) is implemented in software running on a farm of commercial computers which includes approximately 16,000 CPU cores, and reduces the L1 output rate to the sustainable level for storage and physics analysis of about 1 kHz. The HLT software consists of a streamlined version of the offline reconstruction algorithms; it exploits the same software used for offline reconstruction and analysis, optimized in order to comply with the strict time requirements of the online selection.

The L1 trigger decision is made within a fixed time interval of less than 4 µs. The operational L1 output rate of 100 kHz, together with the number of CPUs in the HLT farm, imposes a fundamental constraint on the amount of time available for the HLT to process events. Exceeding this limit impacts the ability of CMS to collect data efficiently. Given the CPUs available in 2015, the timing budget of the HLT is measured to be about 300 ms when compared to the previous year.

Figure 5.39: A summary of the data streams recorded during (left) 2012 and (right) 2015.
Part III

Searches for New Physics with the Compact Muon Solenoid Experiment
RAZOR APPROACH TO SEARCH FOR BSM PHYSICS

6.1 Introduction

The challenges at hadron collider experiments are many: one of the most well known is the fact the the energy and momentum of the parton-parton (hard) interaction is not known. This limitation, in addition with the fact that a large number of the proposed extensions of the SM (e.g. SUSY) predict new particles that are weakly interacting and therefore escape the detector systems without a trace, has made events with large momentum imbalance in the plane transverse to the beam a key signature to search for BSM physics. The momentum imbalance in the transverse plane (missing energy) is quantified by $\not{p}_T^{\text{miss}}$ which is defined as

$$\not{p}_T^{\text{miss}} = -\sum_{i=0}^{n_{\text{pf}}} \vec{p}_T^i,$$

where $\vec{p}_T^i$ is the measured transverse momentum of a PF candidate, and $n_{\text{pf}}$ is the total number of PF candidates reconstructed.

Additionally, in SUSY models with R-parity conservation the originally pair produced super-partners undergo a cascade decay and at least two particles (the LSPs) will escape detection and therefore further reduce the ability to fully reconstruct the event kinematics due to the lost information. Subsequently, all these effects result in lost of sensitivity as the discrimination power between a possible signal and the SM background processes is reduced. In order to recover sensitivity, different kinematic variables are employed which are functions of the visible objects momenta and the $\not{p}_T^{\text{miss}}$. These kinematic variables have been shown to improve signal to background discrimination but are often model dependent. One example of such variables are the razor variables [224, 90], which have been widely used by the CMS collaboration to search for SUSY [98, 234] and recently shown to have good sensitivity for DM direct production at hadron colliders [137]. The razor variables $M_R$ and $R^2$ provide an estimate of the underlying mass scale of the event and a means of significantly suppressing SM backgrounds – particularly QCD multijet – respectively.

Since the two searches for BSM physics presented in this thesis are based on the razor variables, this chapter describes their derivation (see Section 6.2) and main features when searching for new physics (see Section 6.3).
6.2 The Razor Variables

The razor variables were originally derived [224, 90] for squark pair-production in the context of SUSY; this topology is represented by the Feynman diagram shown in Figure 6.1, where the proton-proton collision pair produces two squarks ($\tilde{q}_1, \tilde{q}_2$) which subsequently decay into a SM quark and the LSP ($\tilde{q}_i \rightarrow q_i \tilde{\chi}_1^0$).

One interesting quantity that provides access to the mass scale of the SUSY particles is the magnitude of the 3-momentum of the quark in the rest frame of the squark. It is actually more convenient to write down twice this quantity:

$$2|\vec{p}_q^i| = 2|\vec{p}_{\tilde{\chi}_1^0}| = \frac{\sqrt{m_{\tilde{q}}^4 - 2m_{\tilde{q}}^2m_{\tilde{\chi}_1^0}^2 + m_{\tilde{q}}^4} - 2m_{\tilde{q}}^2m_{\tilde{\chi}_1^0}^2 - 2m_{\tilde{q}}^2m_{\tilde{\chi}_1^0}^2 + m_q^4}}{m_{\tilde{q}}}, \quad (6.2)$$

where $m_{\tilde{q}}$ is the squark mass, $m_{\tilde{\chi}_1^0}$ is the LSP mass, and $m_q$ is the SM quark mass. Eq. 6.2 can be simplified if the SM quarks are assumed massless – which is mostly accurate with the exception of the top-quark. This simplification is also useful to define:

$$M_\Delta = 2|\vec{p}_q^i| = \frac{m_{\tilde{q}}^2 - m_{\tilde{\chi}_1^0}^2}{m_{\tilde{q}}}. \quad (6.3)$$

$M_\Delta$ is sensitive to the mass-splitting between the squark and the LSP and therefore is usually referred to as the characteristic mass scale of the event. For example, in the case of the $W \rightarrow \ell \nu$ decay, $M_\Delta$ is simply the mass of the $W$ boson.

The razor variable $M_R$ provides an estimate of $M_\Delta$ by approximating the boosts needed – since the actual boosts are impossible to reconstruct due to the missing particles, which can be viewed as an undetermined system of equations with not enough constraints – to go from the laboratory frame (lab frame) to the squark rest frame. This approximation is done in two steps: first, there is a common boost to go from the lab frame to the center-of-momentum (CM) frame, and then an equal and opposite boost is applied to each squark to go from the CM frame to their respective
Figure 6.2: An schematic of the different rest frames involved in deriving the razor variables. The lab frame is in the left panel, the CM frame is in the middle panel, and the squark rest frames are in the right panel.

rest frame. Figure 6.2 depicts the three frames and the boosts needed to move from the lab frame to the squark rest frames.

The approximate boost relating the CM frame and the rest frames of each of the squarks ($\tilde{\beta}_R$) is asymmetric since the two squarks are recoiling against each other in the CM frame. $\tilde{\beta}_R$ is obtained by adding the condition that in their respective squark rest frame the magnitude of each quark momentum is the same; this is to say that the two decays are identical up to the decay angle. Since the quarks are assumed to be massless the condition is:

$$E_s^{q_1} = E_s^{q_2}$$  
$$\Rightarrow \gamma_R(E_{CM}^{q_1} - \tilde{\beta}_R \cdot \vec{p}_{CM}^{q_1}) = \gamma_R(E_{CM}^{q_2} + \tilde{\beta}_R \cdot \vec{p}_{CM}^{q_2})$$  
$$\Rightarrow \tilde{\beta}_R \cdot (\vec{p}_{CM}^{q_1} + \vec{p}_{CM}^{q_2}) = E_{CM}^{q_1} - E_{CM}^{q_2},$$

where $E_s^{q_i}$ is the energy of the $i$-th quark on its respective squark rest frame, $E_{CM}^{q_i}$ is the energy of the $i$-th quark in the CM frame, $\vec{p}_{CM}^{q_i}$ is the momentum of the $i$-th quark in the CM frame, and $\gamma_R$ is the gamma factor corresponding to $\tilde{\beta}_R$. This symmetry constraint is not enough to uniquely determine $\tilde{\beta}_R$ and therefore an external condition is required; this external condition is such that the boost minimizes the sum of the quarks energies, i.e.
\[ \frac{\partial (E_{q_1} + E_{q_2})}{\partial \vec{\beta}_R} = 0. \]  

(6.7)

With the addition of this extremal condition, the boost is now found to be

\[ \vec{\beta}_R = \frac{\vec{p}_{CM}^{q_1} - \vec{p}_{CM}^{q_2}}{E_{CM}^{q_1} + E_{CM}^{q_2}}. \]  

(6.8)

Now, let’s turn to the boost that relates the CM and the lab frames. The later is approximated by a purely longitudinal boost (\( \vec{\beta}_L = \vec{\beta}_L \cdot \hat{z} \)). Again, the assumption that the boost is in the longitudinal direction only is not enough to uniquely determine \( \vec{\beta}_L \) and therefore an additional constraint is needed. We require that the longitudinal momentum of the visible system in the CM frame ought to be zero—only resembling the true constraint that the sum of the visible and invisible systems is indeed zero. This additional constraint,

\[ p_{CM}^{1z} + p_{CM}^{2z} = 0, \]  

(6.9)

is sufficient to find the magnitude of the boost:

\[ \vec{\beta}_L = \frac{p_{1z}^{L} + p_{2z}^{L}}{E_{l}^{q_1} + E_{l}^{q_2}}. \]  

(6.10)

With both boost now found, the only remaining task is to transform the quantities in the squark rest frame to the lab frame to be able to use them in a realistic environment. We define the characteristic mass estimator (\( M_R \)), which is related to \( M_\Lambda \), in the following fashion:

\[ M_R \equiv \gamma_R (E_{s}^{q_1} + E_{s}^{q_2}) = \gamma_R M_\Lambda. \]  

(6.11)

When expressed in the corresponding lab frame quantities by applying the boosts just found above, \( M_R \) takes the form:

\[ M_R = \sqrt{(E_{l}^{q_1} + E_{l}^{q_2})^2 - (p_{l}^{1z} + p_{l}^{2z})^2}. \]  

(6.12)

We now proceed to construct another variable purely from the transverse information in the detector. Inspired by the ideal back-to-back topology of QCD dijet events we define the razor transverse mass variable:

\[ M_T^{R} = \sqrt{\frac{E_{T}^{\text{miss}} (p_{T}^{q_1} + p_{T}^{q_2}) - p_{T}^{\text{miss}} \cdot (p_{T}^{q_1} + p_{T}^{q_2})}{2}}. \]  

(6.13)
This variable estimates the transverse momentum imbalance in the event and therefore is useful to discriminate between signal and background. Additionally, $M_R^R$ is strictly smaller than $M_R$ ($M_R < M_R$), with this in mind we define the dimensionless razor variable:

$$R^2 = \left( \frac{M_R^R}{M_R} \right)^2 .$$

(6.14)

Background events with no missing energy will tend to have values of $R^2$ close to zero, while signal events will have values of $R^2$ that are on average larger than zero.

The razor variables have been also generalized to topologies which include more than two visible objects in the detector. In order to achieve this, a simple approach has been taken. Whenever more than two visible objects are present, the event is forced into a dijet-like topology by clustering all visible objects into two megajets. All possible permutations of these megajets are formed by adding the 4-momenta of the visible objects; we choose the configuration that minimizes $M_i^2 + M_j^2$, where $M_i$ is the mass of the $i$-th megajet.

### 6.3 Application of the Razor Variables to Search for BSM Physics

The razor variables have been employed in canonical searches for SUSY at the LHC [90, 234, 159] and have been shown to have good sensitivity in a variety of final states. In this section a review of the main properties of this variables and a summary of the main results of the searches in references [90, 234, 159] are given.

Let’s first examine if the expected behavior of the razor variables for the canonical squark pair production (see Figure 6.1) is indeed observed. Figure 6.3 shows the $M_R$ and $R^2$ for squark pair production in the left and right panel, respectively. The mass of the squark was fixed to 1150 GeV and the LSP mass was varied between 50-900 GeV. As expected, $M_R$ peaks a characteristic value related to $M_\Lambda$. For example, $M_\Lambda$ is approximately 930 GeV when the LSP mass is 500 GeV – this can be calculated by just plugging in the appropriate mass values into Equation 6.3 – and for this case $M_R$ peaks at around $\sim$1000 GeV. Additionally, $R^2$ exhibits a falling distribution that on average is much higher than the expected values for the SM processes – again, especially the daunting QCD dijet production. Finally, Figure 6.4 shows the 2-dimensional $M_R$-$R^2$ distribution for the same model, but adding contours of constant SM background. It is observed that the signals populate very clear regions on this 2-dimensional plane and that the SM background is reduced significantly.
We choose the clustering of the three particles labeled ant masses of the two megajets.

The number of ways of partitioning a set of \( n \) elements into \( k \) non-empty subsets is given by the Stirling number of the second kind, \( S(n;k) \).

Figure 3.6: Distribution of \( R \)

The first result using razor variables was carried out by CMS using data collected at a center-of-mass energy of 7 TeV where an inclusive final state approach was adopted, selecting jets, b-jets, and also leptons in the final state. There was no deviation from the SM background estimation and 95% confidence level (CL) limits on the

Figure 6.3: Razor variables distributions for squark pair-production. \( M_R \) is shown in the left panel and \( R^2 \) is shown in the right panel. The squark mass is set to 1150 GeV while the LSP mass is varied and shown with different color lines.

Figure 6.4: The 2-dimensional \( R^2-M_R \) distribution. The squark mass is set to 1150 GeV while the LSP mass is varied and shown with different color squares. The orange band represents the contour of constant SM background.

(around 5 orders of magnitude between the first and third contour) when more extreme values of the razor variables are required.

The first result using razor variables was carried out by CMS using data collected at a center-of-mass energy of 7 TeV where an inclusive final state approach was adopted, selecting jets, b-jets, and also leptons in the final state. There was no deviation from the SM background estimation and 95% confidence level (CL) limits on the
Figure 6.5: Razor analysis 95% CL. limit in the $m_0$-$m_{1/2}$ plane of the CMSSM model using 7 TeV data. The model parameters have the following values: $\tan(\beta) = 10$, $A_0 = 0$, and $\text{sign}(\mu) = +1$.

CMSSM model were placed. Figure 6.5 shows the combined limit. CMS released another search for SUSY with razor variables using the full dataset ($\sim 20$ fb$^{-1}$) collected at 8 TeV, again with no observed significant deviations from the SM background estimation. It is of note that the background estimation, which employs a fit to the sidebands of the data using an analytical functional form, was much improved with respect to the 7 TeV counterpart. The results were interpreted in the context of SUSY simplified models of gluino and top-squark (stop) pair production where the branching ratios (BRs) of the particles involved were varied in order to produce a more general result. Figure 6.6 shows the 95% CL. limits for gluino and stop pair-production in the left and right panels, respectively. It is observed that the gluino is excluded around 1200-1400 GeV depending on the exact values of the BRs, and the stop is excluded at about 700 GeV regardless of its BRs (these exclusion numbers assume a neutralino mass of about 1 GeV). Recently, an updated search using the first portion of 13 TeV data ($\sim 2.1$ fb$^{-1}$) was released following greatly the approach taken in the 8 TeV counterpart but adding an additional and totally independent background estimation based on scale factors derived in data control regions. Figure 6.7 show the 95% CL. limits for gluino pair-production. It is observed that the gluino is excluded around 1400-1600 GeV depending on the exact values of the BRs. It is of note that with only 10% of the integrated luminosity the 13 TeV result surpasses the corresponding 8 TeV result.
Figure 6.6: Razor analysis 95% CL. limits for (left) gluino and (right) stop pair-production using 8 TeV data. The limits are shown for different branching ratios of the particles involved.

Figure 6.7: Razor analysis 95% CL. limits for gluino pair-production using 13 TeV data. The limits are shown for different branching ratios of the particles involved.
The razor approach has been taken beyond squark and gluino pair-production to probe dark matter direct production and also to look for possible anomalous production of Higgs bosons. Searches for dark matter direct production have been a very hot topic at the LHC where the most common final state includes a single high-$p_T$ jet. It was suggested that the razor variables could have comparable sensitivity to dark matter direct production [137] using a different kinematic phase-space, since they require at least two jets, and therefore increase the overall sensitivity to such a signal. Chapter 7 presents the CMS search that carries out this idea, confirming the good sensitivity to direct dark matter production. Additionally, the razor variables have also been used to search for anomalous Higgs production by selecting events with jets and a diphoton pair whose invariant mass is consistent with the Higgs mass. The first search of this kind was carried out using the entire 8 TeV dataset [236], where an interesting excess of events was observed at high values of $M_R$ and the results interpreted in the context of electroweak SUSY (see Section 8.2). Chapter 8 presents an updated result of this search with an entirely different background estimation technique and using 15.3 fb$^{-1}$ of 13 TeV data.
Chapter 7

SEARCHES FOR DARK MATTER AT THE LHC WITH 8 TEV PP COLLISIONS

7.1 Introduction
The existence of dark matter (DM) in the universe, originally proposed [260] to reconcile observations of the Coma galaxy cluster with the prediction from the virial theorem, is commonly accepted as the explanation of many experimental phenomena in astrophysics and cosmology, such as galaxy rotation curves [158, 231], large structure formation [254, 76, 246], and the observed spectrum [243, 60, 244, 27] of the cosmic microwave background [54]. A global fit to cosmological data in the $\Lambda$CDM model (also known as the standard model of cosmology) [80] suggests that approximately 85% of the mass of the universe is attributable to DM [27]. To accommodate these observations and the dynamics of colliding galaxy clusters [101], it has been hypothesized that DM is made mostly of weakly interacting massive particles (WIMPs), sufficiently massive to be in nonrelativistic motion following their decoupling from the hot particle plasma in the early stages of the expansion of the universe.

While the standard model (SM) of particle physics does not include a viable DM candidate, several models of physics beyond the SM, e.g., supersymmetry (SUSY) [219, 144, 248, 253, 130] with $R$-parity conservation, predicts the existence of WIMPs. In these models, pairs of DM particles can be produced in proton-proton (pp) collisions at the CERN LHC. Dark matter particles would not leave a detectable signal in a particle detector. When produced in association with high-energy quarks or gluons, they could provide event topologies with jets and a transverse momentum ($p_T$) imbalance ($\vec{p}_T^{\text{miss}}$). The magnitude of $\vec{p}_T^{\text{miss}}$ is referred to as missing transverse energy ($E_T^{\text{miss}}$). The ATLAS and CMS collaborations have reported searches for events with one high-$p_T$ jet and large $E_T^{\text{miss}}$ [24, 95], which are sensitive to such topologies. In this chapter, we refer to these studies as monojet searches. Complementary studies of events with high-$p_T$ photons [180, 23]; $W$, $Z$, or Higgs bosons [18, 19, 21, 20]; $b$ jets [7] and top quarks [7, 169, 238]; and leptons [22, 181] have also been performed.

This paper describes a search for dark matter particles $\chi$ in events with at least two jets of comparable transverse momenta and sizable $E_T^{\text{miss}}$. The search is based
on the razor variables $M_R$ and $R^2$ [224, 90]. Given a dijet event, these variables are computed from the two jet momenta $\vec{p}_j^1$ and $\vec{p}_j^2$, according to the following definition:

$$M_R = \sqrt{(|\vec{p}_j^1| + |\vec{p}_j^2|)^2 - (p_{zj}^1 + p_{zj}^2)^2},$$

$$R = \frac{M_T^R}{M_R},$$

with

$$M_T^R = \sqrt{\frac{E_T^{miss}(p_T^{j1} + p_T^{j2}) - \vec{p}_T^{miss} \cdot (\vec{p}_T^{j1} + \vec{p}_T^{j2})}{2}}. \quad (7.1)$$

In the context of SUSY, $M_R$ provides an estimate of the underlying mass scale of the event, and quantity $M_T^R$ is a transverse observable that includes information about the topology of the event. The variable $R^2$ is designed to reduce QCD multijet background; it is correlated with the angle between the two jets, where co-linear jets have large $R^2$ while back-to-back jets have small $R^2$. These variables have been used to study the production of non-interacting particles in cascade decays of heavier partners, such as squarks and gluinos in SUSY models with $R$-parity conservation [98, 234]. The sensitivity of these variables to direct DM production was suggested in Ref. [137], where it was pointed out that the dijet event topology provides good discrimination against background processes, with a looser event selection than that applied in the monojet searches. Sensitivity to DM production is most enhanced for large values of $R^2$, while categorizing events based on the value of $M_R$ improves signal to background discrimination and yields significantly improved search sensitivity to a broader and more inclusive class of DM models. The resulting sensitivity is expected to be comparable to that of monojet searches [137, 209]. This strategy also offers the possibility to search for DM particles that couple preferentially to $b$ quarks [32], as proposed to accommodate the observed excess of photons with energies between 1 and 4 GeV in the gamma ray spectrum of the galactic center data collected by the Fermi-LAT gamma-ray space telescope [156]. The results are interpreted using an effective field theory approach and the Feynman diagrams for DM pair production are shown in Fig. 7.1.

Unlike the SUSY razor searches [234, 90], which focus on events with large values of $M_R$, this study also considers events with small values of $M_R$, using $R^2$ to discriminate between signal and background, in a kinematic region ($R^2 > 0.5$) excluded by the baseline selection of Refs. [234, 90].
Figure 7.1: Feynman diagrams for the pair production of DM particles corresponding to an effective field theory using a vector or axial-vector operator (left), and a scalar operator (right).

A data sample corresponding to an integrated luminosity of 18.8 fb$^{-1}$ of pp collisions at a center-of-mass energy of 8 TeV was collected by the CMS experiment with a trigger based on a loose selection on $M_R$ and $R^2$. This and other special triggers were operated in 2012 to record events at a rate higher than the CMS computing system could process during data taking. The events from these triggers were stored on tape and their reconstruction was delayed until 2013, to profit from the larger availability of processing resources during the LHC shutdown. These data, referred to as “parked data” [104], enabled the exploration of events with small $M_R$ values, thereby enhancing the sensitivity to direct DM production.

This paper is organized as follows: section 7.2 describes the data and simulated samples of events used in the analysis. Sections 7.3 and 7.4 discuss the event selections and categorization, respectively. The estimation of the background is described in Section 8.5. The systematic uncertainties are discussed in Section 7.6, while Section 7.7 presents the results and the implications for several models of DM production. A summary is given in Section 7.8.

7.2 Data set and simulated samples

The analysis is performed on events with two jets reconstructed at L1 in the central part of the detector ($|\eta| < 3.0$). The L1 jet triggers are based on the sums of transverse energy in regions $\Delta \eta \times \Delta \phi$ approximately 1.05x1.05 in size [88] (where $\phi$ is the azimuthal angle in the plane transverse to the LHC beams.). At the HLT, energy deposits in ECAL and HCAL are clustered into jets and the razor variables $R^2$ and $M_R$ are computed. In the HLT, jets are defined using the FastJet [73] implementation of the anti-$k_T$ [74] algorithm, with a distance parameter equal to 0.5. Events with at least two jets with $p_T > 64$ GeV are considered. Events are selected with $R^2 > 0.09$ and $R^2 \times M_R > 45$ GeV. This selection rejects the majority of the background, which tends to have low $R^2$ and low $M_R$ values, while keeping the
events in the signal-sensitive regions of the \((M_R, R^2)\) plane. The trigger efficiency, measured using a pre-scaled trigger with very loose thresholds, is shown in Table 7.1. The requirements described above correspond to the least stringent event selection, given the constraints on the maximum acceptable rate.

Table 7.1: Measured trigger efficiency for different \(M_R\) regions. The selection \(R^2 > 0.35\) is applied. The uncertainty shown represents the statistical uncertainty in the measured efficiency.

<table>
<thead>
<tr>
<th>(M_R) region (GeV)</th>
<th>200–300</th>
<th>300–400</th>
<th>400–3500</th>
</tr>
</thead>
<tbody>
<tr>
<td>Trigger efficiency (%)</td>
<td>91.1±1.5</td>
<td>90.7±2.3</td>
<td>94.4±2.4</td>
</tr>
</tbody>
</table>

Monte Carlo (MC) simulated signal and background samples are generated with the leading order matrix element generator \textsc{MadGraph v5.1.3} [40, 41] and the CTEQ6L parton distribution function set [216]. The generation includes the \textsc{Pythia} 6.4.26 [240] \(Z2^*\) tune, which is derived from \(Z1\) tune [132] based on the CTEQ5L set. Parton shower and hadronization effects are included by matching the generated events to \textsc{Pythia}, using the MLM matching algorithm [154]. The events are processed with a \textsc{Geant4} [31] description of the CMS apparatus to include detector effects. The simulation samples for SM background processes are scaled to the integrated luminosity of the data sample (18.8 fb\(^{-1}\)), using calculations of the inclusive production cross sections at the next-to-next-to-leading order (NNLO) in the perturbative QCD expansion [141, 140, 118]. The signal processes corresponding to pair production of DM particles are simulated with up to two additional partons with \(p_T > 80\) GeV.

### 7.3 Event selection

Events are selected with at least one reconstructed interaction vertex within \(|z| < 24\) cm. If more than one vertex is found, the one with the highest sum of the associated track momenta squared is used as the interaction point for event reconstruction. Events containing calorimeter noise, or large missing transverse momentum due to beam halo and instrumental effects (such as jets near non-functioning channels in the ECAL) are removed from the analysis [82].

A particle-flow (PF) algorithm [105, 102] is used to reconstruct and identify individual particles with an optimized combination of information from the various elements of the CMS detector. The energy of photons is directly obtained from the ECAL measurement, corrected for zero-suppression effects. The energy of elec-
Electrons is determined from a combination of the electron momentum at the primary interaction vertex as measured by the tracker, the energy of the corresponding ECAL cluster, and the energy sum of all bremsstrahlung photons (or emissions) spatially compatible with originating from the electron track. The energy of muons is obtained from the curvature of the associated track. The energy of charged hadrons is determined from a combination of their momentum measured in the tracker and the matching ECAL and HCAL energy deposits, corrected for zero-suppression effects and for the response function of the calorimeters to hadronic showers. Finally, the energy of neutral hadrons is obtained from the corresponding corrected ECAL and HCAL energies. Contamination of the energy determinations from other pp collisions is mitigated by discarding the charged PF candidates incompatible with originating from the main vertex. Additional energy from neutral particles is subtracted on average when computing lepton (electron or muon) isolation and jet energy. This contribution is estimated as the per-event energy deposit per unit area, in the cone $\Delta R = \sqrt{\Delta \eta^2 + \Delta \phi^2} = 0.3$, times the considered jet size or isolation cone area.

Electrons (muons) are required to have $p_T > 15$ GeV and $|\eta| < 2.5$ (2.4). In order to reduce the background from hadrons misidentified as leptons, additional requirements based on the quality of track reconstruction and isolation are applied. Lepton isolation is defined as the scalar $p_T$ sum of all PF candidates other than the lepton itself, within a cone of size $\Delta R = 0.3$, and normalized to the lepton $p_T$. A candidate is identified as a lepton if the isolation variable is found to be smaller than 15%. For electrons [176], a characteristic of the shower shape of the energy deposit in the ECAL (the shower width in the $\eta$ direction) is used to further reduce the contamination from hadrons. PF candidates with $p_T > 10$ GeV that are not consistent with muons and satisfy the same isolation requirements as those used for electrons are also identified to increase the lepton selection efficiency as well as to identify single-prong tau decays.

Jets are formed by clustering the PF candidates, using the anti-$k_T$ algorithm with distance parameter 0.5. Jet momentum is determined as the vectorial sum of all particle momenta in the jet, and is found from simulation to be within 5% to 10% of the generated hadron level jet momentum over the whole $p_T$ spectrum and detector acceptance. Jet energy corrections are derived from simulation, and are confirmed with in situ measurements of the energy balance in dijet and photon+jet events. Additional selection criteria are applied to each event to remove spurious
jet-like features originating from isolated noise patterns in certain HCAL regions. We select events containing at least two jets with $p_T > 80$ GeV and $|\eta| < 2.4$, for which the corresponding L1 and HLT requirements are maximally efficient. The combined secondary vertex (CSV) b-tagging algorithm [212, 89] is used to identify jets originating from b quarks. The loose and tight working points of the CSV algorithm, with 85% (10%) and 50% (0.1%) identification efficiency (misidentification probability) respectively, are used to assign the selected events to categories based on the number of b-tagged jets, as described below.

In order to compute the razor variables inclusively, the event is forced into a two-jet topology, by forming two megajets [98] out of all the reconstructed jets with $p_T > 40$ GeV and $|\eta| < 2.4$. All possible assignments of jets to the megajets are considered, with the requirement that a megajet consist of at least one jet. The sum of the four-momenta of the jets assigned to a megajet defines the megajet four-momentum. When more than two jets are reconstructed, more than one megajet assignment is possible. We select the assignment that minimizes the sum of the invariant masses of the two megajets. In order to reduce the contamination from multijet production, events are rejected if the angle between the two selected megajets in the transverse plane $|\Delta \phi(j_1, j_2)|$ is larger than 2.5 radians. The momenta of the two megajets are used to compute the razor variables, according to Eq. (7.1, 7.2). Events are required to have $M_R > 200$ GeV and $R^2 > 0.5$.

7.4 Analysis Strategy

To enhance the DM signal and suppress background contributions from the $W$+jets and $t\bar{t}$ processes, we veto events with selected electrons, muons, or isolated charged PF candidates. We define three different search regions based on the number of b-tagged jets. The zero b-tag search region contains events where no jets were identified with the CSV loose b-tagging criterion; the one b-tag search region contains events where exactly one jet passed the CSV tight criterion; and the two b-tag search region contains events where two or more jets passed the CSV tight criterion. Events in the zero b-tag search region are further classified into four categories based on the value of $M_R$, to enhance signal to background discrimination for a broad class of DM models: (i) very low $M_R$ (VL), defined by $200 < M_R \leq 300$ GeV; (ii) low $M_R$ (L), with $300 < M_R \leq 400$ GeV; (iii) high $M_R$ (H), with $400 < M_R \leq 600$ GeV; and (iv) very high $M_R$ (VH), including events with $M_R > 600$ GeV. Because of the limited size of the data sample, no further categorization based on $M_R$ is made for the one and two b-tag search regions. Within each category, the
Table 7.2: Observed yield in each in events with 0µ and no b-tagged jets for each MR category. The number overlapping events between the razor and monojet searches is also presented.

<table>
<thead>
<tr>
<th>MR category</th>
<th>Observed</th>
<th>Monojet &amp; Razor</th>
</tr>
</thead>
<tbody>
<tr>
<td>VL</td>
<td>11623</td>
<td>0</td>
</tr>
<tr>
<td>L</td>
<td>3785</td>
<td>3</td>
</tr>
<tr>
<td>H</td>
<td>1559</td>
<td>57</td>
</tr>
<tr>
<td>VH</td>
<td>261</td>
<td>92</td>
</tr>
</tbody>
</table>

search is performed in bins of the $R^2$ variable, with the binning chosen such that the expected background yield in each bin is larger than one event, as estimated from Monte Carlo simulation. In the H and VH categories, 3% and 35% respectively of the selected events were also selected in the monojet search [96], which used data from the same running period. The overlap in the L and VL categories is negligible, while the overlapping events in the H and VH categories were shown not to have an impact on the final sensitivity. Consequently, the results from this analysis and from the monojet analysis are largely statistically independent. Table 7.2 shows the events selected by this analysis and the overlapping events with the monojet search.

The main backgrounds in the zero b-tag search region are from the $W(\ell\nu)$+jets and $Z(\nu\bar{\nu})$+jets processes, while the dominant background in the one and two b-tag search regions is the $t\bar{t}$ process. To estimate the contribution of these backgrounds in the search regions, we use a data-driven method that extrapolates from appropriately selected control regions to the search region, assisted by Monte Carlo simulation. A detailed description of the background estimation method is discussed in Section 8.5.

To estimate the $W(\ell\nu)$+jets and $Z(\nu\bar{\nu})$+jets background in the zero b-tag search region, we define the 1µ control region by selecting events using identical requirements to those used in the search region, with the exception of additionally requiring one selected muon. Events in this control region are extrapolated to the search region in order to estimate the background. In addition, we define the 2µ control region, enhanced in the $Z$+jets process, by requiring two selected muons with invariant mass between 80 GeV and 100 GeV. The 2µ control region is used to perform a cross-check prediction for the 1µ control region, and the systematic uncertainties in background prediction are estimated based on this comparison.

To estimate the $t\bar{t}$ background in the one and two b-tag search regions, we define the 1µb and 2µb control regions, by requiring at least one jet satisfying the CSV tight b-
Table 7.3: Analysis regions for events with zero identified b-tagged jets. The definition of these regions is based on the muon multiplicity, the output of the CSV b-tagging algorithm, and the value of $M_R$. For all the regions, $R^2 > 0.5$ is required.

<table>
<thead>
<tr>
<th>analysis region</th>
<th>purpose</th>
<th>b-tagging selection</th>
<th>$M_R$ category</th>
</tr>
</thead>
<tbody>
<tr>
<td>0$\mu$</td>
<td>signal search region</td>
<td>$200 &lt; M_R \leq 300$ GeV (VL)</td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td>$300 &lt; M_R \leq 400$ GeV (L)</td>
<td></td>
</tr>
<tr>
<td>1$\mu$</td>
<td>$W(\ell \nu)$ control region</td>
<td>no CSV loose jet</td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td>$400 &lt; M_R \leq 600$ GeV (H)</td>
<td></td>
</tr>
<tr>
<td>2$\mu$</td>
<td>$Z(\ell\ell)$ control region</td>
<td>$M_R &gt; 600$ GeV (VH)</td>
<td></td>
</tr>
</tbody>
</table>

Table 7.4: Analysis regions for events with identified b-tagged jets. The definition of these regions is based on the muon multiplicity, the output of the CSV b-tagging algorithm, and the value of $M_R$. For all the regions, $R^2 > 0.5$ is required.

<table>
<thead>
<tr>
<th>analysis region</th>
<th>purpose</th>
<th>b-tagging selection</th>
<th>$M_R$ category</th>
</tr>
</thead>
<tbody>
<tr>
<td>0$\mu$bb</td>
<td>signal search region</td>
<td>$\geq 2$ CSV tight jets</td>
<td></td>
</tr>
<tr>
<td>0$\mu$b</td>
<td></td>
<td>$= 1$ CSV tight jet</td>
<td></td>
</tr>
<tr>
<td>1$\mu$b</td>
<td>$t\bar{t}$ control region</td>
<td>$\geq 1$ CSV tight jets</td>
<td></td>
</tr>
<tr>
<td>2$\mu$b</td>
<td>$t\bar{t}$ control region</td>
<td>$M_R &gt; 200$ GeV</td>
<td></td>
</tr>
<tr>
<td>$Z(\mu\mu)b$</td>
<td>$Z(\ell\ell)$ control region</td>
<td>$\geq 1$ CSV loose jets</td>
<td></td>
</tr>
</tbody>
</table>

tagging criterion along with one and two selected muons respectively. Both of these control regions are dominated by the $t\bar{t}$ process. The $t\bar{t}$ background prediction is estimated by extrapolating from the 2$\mu$b control region, while the 1$\mu$b control region is used as a cross-check to estimate systematic uncertainties. Finally, we define the $Z(\mu\mu)b$ control region by requiring two muons with invariant mass between 80 GeV and 100 GeV. This is used to estimate the $Z(\nu\bar{\nu})$+jets background in the one and two b-tag search regions.

The definitions of the search and control regions, and their use in this analysis are summarized in Tables 7.3 and 7.4.

7.5 Background estimation

The largest background contribution to the zero b-tag search region is from events in which a W or Z boson is produced, in association with jets, decaying to final states with one or more neutrinos. These background processes are referred to as $W(\ell\nu)$+jets and $Z(\nu\bar{\nu})$+jets events. Additional backgrounds arise from events involving the production of top quark pairs, and from events in which a Z boson decays to a pair of charged leptons. These processes are referred to as $t\bar{t}$ and $Z(\ell\ell)$+jets, respectively. Using simulated samples, the contribution from other SM
processes, such as diboson and single top production, is found to be negligible.

The main background in the one and two b-tag search regions comes from \( t \bar{t} \) events. The use of the tight working point of the CSV algorithm reduces the \( Z(\nu \bar{\nu}) + \text{jets} \) and \( W(\ell \nu) + \text{jets} \) contribution as shown in Table 7.8. Multijet production, which is the most abundant source of events with jets and unbalanced \( p_T \), contributes to the search region primarily due to instrumental mismeasurement of the energy of jets. As a result the \( E_T^{miss} \) direction tends to be highly aligned in the azimuthal coordinate with the razor megajets. The requirement on the razor variables and \( |\Delta \phi(j_1,j_2)| \) reduces the multijet background to a negligible level, which is confirmed by checking data control regions with looser cuts on the razor variables. Figure 7.2 shows the 2-dimensional \( R^2-|\Delta \phi(j_1,j_2)| \) distribution, where it is observed that for \( R^2 > 0.5 \) and \( |\Delta \phi(j_1,j_2)| < 2.5 \), the multijet contribution is indeed negligible. Other relevant distributions for the multijet background are shown in Figure 7.3.

**Figure 7.2**: \( R^2-\Delta \phi(J_1,J_2) \) distribution for the QCD background in the 0\( \mu \) box.

**Background estimation for the zero b-tag search region**

To predict the background from \( W(\ell \nu) + \text{jets} \) and \( Z(\nu \bar{\nu}) + \text{jets} \) in the zero b-tag search region, we use a data-driven method that extrapolates the observed data yields in the 1\( \mu \) control region to the search region. Similarly, the observed yield in the 2\( \mu \) control region allows the estimation of the contribution from \( Z(\ell \ell) + \text{jets} \) background process. Each \( M_{R} \) category is binned in \( R^2 \).

The background expected from \( W \) and \( Z \) boson production, in each \( R^2 \) bin and in each \( M_{R} \) category of the 0\( \mu \) sample, is computed as

\[
\hat{n}_{i}^{0\mu} = \left( n_{i}^{1\mu} - n_{i}^{0\mu} \right) \left( \frac{N_{i}^{W(\ell \nu) + \text{jets},1\mu}}{N_{i}^{W(\ell \nu) + \text{jets},0\mu}} + \frac{N_{i}^{Z(\nu \bar{\nu}) + \text{jets},0\mu}}{N_{i}^{W(\ell \nu) + \text{jets},1\mu}} \right) + \left( n_{i}^{2\mu} - n_{i}^{1\mu} \right) \left( \frac{N_{i}^{Z(\ell \ell) + \text{jets},2\mu}}{N_{i}^{Z(\ell \ell) + \text{jets},0\mu}} \right),
\]

(7.3)
Figure 7.3: (a) $R^2$ and (b) $M_R$-$R^2$ razor distributions for the QCD background in the $0\mu$ box.

where $n_{i}^{k\mu}$ labels the data yield in bin $i$ for the sample with $k$ muons, and $N_{i}^{X,k\mu}$ indicates the corresponding yield for process $X$, derived from simulations. This background estimation method relies on the assumption that the kinematic properties of events in which $W$ and $Z$ bosons are produced are similar.

To estimate the accuracy of the background estimation method, we perform a cross-check by predicting the background in the $1\mu$ control region using the observed data yield in the $2\mu$ control region. The Monte Carlo simulation is used to perform this extrapolation analogous to the calculation in Equation 7.3. The small contribution from the $t\bar{t}$ background process is also estimated using the simulated samples. In Tables 7.5 and 7.6, the observed yields in the $1\mu$ and $2\mu$ control regions respectively are compared to the estimate derived from data. In Tables 7.5-7.10, the contribution of each process as predicted directly by simulated samples are also given.

Table 7.5: Comparison of the observed yield in the $1\mu$ control region in each $M_R$ category and the corresponding data-driven background estimate obtained by extrapolating from the $2\mu$ control region. The uncertainty in the estimates takes into account both the statistical and systematic components. The contribution of each individual background process is also shown, as estimated from simulated samples, as well as the total MC predicted yield.

<table>
<thead>
<tr>
<th>$M_R$ category</th>
<th>$Z(\nu\bar{\nu})$+jets</th>
<th>$W(\ell\nu)$+jets</th>
<th>$Z(\ell\ell)$+jets</th>
<th>$t\bar{t}$</th>
<th>MC predicted</th>
<th>Estimated</th>
<th>Observed</th>
</tr>
</thead>
<tbody>
<tr>
<td>VL</td>
<td>0.7 ± 0.3</td>
<td>4558 ± 32</td>
<td>133 ± 3</td>
<td>799 ± 9</td>
<td>5491 ± 33</td>
<td>5288 ± 511</td>
<td>5926</td>
</tr>
<tr>
<td>L</td>
<td>0.5 ± 0.3</td>
<td>1805 ± 17</td>
<td>44 ± 2</td>
<td>213 ± 4</td>
<td>2063 ± 18</td>
<td>1840 ± 233</td>
<td>2110</td>
</tr>
<tr>
<td>H</td>
<td>0.1 ± 0.1</td>
<td>915 ± 11</td>
<td>16 ± 1</td>
<td>66 ± 2</td>
<td>997 ± 11</td>
<td>629 ± 240</td>
<td>923</td>
</tr>
<tr>
<td>VH</td>
<td>&lt;0.1</td>
<td>183 ± 5</td>
<td>2.6 ± 0.2</td>
<td>8.5 ± 0.8</td>
<td>194 ± 5</td>
<td>166 ± 93</td>
<td>143</td>
</tr>
</tbody>
</table>

Figure 7.4 shows the comparison of the $R^2$ distributions between the observed yield and the data-driven background estimate in the $1\mu$ control region. The observed
Table 7.6: Comparison of the observed yield for the 2µ control region in each $M_R$ category and the corresponding prediction from background simulation. The quoted uncertainty in the prediction reflects only the size of the simulated sample. The contribution of each individual background process is also shown, as estimated from simulated samples.

<table>
<thead>
<tr>
<th>$M_R$ category</th>
<th>$Z(\nu\bar{\nu})$+jets</th>
<th>$W(\ell\bar{\nu})$+jets</th>
<th>$Z(\ell\bar{\ell})$+jets</th>
<th>$t\bar{t}$</th>
<th>MC predicted</th>
<th>Observed</th>
</tr>
</thead>
<tbody>
<tr>
<td>VL</td>
<td>&lt;0.1</td>
<td>&lt;0.1</td>
<td>214 ± 4</td>
<td>1.9 ± 0.3</td>
<td>215 ± 4</td>
<td>207</td>
</tr>
<tr>
<td>L</td>
<td>&lt;0.1</td>
<td>0.4 ± 0.3</td>
<td>88 ± 2</td>
<td>0.5 ± 0.2</td>
<td>89 ± 2</td>
<td>78</td>
</tr>
<tr>
<td>H</td>
<td>&lt;0.1</td>
<td>0.1 ± 0.1</td>
<td>48 ± 1</td>
<td>0.1 ± 0.1</td>
<td>48 ± 1</td>
<td>30</td>
</tr>
<tr>
<td>VH</td>
<td>&lt;0.1</td>
<td>&lt;0.1</td>
<td>10 ± 1</td>
<td>0.1 ± 0.1</td>
<td>10 ± 1</td>
<td>7</td>
</tr>
</tbody>
</table>

Table 7.7: Observed yield and predicted background from simulated samples in the 2µ control region. The quoted uncertainty in the prediction only reflects the size of the simulated sample. The contribution of each individual background process is also shown, as estimated from simulated samples.

<table>
<thead>
<tr>
<th>Sample</th>
<th>$Z(\nu\bar{\nu})$+jets</th>
<th>$W(\ell\bar{\nu})$+jets</th>
<th>$Z(\ell\bar{\ell})$+jets</th>
<th>$t\bar{t}$</th>
<th>MC predicted</th>
<th>Observed</th>
</tr>
</thead>
<tbody>
<tr>
<td>2µb</td>
<td>&lt;0.1</td>
<td>0.1 ± 0.1</td>
<td>2.2 ± 0.3</td>
<td>58 ± 2</td>
<td>60 ± 2</td>
<td>60</td>
</tr>
</tbody>
</table>

bin-by-bin difference is propagated as a systematic uncertainty in the data-driven background method, and accounts for the statistical uncertainty in the event yield in the 2µ control region data as well as potential differences in the modeling of the recoil spectra between $W$+jets and $Z$+jets processes. Some bins exhibit relatively large uncertainties primarily due to statistical fluctuations in the 2µ control region from which the background is prediction estimated. Though the uncertainties are rather large in fractional terms, sensitivity to DM signal models is still obtained, because of the enhanced signal to background ratio for the bins at large values of $M_R$ and $R^2$.

The $t\bar{t}$ background is estimated using an analogous data-driven method, where we derive corrections to the Monte Carlo simulation prediction scaled to the $t\bar{t}$ production cross-section computed to NNLO accuracy [141, 140, 118] using data in the 2µ control region for each bin in $R^2$. The correction is then applied to the simulation prediction for the $t\bar{t}$ background contribution to the zero b-tag search region. This correction factor reflects potential mismodeling of the recoil spectrum predicted by the Monte Carlo simulation. The contribution of each background process to the 2µb sample, predicted from simulated samples, is given in Table 7.7. The fraction of $t\bar{t}$ events in the 2µb control sample is $\approx 95\%$. Figure 7.5 shows the comparison of the observed yield and the prediction from simulation, as a
Figure 7.4: Comparison of observed yields in the 1\(\mu\) control region and the data-driven background estimate derived from on the 2\(\mu\) control region data in the four \(M_R\) categories: VL (top left), L (top right), H (bottom left), and VH (bottom right). The bottom panel in each plot shows the ratio between the two distributions. The observed bin-by-bin deviation from unity is interpreted as an estimate of the systematic uncertainty associated to the background estimation methodology for the 0\(\mu\) search region. The dark and light bands represent the statistical and the total uncertainties in the estimates, respectively. The horizontal bars indicate the variable bin widths.
Figure 7.5: Comparison of the observed yield and the prediction from simulation as a function of $R^2$ in the $2\mu b$ control region. The uncertainties in the data and the simulated sample are represented by the vertical bars and the shaded bands, respectively. The horizontal bars indicate the variable bin widths.

Table 7.8: Comparison of the observed yields for the zero b-tag search region in each $M_R$ category and the corresponding background estimates. The uncertainty in the background estimate takes into account both the statistical and systematic components. The contribution of each individual background process is also shown, as estimated from simulated samples, as well as the total MC predicted yield.

<table>
<thead>
<tr>
<th>$M_R$ category</th>
<th>$Z(\nu\bar{\nu})$+jets</th>
<th>$W(\ell\nu)$+jets</th>
<th>$Z(\ell\ell)$+jets</th>
<th>$t\bar{t}$</th>
<th>MC predicted</th>
<th>Estimated</th>
<th>Observed</th>
</tr>
</thead>
<tbody>
<tr>
<td>VL</td>
<td>6231 ± 37</td>
<td>4820 ± 33</td>
<td>49 ± 2</td>
<td>555 ± 7</td>
<td>11655 ± 50</td>
<td>12770 ± 900</td>
<td>11623</td>
</tr>
<tr>
<td>L</td>
<td>2416 ± 19</td>
<td>1513 ± 16</td>
<td>11 ± 1</td>
<td>104 ± 3</td>
<td>4044 ± 25</td>
<td>4170 ± 270</td>
<td>3785</td>
</tr>
<tr>
<td>H</td>
<td>1127 ± 7</td>
<td>625 ± 9</td>
<td>2.9 ± 0.3</td>
<td>24 ± 1</td>
<td>1779 ± 12</td>
<td>1650 ± 690</td>
<td>1559</td>
</tr>
<tr>
<td>VH</td>
<td>229 ± 2</td>
<td>103 ± 3</td>
<td>0.2 ± 0.1</td>
<td>3.1 ± 0.5</td>
<td>335 ± 3</td>
<td>240 ± 160</td>
<td>261</td>
</tr>
</tbody>
</table>

function of $R^2$. We observe no significant deviations between the observed data and the simulation prediction. The uncertainty derived from the data-to-simulation correction factor is propagated to the systematic uncertainty of the $t\bar{t}$ prediction in the zero b-tag search region.

The result of the background estimation in the zero b-tag search region is given in Table 7.8, where it is compared to the observed yields in data. The uncertainty in the background estimates takes into account both the statistical and systematic components. The comparison of the data-driven background estimates and the observations for each $M_R$ category is shown in Fig. 7.6, as a function of $R^2$. The expected event distribution is shown for two signal benchmark models, corresponding to the pair production of DM particles of mass 1 GeV in the effective field theory (EFT) approach with vector coupling to u or d quarks. Details on the signal benchmark models are given in Section 7.7.
Figure 7.6: Comparison of the observed yield in the zero b-tag control region and the background estimates in the four $M_R$ categories: VL (top left), L (top right), H (bottom left), and VH (bottom right). The contribution of individual background processes is shown by the filled histograms. The bottom panels show the ratio between the observed yields and the total background estimate. For reference, the distributions from two benchmark signal models are also shown, corresponding to the pair production of DM particles of mass 1 GeV in the EFT approach with vector coupling to u or d quarks. The horizontal bars indicate the variable bin widths.

**Background estimation for the 0$\mu$b and 0$\mu$bb samples**

A similar data-driven technique is used to determine the expected background for the one and two b-tag search regions. The background from $t\bar{t}$ events for each $R^2$ bin in the one b-tag search region, $n(t\bar{t})_{i}^{1b}$, is computed as:

$$n(t\bar{t})_{i}^{1b} = (n(t\bar{t})_{i}^{2b} - N_{i}^{Z(\ell\bar{\ell})+jets,2b} - N_{i}^{W(\ell\nu)+jets,2b}) \frac{N(t\bar{t})_{i}^{0b}}{N(t\bar{t})_{i}^{2b}},$$

(7.4)

where $n(t\bar{t})_{i}^{2b}$ is the observed yield in the $i$th $R^2$ bin in the 2$\mu$b control region, while $N(t\bar{t})_{i}^{0b}$ and $N(t\bar{t})_{i}^{2b}$ are the $t\bar{t}$ yields in the $i$th $R^2$ bin predicted by the simulation for the one b-tag search region and the 2$\mu$b control region respectively. Similarly,
Table 7.9: Comparison of the observed yields in the $Z(\mu\mu)b$ and $1\mu b$ samples, the corresponding predictions from background simulation, and (for $1\mu b$ only) the cross-check background estimate. The contribution of each individual background process is also shown, as estimated from simulated samples.

<table>
<thead>
<tr>
<th>Sample</th>
<th>$Z(\nu\nu)+$jets</th>
<th>$W(\ell\nu)+$jets</th>
<th>$Z(\ell\ell)+$jets</th>
<th>$t\bar{t}$</th>
<th>MC predicted</th>
<th>Estimated</th>
<th>Observed</th>
</tr>
</thead>
<tbody>
<tr>
<td>$Z(\mu\mu)b$</td>
<td>&lt;0.1</td>
<td>&lt;0.1</td>
<td>134 ± 3</td>
<td>17 ± 1</td>
<td>151 ± 3</td>
<td>—</td>
<td>175</td>
</tr>
<tr>
<td>$1\mu b$</td>
<td>0.2 ± 0.1</td>
<td>279 ± 7</td>
<td>11 ± 1</td>
<td>3038 ± 17</td>
<td>3328 ± 18</td>
<td>3410 ± 540</td>
<td>2920</td>
</tr>
</tbody>
</table>

Figure 7.7: Comparison of the observed yield and the prediction from simulation in the $Z(\mu\mu)b$ control sample (left) and of the observed yield in the $1\mu b$ control sample and the background estimates from the $2\mu b$ and $Z(\mu\mu)b$ control samples (right), shown as a function of $R^2$. The bottom panel of each figure shows the ratio between the data and the estimates. The shaded bands represent the statistical uncertainty in the left plot, and the total uncertainty in the right plot. The horizontal bars indicate the variable bin widths.

the $t\bar{t}$ background in the two b-tag search region is derived from Eq. (7.4), replacing $N(t\bar{t})^0_{b_i}$ with $N(t\bar{t})^0_{bb}$, the $t\bar{t}$ background yield in the $i$th bin of the two b-tag search region predicted by the simulation. The data yield in the $2\mu b$ control region is corrected to account for the small contamination from $Z+$jets and $W+$jets, predicted with the simulated yields $N_i^{Z(\ell\ell)+jets,2\mu b}$ and $N_i^{W(\ell\nu)+jets,2\mu b}$, respectively.

The background contribution from $W(\ell\nu)+$jets and $Z(\nu\nu)+$jets events is predicted using the $Z(\mu\mu)b$ control region, and summarized in Table 7.9. The $Z+$jets purity of this control region is $\approx 89\%$. The observed yield in the $Z(\mu\mu)b$ control region is shown in the left plot of Fig. 7.7, as a function of $R^2$, along with the Monte Carlo simulation prediction. The uncertainty on the simulation prediction accounts only for the statistical uncertainty of the simulated sample. This contribution, scaled by the ratio of the predicted $V+$jets background in the search regions to that in the control region, obtained from simulation, provides an estimate for each $R^2$ bin.
Figure 7.8: Comparison of observed event yields and background estimates as a function of $R^2$, for the one (left) and two (right) b-tag search regions. The shaded bands represent the total uncertainty in the estimate. The horizontal bars indicate the variable bin widths.

Table 7.10: Comparison of the observed yield for events in the one and two b-tag search regions and the corresponding background estimates. The uncertainty in the estimates takes into account both the statistical and systematic components. The contribution of each individual background process is also shown, as estimated from simulated samples, as well as the total MC predicted yield.

<table>
<thead>
<tr>
<th>Sample</th>
<th>$Z(\nu\bar{\nu})$+jets</th>
<th>$W(\ell\nu)$+jets</th>
<th>$Z(\ell\ell)$+jets</th>
<th>$\bar{t}t$</th>
<th>MC predicted</th>
<th>Estimated</th>
<th>Observed</th>
</tr>
</thead>
<tbody>
<tr>
<td>0$\mu$bb</td>
<td>44 ± 3</td>
<td>14 ± 2</td>
<td>0.2 ± 0.1</td>
<td>204 ± 4</td>
<td>262 ± 5</td>
<td>271 ± 37</td>
<td>247</td>
</tr>
<tr>
<td>0$\mu$b</td>
<td>417 ± 8</td>
<td>216 ± 7</td>
<td>2.4 ± 0.4</td>
<td>1480 ± 12</td>
<td>2115 ± 16</td>
<td>2230 ± 280</td>
<td>2282</td>
</tr>
</tbody>
</table>

We perform a cross-check of the method on the 1$\mu$b control region by predicting the background from the 2$\mu$b control region data. The data and prediction are compared on the right of Fig. 7.7, where we observe reasonable agreement. The difference between the prediction and the observed data in this cross-check region is propagated as a systematic uncertainty of the method.

The estimated background in the one and two b-tag search regions is given in Table 7.10 and shown in Fig. 7.8, where it is compared to the observed yields in data. The uncertainty in the estimates take into account both the statistical and systematic components.

### 7.6 Systematic uncertainties

For each $R^2$ bin in each $M_R$ category, the difference between the observed and estimated yields in the crosscheck analysis (see Section 8.5) is taken as the estimate of the uncertainty associated with the method. The uncertainty is found to be typically $\approx 20$–$40\%$, depending on the considered bin in the $(M_R, R^2)$ plane. Other
sources of systematic uncertainties such as the modeling of the jet energy scale correction, and the initial-state radiation in the event are found to be negligible compared to the systematic from the cross-check. Figures 7.9 and 7.10 show the individual systematic uncertainties just mentioned and the systematic uncertainty from the cross-check.

Figure 7.9: Total (estimated using the cross-check analysis) and JES systematic uncertainties. The green band corresponds to the systematic uncertainty associated with the background prediction method, while the red band corresponds to the JES systematic only. Panels (a) and (b) show the VL and L $M_R$ categories, respectively. Panels (c) and (d) show the H and VH $M_R$ categories, respectively.

The largest systematic uncertainty arises from the cross-check analysis. This uncertainty is affected by statistical fluctuations from the limited number of selected
Figure 7.10: Total (estimated using the cross-check analysis) and ISR systematic uncertainties. The green band corresponds to the systematic uncertainty associated with the background prediction method, while the red band corresponds to the ISR systematic only. Panels (a) and (b) show the VL and L M_R categories, respectively. Panels (c) and (d) show the H and VH M_R categories, respectively.

events in the 2µ control region. This uncertainty covers the differences in the modeling of the recoil spectra between W+jets and Z+jets processes as well as the cross section uncertainties.

For the 0µ analysis, differences between the kinematic properties of W+jets and Z+jets events are additional sources of systematic uncertainty. These differences arise from the choice of the PDF set, jet energy scale corrections, b tagging efficiency corrections, and trigger efficiency. These effects largely cancel when taking the ratio
Table 7.11: Systematic uncertainties associated with the description of the DM signal. The values indicated represent the typical size. The dependence of these systematic uncertainties on the $R^2$ and $M_R$ values is taken into account in the determination of the results.

<table>
<thead>
<tr>
<th>Effect</th>
<th>Uncertainty</th>
</tr>
</thead>
<tbody>
<tr>
<td>Jet energy scale</td>
<td>3–6%</td>
</tr>
<tr>
<td>Luminosity</td>
<td>2.6%</td>
</tr>
<tr>
<td>Parton distribution functions</td>
<td>3–6%</td>
</tr>
<tr>
<td>Initial-state radiation</td>
<td>8–15%</td>
</tr>
</tbody>
</table>

of the two processes, and the resulting uncertainty is found to be smaller than one fifth of the total uncertainty. The quoted uncertainty is an upper estimate of the total systematic uncertainty.

For the $0 \mu b$ and $0 \mu bb$ samples, both the signal and control samples are dominated by $t \bar{t}$ events. The cancellation of the systematic uncertainties is even stronger in this case, since it does not involve different processes, and different PDFs. The remaining uncertainty is dominated by the contribution arising from the small size of the control sample.

Systematic uncertainties in the signal simulation originate from the choice of the PDF set, the jet energy scale correction, the modeling of the initial-state radiation in the event generator, and the uncertainty in the integrated luminosity. The luminosity uncertainty changes the signal normalization while the other uncertainties also modify the signal shape. These effects are taken into account by propagating these uncertainties into the $M_R$ category and the $R^2$ bin. Figures 7.11, 7.12, and 7.13 show the PDF, jet energy scale, and the initial-state radiation systematic uncertainties for a vector-mediated EFT signal model with DM mass of 700 GeV, respectively. These uncertainties are considered to be fully correlated across $M_R$ categories and $R^2$ bins. Typical values for the individual contributions are given in Table 7.11. The total uncertainty in the signal yield is obtained by propagating the individual effects into the $M_R$ and $R^2$ variables and comparing the bin-by-bin variations with respect to the central value of the prediction based on simulation. In the particular case of the uncertainties due to the choice of the PDF set we have followed the PDF4LHC [66, 37, 65] prescription, using the CTEQ-6.6[205] and MRST-2006-NNLO [200] PDF sets.
Figure 7.11: PDF systematic uncertainty for a vector mediated EFT signal model with DM mass = 700 GeV. The blue band corresponds to the systematic error associated with PDF uncertainty. Panels (a) and (b) show the VL and L \( M_R \) categories, respectively. Panels (c) and (d) show the H and VH \( M_R \) categories, respectively.

7.7 Results and interpretation
In Figs. 7.6 and 7.8 the estimated backgrounds are compared to the observed yield in each \( M_R \) region, for events without and with b-tagged jets, respectively. The background estimates agree with the observed yields, within the uncertainties. This result is interpreted in terms of exclusion limits for several models of DM production.
Figure 7.12: JES systematic uncertainty for a vector mediated EFT signal model with DM mass = 700 GeV. The blue band corresponds to the systematic error associated with JES uncertainty. Panels (a) and (b) show the VL and L $M_R$ categories, respectively. Panels (c) and (d) show the H and VH $M_R$ categories, respectively.

**Limits on dark matter production from the 0$\mu$ sample**

The result is interpreted in the context of a low-energy effective field theory, in which the production of DM particles is mediated by six or seven dimension operators [58, 49]. This choice allows the results to be compared with those of previous analyses [24, 95], and shows that a similar sensitivity is achieved.

Operators of dimension six and seven are generated assuming the existence of a heavy particle, mediating the interaction between the DM and SM fields. To describe DM production as a local interaction, the propagator of the heavy mediator is expanded...
Figure 7.13: ISR systematic uncertainty for a vector mediated EFT signal model with DM mass = 700 GeV. The blue band corresponds to the systematic error associated with ISR uncertainty. Panels (a) and (b) show the VL and L M\(_R\) categories, respectively. Panels (c) and (d) show the H and VH M\(_R\) categories, respectively.

The nature of the mediator determines the nature of the effective interaction. Two benchmark scenarios are considered in this study, axial-vector (AV), and vector (V) interactions [136], described by the following operators:

\[
\hat{\mathcal{O}}_{AV} = \frac{1}{\Lambda^2} (\bar{\chi} \gamma^\mu \gamma_5 \chi) (\bar{q} \gamma_\mu q) \quad \text{and} \quad \hat{\mathcal{O}}_{V} = \frac{1}{\Lambda^2} (\bar{\chi} \gamma^\mu \chi) (\bar{q} \gamma_\mu q). \quad (7.5)
\]

Here \(\gamma_\mu\) and \(\gamma_5\) are the Dirac matrices, \(\chi\) is the DM field, and \(q\) is an SM quark field. The DM particle is assumed to be a Dirac fermion where both operators will
contribute in the low-energy theory, while in the case of a Majorana DM particle the vector coupling $\hat{O}_V$ will vanish in the low-energy theory. Below the cutoff energy scale $\Lambda$, DM production is described as a contact interaction between two quarks and two DM particles. In the case of $s$-channel production through a heavy mediator, the energy scale $\Lambda$ is identified with $M/\sqrt{g_{\text{eff}}}$, where $M$ is the mediator mass and $g_{\text{eff}} = \sqrt{g_q g_X}$ is an effective coupling, determined by the coupling of the mediator to quark and DM fields, $g_q$ and $g_X$, respectively.

The results in Tables 7.15-7.18 in the Appendix are used to obtain an upper limit at 90% confidence level (CL) on the DM production cross section, $\sigma^{i}_{\text{UL}}$ (where the superscript denotes the coupling to an up or down quark). The limits are obtained using the LHC CL$_{s}$ procedure [48, 107] and a global likelihood determined by combining the likelihoods of the different search categories. Each systematic uncertainty (see Section 7.6) is incorporated in the likelihood with a dedicated nuisance parameter, whose value is not known a priori but rather must be estimated from the data.

Subsequently, the cross section ($\sigma^{i}_{\text{UL}}$) limit is translated into a lower limit $\Lambda_{\text{LL}}$ on the cutoff scale, through the relation:

$$\Lambda_{\text{LL}} = \Lambda_{\text{GEN}} \left( \frac{\sigma_{\text{GEN}}}{\sigma_{\text{UL}}} \right)^{\frac{1}{2}}.$$  \hspace{1cm} (7.6)

Here $\Lambda_{\text{GEN}}$ and $\sigma_{\text{GEN}}$ are the cutoff energy scale and cross section of the simulated sample, respectively. The derived values of $\Lambda_{\text{LL}}$ as a function of the DM mass, shown in Fig. 7.14, are comparable to those derived for the CMS monojet search [96]. The exclusion limits on $\Lambda$ weaken at large DM masses since the cross section for DM production is reduced. The analysis has been repeated removing the events also selected by the monojet search. The reduction in background yields due to this additional requirement compensates for the reduction in signal efficiency, resulting in a negligible difference in the exclusion limit on $\Lambda$.

The EFT framework provides a benchmark scenario to compare the sensitivity of this analysis with that of previous searches for similar signatures. However, the validity of an EFT approach is limited at the LHC because a fraction of events under study are generated at a $\sqrt{s}$ comparable to the cutoff scale $\Lambda$ [146, 49, 138, 68]. For theories to be perturbative, $g_{\text{eff}}$ is typically required to be smaller than $4\pi$, and this condition is unlikely to be satisfied for the entire region of phase space probed by the collider searches. In addition, the range of values for the couplings being probed within the EFT may be unrealistically large. Following the study presented
in Refs. [69, 70, 71], we quantify this effect through two EFT validity measures. The first is a minimal kinematic constraint on $\Lambda$ obtained by requiring $Q_{tr} < g_{eff}\Lambda$ and $Q_{tr} > 2M_X$, where $Q_{tr}$ is the momentum transferred from the mediator to the DM particle pair, which yields $\Lambda > 2M_X/g_{eff}$. The second is more stringent and uses the quantity:

$$R_\Lambda = \frac{\int dR^2 \int dM_R \frac{d^2\sigma}{dR^2dM_R} \biggr|_{Q_{tr}<g_{eff}\Lambda}}{\int dR^2 \int dM_R \frac{d^2\sigma}{dR^2dM_R}}.$$  \hspace{1cm} (7.7)

Values of $R_\Lambda$ close to unity indicate a regime in which the assumptions of the EFT approximation hold, while a deviation from unity quantifies the fraction of events for which the EFT approximation is still valid. We consider the case of $s$-channel production, and we compute $R_\Lambda$ as a function of the effective coupling $g_{eff}$ in the range $0 < g_{eff} \leq 4\pi$. The contours corresponding to $R_\Lambda = 80\%$ for different values of $g_{eff}$ are shown in Fig. 7.14. For values of $g_{eff} \gtrsim 2$, the limit set by the analysis lies above the $R_\Lambda = 80\%$ contour.

The exclusion limits on $\Lambda$ for the axial-vector and vector operators are transformed into upper limits on the spin-dependent ($\sigma_{N_X}^{SD}$) [43, 204, 134, 133, 42, 47, 46] and spin-independent ($\sigma_{N_X}^{SI}$) [133, 134, 120, 232, 119, 135, 45, 44] DM-nucleon...
scattering cross section, respectively; using the following expressions [136]:

\[
\sigma_{N_X}^{SD} = 0.33 \frac{\mu^2}{\pi \Lambda_{LL}^4},
\]

(7.8)

\[
\sigma_{N_X}^{SI} = 9 \frac{\mu^2}{\pi \Lambda_{LL}^4},
\]

(7.9)

where

\[
\mu = \frac{M_X M_p}{M_X + M_p},
\]

(7.10)

with \(M_p\) and \(M_X\) indicating the proton and DM masses, respectively. The numerical values of the derived limits are given in Tables 7.12 and 7.13. The bound on \(\sigma_{N_X}\) as a function of \(M_X\) is shown in Fig. 7.15 for spin-dependent and spin-independent DM-nucleon scattering. A summary of the observed limits for the axial-vector and vector operators can be found in Tables 7.12 and 7.13 respectively. It is observed that the spin-independent bounds obtained by direct detection experiments are more stringent than those obtained by the present result for masses above \(\approx 5\) GeV. Such an effect is expected since the spin-independent DM-nucleus cross section is enhanced by the coherent scattering of DM off nucleons in the case of spin-independent operators. We note that the present result is more sensitive for small DM mass because the recoil energy in direct detection experiments is lower in this region and therefore more difficult to detect. In the case of spin-dependent DM-nucleus scattering, the present results are more stringent than those obtained by direct detection experiments because the DM-nucleus cross section does not benefit from the coherent enhancement. A summary of the observed limits for the axial-vector and vector operators can be found in Tables 7.12 and 7.13 respectively.

In order to compare our results with those from direct detection experiments, the experimental bounds in [133, 134, 120, 232, 119, 135, 43, 204, 134, 133] are translated into bounds on \(\Lambda\). This comparison is shown in Fig. 7.16. This translation is well defined since the momentum transfer in most direct detection experiments is low compared to the values of \(\Lambda\) being probed, and thus the EFT approximations in question are mostly valid.

**Limits on dark matter production from the 0\(\mu\)b and 0\(\mu\)bb samples**

The results from the 0\(\mu\)b and 0\(\mu\)bb samples are interpreted in an EFT scenario, following a methodology similar to that of Section 7.7. In this case, a heavy scalar
Table 7.12: The 90% CL limits on DM production in the case of axial-vector couplings. Here, $\sigma^u_{UL}$ and $\sigma^d_{UL}$ are the observed upper limits on the production cross section for u and d quarks, respectively; $\Lambda_{LL}$ is the observed cutoff energy scale lower limit, and $\sigma_N$ is the observed DM-nucleon scattering cross section upper limit.

<table>
<thead>
<tr>
<th>$M_X$ (GeV)</th>
<th>$\sigma^u_{UL}$ (pb)</th>
<th>$\sigma^d_{UL}$ (pb)</th>
<th>$\Lambda_{LL}$ (GeV)</th>
<th>$\sigma_N$ (cm$^2$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>0.39</td>
<td>0.45</td>
<td>1029</td>
<td>$8.5 \times 10^{-42}$</td>
</tr>
<tr>
<td>10</td>
<td>0.43</td>
<td>0.45</td>
<td>1012</td>
<td>$2.9 \times 10^{-41}$</td>
</tr>
<tr>
<td>100</td>
<td>0.30</td>
<td>0.37</td>
<td>1017</td>
<td>$3.3 \times 10^{-41}$</td>
</tr>
<tr>
<td>400</td>
<td>0.25</td>
<td>0.26</td>
<td>752</td>
<td>$1.1 \times 10^{-40}$</td>
</tr>
<tr>
<td>700</td>
<td>0.21</td>
<td>0.26</td>
<td>524</td>
<td>$4.7 \times 10^{-40}$</td>
</tr>
<tr>
<td>1000</td>
<td>0.17</td>
<td>0.22</td>
<td>360</td>
<td>$2.1 \times 10^{-39}$</td>
</tr>
</tbody>
</table>

Table 7.13: The 90% CL limits on DM production in the case of vector couplings. Here, $\sigma^u_{UL}$ and $\sigma^d_{UL}$ are the observed upper limits on the production cross section for u and d quarks, respectively; $\Lambda_{LL}$ is the observed cutoff energy scale lower limit; and $\sigma_N$ is the observed DM-nucleon scattering cross section upper limit.

<table>
<thead>
<tr>
<th>$M_X$ (GeV)</th>
<th>$\sigma^u_{UL}$ (pb)</th>
<th>$\sigma^d_{UL}$ (pb)</th>
<th>$\Lambda_{LL}$ (GeV)</th>
<th>$\sigma_N$ (cm$^2$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>0.41</td>
<td>0.38</td>
<td>1038</td>
<td>$2.3 \times 10^{-40}$</td>
</tr>
<tr>
<td>10</td>
<td>0.36</td>
<td>0.45</td>
<td>1043</td>
<td>$6.9 \times 10^{-40}$</td>
</tr>
<tr>
<td>100</td>
<td>0.33</td>
<td>0.44</td>
<td>1036</td>
<td>$8.3 \times 10^{-40}$</td>
</tr>
<tr>
<td>400</td>
<td>0.23</td>
<td>0.35</td>
<td>893</td>
<td>$1.5 \times 10^{-39}$</td>
</tr>
<tr>
<td>700</td>
<td>0.22</td>
<td>0.27</td>
<td>674</td>
<td>$4.7 \times 10^{-39}$</td>
</tr>
<tr>
<td>1000</td>
<td>0.22</td>
<td>0.27</td>
<td>477</td>
<td>$1.8 \times 10^{-38}$</td>
</tr>
</tbody>
</table>

Figure 7.15: Upper limit at 90% CL on the DM-nucleon scattering cross section $\sigma_N$ as a function of the DM mass $M_X$ in the case of spin-dependent axial-vector (left) and spin-independent vector (right) currents. A selection of representative direct detection experimental bounds are also shown.
mediator is considered [198], generating an operator:

\[ \hat{O}_S = \frac{M_q}{\Lambda^3} \bar{\chi} \chi \bar{q} q. \]  

(7.11)

The dependence on the mass, induced by the scalar nature of the mediator, implies a stronger coupling to third-generation quarks, enhancing the sensitivity of the \( 0\mu b\) and \( 0\mu bb\) samples to this scenario. Unlike the case of \( V \) and \( AV \) operators, the production cross section for this process is proportional to \( 1/\Lambda^6 \). The value of \( \Lambda_{LL} \) is then derived as

\[ \Lambda_{LL} = \Lambda_{\text{GEN}} \left( \frac{\sigma_{\text{GEN}}}{\sigma_{\text{UL}}} \right)^{1/6}. \]  

(7.12)

Given the results of Table 7.10 we proceed to set limits at 90% CL on the cutoff scale \( \Lambda \) using the LHC \( \text{CL}_{s} \) procedure. To quantify the validity of the EFT we follow the discussion in Section 7.7, considering an interaction mediated by an \( s \)-channel produced particle. The operator of Eq. (7.11) is suppressed by an additional factor \( m_b/\Lambda \) with respect to the operators in Eq. (7.5). As a result, for a given value of the coupling \( g_{\text{eff}} \), smaller values of \( \Lambda \) are probed in this case. The observed limit stays below the contours derived for \( R_\Lambda = 80\% \), even when the coupling is fixed to the largest value considered, \( g_{\text{eff}} = 4\pi \), as shown in the left plot of Fig. 7.17. For the same choice of coupling, the derived limit on \( \Lambda \) would correspond to \( R_\Lambda \approx 25\% \), as shown in the right plot of Fig. 7.17. Only for \( g_{\text{eff}} > 4\pi \) does the observed limit correspond to values of \( R_\Lambda > 80\% \). This requirement implies a UV completion of the EFT beyond the perturbative regime. For this reason, this result is not interpreted in terms of an exclusion limit on \( \sigma_{N\chi} \).
Table 7.14: The 90% CL limits on DM production in the case of scalar couplings. Here, $\sigma_{UL}^{obs}$ is the observed upper limit on the production cross section, $\Lambda_{LL}^{obs}$ and $\Lambda_{LL}^{exp}$ are the observed and expected cutoff energy scale lower limit, respectively.

<table>
<thead>
<tr>
<th>$M_\chi$ (GeV)</th>
<th>$\sigma_{UL}^{obs}$ (pb)</th>
<th>$\Lambda_{LL}^{obs}$ (GeV)</th>
<th>$\Lambda_{LL}^{exp}$ (GeV)</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.1</td>
<td>5.4</td>
<td>43.0</td>
<td>48.2</td>
</tr>
<tr>
<td>1</td>
<td>3.8</td>
<td>45.3</td>
<td>49.9</td>
</tr>
<tr>
<td>10</td>
<td>6.3</td>
<td>43.2</td>
<td>48.4</td>
</tr>
<tr>
<td>100</td>
<td>0.8</td>
<td>53.7</td>
<td>55.1</td>
</tr>
<tr>
<td>200</td>
<td>0.7</td>
<td>47.2</td>
<td>48.3</td>
</tr>
<tr>
<td>300</td>
<td>2.8</td>
<td>32.5</td>
<td>35.8</td>
</tr>
<tr>
<td>400</td>
<td>2.8</td>
<td>28.3</td>
<td>30.8</td>
</tr>
<tr>
<td>1000</td>
<td>1.7</td>
<td>13.2</td>
<td>13.8</td>
</tr>
</tbody>
</table>

Figure 7.17: Lower limit at 90% CL on the cutoff scale $\Lambda$ for the scalar operator $\hat{O}_S$ as a function of the DM mass $M_\chi$. The validity of the EFT is quantified by $R_\Lambda = 80\%$ (left) and $R_\Lambda = 25\%$ (right) contours, corresponding to different values of the effective coupling $g_{eff}$. For completeness, regions forbidden by the EFT validity condition $\Lambda > 2M_\chi/g_{eff}$ are shown for two choices of the effective coupling: $g_{eff} = 1$ (light gray) and $g_{eff} = 4\pi$ (dark gray).
7.8 Summary
A search for dark matter has been performed studying proton-proton collisions collected with the CMS detector at the LHC at a center-of-mass energy of 8 TeV. The data correspond to an integrated luminosity of 18.8 fb$^{-1}$, collected with a dedicated high-rate trigger in 2012, made possible by the creation of parked data, and processed during the LHC shutdown in 2013.

Events with at least two jets are analyzed by studying the distribution in the $(M_{R}, R^2)$ plane, in an event topology complementary to that of monojet searches. Events with one or two muons are used in conjunction with simulated samples, to predict the expected background from standard model processes, mainly Z+jets and W+jets. The analysis is performed on events both with and without b-tagged jets, originating from the hadronization of a bottom quark, where in the latter case the dominant background comes from $t\bar{t}$.

No significant excess is observed. The results are presented as exclusion limits on dark matter production at 90% confidence level for models based on effective operators and for different assumptions on the interaction between the dark matter particles and the colliding partons. Dark matter production at the LHC is excluded for a mediator mass scale $\Lambda$ below 1 TeV in the case of a vector or axial vector operator. While the sensitivity achieved is similar to those of previously published searches, this analysis complements those results since the use of razor variables provides more inclusive selection criteria and since the exploitation of parked data allows events with small values of $M_{R}$ to be included.

7.9 Appendix: background estimation and observed yield
In this section, we provide the background estimate and the observed yield for each bin of the $(M_{R}, R^2)$ plane.

Tables 7.15-7.18 show the expected and observed yields in each $R^2$ bin of each $M_{R}$ category for the $0\mu$ sample. Tables 7.19 and 7.20 show the corresponding values for the $0\mu b$ and the $0\mu bb$ samples, respectively.
### Table 7.15: Background estimates and observed yield for each $R^2$ bin in the VL $M_R$ category.

<table>
<thead>
<tr>
<th>$R^2$ range</th>
<th>0.5–0.55</th>
<th>0.55–0.6</th>
<th>0.6–0.65</th>
<th>0.65–0.7</th>
</tr>
</thead>
<tbody>
<tr>
<td>Observed</td>
<td>2049</td>
<td>1607</td>
<td>1352</td>
<td>1147</td>
</tr>
<tr>
<td>Estimated</td>
<td>2350 ± 720</td>
<td>1810 ± 450</td>
<td>1530 ± 180</td>
<td>1240 ± 110</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>$R^2$ range</th>
<th>0.7–0.75</th>
<th>0.75–0.8</th>
<th>0.8–0.85</th>
<th>0.85–0.9</th>
</tr>
</thead>
<tbody>
<tr>
<td>Observed</td>
<td>1026</td>
<td>896</td>
<td>880</td>
<td>744</td>
</tr>
<tr>
<td>Estimated</td>
<td>1090 ± 140</td>
<td>1081 ± 76</td>
<td>876 ± 97</td>
<td>909 ± 63</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>$R^2$ range</th>
<th>0.9–0.95</th>
<th>0.95–1.0</th>
<th>1.0–2.5</th>
</tr>
</thead>
<tbody>
<tr>
<td>Observed</td>
<td>688</td>
<td>499</td>
<td>735</td>
</tr>
<tr>
<td>Estimated</td>
<td>674 ± 67</td>
<td>521 ± 43</td>
<td>694 ± 62</td>
</tr>
</tbody>
</table>

### Table 7.16: Background estimates and observed yield for each $R^2$ bin in the L $M_R$ category.

<table>
<thead>
<tr>
<th>$R^2$ range</th>
<th>0.5–0.575</th>
<th>0.575–0.65</th>
<th>0.65–0.75</th>
</tr>
</thead>
<tbody>
<tr>
<td>Observed</td>
<td>1088</td>
<td>765</td>
<td>682</td>
</tr>
<tr>
<td>Estimated</td>
<td>1220 ± 120</td>
<td>828 ± 65</td>
<td>810 ± 210</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>$R^2$ range</th>
<th>0.75–0.85</th>
<th>0.85–0.95</th>
<th>0.95–2.5</th>
</tr>
</thead>
<tbody>
<tr>
<td>Observed</td>
<td>565</td>
<td>395</td>
<td>290</td>
</tr>
<tr>
<td>Estimated</td>
<td>551 ± 59</td>
<td>454 ± 32</td>
<td>304 ± 43</td>
</tr>
</tbody>
</table>

### Table 7.17: Background estimates and observed yield for each $R^2$ bin in the H $M_R$ category.

<table>
<thead>
<tr>
<th>$R^2$ range</th>
<th>0.5–0.575</th>
<th>0.575–0.65</th>
<th>0.65–0.75</th>
</tr>
</thead>
<tbody>
<tr>
<td>Observed</td>
<td>513</td>
<td>328</td>
<td>279</td>
</tr>
<tr>
<td>Estimated</td>
<td>560 ± 550</td>
<td>330 $^{+360}_{-330}$</td>
<td>275 ± 41</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>$R^2$ range</th>
<th>0.75–0.85</th>
<th>0.85–0.95</th>
<th>0.95–2.5</th>
</tr>
</thead>
<tbody>
<tr>
<td>Observed</td>
<td>203</td>
<td>151</td>
<td>85</td>
</tr>
<tr>
<td>Estimated</td>
<td>242 ± 18</td>
<td>171 $^{+173}_{-171}$</td>
<td>74 ± 17</td>
</tr>
</tbody>
</table>

### Table 7.18: Background estimates and observed yield for each $R^2$ bin in the VH $M_R$ category.

<table>
<thead>
<tr>
<th>$R^2$ range</th>
<th>0.5–0.6</th>
<th>0.6–0.7</th>
<th>0.7–0.95</th>
<th>0.95–2.5</th>
</tr>
</thead>
<tbody>
<tr>
<td>Observed</td>
<td>117</td>
<td>58</td>
<td>75</td>
<td>11</td>
</tr>
<tr>
<td>Estimated</td>
<td>100 $^{+150}_{-100}$</td>
<td>59 ± 36</td>
<td>75 ± 30</td>
<td>9 ± 7</td>
</tr>
</tbody>
</table>
Table 7.19: Background estimates and observed yield for each bin in the 0µb signal region.

<table>
<thead>
<tr>
<th>R² range</th>
<th>0.5–0.6</th>
<th>0.6–0.75</th>
<th>0.75–0.9</th>
<th>0.9–2.5</th>
</tr>
</thead>
<tbody>
<tr>
<td>Observed</td>
<td>760</td>
<td>807</td>
<td>469</td>
<td>246</td>
</tr>
<tr>
<td>Estimated</td>
<td>850 ± 170</td>
<td>620 ± 120</td>
<td>470 ± 110</td>
<td>320 ± 160</td>
</tr>
</tbody>
</table>

Table 7.20: Background estimates and observed yield for each bin in the 0µbb signal region.

<table>
<thead>
<tr>
<th>R² range</th>
<th>0.5–0.6</th>
<th>0.6–0.75</th>
<th>0.75–0.9</th>
<th>0.9–2.5</th>
</tr>
</thead>
<tbody>
<tr>
<td>Observed</td>
<td>122</td>
<td>80</td>
<td>31</td>
<td>14</td>
</tr>
<tr>
<td>Estimated</td>
<td>135 ± 30</td>
<td>81 ± 18</td>
<td>36 ± 8</td>
<td>19 ± 9</td>
</tr>
</tbody>
</table>
Chapter 8

SEARCHES FOR ANOMALOUS HIGGS BOSON PRODUCTION

8.1 Introduction

The discovery of the standard model (SM) Higgs boson at the LHC [16, 93] presents a unique opportunity to search for physics beyond the SM (BSM) using the Higgs boson as a search tool. Given the small value of the Higgs production cross section in the standard model, any BSM scenario predicting new mechanisms for Higgs boson production can be investigated with dedicated searches, using the known Higgs mass to suppress SM background processes.

This Chapter presents a search of this kind in pp collisions at 13 TeV using data from the CMS detector at the CERN LHC. Events with two photons consistent with a Higgs candidate are selected and categorized according to the $p_T$ of the Higgs candidate, the presence of additional Higgs to $b\bar{b}$ or $Z$ to $b\bar{b}$ candidates, and the estimated resolution of the diphoton pair. Motivated by supersymmetric (SUSY) scenarios, we use the razor variables [90, 224] $M_R$ and $R^2$ – extensively discussed and illustrated in Chapter 6 – to define search regions that may contain additional events above the SM prediction if a BSM Higgs production mechanism is present. The contribution in the search regions from the non-resonant QCD background is distinguished from a potential BSM Higgs signal using the shape of the diphoton mass distribution. The search uses 2.3 fb$^{-1}$ of integrated luminosity collected in 2015 and 12.9 fb$^{-1}$ collected in 2016.

In Run 1 of the LHC, a similar CMS analysis [236] reported an excess of $H \rightarrow \gamma\gamma$ events with $M_R \approx 400$ GeV and $R^2 > 0.05$ with a local (global) significance of $2.9\sigma$ ($1.6\sigma$). Motivated by the Run I result, we consider a SUSY simplified model in which bottom squarks are pair produced and decay to a bottom quark and the next-to-lightest supersymmetric particle (NLSP), $\tilde{\chi}^0_2$, with 100% branching ratio. The NLSP subsequently decays to a Higgs boson and the lightest supersymmetric particle (LSP), $\tilde{\chi}^0_1$, with 100% branching ratio. We assume that the mass difference between the NLSP and the LSP is 130 GeV, just above the Higgs boson mass. The relevant decay topology in the simplified model is shown in Figure 8.1. The cross section for this simplified model is assumed to be the same as the standard sbottom pair production cross section [64]. Such a signal model is observed to produce event
kinematics consistent with the excess observed in Run I data and is not ruled out by searches in other final states and decay channels. This search is interpreted using the sbottom pair production model as the benchmark, and we derive limits on the production cross section as a function of the sbottom mass and the LSP mass.

Figure 8.1: Diagram illustrating the SUSY benchmark simplified model of bottom squark decays to a Higgs boson, a b-jet, and the LSP.

8.2 Summary of the 8 TeV Results

The first version of the analysis to be presented in this Chapter was carried out by CMS [236] and studied in more detailed in Alex Mott’s thesis [202]. Here, a summary of the main results is given as is relevant for the discussions to follow.

The 8 TeV analysis selects events in a very similar fashion to the one presented in this Chapter. It categorizes events based on the Higgs candidate $p_T$, the photons energy resolution, and the invariant masses of the possible b-jet pairs – indeed, intended to target an extra Higgs or Z boson on the event. The final results yield that most of the search bins were consistent with the SM expectations, and the results were interpreted as cross section limits on the neutralino/chargino production in the context of SUSY simplified models. The observed significances for all the search bins are shown in Figure 8.2, while the limit on the neutralino/chargino production as a function of the chargino mass is shown in Figure 8.3. Although most of the search bins were consistent with the SM expectations, an interesting excess of events was observed in the most extreme bin – that with the highest $M_R$ and $R^2$ boundaries – in the High-Resolution (HighRes) event category; see Figures 8.4 and 8.5, where both photons forming the Higgs candidate are require to have an energy resolution better than 1.5%. This excess corresponds to a $2.9\sigma$ ($1.6\sigma$) local (global) significance. Such an excess, despite the limited number of events, is interesting for mainly two reasons: first, it is located at relative high values of $M_R$ (~ 400 GeV) and low values of $R^2$ (below 0.05), see 8.5 for more detail, and therefore suggest a
characteristic mass scale and that they contain relative low $E_T^{\text{miss}}$ values. Second, that the diphoton invariant mass is consistent with that of the SM Higgs boson and therefore any possible model to explain such an excess should at least contain a one SM Higgs boson. The diphoton invariant mass for the events that lie in the bin with the excess are shown in 8.6. The search presented in this Chapter is largely inspired on its 8 TeV counterpart, but with significant differences when it comes to the background estimation techniques. In addition, the proposed simplified model shown in Figure 8.1 – which is studied in great detail in Chapter B – shows some consistency with the excess observed in the 8 TeV CMS result.

![Figure 8.2: Summary of the results in the HighRes category for the 8 TeV version of the analysis.](image)

![Figure 8.3: Summary of the results in the HighRes category for the 8 TeV version of the analysis.](image)
<table>
<thead>
<tr>
<th>M_{\ell\ell} region (GeV)</th>
<th>E^{*} region (GeV)</th>
<th>observed events</th>
<th>expected background</th>
<th>p-value</th>
<th>significance (\sigma)</th>
</tr>
</thead>
<tbody>
<tr>
<td>100 - 250</td>
<td>0.00 - 0.05</td>
<td>464</td>
<td>569\pm_{-20}^{+20} (syst.)</td>
<td>0.40</td>
<td>0.3</td>
</tr>
<tr>
<td>150 - 250</td>
<td>0.05 - 0.10</td>
<td>149</td>
<td>139.4\pm_{-3.2}^{+3.2} (syst.)</td>
<td>0.23</td>
<td>0.7</td>
</tr>
<tr>
<td>150 - 250</td>
<td>0.10 - 0.15</td>
<td>35</td>
<td>32.0\pm_{-1.0}^{+1.0} (syst.)</td>
<td>0.34</td>
<td>0.4</td>
</tr>
<tr>
<td>150 - 250</td>
<td>0.15 - 1.00</td>
<td>7</td>
<td>8.0\pm_{-1.0}^{+1.0} (syst.)</td>
<td>0.40</td>
<td>-0.3</td>
</tr>
<tr>
<td>250 - 400</td>
<td>0.00 - 0.05</td>
<td>218</td>
<td>207.9\pm_{-2.7}^{+2.7} (syst.)</td>
<td>0.27</td>
<td>0.6</td>
</tr>
<tr>
<td>250 - 400</td>
<td>0.05 - 0.10</td>
<td>20</td>
<td>14.7\pm_{-1.7}^{+1.7} (syst.)</td>
<td>0.11</td>
<td>1.1</td>
</tr>
<tr>
<td>250 - 400</td>
<td>0.10 - 1.00</td>
<td>3</td>
<td>2.7\pm_{-0.7}^{+0.7} (syst.)</td>
<td>0.41</td>
<td>0.2</td>
</tr>
<tr>
<td>400 - 1400</td>
<td>0.00 - 0.05</td>
<td>109</td>
<td>101.6\pm_{-2.4}^{+2.4} (syst.)</td>
<td>0.26</td>
<td>0.7</td>
</tr>
<tr>
<td>400 - 1400</td>
<td>0.05 - 1.00</td>
<td>5</td>
<td>0.9\pm_{-0.1}^{+0.1} (syst.)</td>
<td>0.002</td>
<td>2.9</td>
</tr>
<tr>
<td>1400 - 3000</td>
<td>0.00 - 1.00</td>
<td>0</td>
<td>0.9\pm_{-0.1}^{+0.1} (syst.)</td>
<td>0.44</td>
<td>-0.1</td>
</tr>
</tbody>
</table>

Figure 8.4: Summary of the results in the HighRes category for the 8 TeV version of the analysis.

![Figure 8.4](image1.png)

Figure 8.5: Summary of the results in the HighRes category for the 8 TeV version of the analysis.

![Figure 8.5](image2.png)

Figure 8.6: Summary of the results in the HighRes category for the 8 TeV version of the analysis.

8.3 Object Selection

Photon candidates with $p_T > 25$ GeV falling in the barrel region ($|\eta| < 1.4442$) are selected if they satisfy identification requirements based on the shower shape in the electromagnetic calorimeter, the hadronic to electromagnetic energy ratio, and
the isolation in a cone around the photon direction [174]. To satisfy the isolation requirement, the sum of the energies of PF candidates near the photon must be smaller than a specified cut value. Isolation cuts are placed separately on energy from charged hadrons, neutral hadrons, and photons. Each isolation sum is corrected for the effect of pileup by subtracting the average energy deposited into the isolation cone estimated using a random sampling of energy density in the event. Photon objects are rejected if they match an electron candidate. The photon identification requirements correspond to a loose working point with an efficiency of about 90%.

The measured energies of the photons are corrected for clustering and local geometric effects using an energy regression trained on Monte Carlo simulation [177]. This regression gives a significant improvement to the energy resolution of the photons and provides an estimate of the uncertainty of the energy measurement. This uncertainty estimate is used in this analysis to categorize events into high and low resolution categories.

Jets are reconstructed using a global event description based on the CMS particle flow (PF) algorithm [105, 103]. Individual particles (PF candidates) are reconstructed by combining the information from the inner tracker, the calorimeters, and the muon system. Charged PF candidates associated to a vertex other than the primary one are considered pileup and are rejected. The remaining particles are clustered into jets, using the FASTJet [73] implementation of the anti-$k_T$ [74] algorithm with the distance parameter $R = 0.4$. Jets are required not to overlap with either of the two photons; this requirement is imposed by the condition $\Delta R = \sqrt{\Delta \eta^2 + \Delta \phi^2} > 0.5$. The vector sum of the reconstructed $p_T$ of the PF particles is used to quantify the missing transverse momentum $p_T^{\text{miss}}$ in the event. Events with detector- and beam-related noise that can mimic event topologies with high energy and large $E_T^{\text{miss}}$ are filtered using dedicated noise reduction algorithms [92, 97, 106].

The combined secondary vertex (CSV) tagging algorithm [212] is used to identify jets originating from the showering and hadronization of b quarks. A loose working point is used which yields a mistag rate that is approximately 10%. Jet pairs are identified as $b\bar{b}$ candidates if the two jets satisfy the CSV requirement. Among all $b\bar{b}$ candidates in the event (if there are any), the pair with mass closest to 125 GeV (91.2 GeV) is chosen as a $H \to b\bar{b}$ ($Z \to b\bar{b}$) candidate. Events are not required to contain a $b\bar{b}$ pair; the presence or absence of a $H \to b\bar{b}$ or $Z \to b\bar{b}$ candidate with mass in the specified range is used in the event classification procedure described in Section 8.4.
8.4 Event Selection and Analysis Strategy

We select events with two photons that satisfy the identification criteria described above. If multiple photon pairs are identified, the pair with the largest scalar sum of the transverse momenta of the photons is chosen as the Higgs candidate. The Higgs candidate must additionally have leading photon $p_T$ greater than 40 GeV, and diphoton mass between 103 GeV and 160 GeV.

In addition to the diphoton Higgs candidate, we require at least one additional jet with $p_T > 30$ GeV and $|\eta| < 3.0$. The Higgs candidate and all identified jets are clustered into hemispheres according to the Razor megajet algorithm[99], and the razor variables [90, 224] $M_R$ and $R^2$ are computed as follows:

$$M_R \equiv \sqrt{(|\vec{p}_j^1| + |\vec{p}_j^2|)^2 - (p_{z1}^f + p_{z2}^f)^2}, \quad (8.1)$$

$$R^2 \equiv \left( \frac{M_T^R}{M_R} \right)^2, \quad (8.2)$$

where $\vec{p}$ is the momentum of a hemisphere and $p_z$ is its longitudinal component, and $j_1$ and $j_2$ are used to label the two hemispheres. In the definition of $R^2$, the variable $M_T^R$ is defined as:

$$M_T^R \equiv \sqrt{E_T^\text{miss}(p_T^{j_1} + p_T^{j_2}) - \vec{p}_T^\text{miss} \cdot (\vec{p}_T^{j_1} + \vec{p}_T^{j_2})}. \quad (8.3)$$

The razor variables $M_R$ and $R^2$ provide discrimination between SUSY signal models and standard model background processes. SUSY signals typically have large values of $M_R$ and $R^2$, while the standard model background exhibits an exponentially falling spectrum in both variables.

The selected events are categorized into four mutually exclusive categories. An event is categorized as “HighPt” if the $p_T$ of the selected Higgs candidate is larger than 110 GeV. Otherwise it is categorized as “H(\gamma\gamma)-H/Z(bb)” if the event contains two b-tagged jets whose invariant mass is in the Z mass region between 76 GeV and 106 GeV, or in the Higgs mass region between 110 GeV and 140 GeV. Remaining events are categorized as “HighRes” (“LowRes”) if the mass resolution estimate $\sigma_M/M$ is less (greater) than 0.85%, where $\sigma_M$ is computed as $1/2 \times \sqrt{(\sigma_{E,\gamma1}/E_{\gamma1})^2 + (\sigma_{E,\gamma2}/E_{\gamma2})^2}$. The “HighPt” category is intended to isolate events from SUSY signals that produce high-$p_T$ Higgs bosons. The “H(\gamma\gamma)-H/Z(bb)” category is motivated by the fact that many SUSY signal models predict events with two Higgs bosons or a Higgs boson and a Z boson in the final state.
Finally, the “HighRes” and “LowRes” categories are intended to capture other SUSY signals, including compressed models. The categorization procedure is illustrated in Figure 8.7.

![Event Categorization Diagram](image)

**Figure 8.7:** Diagram illustrating the event categorization used in the analysis.

Each event category is divided into bins by rectangular cuts on $M_R$ and $R^2$. The binning is chosen via an optimization procedure that uses the sbottom pair production simplified model discussed in Section A.1 as a benchmark model to determine the best bin boundaries. The algorithm begins with a single bin covering the entire $M_R$-$R^2$ plane. A division is made in either $M_R$ or $R^2$ at the value, which maximizes the expected statistical significance. This process is repeated on each newly created bin, and until convergence is achieved. Each bin returned by the algorithm is treated as a separate analysis search region. This procedure is not performed on the LowRes category; the binning in the LowRes category is instead taken to be the same as that in the HighRes category. The definition of the individual search regions is summarized in Table 8.1.

To illustrate how events from a typical SUSY signal might be distributed in these bins, the distribution of events in the $M_R$ and $R^2$ plane for the sbottom pair production signal model discussed in Section A.1 is shown in Figures 8.8 and 8.9 for the HighPt, HighRes, and LowRes categories, respectively.
Table 8.1: A summary of the search region bins in each category is presented. The functional form used to model the non-resonant background is also listed. An exponential function of the form \( e^{-ax} \) is denoted as “singleExp”; a modified exponential function of the form \( e^{-ax^b} \) is denoted as “modExp”; and an N’th order Bernstein polynomial is denoted by “polyN”.

<table>
<thead>
<tr>
<th>Bin Number</th>
<th>Category</th>
<th>( M_R ) Bin</th>
<th>( R^2 ) Bin</th>
<th>Non-Resonant Bkg Model</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>HighPt</td>
<td>600 - ( \infty )</td>
<td>0.025 - ( \infty )</td>
<td>poly3</td>
</tr>
<tr>
<td>1</td>
<td>HighPt</td>
<td>150 - 600</td>
<td>0.130 - ( \infty )</td>
<td>singleExp</td>
</tr>
<tr>
<td>2</td>
<td>HighPt</td>
<td>1250 - ( \infty )</td>
<td>0.000 - 0.025</td>
<td>poly2</td>
</tr>
<tr>
<td>3</td>
<td>HighPt</td>
<td>150 - 450</td>
<td>0.000 - 0.130</td>
<td>poly2</td>
</tr>
<tr>
<td>4</td>
<td>HighPt</td>
<td>450 - 600</td>
<td>0.000 - 0.035</td>
<td>singleExp</td>
</tr>
<tr>
<td>5</td>
<td>HighPt</td>
<td>450 - 600</td>
<td>0.035 - 0.130</td>
<td>singleExp</td>
</tr>
<tr>
<td>6</td>
<td>HighPt</td>
<td>600 - 1250</td>
<td>0.000 - 0.015</td>
<td>singleExp</td>
</tr>
<tr>
<td>7</td>
<td>HighPt</td>
<td>600 - 1250</td>
<td>0.015 - 0.025</td>
<td>singleExp</td>
</tr>
<tr>
<td>8</td>
<td>( H(\gamma\gamma) - H/Z(bb) )</td>
<td>150 - ( \infty )</td>
<td>0.000 - ( \infty )</td>
<td>singleExp</td>
</tr>
<tr>
<td>9</td>
<td>HighRes</td>
<td>150 - 250</td>
<td>0.000 - 0.175</td>
<td>modExp</td>
</tr>
<tr>
<td>10</td>
<td>HighRes</td>
<td>150 - 250</td>
<td>0.175 - ( \infty )</td>
<td>singleExp</td>
</tr>
<tr>
<td>11</td>
<td>HighRes</td>
<td>250 - ( \infty )</td>
<td>0.05 - ( \infty )</td>
<td>singleExp</td>
</tr>
<tr>
<td>12</td>
<td>HighRes</td>
<td>250 - 600</td>
<td>0.000 - 0.05</td>
<td>modExp</td>
</tr>
<tr>
<td>13</td>
<td>HighRes</td>
<td>600 - ( \infty )</td>
<td>0.000 - 0.05</td>
<td>singleExp</td>
</tr>
<tr>
<td>9</td>
<td>LowRes</td>
<td>150 - 250</td>
<td>0.000 - 0.175</td>
<td>modExp</td>
</tr>
<tr>
<td>10</td>
<td>LowRes</td>
<td>150 - 250</td>
<td>0.175 - ( \infty )</td>
<td>singleExp</td>
</tr>
<tr>
<td>11</td>
<td>LowRes</td>
<td>250 - ( \infty )</td>
<td>0.05 - ( \infty )</td>
<td>modExp</td>
</tr>
<tr>
<td>12</td>
<td>LowRes</td>
<td>250 - 600</td>
<td>0.000 - 0.05</td>
<td>modExp</td>
</tr>
<tr>
<td>13</td>
<td>LowRes</td>
<td>600 - ( \infty )</td>
<td>0.000 - 0.05</td>
<td>singleExp</td>
</tr>
</tbody>
</table>

Figure 8.8: Distribution of events in the \( M_R \) and \( R^2 \) plane for the HighPt and \( H(\gamma\gamma) - H/Z(bb) \) category for sbottom pair production with \( m_{\tilde{b}} = 300 \) GeV and \( m_\chi = 1 \) GeV. The signal expectation is shown in the color scale and the bin numbers show where each bin is located in the \( M_R \) and \( R^2 \) plane.
Figure 8.9: Distribution of events in the $M_R$ and $R^2$ plane for the HighRes and LowRes categories for sbottom pair production with $m_{\tilde{b}} = 300$ GeV and $m_{\chi} = 1$ GeV. The signal expectation is shown in the color scale and the bin numbers show where each bin is located in the $M_R$ and $R^2$ plane.

### 8.5 Background Estimation

Within each search bin, we extract a potential signal by fitting to the diphoton mass spectrum. There are two types of backgrounds: a non-resonant background that is primarily due to QCD production of two photons or one photon and one jet, and a resonant background from standard model Higgs production. The non-resonant background is modeled with the functional form given in Table 8.1 for each individual search region bin, and all parameters of the function are unconstrained in the fit. The functional form model for each search region bin is selected on the basis of its Akaike Information Criterion (AIC) score [33], as well as tests of fit biases for a set of alternative models that all describe the data in the sideband well.

The standard model Higgs background and the SUSY signal are each modeled with a double-sided crystal ball function fit to the diphoton mass distribution obtained from the Monte Carlo simulation. The parameters of each double-sided crystal ball function are held constant in the signal extraction procedure, with the exception of the parameter that determines the location of the peak. This parameter is allowed to float but is restricted via a Gaussian constraint to the region around the Higgs mass. The width of the Gaussian constraint is 1%, corresponding to the systematic uncertainty on the photon energy scale.

The normalization of the standard model Higgs background in each bin is predicted from the Monte Carlo simulation, and is constrained to that value in the fit within uncertainties. Signal yields are also predicted from the Monte Carlo simulation.

Each bin in the HighRes category is fit simultaneously with the corresponding bin
in the LowRes category. The relative SM Higgs and SUSY signal yields in the two categories are constrained according to the simulation prediction. The ratio of the yields in the HighRes and LowRes categories is expected to be independent of the signal model and background process.

Nuisance parameters for various theoretical and instrumental uncertainties that can affect the SM Higgs and signal normalization and are profiled to propagate systematic uncertainties. A more detailed discussion of systematic uncertainties can be found below in Section 8.7. The Monte Carlo simulation predictions for the standard model Higgs background normalization are shown in Table 8.2 for each search region bin.

8.6 Nos-resonant Background Functional Form Selection: AIC Criterion and Bias Tests

For each signal region – i.e. every $M_R^2$ bin in the search – a functional form is needed to estimate the non-resonant contribution from SM QCD production. This selection process has two steps: 1) the AIC criterion, and 2) the bias test.

The AIC criterion step is used to decide what functions described reasonable well the observed data and therefore describe better the QCD background in each signal region. The AIC criterion, first introduced by Akaike in 1973 [33], is an estimate of the Kullback-Leibler divergence [190] – the later is a measure of the distance between two probability density functions. Therefore the AIC criterion is a measure of the distance between the data and a particular probability density function (p.d.f). An advantage over other goodness of fit quantities is that the AIC criterion also accounts for the fact that a function may have move free parameters and thus more flexibility to accommodate the observed data. It is useful to define the AIC score:

$$AIC_i = -2\log(L) + 2k - \frac{2k(k+1)}{n-k-1},$$  \hspace{1cm} (8.4)

where $i$ represents the $i$-th p.d.f under study, $L$ is the likelihood after the minimization process, $k$ is the number of free parameters of the p.d.f, and $n$ is the total number of observed events. The procedure is as follows: from a set of functions, all AIC scores are computed, then AIC score differences with respect to the minimum AIC score ($\Delta_i = AIC_i - AIC_{\text{min}}$) are calculated. The AIC weight, which could be interpreted as the probability that the p.d.f under study is the true p.d.f from where the observed
dataset was drawn, is defined as

$$\omega_i = \frac{e^{-\frac{1}{2} \Delta_i}}{\sum_{j=0}^{7} e^{-\frac{1}{2} \Delta_j}}. \quad (8.5)$$

Only p.d.fs with AIC weight larger than 0.1 pass the first step and are then tested for the bias test described below. Table 8.3 shows the full list of p.d.fs used in these studies. Tables 8.4, 8.5, 8.6, and 8.7 summarize four examples of the AIC results obtained for four search regions – one per each category in the analysis – Figures 8.10, 8.11, 8.12, and 8.13 show the corresponding fits to the observed data. It is of note that the AIC fits are done only to the $m_{\gamma\gamma} \in ([103 - 121], [129 - 160])$ GeV region.

Figure 8.10: sideband fits for the search region: HighPt, $M_R > 600$ GeV, $R^2 > 0.025$. 

Figure 8.11: sideband fits for the search region: HighRes, $150 < M_R < 250$ GeV, $R^2 > 0$

Figure 8.12: Sideband fits for the search region: LowRes, $150 < M_R < 250$ GeV, $R^2 > 0.175$. 
Table 8.2: The predicted yields for the standard model Higgs background processes are shown for an integrated luminosity corresponding to 15.2 fb\(^{-1}\) for each search region considered in this analysis. The contributions from each standard model Higgs process is shown separately, and the total is shown on the rightmost column along with its full uncertainty.

<table>
<thead>
<tr>
<th>Bin</th>
<th>Category</th>
<th>ggH</th>
<th>t(\bar{t})</th>
<th>VBF H</th>
<th>VH</th>
<th>bbH</th>
<th>Total</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>HighPt</td>
<td>1.09</td>
<td>0.49</td>
<td>0.17</td>
<td>0.25</td>
<td>0.01</td>
<td>2.0 ± 0.4</td>
</tr>
<tr>
<td>1</td>
<td>HighPt</td>
<td>0.45</td>
<td>0.22</td>
<td>0.07</td>
<td>0.60</td>
<td>0.00</td>
<td>1.4 ± 0.3</td>
</tr>
<tr>
<td>2</td>
<td>HighPt</td>
<td>1.75</td>
<td>0.23</td>
<td>0.89</td>
<td>0.07</td>
<td>0.02</td>
<td>3.0 ± 0.6</td>
</tr>
<tr>
<td>3</td>
<td>HighPt</td>
<td>20.82</td>
<td>0.38</td>
<td>4.05</td>
<td>2.36</td>
<td>0.16</td>
<td>27.7 ± 8.0</td>
</tr>
<tr>
<td>4</td>
<td>HighPt</td>
<td>6.30</td>
<td>0.20</td>
<td>1.77</td>
<td>0.45</td>
<td>0.06</td>
<td>8.8 ± 2.5</td>
</tr>
<tr>
<td>5</td>
<td>HighPt</td>
<td>1.09</td>
<td>0.23</td>
<td>0.18</td>
<td>0.19</td>
<td>0.01</td>
<td>1.7 ± 0.4</td>
</tr>
<tr>
<td>6</td>
<td>HighPt</td>
<td>7.15</td>
<td>0.21</td>
<td>2.91</td>
<td>0.28</td>
<td>0.05</td>
<td>10.7 ± 2.7</td>
</tr>
<tr>
<td>7</td>
<td>HighPt</td>
<td>1.94</td>
<td>0.19</td>
<td>0.37</td>
<td>0.17</td>
<td>0.01</td>
<td>2.7 ± 0.8</td>
</tr>
<tr>
<td>8</td>
<td>H((\gamma\gamma))-H/Z(bb)</td>
<td>0.35</td>
<td>0.51</td>
<td>0.03</td>
<td>0.10</td>
<td>0.06</td>
<td>1.0 ± 0.2</td>
</tr>
<tr>
<td>9</td>
<td>HighRes</td>
<td>27.57</td>
<td>0.10</td>
<td>3.49</td>
<td>1.97</td>
<td>0.43</td>
<td>33.5 ± 10.4</td>
</tr>
<tr>
<td>10</td>
<td>HighRes</td>
<td>0.26</td>
<td>0.06</td>
<td>0.04</td>
<td>0.20</td>
<td>0.01</td>
<td>0.6 ± 0.1</td>
</tr>
<tr>
<td>11</td>
<td>HighRes</td>
<td>0.94</td>
<td>0.33</td>
<td>0.21</td>
<td>0.19</td>
<td>0.05</td>
<td>1.7 ± 0.4</td>
</tr>
<tr>
<td>12</td>
<td>HighRes</td>
<td>16.16</td>
<td>0.31</td>
<td>3.99</td>
<td>0.64</td>
<td>0.39</td>
<td>21.5 ± 5.4</td>
</tr>
<tr>
<td>13</td>
<td>HighRes</td>
<td>1.83</td>
<td>0.23</td>
<td>1.25</td>
<td>0.10</td>
<td>0.09</td>
<td>3.5 ± 1.0</td>
</tr>
<tr>
<td>9</td>
<td>LowRes</td>
<td>9.55</td>
<td>0.039</td>
<td>1.18</td>
<td>0.72</td>
<td>0.14</td>
<td>11.6 ± 3.8</td>
</tr>
<tr>
<td>10</td>
<td>LowRes</td>
<td>0.12</td>
<td>0.02</td>
<td>0.01</td>
<td>0.07</td>
<td>0.00</td>
<td>0.2 ± 0.1</td>
</tr>
<tr>
<td>11</td>
<td>LowRes</td>
<td>0.32</td>
<td>0.11</td>
<td>0.06</td>
<td>0.08</td>
<td>0.02</td>
<td>0.6 ± 0.2</td>
</tr>
<tr>
<td>12</td>
<td>LowRes</td>
<td>6.02</td>
<td>0.11</td>
<td>1.46</td>
<td>0.24</td>
<td>0.12</td>
<td>7.9 ± 2.3</td>
</tr>
<tr>
<td>13</td>
<td>LowRes</td>
<td>0.82</td>
<td>0.09</td>
<td>0.46</td>
<td>0.04</td>
<td>0.03</td>
<td>1.4 ± 0.4</td>
</tr>
</tbody>
</table>
Table 8.3: Full list of p.d.f (function) used in the AIC test.

<table>
<thead>
<tr>
<th>function name</th>
<th>short name</th>
<th>functional form</th>
</tr>
</thead>
<tbody>
<tr>
<td>single exponential</td>
<td>singleExp</td>
<td>$e^{-\alpha_m \gamma}$</td>
</tr>
<tr>
<td>double exponential</td>
<td>doubleExp</td>
<td>$f e^{-\alpha_1 \gamma} + (1-f)e^{-\alpha_2 \gamma}$</td>
</tr>
<tr>
<td>single power law</td>
<td>singlePow</td>
<td>$m_{\gamma}^{\alpha_1}$</td>
</tr>
<tr>
<td>double power law</td>
<td>doublePow</td>
<td>$f m_{\gamma}^{\alpha_1} + (1-f)m_{\gamma}^{\alpha_2}$</td>
</tr>
<tr>
<td>modified exponential</td>
<td>modExp</td>
<td>$e^{-\alpha m_{\gamma}^2}$</td>
</tr>
<tr>
<td>Bernstein polynomial order 2</td>
<td>poly2</td>
<td></td>
</tr>
<tr>
<td>Bernstein polynomial order 3</td>
<td>poly3</td>
<td>$p_0(1-t)^2 + p_1 2t(1-t) + p_2 t^2$</td>
</tr>
<tr>
<td>Bernstein polynomial order 4</td>
<td>poly4</td>
<td>$p_0(1-t)^3 + p_1 3t(1-t)^2 + p_2 3t^2(1-t) + p_3 t^3$</td>
</tr>
</tbody>
</table>

Table 8.4: AIC results summary for the search region: HighPt, $M_R > 600$ GeV, $R^2 > 0.025$.

<table>
<thead>
<tr>
<th>function</th>
<th>#P</th>
<th>$\Delta AIC$</th>
<th>$\omega$</th>
<th>$\omega_{max}/\omega$</th>
<th>status</th>
</tr>
</thead>
<tbody>
<tr>
<td>singlePow</td>
<td>1</td>
<td>0.000</td>
<td>0.247</td>
<td>1.000</td>
<td>0, 3</td>
</tr>
<tr>
<td>singleExp</td>
<td>1</td>
<td>0.128</td>
<td>0.232</td>
<td>1.066</td>
<td>0, 3</td>
</tr>
<tr>
<td>poly3</td>
<td>4</td>
<td>0.605</td>
<td>0.183</td>
<td>1.353</td>
<td>0, 3</td>
</tr>
<tr>
<td>poly2</td>
<td>3</td>
<td>0.673</td>
<td>0.177</td>
<td>1.400</td>
<td>0, 3</td>
</tr>
<tr>
<td>modExp</td>
<td>2</td>
<td>2.738</td>
<td>0.063</td>
<td>3.932</td>
<td>0, 3</td>
</tr>
<tr>
<td>poly4</td>
<td>5</td>
<td>2.916</td>
<td>0.058</td>
<td>4.297</td>
<td>0, 3</td>
</tr>
<tr>
<td>doubleExp</td>
<td>3</td>
<td>4.958</td>
<td>0.021</td>
<td>11.929</td>
<td>0, 3</td>
</tr>
<tr>
<td>doublePow</td>
<td>3</td>
<td>5.031</td>
<td>0.020</td>
<td>12.371</td>
<td>0, 3</td>
</tr>
</tbody>
</table>

Table 8.5: AIC results summary for the search region: HighRes, $150 < M_R < 250$ GeV, $R^2 > 0$.

<table>
<thead>
<tr>
<th>function</th>
<th>#P</th>
<th>$\Delta AIC$</th>
<th>$\omega$</th>
<th>$\omega_{max}/\omega$</th>
<th>status</th>
</tr>
</thead>
<tbody>
<tr>
<td>ModExp</td>
<td>2</td>
<td>0.000</td>
<td>0.484</td>
<td>1.000</td>
<td>1, 2</td>
</tr>
<tr>
<td>singleExp</td>
<td>1</td>
<td>1.704</td>
<td>0.206</td>
<td>2.344</td>
<td>0, 3</td>
</tr>
<tr>
<td>poly2</td>
<td>3</td>
<td>2.173</td>
<td>0.163</td>
<td>2.964</td>
<td>0, 3</td>
</tr>
<tr>
<td>poly3</td>
<td>4</td>
<td>4.028</td>
<td>0.065</td>
<td>7.492</td>
<td>1, 2</td>
</tr>
<tr>
<td>poly4</td>
<td>5</td>
<td>4.714</td>
<td>0.046</td>
<td>10.560</td>
<td>0, 3</td>
</tr>
<tr>
<td>doubleExp</td>
<td>3</td>
<td>5.708</td>
<td>0.028</td>
<td>17.359</td>
<td>1, 2</td>
</tr>
<tr>
<td>singlePow</td>
<td>1</td>
<td>8.492</td>
<td>0.007</td>
<td>69.817</td>
<td>0, 3</td>
</tr>
<tr>
<td>doublePow</td>
<td>3</td>
<td>12.496</td>
<td>0.001</td>
<td>517.007</td>
<td>0, 3</td>
</tr>
</tbody>
</table>
Table 8.6: AIC results summary for the search region: LowRes, LowRes, 150 < $M_R < 250$ GeV, $R^2 > 0.175$

<table>
<thead>
<tr>
<th>function</th>
<th>#P</th>
<th>$\Delta AIC$</th>
<th>$\omega$</th>
<th>$\omega_{max}/\omega$</th>
<th>status</th>
</tr>
</thead>
<tbody>
<tr>
<td>singleExp</td>
<td>1</td>
<td>0.000</td>
<td>0.529</td>
<td>1.000</td>
<td>0, 3</td>
</tr>
<tr>
<td>modExp</td>
<td>2</td>
<td>1.883</td>
<td>0.206</td>
<td>2.564</td>
<td>1, 2</td>
</tr>
<tr>
<td>doubleExp</td>
<td>3</td>
<td>3.646</td>
<td>0.085</td>
<td>6.191</td>
<td>0, 3</td>
</tr>
<tr>
<td>singlePow</td>
<td>1</td>
<td>3.698</td>
<td>0.083</td>
<td>6.353</td>
<td>0, 3</td>
</tr>
<tr>
<td>poly2</td>
<td>3</td>
<td>4.925</td>
<td>0.045</td>
<td>11.736</td>
<td>0, 3</td>
</tr>
<tr>
<td>poly3</td>
<td>4</td>
<td>5.892</td>
<td>0.028</td>
<td>19.029</td>
<td>0, 3</td>
</tr>
<tr>
<td>poly4</td>
<td>5</td>
<td>7.657</td>
<td>0.012</td>
<td>45.992</td>
<td>0, 3</td>
</tr>
<tr>
<td>doublePow</td>
<td>3</td>
<td>7.703</td>
<td>0.011</td>
<td>47.065</td>
<td>1, 2</td>
</tr>
</tbody>
</table>

Figure 8.13: Sideband fits for the search region: $H(\gamma\gamma)$-H/Z(bb), $M_R > 150$ GeV, $R^2 > 0$.

Table 8.7: AIC results summary for the search region: $H(\gamma\gamma)$-H/Z(bb), $M_R > 150$ GeV, $R^2 > 0$.

<table>
<thead>
<tr>
<th>function</th>
<th>#P</th>
<th>$\Delta AIC$</th>
<th>$\omega$</th>
<th>$\omega_{max}/\omega$</th>
<th>status</th>
</tr>
</thead>
<tbody>
<tr>
<td>singleExp</td>
<td>1</td>
<td>0.000</td>
<td>0.323</td>
<td>1.000</td>
<td>0, 3</td>
</tr>
<tr>
<td>singlePow</td>
<td>1</td>
<td>0.247</td>
<td>0.285</td>
<td>1.131</td>
<td>0, 3</td>
</tr>
<tr>
<td>modExp</td>
<td>2</td>
<td>1.619</td>
<td>0.144</td>
<td>2.247</td>
<td>1, 2</td>
</tr>
<tr>
<td>poly2</td>
<td>3</td>
<td>3.252</td>
<td>0.063</td>
<td>5.083</td>
<td>0, 3</td>
</tr>
<tr>
<td>poly4</td>
<td>5</td>
<td>3.334</td>
<td>0.061</td>
<td>5.297</td>
<td>0, 3</td>
</tr>
<tr>
<td>poly3</td>
<td>4</td>
<td>3.858</td>
<td>0.047</td>
<td>6.881</td>
<td>0, 3</td>
</tr>
<tr>
<td>doubleExp</td>
<td>3</td>
<td>4.134</td>
<td>0.041</td>
<td>7.901</td>
<td>0, 3</td>
</tr>
<tr>
<td>doublePow</td>
<td>3</td>
<td>4.382</td>
<td>0.036</td>
<td>8.946</td>
<td>0, 3</td>
</tr>
</tbody>
</table>
The second step is the bias test, where only functions that passed the AIC test are considered. The bias test quantifies the error on the measured signal made when performing a signal-plus-background fit to the entire $m_{\gamma\gamma}$ region in the final stage of the analysis. By requiring the selected function to have a small bias relative to any of the functions passing the AIC test, the error on the measured signal strength is reduced. In this analysis, the bias is defined relative to the fit uncertainty on the signal, i.e.

$$\delta_s = \frac{\hat{N}_s - N_s}{\sigma_{N_s}},$$

(8.6)

where $\hat{N}_s$ is the fitted signal, $N_s$ is the actual value of the signal, and $\sigma_{N_s}$ is the uncertainty on $\hat{N}_s$. The bias estimation is obtained by carrying a large number of pseudo-experiments (toys), each function passing the AIC test will be treated as the parent function from where the data was drawn, then several (10,000) toy datasets will be drawn from it containing the same amount of event as in the real dataset. For each toy dataset a known number of signal event will be injected ($N_s$) and a signal-plus-background fit will be carried out and the bias will be calculated. After this procedure is done, the resulting bias distribution will be fitted with a double-sided crystal ball function, where the most probable value after the fit is taken as an estimate of the bias. Figure 8.14 shows the resulting bias distribution and fit for two different cases. The studies carried out indicate that the most stringent test occurs when the number of injected signal events is small (signal to background ratio or S/B equal to zero) and therefore the results shown here correspond to that case. Table 8.8 shows the bias estimates for one of the search regions, where you can see the relative biases for all possible function passing the AIC test. Finally, the function with the least number of free parameters and having a relative bias smaller than 30% — which yield only an additional error of 5% — is selected as the background model. The final selection for all the signal regions is shown in Table 8.9.

### 8.7 Systematic Uncertainties

The dominant systematic uncertainty is the uncertainty on the prediction of the non-resonant background shape and normalization. These are propagated by profiling the overall normalization and the shape parameters of the non-resonant background functional form.

Sub-dominant systematic uncertainties on the SM Higgs background are propagated through log-normal nuisance parameters, and take into account both theoretical and instrumental effects. The effects considered include missing higher order correc-
Figure 8.14: Examples of the bias distribution for bin0 (HighPt, $M_R > 600$, $R^2 > 0.025$). Left: $f_1$ (assumed parent function) = poly3, $f_2$ (tested function) = singleExp; right: $f_1$ = poly3, $f_2$ = poly3. From the left plot we can see that singleExp does not pass the bias test since it has large bias to fit poly3.

Table 8.8: Examples of the bias estimate for different function pairs passing the AIC test for bin0 (HighPt, $M_R > 600$, $R^2 > 0.025$). Functions in the first column are the assumed parent functions ($f_1$), while functions in the first row are the ones being tested ($f_2$). In the first row, the numbers in brackets are the AIC weights.

<table>
<thead>
<tr>
<th></th>
<th>singlePow(0.247)</th>
<th>singleExp(0.232)</th>
<th>poly3(0.183)</th>
<th>poly2(0.177)</th>
</tr>
</thead>
<tbody>
<tr>
<td>singlePow</td>
<td>(21.3 ± 1.0)%</td>
<td>(19.3 ± 1.0)%</td>
<td>(17.8 ± 1.0)%</td>
<td>(18.5 ± 1.4)%</td>
</tr>
<tr>
<td>singleExp</td>
<td>(22.9 ± 2.0)%</td>
<td>(18.3 ± 1.0)%</td>
<td>(7.9 ± 1.3)%</td>
<td>(18.7 ± 2.0)%</td>
</tr>
<tr>
<td>poly3</td>
<td>(69.9 ± 1.5)%</td>
<td>(70.7 ± 0.9)%</td>
<td>(24.6 ± 1.3)%</td>
<td>(33.5 ± 1.0)%</td>
</tr>
<tr>
<td>poly2</td>
<td>(60.6 ± 0.9)%</td>
<td>(62.6 ± 0.9)%</td>
<td>(15.7 ± 1.9)%</td>
<td>(17.4 ± 1.4)%</td>
</tr>
</tbody>
</table>

tions, parton distribution functions, trigger and selection efficiencies, jet energy scale uncertainties, b-tagging efficiencies, and the uncertainty on the integrated luminosity. The typical size of these effects on the expected limit is summarized in Table 8.10.

The systematic uncertainty on the photon energy scale is implemented as a nuisance parameter that shifts the Higgs peak position, and is Gaussian constrained in the fit to lie within 1% of the nominal Higgs mass peak predicted by the Monte Carlo simulation. There is also a systematic uncertainty on the shape of the $\sigma_M/M$ distribution, which allows for migration of SM Higgs background and signal events between the HighRes and the LowRes categories.
Table 8.9: List of the selected background functions for different search regions.

<table>
<thead>
<tr>
<th>Bin</th>
<th>Category</th>
<th>LowMR</th>
<th>HighMR</th>
<th>LowRsq</th>
<th>HighRsq</th>
<th>Function</th>
<th>AIC weight</th>
<th>Max bias / σ_{stat}</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>highpt</td>
<td>600</td>
<td>10000</td>
<td>0.025</td>
<td>10.000</td>
<td>poly3</td>
<td>0.183</td>
<td>24.6%</td>
</tr>
<tr>
<td>1</td>
<td>highpt</td>
<td>150</td>
<td>600</td>
<td>0.130</td>
<td>10.000</td>
<td>singleExp</td>
<td>0.356</td>
<td>17.7%</td>
</tr>
<tr>
<td>2</td>
<td>highpt</td>
<td>1250</td>
<td>10000</td>
<td>0.000</td>
<td>0.025</td>
<td>singleExp</td>
<td>0.359</td>
<td>16.4%</td>
</tr>
<tr>
<td>3</td>
<td>highpt</td>
<td>150</td>
<td>450</td>
<td>0.000</td>
<td>0.130</td>
<td>-</td>
<td>-</td>
<td>-%</td>
</tr>
<tr>
<td>4</td>
<td>highpt</td>
<td>450</td>
<td>600</td>
<td>0.000</td>
<td>0.035</td>
<td>poly2</td>
<td>0.348</td>
<td>16.1%</td>
</tr>
<tr>
<td>5</td>
<td>highpt</td>
<td>600</td>
<td>1250</td>
<td>0.000</td>
<td>0.015</td>
<td>singleExp</td>
<td>0.295</td>
<td>-3.6%</td>
</tr>
<tr>
<td>6</td>
<td>highpt</td>
<td>600</td>
<td>1250</td>
<td>0.015</td>
<td>0.025</td>
<td>singleExp</td>
<td>0.344</td>
<td>14.8%</td>
</tr>
<tr>
<td>7</td>
<td>highpt</td>
<td>600</td>
<td>1250</td>
<td>0.015</td>
<td>0.025</td>
<td>singleExp</td>
<td>0.344</td>
<td>14.8%</td>
</tr>
<tr>
<td>8</td>
<td>highpt</td>
<td>600</td>
<td>1250</td>
<td>0.015</td>
<td>0.025</td>
<td>singleExp</td>
<td>0.344</td>
<td>14.8%</td>
</tr>
<tr>
<td>9</td>
<td>hzbb</td>
<td>150</td>
<td>2000</td>
<td>0.00</td>
<td>10.000</td>
<td>singleExp</td>
<td>0.323</td>
<td>4.5%</td>
</tr>
<tr>
<td>10</td>
<td>highres</td>
<td>150</td>
<td>250</td>
<td>0.175</td>
<td>10.000</td>
<td>poly2</td>
<td>0.132</td>
<td>16.9%</td>
</tr>
<tr>
<td>11</td>
<td>highres</td>
<td>250</td>
<td>10000</td>
<td>0.05</td>
<td>10.000</td>
<td>singlePow</td>
<td>0.237</td>
<td>-19.1%</td>
</tr>
<tr>
<td>12</td>
<td>highres</td>
<td>250</td>
<td>600</td>
<td>0.000</td>
<td>0.05</td>
<td>singlePow</td>
<td>0.118</td>
<td>25.7%</td>
</tr>
<tr>
<td>13</td>
<td>highres</td>
<td>600</td>
<td>10000</td>
<td>0.000</td>
<td>0.05</td>
<td>singleExp</td>
<td>0.256</td>
<td>-3.4%</td>
</tr>
<tr>
<td>14</td>
<td>lowres</td>
<td>150</td>
<td>250</td>
<td>0.175</td>
<td>10.000</td>
<td>singleExp</td>
<td>0.365</td>
<td>7.9%</td>
</tr>
<tr>
<td>15</td>
<td>lowres</td>
<td>250</td>
<td>10000</td>
<td>0.05</td>
<td>10.000</td>
<td>singleExp</td>
<td>0.358</td>
<td>-13.9%</td>
</tr>
<tr>
<td>16</td>
<td>lowres</td>
<td>250</td>
<td>600</td>
<td>0.000</td>
<td>0.05</td>
<td>-</td>
<td>-</td>
<td>-%</td>
</tr>
<tr>
<td>17</td>
<td>lowres</td>
<td>600</td>
<td>10000</td>
<td>0.000</td>
<td>0.05</td>
<td>singleExp</td>
<td>0.364</td>
<td>-9.0%</td>
</tr>
</tbody>
</table>

Table 8.10: Summary of systematic uncertainties and their size.

<table>
<thead>
<tr>
<th>Uncertainty Source</th>
<th>Size</th>
</tr>
</thead>
<tbody>
<tr>
<td>Luminosity</td>
<td>5.7%</td>
</tr>
<tr>
<td>PDFs and QCD Scale Variations</td>
<td>15-30%</td>
</tr>
<tr>
<td>Trigger and selection efficiency</td>
<td>3%</td>
</tr>
<tr>
<td>Jet energy scale</td>
<td>1-5%</td>
</tr>
<tr>
<td>Photon Energy Scale</td>
<td>1%</td>
</tr>
<tr>
<td>B-tagging efficiency</td>
<td>4%</td>
</tr>
<tr>
<td>σ_{M}/M categorization</td>
<td>4%</td>
</tr>
</tbody>
</table>

8.8 Results and Interpretations

The fit results for all search regions using the combination of the 2015 dataset (2.3 fb^{-1}) and the 2016 dataset (12.9 fb^{-1}) are shown below. Figures 8.15, 8.16, and 8.17 show the results for the HighPt event category. The results for the H(γγ)-H/Z(bb) category are shown in Figure 8.18. Finally, the results for the HighRes and LowRes categories are shown in Figures 8.19 to 8.23.

The data yields, expected background yields, and best fit signal yields are summarized in Table 8.11 for all search region bins, together with the local statistical significance of the excess for each bin. The observed signal significance is summarized in Figure 8.24 for all statistically independent bins. The bin with the largest significance occurs in the HighPt category with M_{R} > 600 GeV and R^{2} > 0.025, and has a local significance of 2.5σ. Accounting for the number of search region
Figure 8.15: The diphoton mass distribution for various search region bins in the HighPt category are shown along with the background-only fit (left) and the signal plus background fit (right). The red curve represents the background prediction, the green curve represents the signal, and the blue curve represents the sum of the signal and background. The definition of the search bin is labeled above each pair of plots.

bins, this corresponds to a global significance of 1.4σ.

We interpret these results in terms of limits on the production cross-section times branching ratio for sbottom pair production with a cascade decay to a Higgs boson, a bottom quark, and the LSP. The expected and observed limits on the sbottom pair production cross section is shown in Figure 8.25 as a function of the sbottom mass and the LSP mass. The observed significance is also computed for this simplified
Figure 8.16: The diphoton mass distribution for various search region bins in the HighPt category are shown along with the background-only fit (left) and the signal plus background fit (right). The red curve represents the background prediction, the green curve represents the signal, and the blue curve represents the sum of the signal and background. The definition of the bin is labeled above each pair of plots.

8.9 Summary
A search for anomalous Higgs boson production through decays of supersymmetric particles is performed with data collected in 2015 and 2016 by the CMS experiment at the CERN LHC. Proton collisions collected at a center-of-mass energy $\sqrt{s} = 13$ TeV are considered, corresponding to an integrated luminosity of about
HighPt Category: $600 < M_R < 1250$ GeV, $0 < R^2 < 0.015$

![Graph](image1)

**Figure 8.17:** The diphoton mass distribution for various search region bins in the HighPt category are shown along with the background-only fit (left) and the signal plus background fit (right). The red curve represents the background prediction, the green curve represents the signal, and the blue curve represents the sum of the signal and background. The definition of the bin is labeled above each pair of plots.

H($\gamma\gamma$)-H/Z(bb) Category: $M_R > 150$ GeV

![Graph](image2)

**Figure 8.18:** The diphoton mass distribution for various search region bins in the H($\gamma\gamma$)-H/Z(bb) category are shown along with the background-only fit (left) and the signal plus background fit (right). The red curve represents the background prediction, the green curve represents the signal, and the blue curve represents the sum of the signal and background. The definition of the bin is labeled above each pair of plots.

15.2 fb$^{-1}$ (2.3 fb$^{-1}$ from 2015 and 12.9 fb$^{-1}$ from 2016). Higgs boson candidates are reconstructed from pairs of photons in the central part of the detector. The razor
variables $M_R$ and $R^2$ are used to suppress SM Higgs boson production and other SM processes. The non-resonant background is estimated through a data-driven fit to the diphoton mass distribution using a functional form model selected by a combination of the AIC score and the result of a series of bias tests. The standard model Higgs background is estimated using the Monte Carlo simulation, with systematics on instrumental and theoretical uncertainties propagated. We interpret the results in terms of production cross-section limits on sbottom pair production each decaying to a Higgs boson, a $b$-quark, and the LSP, and exclude sbottoms with mass below 350 GeV.
HighRes: $150 < M_R < 250$ GeV, $0 < R^2 > 0.175$

LowRes: $150 < M_R < 250$ GeV, $0 < R^2 > 0.175$

Figure 8.20: The diphoton mass distribution for the search region bin 10 are shown along with the background-only fit (left) and the signal plus background fit (right). The top row shows the HighRes category, while the bottom row shows the LowRes category. The red curve represents the background prediction, the green curve represents the signal, and the blue curve represents the sum of the signal and background. The definition of the bin is labeled above each pair of plots.
HighRes: $150 < M_R < 250$ GeV, $0 < R^2 > 0.175$

LowRes: $150 < M_R < 250$ GeV, $0 < R^2 > 0.175$

Figure 8.21: The diphoton mass distribution for the search region bin 11 are shown along with the background-only fit (left) and the signal plus background fit (right). The top row shows the HighRes category, while the bottom row shows the LowRes category. The red curve represents the background prediction, the green curve represents the signal, and the blue curve represents the sum of the signal and background. The definition of the bin is labeled above each pair of plots.
Figure 8.22: The diphoton mass distribution for the search region bin 12 are shown along with the background-only fit (left) and the signal plus background fit (right). The top row shows the HighRes category, while the bottom row shows the LowRes category. The red curve represents the background prediction, the green curve represents the signal, and the blue curve represents the sum of the signal and background. The definition of the bin is labeled above each pair of plots.
Figure 8.23: The diphoton mass distribution for the search region bin 13 are shown along with the background-only fit (left) and the signal plus background fit (right). The top row shows the HighRes category, while the bottom row shows the LowRes category. The red curve represents the background prediction, the green curve represents the signal, and the blue curve represents the sum of the signal and background. The definition of the bin is labeled above each pair of plots.
Table 8.11: The non-resonant background yields, SM Higgs background yields, best fit signal yields, and observed local significance are shown for the signal plus background fit in each search region bin. The uncertainties include both statistical and systematic components. The non-resonant background yields shown correspond to the yield within the window between 122 GeV and 129 GeV and is intended to better reflect the background under the signal peak. The observed significance for the bins in HighRes and LowRes categories are identical because they are the result of a simultaneous fit. The significance is computed using the profile likelihood, where the sign reflects whether an excess (positive sign) or deficit (negative sign) is observed.

<table>
<thead>
<tr>
<th>Bin</th>
<th>Category</th>
<th>Non-Resonant Bkg</th>
<th>Exp. SM Higgs</th>
<th>Fitted SM Higgs</th>
<th>Best Fit Signal</th>
<th>Obs. Local Significance</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>HighPt</td>
<td>10.2 ± 1.4</td>
<td>2.0 ± 0.4</td>
<td>2.0 ± 0.7</td>
<td>9.7 ± 5.1</td>
<td>2.8σ</td>
</tr>
<tr>
<td>1</td>
<td>HighPt</td>
<td>10.5 ± 1.3</td>
<td>1.4 ± 0.3</td>
<td>1.4 ± 0.3</td>
<td>0.5 ± 3.4</td>
<td>0.2σ</td>
</tr>
<tr>
<td>2</td>
<td>HighPt</td>
<td>10.5 ± 1.6</td>
<td>3.0 ± 0.6</td>
<td>2.9 ± 0.9</td>
<td>-5.2 ± 2.5</td>
<td>-1.4σ</td>
</tr>
<tr>
<td>3</td>
<td>HighPt</td>
<td>304 ± 16.6</td>
<td>27.7 ± 8.0</td>
<td>27.7 ± 11.2</td>
<td>-7.9 ± 18.1</td>
<td>-0.4σ</td>
</tr>
<tr>
<td>4</td>
<td>HighPt</td>
<td>60 ± 3.0</td>
<td>8.8 ± 2.5</td>
<td>8.8 ± 3.5</td>
<td>-13.9 ± 6.6</td>
<td>-1.6σ</td>
</tr>
<tr>
<td>5</td>
<td>HighPt</td>
<td>12.1 ± 1.4</td>
<td>1.7 ± 0.4</td>
<td>1.7 ± 0.6</td>
<td>8.3 ± 4.7</td>
<td>1.9σ</td>
</tr>
<tr>
<td>6</td>
<td>HighPt</td>
<td>47.6 ± 2.6</td>
<td>10.7 ± 2.7</td>
<td>10.7 ± 3.7</td>
<td>4.1 ± 7.3</td>
<td>0.6σ</td>
</tr>
<tr>
<td>7</td>
<td>HighPt</td>
<td>13.1 ± 1.4</td>
<td>2.7 ± 0.8</td>
<td>2.7 ± 1.0</td>
<td>3.2 ± 4.1</td>
<td>0.8σ</td>
</tr>
<tr>
<td>8</td>
<td>H(γγ)-HZ(bb)</td>
<td>21.6 ± 1.8</td>
<td>1.0 ± 0.2</td>
<td>1.0 ± 0.2</td>
<td>5.3 ± 4.6</td>
<td>1.0σ</td>
</tr>
<tr>
<td>9</td>
<td>HighRes</td>
<td>697 ± 10.6</td>
<td>33.5 ± 10.4</td>
<td>33.2 ± 12.1</td>
<td>0.0 ± 21.4</td>
<td>-0.2σ</td>
</tr>
<tr>
<td>10</td>
<td>HighRes</td>
<td>9.8 ± 1.2</td>
<td>0.6 ± 0.1</td>
<td>0.6 ± 0.1</td>
<td>8.2 ± 4.1</td>
<td>1.7σ</td>
</tr>
<tr>
<td>11</td>
<td>HighRes</td>
<td>40.7 ± 2.4</td>
<td>1.7 ± 0.4</td>
<td>1.7 ± 0.6</td>
<td>0.2 ± 5.5</td>
<td>0.0σ</td>
</tr>
<tr>
<td>12</td>
<td>HighRes</td>
<td>387 ± 14.6</td>
<td>21.5 ± 5.4</td>
<td>21.5 ± 9.1</td>
<td>8.1 ± 14.9</td>
<td>0.5σ</td>
</tr>
<tr>
<td>13</td>
<td>HighRes</td>
<td>46.8 ± 2.6</td>
<td>3.5 ± 1.0</td>
<td>3.5 ± 1.2</td>
<td>1.3 ± 6.0</td>
<td>0.2σ</td>
</tr>
<tr>
<td>9</td>
<td>LowRes</td>
<td>591 ± 9</td>
<td>11.6 ± 3.8</td>
<td>11.9 ± 5.1</td>
<td>0.2 ± 10.1</td>
<td>-0.2σ</td>
</tr>
<tr>
<td>10</td>
<td>LowRes</td>
<td>14.1 ± 1.4</td>
<td>0.2 ± 0.1</td>
<td>0.2 ± 0.1</td>
<td>1.1 ± 0.8</td>
<td>1.7σ</td>
</tr>
<tr>
<td>11</td>
<td>LowRes</td>
<td>36.6 ± 9.2</td>
<td>0.6 ± 0.3</td>
<td>0.6 ± 0.3</td>
<td>0.1 ± 1.8</td>
<td>0.0σ</td>
</tr>
<tr>
<td>12</td>
<td>LowRes</td>
<td>341 ± 7</td>
<td>7.9 ± 2.3</td>
<td>7.9 ± 3.5</td>
<td>2.8 ± 5.0</td>
<td>0.5σ</td>
</tr>
<tr>
<td>13</td>
<td>LowRes</td>
<td>44.3 ± 2.4</td>
<td>1.4 ± 0.4</td>
<td>1.4 ± 0.7</td>
<td>0.5 ± 2.6</td>
<td>0.2σ</td>
</tr>
</tbody>
</table>
Figure 8.24: The observed significance in units of standard deviations is plotted for each search bin. The significance is computed using the profile likelihood, where the sign reflects whether an excess (positive sign) or deficit (negative sign) is observed. The categories that the bins belong to are labeled at the bottom. The yellow and green bands represent the $1\sigma$ and $2\sigma$ regions, respectively.

Figure 8.25: The observed 95% confidence level (C.L.) upper limits on the production cross section for sbottom pair production decaying to a bottom quark, a Higgs boson, and the LSP are shown. The solid and dotted black contours represent the observed exclusion region and its $1\sigma$ bands, while the analogous blue contours represent the expected exclusion region and its $1\sigma$ bands.
Figure 8.26: The observed significance scan for sbottom pair production decaying to a bottom quark, a Higgs boson, and the LSP is shown.
Part IV

Precision Timing Calorimetry
Chapter 9

INTRODUCTION

Calorimeters are key detector systems in high energy physics experiments ranging from neutrino to particle collider detectors. In particular, electromagnetic (EM) calorimeters are designed to fully contain the energy deposited by electrons, positrons, and photons (e/γ); as well as to provide position information by means of their granular design. They are usually divided in two types: homogeneous and sampling, homogenous calorimeters are those in which their entire volume is composed of sensitive media, while sampling calorimeters are composed of alternating layers of sensitive and absorber media.

Homogenous EM calorimeters are usually made out of dense scintillating crystals (BGO, BaF$_2$, LYSO, PbWO$_4$, among others) or liquid noble gases (Ar, Kr, Xe) and they provide an outstanding energy resolution for e/γ. For example, the CMS EM calorimeter [59] is composed of PbWO$_4$ scintillating crystals coupled to avalanche photodiodes and with an energy resolution of

$$\frac{\sigma_E}{E} = \frac{2.8\% \sqrt{\text{GeV}}}{\sqrt{E}} \oplus \frac{12\% \text{GeV}}{E} \oplus 0.3\%.$$ \hspace{1cm} (9.1)

Sampling EM calorimeters use a sensitive medium such as scintillating crystals, liquid noble gases, and silicon, among others to measure the energy the incoming particle; while the absorber medium is a high density material such as lead or tungsten in order to require less volume to completely contain the impinging particle’s energy and thus result in a compact design. An example of such an EM calorimeter is the ATLAS lead-liquid argon (LAr) sampling calorimeter with an energy resolution of

$$\frac{\sigma_E}{E} = \frac{10.1\% \sqrt{\text{GeV}}}{\sqrt{E}} \oplus \frac{0.25\% \text{GeV}}{E} \oplus 0.17\%.$$ \hspace{1cm} (9.2)

Particle collider experiments at the LHC such as ATLAS and CMS use EM calorimeters in the e/γ four-momentum and jet energy measurements, particle identification algorithms, trigger systems, and the measurement of the missing transverse energy in each proton-proton collision. Therefore, maintaining the current performance of
the EM calorimeters is critical for the current and future physics measurements of those experiments.

In order to provide the necessary datasets to perform precision measurements of the Higgs couplings, probe rare Higgs processes, study the scattering of longitudinally polarized W bosons, and search for new physics, the LHC has to deliver a larger number of instantaneous proton-proton collisions. The high luminosity upgrade of the Large Hadron Collider (HL-LHC) at CERN [192] is expected to provide instantaneous luminosities of $5 \times 10^{34}$ cm$^{-2}$s$^{-1}$. This enhanced data rate will increase the simultaneous interactions per bunch crossing (pileup) from an average of 20-40 to 140-200.

The large amount of pileup foreseen for the HL-LHC will increase the likelihood of confusion in the reconstruction of events of interest, due to the contamination from particles produced in different pileup interactions. The ability to discriminate between jets produced in the events of interests – especially those associated with the vector boson fusion processes – and jets produced by pileup interactions will be degraded, the missing transverse energy resolution will deteriorate, and several other physics objects performance metrics will suffer.

One way to mitigate the detrimental pileup effects, complementary to precision tracking methods, is to perform a time of arrival measurement associated with a particular layer of the calorimeter, allowing for a time assignment for both charged particles and photons. Such a measurement with a precision of about 20 to 30 ps, when unambiguously associated to the corresponding energy measurement, will significantly reduce – approximately a factor of 10 – the inclusion of pileup particles in the reconstruction of the event of interest given that the spread in collision time of pileup interactions is about 200 ps. The association of the time measurement to the energy measurement is crucial, leading to a prototype design that requires the time and energy measurements to be performed in the same sensitive medium. It is in this context that this thesis presents various prototype calorimeters equipped with precision timing capabilities and studies the current limits on their time resolution.

This part of the thesis is organized as follows: section 9.1 provides a brief and general introduction to EM calorimeters, chapter 10 is dedicated to the timing properties of LYSO crystal scintillator based calorimeters, chapter 11 discusses the possibility of a precision timing sampling calorimeter where the sensitive medium is a microchannel plate (MCP), chapter 12 discusses the timing capabilities of a sampling calorimeter where the sensitive medium is a 350 microns silicon sensor.
Finally, chapter 13 presents timing measurements and results of a high-granularity calorimeter layer from the CMS experiment.

9.1 EM Calorimeter Preliminaries

Calorimeters are highly complex instruments and therefore some background is required to understand the subsequent sections in this chapter; this section is intended to provide a short overview of the most important effects – mostly different physical processes in different energy regimes – and the relevant considerations when designing a calorimeter.

EM Shower Development

High energy $e^{+}/\gamma$ (with energies above 1 GeV) will develop an EM shower upon entering the calorimeter. The processes involved in the EM shower development are few and well understood. Photons lose energy mostly by photoelectric effect, Compton scattering, or pair production of electrons and positrons. The later dominates at high energies and it is responsible for the shower development, while photoelectric effect overwhelmingly dominates at low energies (typically below 10 MeV), Figure 9.1 shows the photon cross section as a function of the incoming photon energy in lead. Electrons and positrons lose energy mainly due to two processes: ionization and radiation, hereafter referred to as bremsstrahlung; see Figure 9.2. The later dominates at high energies while the former dominates at low energies. The energy at which these two processes are equally relevant is defined as the critical energy ($E_c$), and Figure 9.3 shows a graphical representation of this definition.

Empirical functional forms for $E_c$ can be obtained when a distinction between gas and liquid or solid media is made, since there are significant difference in ionization that arise mainly due to the density effect. Figure 9.4 shows the experimental data for $E_c$ as a function of the atomic number (Z) along with the corresponding fits, and the functional forms for $E_c$ are

\[
E_{c_{gas}} = \frac{710 \text{ MeV}}{Z + 0.92}, \quad \text{and} \quad E_{c_{solid}} = \frac{610 \text{ MeV}}{Z + 1.24}.
\]  

(9.3)

EM showers are then produced when high energy photons (electron/positron) enters the calorimeter media and loses energy by pair production (bremsstrahlung), the subsequently $e^{+}/e^{-}$ pair (high energy photon produced by radiation) loses energy by bremsstrahlung (pair production). The number of particles produced by this multiplicative process increases until a maximum is reached (shower maximum) at the certain depth inside the calorimeter. After this point the newly created
particles have low energies and therefore other processes such as photoelectric effect, Compton scattering, and ionization start to become relevant. The shower profile in the longitudinal direction for a 30 GeV electron in iron is shown in Figure 9.5. The longitudinal shower profile is also a function of the incoming particle energy. Figure 9.5 shows this effect for electrons of different energies in copper.

Shower development is described independently of the calorimeter material by two quantities: the radiation length ($X_0$) and the Molière radius ($R_M$). The radiation length is the characteristic amount traversed by high energy e/γs in the longitudinal direction (along the original particle’s direction), it is usually measured in g cm$^{-2}$. The quantitative definition is (a) the mean distance over which an electron loses 1/e of its initial energy, and (b) 7/9 of the pair production mean free path for high energy photons. $X_0$ has been tabulated and calculated by Y. S Tsai [], the analytical expression is the following:

$$\frac{1}{X_0} = 4\alpha r_e^2 \frac{N_A}{A} \left[ Z^2 (L_{rad} - f(Z)) + ZL'_{rad} \right], \quad (9.4)$$
where \( \alpha \) is the fine structure constant, \( r_e \) is the classical electron radius, \( N_A \) is Avogadro’s number, \( A \) is the atomic mass, \( Z \) is the atomic number, \( L_{\text{rad}} \) and \( L'_{\text{rad}} \) are shown in Table 9.1, and \( f(Z) \) is an infinite sum, nonetheless for chemical elements up to uranium can be expressed to the 4-decimal place accuracy by

\[
f(Z) = (\alpha Z)^2 \left[ (1 + (\alpha Z)^2)^2 + 0.2020 - 0.0369(\alpha Z)^2 + 0.0083(\alpha Z)^4 - 0.0020(\alpha Z)^6 \right].
\] (9.5)

<table>
<thead>
<tr>
<th>Element</th>
<th>( Z )</th>
<th>( L_{\text{rad}} )</th>
<th>( L'_{\text{rad}} )</th>
</tr>
</thead>
<tbody>
<tr>
<td>H</td>
<td>1</td>
<td>5.31</td>
<td>6.144</td>
</tr>
<tr>
<td>He</td>
<td>2</td>
<td>4.79</td>
<td>5.621</td>
</tr>
<tr>
<td>Li</td>
<td>3</td>
<td>4.74</td>
<td>5.805</td>
</tr>
<tr>
<td>Be</td>
<td>4</td>
<td>4.71</td>
<td>5.924</td>
</tr>
<tr>
<td>Others</td>
<td>&gt; 4</td>
<td>( \ln(184.15Z^{-1/3}) )</td>
<td>( \ln(1194Z^{-2/3}) )</td>
</tr>
</tbody>
</table>

The Molière radius is the characteristic size of the shower in the transverse direction and is defined as the ratio of the radiation length and the critical energy:

\[
R_M = \frac{X_0}{E_c}.
\] (9.6)
Figure 9.3: Graphical definition of the critical energy ($E_c$). The intersection of the solid lines is the definition used in this thesis. The intersection between the solid (ionization) and dashed line is alternative definition [210, 255, 256].

The transverse spread of the shower is the result of high energy $e^\pm$ moving away from the shower axis due to multiple scattering, as well as the isotropic production of low energy electrons and photons. Multiple scattering dominates the lateral evolution in the early stages while isotropic production dominates at the later stages of the shower evolution, after the shower maximum. This two components exhibit a characteristic exponential decay (see Figure 9.7), where the transverse energy density for electron showers in copper is shown.
32.4.4. Critical energy: A n electron loses energy by bremsstrahlung at a rate nearly proportional to its energy, while the ionization loss rate varies only logarithmically with the electron energy. The critical energy \( E_c \) is sometimes defined as the energy at which the two loss rates are equal [50]. Among alternate definitions is that of Rossi [2], who defines the critical energy as the energy at which the ionization loss per radiation length is equal to the electron energy. Equivalently, it is the same as the first definition with the approximation \( |dE/dx|_{\text{brems}} \approx E/X_0 \). This has been found to describe transverse electromagnetic shower development more accurately (see below). These definitions are illustrated in the case of copper in Fig. 32.13.

The accuracy of approximate forms for \( E_c \) has been limited by the failure to distinguish between gases and solid or liquids, where there is a substantial difference in ionization at the relevant energy because of the density effect. We distinguish these two cases in Fig. 32.14. Fits were also made with functions of the form \( a/(Z+b) \), but \( b \) was found to be essentially unity. Since \( E_c \) also depends on \( A \), \( I \), and the factors, such forms are at best approximate.

Values of \( E_c \) for both electrons and positrons in more than 300 materials can be found at pdg.lbl.gov/AtomicNuclearProperties.

32.4.5. Energy loss by photons: Contributions to the photon cross section in light element (carbon) and a heavy element (lead) are shown in Fig. 32.15. At low energies it is seen that the photoelectric effect dominates, although Compton scattering, Rayleigh scattering, and photonuclear absorption also contribute. The photoelectric cross section is characterized by discontinuities (absorption edges) as thresholds for photoionization of various atomic levels are reached. Photon attenuation lengths for a variety of elements are shown in Fig. 32.16, and data for 30 eV < \( k < 100 \) GeV for all elements are available from the web pages given in the caption. Here \( k \) is the photon energy.
When a high-energy electron or photon is incident on a thick absorber, it initiates an electromagnetic cascade as pair production and bremsstrahlung generate more electrons and photons with lower energy. The longitudinal development is governed by the high-energy part of the cascade, and therefore scales as the radiation length in the material. Electron energies eventually fall below the critical energy, and then dissipate their energy by ionization and excitation rather than by the generation of more shower particles. In describing shower behavior, it is therefore convenient to introduce the scale variables

\[ t = \frac{x}{X_0}, y = \frac{E}{E_c}, \]

so that distance is measured in units of radiation length and energy in units of critical energy.

![Figure 9.5: Shower profile in the longitudinal direction for a 30 GeV electron in iron from an EGS4 simulation. The solid line histogram shows the fractional energy per radiation length, and the solid line curve is a fit to the distribution using a gamma function. The number of electrons (solid circles) and photons (hollowed squares) with energies larger than 1.5 MeV and crossing planes at \( X_0/2 \) intervals (scale on the right) is also shown. The number of photons has been scaled down to have the same area as the number of electrons distribution.](image-url)
Fig. 1: The energy domains in which photoelectric effect, Compton scattering and pair production are the most likely processes to occur, as a function of the $Z$ of the absorber material.

Fig. 2: The energy deposited as a function of depth for 1, 10, 100 and 100 GeV electron showers developing in a block of copper. In order to compare the shower profiles, the integrals of these curves have been normalized to the same value. The radial distributions of the energy deposited by 10 GeV electron showers in copper, at various depths. Results of EGS4 calculations.

The lateral development of em showers is governed by two types of processes:

1. Electrons and positrons move away from the shower axis because of multiple scattering.
2. Photons and electrons produced in isotropic processes (Compton scattering, photoelectric effect) move away from the shower axis.

The first process dominates in the early stages of the shower development, the second one beyond the shower maximum. Both processes have their own characteristic, exponential scale. The two components

Figure 9.6: Shower profile in the longitudinal direction for electrons in copper. The different curves and points represent different electron energies ranging from 1 GeV-1 TeV [255, 256].

*Figure 9.6: Shower profile in the longitudinal direction for electrons in copper. The different curves and points represent different electron energies ranging from 1 GeV-1 TeV [255, 256].*
The energy domains in which photoelectric effect, Compton scattering and pair production are the most likely processes to occur, as a function of the $Z$ of the absorber material.

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Results of EGS4 calculations.

The lateral development of em showers is governed by two types of processes:

1. Electrons and positrons move away from the shower axis because of multiple scattering.
2. Photons and electrons produced in isotropic processes (Compton scattering, photoelectric effect) move away from the shower axis.

The first process dominates in the early stages of the shower development, the second one beyond the shower maximum. Both processes have their own characteristic, exponential scale. The two components.

Figure 9.7: Energy deposited per unit length in the transverse direction for 10 GeV electrons in copper. The shower has been sampled in three different places: at $2X_0$ (red circles), $6X_0$ (black dots), and $15X_0$ (blue crosses) [210, 255, 256].
Chapter 10

LYSO-BASED CALORIMETERS

This chapter presents studies on measurements of the time of flight (TOF) using sampling calorimeters based on LYSO crystals.

10.1 Introduction

Due to its very high light yield (∼30K photons/MeV) [194], and radiation tolerance [217, 161, 193, 124], LYSO is the active element of one of the options considered for the upgrade of the Compact Muon Solenoid (CMS) detector for the HL-LHC [112].

In Figure 10.1 presents a simplified illustration of the major time scales associated to the timing measurement using a monolithic crystal calorimeter. Upon entering the crystal the photon or electron travels at the speed of light, interacts, and begins to shower, producing scintillation light in the crystal. The time between the entry of the photon into the crystal and the first interaction is denoted by $t_I$ and for high energy impinging particles it is the shower development time. The time associated with the conversion of the incident photon to scintillation light is denoted by $t_S$. The scintillation light travels from the point of interaction to the photodetector at the velocity $c/\hat{n}$, where $\hat{n}$ is the effective index of refraction of the crystal [249]. The time associated with the propagation of the scintillation light to the photodetector is denoted by $t_P$. Once the scintillation light reaches the photodetector, the photons are converted into an electrical signal. The time associated with this process is known as the photodetector signal transit time, $t_T$. Finally, data acquisition (DAQ) system has a characteristic time constant $t_D$. Each of these time intervals will fluctuate or jitter on an event-by-event basis, contributing to the time resolution. Previous studies [225], measured the time resolution at different absorber thickness for electron beams with energies varying from 12 to 32 GeV, and showed that the time of arrival of the front of an electromagnetic shower can be determined with a precision better than 20 ps. The electronic time resolution of the DAQ system was measured to be about 6 ps. Using the same techniques, the time resolution of the MCP-PMT photodetectors used in the studies presented in this paper have been measured to be between 11 ps and 14 ps, depending on the exact device.
To characterize the time resolution of an inorganic crystal scintillator calorimeter we study the contributions due to fluctuations in the shower development, scintillation process, and light propagation to the photodetector. We take advantage of the very large number of scintillation photons in a LYSO crystal which result in modest fluctuations associated with the creation and transit of each particular scintillation photon for a LYSO-based detector.

10.2 Experimental Setup

A schematic diagram of a typical TOF measurement setup is shown in Figure 10.2. All measurements involve a fast photodetector, typically a micro-channel-plate photo-multiplier-tube (MCP-PMT), which measures the reference timestamp ($t_0$), and a photodetector further downstream that detects the signal associated with the electromagnetic shower and provides a simultaneous energy and time ($t_1$) measurement.

In these studies, two types of MCP-PMT photodetectors are used, one produced by Hamamatsu (model R3809-52) [1], and one produced by Photek (model PMT240) [2]. A DRS4 waveform digitizer V4 evaluation board [223] was used as the primary DAQ system, connected to a laptop via USB interface. The DRS chip contains a switched capacitor array (SCA) with 1024 cells, capable of digitizing eight analog signals with high speed (5 GSPS) and high accuracy (11.5 bit SNR). All experimental beam studies were performed at the Fermilab Test Beam Facility (FTBF), which provided proton beams from the Fermilab Main Injector accelerator at 120 GeV, and secondary electron beams of energies ranging from 4 to 32 GeV. All detector elements were placed inside of a dark box lined with copper foil, providing RF shielding. A 2x2 mm$^2$ scintillator was placed inside the box at the upstream extrem-
Figure 10.2: The basic schematic diagram of the experimental setup for a typical TOF measurement is shown to illustrate the basic detector elements. One photodetector is used as a time reference and the second measures energy and time simultaneously.

ity and used to trigger the DAQ readout, providing a strict constraint on the location and directionality of the beam particles used in the TOF studies. A differential Cherenkov counter (not shown in the schematic) provided by the FTBF facility and located upstream of our experimental hall was used for electron identification.

10.3 Event Selection and Data Analysis
The primary target is to reconstruct the TOF of beam particles between different detector elements. Different time reconstruction algorithms are used for different detector elements, and all involve the assignment of a timestamp using specific features of each corresponding signal pulse. The signal pulse for the reference time detector is very sharp and symmetric around its maximum amplitude, as shown in Figure 10.3. Therefore for the reference detector we determine the time position of the pulse peak by fit a Gaussian function to the peak of the pulse, using three sampling points before the pulse maximum and four sampling points after. The fitted mean parameter of the Gaussian function is assigned as the timestamp $t_0$. The signal pulse for the downstream time measurement is the result of scintillation light, and exhibits a fast rising edge and a significantly slower decay. Therefore, we assign the timestamp $t_1$ using a constant fraction of the rising edge. A linear function is fit to the sampling points between 10% and 60% of the pulse maximum and the timestamp is assigned as the time at which the fitted linear function rises to 20% of the pulse maximum. Examples of fits performed to assign a time stamp from each pulse are shown in Figure 10.4. The impact from the choice of the functional
forms is studied by using a set of alternative functions in the fits, and choosing the
one that results in the best time resolution. Among the functions that we tested, the
difference between the best and worst performing functions was about 8 psec.

Figure 10.3: Sample pulses as digitized by the DRS4 board. On the left a pulse is shown
from the reference Hamamatsu R3809 MCP-PMT, and on the right is a pulse from the
Hamamatsu R3809 MCP-PMT optically coupled to a (1.7 cm)$^3$ LYSO crystal cube recorded
using 8 GeV electron beam.

Event selection and pulse cleaning procedures are used to eliminate abnormal pulses
in the readout, as described in [225]. Large signals above 500 mV are rejected
because they saturate the DRS4 inputs. Only pulses with amplitude larger than 20
mV are used for TOF measurements, in order to reduce the impact of noise from
the DRS waveform digitizer DAQ system. Events containing more than one pulse
within the 200 ns readout window are not used. Attenuators were used to extend
the dynamic range of the DRS4 waveform digitizer in cases when a large fraction
of signal pulses are saturated.

Figure 10.4: Sample fits used to assign timestamps to digitized MCP-PMT pulses. On
the left is a pulse from the reference Hamamatsu R3809 MCP-PMT, and on the right is a
pulse from the Hamamatsu R3809 MCP-PMT optically coupled to a (1.7 cm)$^3$ LYSO crystal
recorded during an 8 GeV electron run.
10.4 Timing in LYSO-based Calorimeters

The timing measurement in LYSO-based calorimeters is driven by three main factors – other than the intrinsic transit time of the photodetector itself and the DAQ electronics: a) the shower profile fluctuations, b) the scintillation time, and c) the light propagation time. Stochastic processes during the development of an electromagnetic shower affect the time of observed signals, as both the transverse size and the depth of the shower can fluctuate event-by-event. Random processes in the scintillation mechanism and the randomization of the optical paths for the scintillation light affect both the speed of the signal formation and the time jitter. We study these effects using two independent experimental setups.

For a homogeneous crystal calorimeter we are interested in the characterization and optimization of the light propagation time, i.e. the time the scintillation light travels down the length of the crystal. Our setup uses a small LYSO cube with linear dimensions of 17mm as the active scintillation element. The size of this element reduces the effect of the light propagation time and jitter. The LYSO cube is placed behind about 4.5 $X_0$ radiation lengths of lead. Using this LYSO-based sampling calorimeter, we measure the time resolution of electrons.

We also study a shashlik calorimeter composed of alternating layers of tungsten and LYSO, in which scintillation light is extracted through wavelength shifting (WLS) fibers. In this setup, the light propagation time through the fiber is the dominant factor of the timing measurement. We study as a baseline an alternate version of this calorimeter where the light is extracted through direct optical coupling of the photodetectors at the edges of a few LYSO layers to minimize the light propagation time.

**Timing Studies of the LYSO-based Sampling Calorimeter**

We study the combined impact of the shower profile fluctuations, the scintillation mechanism in LYSO, and the light propagation time resolution using a sampling calorimeter with a $(1.7 \text{ cm})^3$ LYSO cube as active element. The LYSO crystal is wrapped in Tyvek and attached to the Hamamatsu R3809 MCP-PMT (HAMB) with optical coupling [3]. A second Hamamatsu MCP-PMT photodetector (HAMA) is placed upstream of the calorimeter and is used to measure the reference time. A schematic diagram and a photograph of the experimental setup are shown in Figure 10.5.

To ensure that the electron beam is constrained to within a $2 \times 2 \text{ mm}^2$ region,
Figure 10.5: A schematic diagram of the experimental setup for the TOF measurement using the LYSO sampling calorimeter is shown on the left, along with a picture of the experimental setup shown on the right.

A plastic scintillator placed upstream and approximately 2 mm by 2 mm in cross sectional area is used to trigger the DAQ readout on the DRS digitizer. Electron events are identified by requiring a signal with amplitude larger than 10 mV in a Cherenkov counter located upstream. Large lead bricks are placed upstream of the Hamamatsu R3809 MCP-PMT (HAMB), out of the path of the beam. These shield the photodetector from stray particles produced in events where an electromagnetic shower occurs upstream of the lead radiator. Such stray shower particles yield very fast signals which can significantly contaminate the scintillation signal. Using the same experimental setup without the LYSO active element in place, we find that stray shower type events yield less than 10% contamination and give a negligible effect on the scintillation signal.

The thickness of the LYSO active element is relatively small and captures only a fraction of the total energy of the electron, but yields a reasonable energy measurement as it is close to the shower maximum.

The TOF measurement is performed using the LYSO sampling calorimeter for electron beams with energies varying from 4 GeV to 32 GeV. The corresponding measured TOF distributions are shown in Figure 10.6. We achieve the best time resolution of 34 ps for electrons with beam energy of 32 GeV.

The time resolution measurement is plotted as a function of the beam energy in Figure 10.15 (left). We fit the result to the sum of a $1/\sqrt{E}$ term and a constant term of about 11 ps. Given that we measure the contribution to the intrinsic time resolution...
Figure 10.6: TOF distributions for the LYSO cube sampling calorimeter for 4 GeV (top left), 8 GeV (top right), 16 GeV (bottom left), 32 GeV (bottom right) electron beam energy.

of the photodetector and the DAQ electronics to be about 20 ps [225], using the results from the 32 GeV electron beam, we infer that the combined contribution to the time resolution from the shower profile fluctuations, the scintillation mechanism, and the light propagation time inside the LYSO cube is about 27 ps.

### Timing Studies of the LYSO-Tungsten Shashlik Calorimeter

**Wavelength shifting fibers readout (WLS Y11 & DSB1)**

We study the time resolution of a LYSO-tungsten Shashlik calorimeter, one of the proposed choices for the Phase 2 upgrade of the CMS endcap calorimeter system [112]. We compare the time resolution performance for two alternative light propagation schemes.

In our setup the scintillation light is collected by WLS fibers that pass through a set of four holes in the LYSO and tungsten layers. In Figure 10.7, a shashlik cell and the light extraction scheme is illustrated. A schematic diagram and a photograph showing this experimental setup are shown in Figure 10.8. Two MCP-PMTs by Hamamatsu (R3809) are used to collect the scintillation light, while a Photek 240 MCP-PMT is used as a reference time detector.

We compare the signal pulses obtained using two different types of WLS fiber in the same LYSO-tungsten shashlik calorimeter. In Figure 10.9 (a) and (b) and we show the pulse shapes averaged over a few hundred events obtained using DSB1 fibers [36] and Y11 fibers, plotted in blue and red respectively. We find that the rise time of the pulse obtained using the DSB1 fibers, about 2.4 ns, is significantly faster than the rise time of the pulse obtained using the Y11 fibers, which is about 7.1 ns. To optimize the time resolution of this type of calorimeter the DSB1 fiber provides a better choice than Y11 if only this parameter is considered. The signal rise times we observe are comparable to the measured decay times of the corresponding WLS fibers [36].
Figure 10.7: The shashlik configuration based upon interleaved W and LYSO layers. Twenty-eight LYSO crystal plates and twenty-seven W plates comprise the module. Four WLS fibers are used to read out the scintillation light from the tiles.

Figure 10.8: A schematic diagram of the experimental setup for the TOF measurement using the LYSO-tungsten shashlik calorimeter with fiber signal extraction, along with a photograph of the experimental setup.

Using the shashlik calorimeter cell with DSB1 fibers, we measure the time resolution for electron beams with energy varying between 4 GeV and 32 GeV. In Figure 10.10 (b) we show the distribution of the pulse integral which is proportional to the total collected charge, for the 32 GeV beam, and observe an energy resolution of about 5%, while for the small LYSO cube shown in 10.10 (a) the energy resolution was
Figure 10.9: (a) Pulse shapes digitized by the DRS4 board and averaged over several hundred events obtained from the LYSO-tungsten shashlik calorimeter with light extracted using DSB1 (blue) and Y11 (red) WLS fibers. (b) DSB1(blue) shashlik average light pulse shape compared with the averaged pulse shape obtained from direct optical coupling of the photodetector to one edge of a LYSO tile in the shashlik calorimeter. (green)

about 20%. For this particular run in the Shashlik setup, no electron identification requirements could be made due to a misconfiguration of the upstream Cherenkov counter, so the background is visible.

TOF distributions, fitted to gaussian functions, are shown in Figure 10.11, and the $\sigma$ parameter of the gaussian fit is plotted as a function of the beam energy in Figure 10.16. We find that the dependence of the time resolution on beam energy follows a $1/\sqrt{E}$ functional form, indicating that the current calorimeter setup remains in the photostatistics limited regime. The best time resolution we obtain with this setup is 104 ps. As the measurements are photostatistics limited, the result can be improved in the future if the light collection efficiency is increased.

**Directly coupled MCP-PMTs to LYSO shashlik plates**

In this setup the MCP-PMT photodetectors are directly coupled to the edges of two adjacent LYSO layers in the shashlik calorimeter and scintillation light is directly transported to the photodetector through the edges of the tile layers. A schematic diagram and corresponding picture of the experimental setup are shown in Figure 10.12. In Figure 10.13, we show a zoomed-in photograph of the exposed LYSO plates from which the scintillation light signal is extracted.

With this setup we invoke an interplay between the light propagation jitter and the limited photostatistics. By placing the photodetectors in direct contact with the edges of two LYSO layers, we minimize the distance the scintillation light travels to reach the photodetectors, and reduce the impact of light propagation jitter on
Figure 10.10: (Left) Histogram of the pulse integral which is proportional to the total collected charge is shown for events recorded using the LYSO cube sampling calorimeter for a 32 GeV electron beam. (Right) Histogram of the pulse integral for events recorded using the LYSO-tungsten shashlik calorimeter using DSB1 fibers, for a 32 GeV electron beam. The background is included due to a misconfiguration of the Cherenkov counter.

Figure 10.11: TOF distributions for the LYSO-tungsten shashlik calorimeter using DSB1 fibers for electron beams with varying beam energies.

the time measurement resolution. However in this setup we have also reduced the available photostatistics, as we collect light from only a small fraction of the shashlik cell. In Figure 10.14, we show the TOF distributions for electron beams at various energies, fitted to gaussian functions. The width of the best-fit gaussian is plotted as a function of the beam energy in Figure 10.16. The best time resolution that we obtain is about 55 ps, and fitting the result to the sum of a $1/\sqrt{E}$ term and a constant term, we find a constant term of about 30 ps.

In summary, we find that removing the impact of the wavelength shifting mechanism and minimizing the impact of optical transit does indeed improve the time resolution, but at a cost in photostatistics. Results obtained in this experiment suggest that a LYSO-tungsten shashlik calorimeter with edge readout can likely achieve 30 ps resolution provided there is some improvement to the light collection efficiency.
10.5 Results Discussion and Summary

This section described studies characterizing the timing performance of LYSO-based calorimeters. Using a (1.7 cm)$^3$ LYSO crystal that samples the electromagnetic showers created by electrons of various energies ranging from 4 GeV to 32 GeV at about 4.5 $X_0$, we infer that the contribution to the time resolution from event-by-event fluctuations of the shower profile, the scintillation process, and the light propagation is less than 30 ps. Studies using different wavelength shifting fibers in a LYSO-tungsten shashlik calorimeter demonstrates that the choice of the fiber affects the timing performance. Besides the absorption and re-emission processes in the fibers, we found that another important factor influencing the timing performance
Figure 10.14: TOF distributions for the LYSO-tungsten shashlik calorimeter with signal extracted from the edges of two LYSO layers.

Figure 10.15:

Figure 10.16: Timing resolution measurement as a function of the electron beam energy for (left) the LYSO cube sampling calorimeter (middle) the LYSO-tungsten shashlik calorimeter read-out with DSB1 fibers (right) the LYSO-tungsten shashlik calorimeter read-out directly by optically coupling to the edges of two LYSO layers. In all cases we fit the data with a function of $1/\sqrt{E}$ and a constant term.

is the light extraction efficiency. Using DSB1 fibers, despite being photostatistics limited, we obtained a best time resolution of about 100 ps. A future development of such a detector will be focused on increasing the light collection efficiency. In a setup where the scintillation light from the LYSO-tungsten shashlik calorimeter is extracted via the edges of two LYSO layers, thereby removing completely the wavelength shifting mechanism and long light propagation distance, we achieve a best time resolution of 55 ps. The result indicates that such a calorimeter design can achieve the 30 ps time resolution benchmark obtained with the LYSO cube provided some improvement to the light collection efficiency.

In comparing results using different light extraction schemes, we find that at a given light yield the time resolution depends significantly on the light propagation
fluctuations. As the light yield increases the dependence on the light propagation fluctuations is reduced. The effect can be seen in the summary Figure 10.17 where we show the dependence of the time resolution on the average pulse height for the shashlik cell with light extracted through the DSB1 fibers and for the sampling calorimeter with the LYSO cube. For the same average pulse height of 500 mV, the LYSO cube time resolution is about half of the shashlik using the DSB1 fibers which have also twice the rise time. As the pulse height increases the time resolution improves. Extrapolating to the regime of very large light yield, we should be able to reach asymptotically the best resolution without limitations from the light propagation fluctuations.

![Figure 10.17: Comparison of time resolutions obtained with the (1.7 cm)³ LYSO cube (blue), and the LYSO-tungsten shashlik calorimeter with light extracted using DSB1 fibers (red). The x-axis in this figure displays the amplitude of the signal, corrected for the attenuation factors.](image)

In summary, using a LYSO-based calorimeter and different light propagation experimental setups we obtain about 30 ps resolution time measurement for the maximum light yield achieved. As a follow-up we will investigate the time resolution in the limit of very large light yield, and attempt to improve the light collection efficiency in these types of detectors.
In this chapter another precision timing calorimetric prototype using MCPs as the sensitive medium is studied.

11.1 Introduction

The use of MCPs as the sensitive element of a shower-maximum detector or a calorimeter has been studied in the past [123, 35]. These studies demonstrated the linearity in the multiplicity of secondary shower particles that have energies that the MCP can detect. Such detectors are also a promising option for achieving time measurement precision at the level of a few tens of picoseconds [225, 227, 228, 191]. Moreover, such devices are intrinsically radiation hard and thus would tolerate the harsh radiation environment at future hadron colliders, particularly when operated without the reliance on a photocathode. In reference [228], it has been demonstrated that the intrinsic fluctuations of electromagnetic showers induce jitter on the time measurement that is less than 10 ps, removing one important potential fundamental limitation. A further advantage of MCPs is their capability for highly segmented readout, allowing for the possibility of a highly granular calorimeter with sub-millimeter spatial resolution. Such high-granularity calorimeters have been studied in the context of detector concepts for the ILC [148] and the HL-LHC upgrade of the CMS experiment [72], indicating that such calorimeters have promising potential for substantial improvement in physics reach at the TeV scale. The results in this chapter complement past results [211, 225, 227, 228] with additional studies of the position and time resolution for a calorimeter prototype with highly granular readout.

The studies in this chapter use three different MCP-PMTs:

- Photek 240: the most performant of the three devices, which provides the best time resolution, and excellent uniformity across the detector. The main parameters of the Photek 240 were reported in Ref. [225]. The pore size is 10 µm and the distance from the photocathode to the first amplification stage is 5.3 mm. The Photek 240 has a 41 mm² circular sensitive area, and it was operated at -4.8 kV high voltage (HV). The gain at this voltage is about $10^6$. 
The non-uniformity of the time response of the signal is limited to below 3.9 ps across the full sensitive area.

- Photonis XP85011: the anode of this MCP is composed of 64 pads, arranged as an $8 \times 8$ matrix. The size of each pad is $6 \times 6 \text{ mm}^2$. The pore size is $25 \mu\text{m}$. The non-uniformity of the time response across the photocathode is 37 ps [225, 228]. The HV applied to the Photonis XP85011 was 2.4 kV, with a corresponding gain of $10^6$.

- Photonis XP85012: mostly identical to XP85011, also composed of 64 pixels arranged as an $8 \times 8$ matrix. Additionally it can be operated in a mode with a reverse voltage applied to photocathode, which enables us to effectively turn off any signals from the photocathode. When operated in this mode, the only signals are directly from secondary shower particles [227].

This chapter reports on the studies of the high-granularity shower-maximum detector prototype that uses the Photonis XP85011 MCP as the active element. As demonstrated in reference [225], due to the fact that the input window is very thin, the signal in this device is dominated by direct detection of secondary shower particles, while Cherenkov photon signals contribute only 30% of the amplitude. The MCP is used to sample the electromagnetic shower induced by a beam of electrons impinging into a tungsten absorber layer that has a thickness of about 4 radiation lengths ($X_0$). The MCP-PMT is read out with a pixelated anode, with square pixels of size $6 \times 6 \text{ mm}^2$. The energy of the electromagnetic showers is reconstructed using the total collected charge and the positions are reconstructed using a simple energy-weighting algorithm, described in Section 11.4. Through the use of a high-precision motorized stage, a position scan is performed during beam-tests and the position resolution of the shower-maximum detector is obtained. Finally, the precision of measuring the arrival time of electromagnetic showers with such high-granularity shower-maximum detector is investigated.

This chapter is organized as follows. Section 11.2 gives a description of the experimental setup, Section 11.3 presents the event selection and pulse reconstruction, Section 11.4 and 11.5 present the results on position measurements and timing resolutions, respectively.
11.2 Experimental Setup

The experiment was performed at the MTEST location of the FTBF using an 8 GeV beam primarily comprised of electrons. A differential Cherenkov counter, located further upstream of the MTEST location, was used to enhance the purity of electrons and to suppress pions, by requiring a signal consistent with the passage of electrons through the device. All other detectors were placed inside a dark box lined with copper foil for electromagnetic shielding. A photograph of the experimental setup within the dark box is shown in Figure 11.1. A scintillator of size 1.7 mm× 2.0 mm optically coupled to two photomultiplier tubes, one on each side, was used to trigger the data acquisition and to constrain the trajectory of the electrons. Downstream from the trigger, a tungsten absorber with a thickness of about 1 cm, equivalent to about 4 $X_0$, was placed. The Photonis XP85011 MCP-PMT with pixelated readout was set on a high precision motorized stage and placed behind the tungsten absorber. The precision of the motorized stage is about 0.1 mm. To avoid unintended early showers due to interactions with the material of the casing and reference MCP-PMT device, the Photek 240 MCP-PMT was placed behind the Photonis XP85011 MCP-PMT. An external view of the Photonis XP85011 MCP-PMT is shown on the left of Figure 11.2, and a schematic diagram is shown on the right. There are a total of 64 pixels arranged in an 8 × 8 square matrix that can be read out individually. Only the nine pixels shown within the red square are used (see Figure 11.2). During the
course of the experiment it was found that the pixel labelled 44 in Figure 11.2 did not function properly and was therefore not used in the analysis of the data. Four DRS4 high speed waveform digitizers were used to acquire the signals from the Photek 240 MCP-PMT, the Cherenkov counter, and the eight operational channels from the Photonis XP85011 MCP-PMT. In order to allow a synchronized readout of four separate DRS4 units we split the signals from the Photek 240 MCP-PMT into four, and connected them to each of the four DRS4 units, thus achieving a “calibration” between the four different units.

11.3 Event Selection and Pulse Reconstruction

Reconstruction of the signal pulses and timestamps is performed using the identical methods described in Chapter 10 and other studies [211, 225, 227]. Figure 11.3 shows example pulses from one pixel channel of the Photonis XP85011 MCP-PMT and the Photek 240 MCP-PMT digitized by the DRS4.

The time resolution is measured as the standard deviation of the Gaussian fit to the TOF distribution $t_0 - t_1$, where $t_0$ is the time recorded at the “start” detector, and $t_1$ is that of the “stop” detector. To assign a time stamp for each signal pulse, we
first determine the time position of the pulse peak. A Gaussian function is fitted to the pulse maximum using three points before the maximum of the pulse peak and four points after the maximum. The mean value of the Gaussian was used as the time stamp for each pulse. A Photek 240 MCP-PMT, whose time resolution was previously measured to be less than 10 ps [227] was used as a “start” signal, while pulses from individual pixels on the Photonis XP85011 MCP-PMT were used as “stop” signals. The integrated charge for each pulse is used as a proxy for the measured energy deposit in each channel, and is computed using four time samples before and after the peak of the pulse. Each time sample is approximately 0.2 ns in time. Events containing pulses above 500 mV in amplitude are rejected as they saturate the DRS4. Only pulses with amplitude larger than 20 mV are used for time measurements, to reduce the impact of the electronics noise in the DRS4. Other event selection and pulse cleaning procedures are used to eliminate abnormal pulses in the readout, as described in [225].

![Figure 11.3](image.png)

**Figure 11.3:** Example of a digitized signal from a single Photonis pixel (left) and Photek (right) MCP-PMT following a high-energy electron shower, via DRS4.

### 11.4 Electromagnetic Shower Position Reconstruction and Resolution

The transverse shape of electromagnetic showers is very well known and has a characteristic width given by the Moliere radius, see Section 9.1. For tungsten, the Moliere radius is about 9 mm and therefore the shower is expected to be contained within two of the pixels in the Photonis XP85011 MCP-PMT. In Figure 11.4 shows the mean charge measured in each of the pixels for one example run where the Photonis MCP-PMT was held in a fixed location approximately centered on the beam. The electron beam has a width of about 1 cm.

Each electron impacting the shower-maximum detector will induce an electromag-
Figure 11.4: The mean charge measured for each pixel for one example run is shown. During this run, the Photonis MCP-PMT was held in the same location. Based on the distribution of the mean charge among the pixels, we can infer that the beam center is located in the upper half of the center pixel. Pixel 44 is not shown as it was found to be not operational.

Figure 11.5 shows the distributions of the reconstructed shower positions for three example runs in which the beam was located near the top, center, and bottom of the central pixel. The distributions of the reconstructed $y$ coordinate for the three corresponding runs are shown together in Figure 11.6. The measured beam-spot is observed to move consistent with the known movement of the motorized stage. In each run, the center of the beam-spot is determined by fitting the measured $x$ and $y$ coordinates with a Gaussian function. The data from all runs are combined by considering the measured $x$ and $y$ coordinates relative to the center of the beam-spot (see Fig 11.7). We model...
Electromagnetic Shower Time Resolution

The timestamps of the individual pixels of the Photonis MCP-PMT for each event are reconstructed as described in Section 11.3. The timestamp of the entire electromagnetic shower \( t \) is estimated using the same energy weighting procedure that was used above for the shower position reconstruction, i.e.

\[
    t = \frac{\sum_{i \in \text{pixels}} Q_i t_i}{\sum_{i \in \text{pixels}} Q_i},
\]

(11.2)
where $i$ labels the individual pixels, $Q_i$ is the charge collected in pixel $i$, and $t_i$ is the reconstructed time-stamp for pixel $i$. Alternatively, the time resolution using the single pixel with the highest energy deposit measurement is used. Figure 11.8 shows the time distributions for these two methods of shower time reconstruction.

Figure 11.9 shows the time resolution for electromagnetic showers measured using the two methods described above. The time resolution for the pixel with the largest energy deposit is around 70 ps and 85 ps, depending on the run. Using the energy weighted algorithm improves the time resolution consistently to about 50 ps. The time measurement obtained using the Photonis MCP-PMT typically exhibit a dependence on the pulse amplitude or integrated charge. This dependence is shown on the left of Figure 11.10, and is observed to be approximately the same for all pixels. We perform a correction to the time measurement based on the measured integrated charge, and we verify that the correction does flatten the dependence of the time measurement on the integrated charge as shown on the right panel of Figure 11.10. After performing this time measurement correction, the time resolution measurements improve to about 35 ps and is shown in Figure 11.11. We performed two sets of correction procedures. In one set, labelled as “Self-Calibrated”, an independent
correction is derived for each run and for each pixel. In the second set, labelled as “Calibrated”, a single correction is obtained for each pixel from a single run, and this correction is applied to all other runs. Figure 11.11 shows that this single correction is applicable to all other runs without loss of the precision of the measurements.

Finally, the dependence of the electromagnetic shower time resolution on of the number of pixels included in the energy-weighted algorithm is studied. Figure 11.12 shows this dependence for one example run. It is observed that the time resolution improves according to a $1/\sqrt{N}$ scaling up to about 5–6 pixels, and then becomes flat as more pixels are included. The initial $1/\sqrt{N}$ scaling is encouraging as it indicates that the time jitter across different pixel channels arise primarily from uncorrelated sources, and that further granularity may improve the time resolution provided that the signal is sufficiently large compared to noise. As the majority of the shower is covered by the pixels closest to the center of the shower – usually 5-6 pixels – it is not surprising that the time resolution does not further improve by adding the remainder of pixels.

11.6 Summary

Studies towards the development of future electromagnetic calorimeters capable of high precision energy and time measurements have been carried out. Such calorimeters should ultimately provide both spatial resolution below the mm level and time resolution of 20 – 30 ps, in order to mitigate the detrimental effects of pileup. A highly granular readout is required to achieve these goals.
This chapter reports the results on position and time resolution measurements of a secondary emission based calorimeter prototype that used the Photonis XP85011 MCP-PMT as the sensitive element. Using a pixelated readout of the MCP-PMT a highly granular information of the shower development in the transverse plane is obtained. Combining the measurements from a $3 \times 3$-pixel readout a sub-millimeter position resolution is measured, which far exceeds the 6 mm size of the individual pixels. While the more granular readout degrades the signal to noise for each individual pixel, the proper combination from independent pixels preserves a good time resolution. The measured time resolution improves with the increase in the number of pixels used as $1/\sqrt{N}$, and when using all pixels, the time resolution is
Figure 11.9: Time resolution found for each run. The time-stamp obtained using the energy weighting method yields time resolutions consistently below 60 ps. The time resolution measured using the single pixel with the largest signal is significantly worse.

30 – 40 ps. Future measurements could include larger prototypes with several layers of sensitive material that will allow the study of the longitudinal development of the showers.
Figure 11.10: The correlation between the time measurement and the measured integrated charge is shown on the left for one example pixel. The same correlation after performing the time measurement correction is shown on the right.

Figure 11.11: The time resolution of the electromagnetic shower for various runs is shown after performing the time measurement correction based on the measured integrated charge.
Figure 11.12: The time resolution is plotted as a function of the number of pixels included in the energy-weighted algorithm for one example run.

\[ \chi^2/2: 1.02 \]
\[ \frac{(61.4 \pm 3.2)}{\sqrt{N}} + (15.4 \pm 1.6) \]


Chapter 12

SILICON-BASED SAMPLING CALORIMETERS

12.1 Introduction

Several alternative options to combine high resolution energy and timing measurements for calorimetry have been reported in Refs. [228, 226, 191, 257, 245] as well as those described in Chapters 10 and 11. This chapter describes the continuation of this program by using a calorimeter prototype employing a 300 \( \mu \mathrm{m} \) thick silicon pad sensor of \( 6 \times 6 \, \text{mm}^2 \) size as the sensitive element. Silicon-based calorimeters have recently become a viable choice for future colliders due to the radiation hardness of silicon, and the ability to construct highly granular detectors [28]. An important example is the forward calorimeter proposed for the CMS Phase 2 Upgrade [72]. We study the timing properties of silicon-based calorimeter using a prototype composed of tungsten absorber and a silicon sensor produced by Hamamatsu [4].

This chapter is organized as follows. General silicon timing properties and bench test results are described in Section 12.2. The test beam setup and experimental apparatus are presented in Section 13.3. The results of the test beam measurements are presented in Section B.7. Finally, Sections 12.5 and 12.6 are devoted to discussion and conclusion, respectively.

12.2 General Properties of Silicon Timing and Bench Test Studies

All measurements presented in this chapter were carried out using a silicon sensor produced by Hamamatsu [4]. The thickness of the silicon sensor was measured to be \( 325 \, \mu \mathrm{m} \), while its transverse size is \( 6 \times 6 \, \text{mm}^2 \). The negative bias voltage was applied to the p-side of the silicon. The capacitance of the silicon diode is measured as a function of the bias voltage and shown in Figure 12.1. The silicon is fully depleted above about 120 V.

The electric diagram of the silicon diode connections is presented in left panel of Figure 12.2. Attention was paid to provide good filtering for the bias voltage, to reduce ground loop effects, and to minimize inductive loop for the signal readout. The timing characteristics of the signal pulses are therefore dominated primarily by properties of the silicon sensor rather than the details of the circuit. The silicon diode was placed inside a light-tight box (silicon box) of thickness 1.5 cm, which
Depletion Voltage: \(~120\) V
Capacitance at \(V_{dep}\): \(1.7E-11\) F

Figure 12.1: The measured capacitance as a function of the applied bias voltage.

also provides electromagnetic shielding. The box is made of 0.2 mm steel. The bias voltage was supplied to the circuitry by a cable with a balun filter, terminated with an SHV connector. The silicon diode output signal was read out through an SMA connector electrically grounded to the box. The dark current was measured at several values of the bias voltage. The maximum value of the dark current was less than \(1.0\) nA at \(-500\) V, which is the largest bias voltage used in the measurements reported. The silicon box is presented in the right panel of Figure 12.2. Signals from the silicon sensor were amplified by two fast, high-bandwidth pre-amplifiers connected in series. The first amplifier is an ORTEC VT120C pre-amplifier, and the second is a Hamamatsu C5594 amplifier. The combined gain of the two amplifiers in series as a function of the input signal amplitude was measured using a pulse-
12.3 Test-beam Setup and Experimental Apparatus

Test-beam measurements were carried out at the FTBF which provided a 120 GeV proton beam from the Fermilab Main Injector accelerator, and secondary beams composed of electrons, pions, and muons of energies ranging from 4 GeV to 32 GeV. A simple schematic diagram of the experimental setup is shown in Figure 12.3. A small plastic scintillator of transverse dimensions 1.7 mm × 2 mm is used as a trigger counter to initiate the read out of the DAQ system and to select incident beam particles from a small geometric area, allowing us to center the beam particles on the silicon sensor. Next, we place a stack of tungsten absorbers of various thicknesses for measurements of the longitudinal profile of the electromagnetic shower. The silicon pad sensor is located within a metal box covered by copper foil, and is placed immediately downstream of the absorber plates. Finally, a Photek 240 MCP-PMT detector [211, 225, 228, 226] is placed furthest downstream, and serves to provide a very precise reference timestamp. Its precision was previously measured to be less than 10 ps [228]. A photograph showing the various detector components is presented in Figure 12.4. A differential Cherenkov counter is located further upstream of our experimental setup and provides additional particle identification capability. More details of the experimental setup are described in our previous studies using the same experimental facility in references [211, 225, 228, 226] as well as in Chapters 10 and 11.

The DAQ system is based on a CAEN V1742 digitizer board [5], which provides digitized waveforms sampled at 5 GS/s. The metal box containing the silicon sensor was located on a motorized X-Y moving stage allowing us to change the location of the sensor in the plane transverse to the beam at an accuracy better than 0.1 mm. A nominal bias voltage of 500 V was applied to deplete the silicon sensor in most of the studies shown below, unless noted otherwise.

12.4 Test Beam Measurements and Results

Measurements were performed in 2015, using the primary 120 GeV proton beam, and secondary electron beam provided for the FTBF. Secondary beams with energies ranging from 4 GeV to 32 GeV were used. Electron purity for those beams ranges between 70% at the lowest energy to about 10% at the highest energy. Stacks of tungsten plates with varying thicknesses were placed immediately upstream of the
Figure 12.3: A schematic diagram of the test-beam setup is shown. The \( t_0 \) and \( t_1 \) are defined in Section B.7.

Figure 12.4: Test beam setup.

silicon device in order to measure the response along the longitudinal direction of the electromagnetic shower. The radiation length of tungsten is 3.5 mm, and the Moliere radius is 9.3 mm. The tungsten plate dimensions are sufficient to fully contain the shower in the transverse dimension. Signals from the silicon sensor and the Photek 240 MCP-PMT are read out and digitized by the CAEN V1742 digitizer,
and example signal waveforms are shown in Figure 12.5. The signal pulse in the silicon sensor has a rise time of about 1.5 ns, and a full pulse width of around 7 ns. This rise time is consistent with a time constant of a silicon sensor coupled to a 50 Ohm amplifier.

![Figure 12.5: Examples of the signal pulse waveform for the silicon sensor (left) and the Photek MCP-PMT (right) digitized by CAEN V1742 digitizer board. The bias voltage applied to the silicon pad sensor is 500 V.](image)

The CAEN digitizer is voltage and time calibrated using the procedure described in Ref. [185]. The total collected charge for each signal pulse is computed by integrating a 10 ns window around the peak of the pulse. The time for the reference Photek MCP-PMT detector is obtained by fitting the peak region of the pulse to a Gaussian function and the mean parameter of the Gaussian is assigned as the timestamp \( t_0 \). The time for signals from the silicon sensor is obtained by performing a linear fit to the rising edge of the pulse and the time at which the pulse reaches 30% of the maximum amplitude is assigned as its timestamp \( t_1 \). The electronic time resolution of the CAEN V1742 digitizer was measured to be \( \sim 4 \) ps and neglected on the timing measurements described below.

Electrons were identified by requiring that the signal amplitude of the gas Cherenkov counter provided by the FTBF and the Photek 240 MCP-PMT detector located further downstream of the silicon sensor exceed certain thresholds because electromagnetic showers induced by electrons produce significantly larger signals, while pions produce much smaller signals. After imposing the electron identification requirements the electron purity is between 80% and 90% for all beam conditions. The purity was determined by comparing the calorimetric measurements with those from the Cherenkov detector.

Let’s begin by establishing the signal characteristics of a minimum-ionizing particle (MIP) using beams of 120 GeV protons and 8 GeV electrons with no absorbers
upstream of the silicon pad sensor. To separate MIP signals from noise, separate data events with no beam and a random trigger are recorded. The charge distribution for these noise runs is presented in Figure 12.6. As expected, the charge distribution is centered at 0, and the RMS is about 2 fC. Figure 12.7 shows the silicon sensor response to 120 GeV protons and 8 GeV electrons without any absorber. We observe a very similar response for these two cases, and measure a mean integrated charge of 4.5 fC and 5.0 fC for proton and electrons, respectively. The measured signals are corrected for the gain of the amplifiers used, and hence is the output charge of the silicon sensor. We expect peak charge of 28,000 and 31,000 electron-hole pairs in a 325 µm thick silicon detector for ionizing particles with Lorentz factor \( \gamma = 120 \) (protons) and 16,000 (electrons) [207], which is in a good agreement with the measured values. Having established the absolute scale of the response using single particles, the remaining studies normalize all charge measurements to the 120 GeV proton signal, which hereafter is referred to as \( Q_{MIP} \). The response of the silicon sensor to electron beams of various energies after 6 radiation lengths (\( X_0 \)) of tungsten absorber is presented. The silicon sensor is expected to be sensitive to the number of secondary electrons produced within the electromagnetic shower, and therefore its response is expected to scale up with higher incident electron energies. Figure 12.8 shows an example of the integrated charge distribution measured in the silicon sensor after 6 radiation lengths of tungsten, for runs with 32 GeV electrons. The mean and RMS of these distributions as a function of incident electron beam energy are shown in Figure 12.8. The plotted uncertainties represent the RMS of the charge distribution. Since the electron beam profile and purity varies at different

![Figure 12.6: The distribution of charge integrated in the silicon sensor is shown for data events with no beam and random trigger.](image)
Figure 12.7: The distribution of charge integrated in the silicon sensor is shown for a beam of 120 GeV protons (left) and 8 GeV electrons (right) without any absorber upstream of the silicon sensor. These conditions mimic the response of the silicon sensor to a minimum-ionizing particle. All triggered events were used in these distributions.

beam energies, we collected between 10 and 50 thousand events for each beam energy, in order to ensure sufficiently large data samples. A fairly linear dependence between the measured charge and the incident beam energy is observed, see the right panel of Figure 12.8. The measured time resolution between the silicon sensor

Figure 12.8: Left: An example of the distribution of integrated charge in the silicon sensor for 32 GeV electrons and 6 $X_0$ absorber shown in units of $Q_{\text{MIP}}$. Right: The integrated charge in the silicon sensor expressed in units of $Q_{\text{MIP}}$ is shown for the same 6 $X_0$ absorber as a function of the electron beam energy. The uncertainty bands show the RMS of the measured charge distribution. The red line is the best fit to a linear function..
and the Photek MCP-PMT was obtained by measuring the standard deviation of the Gaussian fit to the TOF distribution, i.e. $\Delta t = t_0 - t_1$. The later exhibits a systematic dependence on the total charge measured in the silicon detector, as shown on the left panel in Figure 12.9. This dependence on the integrated charge of the amplified signal was reproduced when the output of the pulse-generator was connected to the same amplifiers as used in the measurements. Therefore a correction to $\Delta t$ for each event using the measured charge in the silicon sensor was applied. This procedure is referred to in the following as time correction. The correction is obtained by fitting a second degree polynomial to the profiled distribution of the $\Delta t$ versus total charge collected in the silicon sensor, as shown in Figure 12.9. The cross-check that the time correction flattens the dependence of the time measurement on the integrated charge is shown on the right panel of Figure 12.9. The time correction improves the time resolution measurement by $30\% - 35\%$. All time resolution measurements in the rest of this study are performed after such a time correction. An example of a corrected $\Delta t$ distribution for 32 GeV electrons after 6 $X_0$ is shown on the left panel of Figure 12.10. Other than the electron identification requirements, no additional selection requirements on the amplitude of the signal in the silicon sensor were made. The dependence of the measured time resolution on the beam energy is shown on the right panel of Figure 12.10. The time resolution improves as the beam energy increases, with a time resolution of 23 ps for the 32 GeV electron beam. Furthermore, the response and time resolution of the silicon sensor along the longitudinal direction of the shower development is studied. The integrated charge and the time resolution as a function of the absorber thickness is shown in Figure 12.11, for an 8 GeV electron beam. A typical longitudinal shower profile is observed, consistent with previous studies performed using a secondary emission calorimeter prototype based on MCP’s [228], as well as independent studies of silicon-based calorimeter prototypes [203]. The RMS of the integrated charge distribution at each absorber thickness is relatively large, due to the small transverse size of the active element used in the experiment. It is of note that the time resolution improves as the shower develops towards its maximum in the longitudinal direction. Finally, the dependence of the time resolution as a function of the bias voltage applied to deplete the silicon sensor is also studied. The measurements are shown in Figure 12.12 for 16 GeV electrons after 6 $X_0$ of tungsten absorber. As presented in Figure 12.12, the time resolution improves as the bias voltage is increased, which is expected on the basis of increased velocity of electrons and holes in silicon at larger bias voltage.
Figure 12.9: The dependence of $\Delta t$ on the integrated charge in the silicon sensor is shown on the left. The red curve represents the fit to the profile plot of the two dimensional distribution, and is used to correct $\Delta t$ for this effect. On the right, we show the corresponding two dimensional distribution after performing the correction. A 16 GeV electron beam is used, and the silicon sensor is placed after $6X_0$ of tungsten absorber.

### 12.5 Discussion

From Figures 12.6 and 12.7, it is observed that the noise of the prototype calorimetric system is sufficiently low to extract signals from MIPs. Comparing the RMS of the noise distribution with the mean of the MIP signal, a signal-to-noise ratio around 2 to 2.5 is extracted. A rough estimate from Figure 12.7 demonstrates that the efficiency to detect 120 GeV protons and 8 GeV electrons with no absorber present is larger than 80%. The signal distributions for electromagnetic showers are normalized to the MIP response, and a linear response as a function of the beam energy is observed, as shown in Figure 12.10. The measured longitudinal shower profile in, shown in Figure 12.11, is consistent with similar past measurements.

The TOF associated with the detection of electromagnetic showers induced by electrons with energy between 20 GeV and 30 GeV can be measured with a precision better than 25 ps. Results of the measurements reported in Ref. [34] showed that a time resolution below 50 ps could be achieved for signals larger than 10 equivalent MIPs. To achieve this. Taking into account the 13 ps time resolution of the reference Photek MCP-PMT detector measured to electromagnetic showers [228] yields a precision close to 20 ps. Moreover, the time resolution improves with larger electron beam energy, and more generally with larger signal amplitudes. These measurements demonstrate that a calorimeter based on silicon sensors as the
Figure 12.10: Left: The distribution of $\Delta t$ between the silicon sensor and the Photek MCP-PMT. A 32 GeV electron beam is used, and the silicon sensor is placed after $6 X_0$ of tungsten absorber. Right: The measured time resolution between the silicon sensor and the Photek MCP-PMT reference is shown as a function of the electron beam energy. The silicon sensor is placed after $6 X_0$ of tungsten absorber.

Figure 12.11: On the left, the integrated charge in the silicon sensor expressed in units of $Q_{\text{MIP}}$ is shown as a function of the absorber (W) thickness measured in units of radiation lengths ($X_0$). The electron beam energy was 8 GeV. The uncertainty bands show the RMS of the measured charge distribution. On the right, the time resolution between the silicon sensor and the Photek MCP-PMT reference is shown as a function of the absorber thickness.

A sensitive medium can achieve intrinsic time resolution at the 20 ps level, as long as noise is kept under control. Time jitter arising from intrinsic properties of the silicon sensor is demonstrated to be well below the 20 ps level.
Figure 12.12: The time resolution between the silicon sensor and the Photek MCP-PMT reference is shown as a function of bias voltage applied on the silicon sensor. The electron beam energy was 16 GeV, and the silicon sensor is placed after 6 $X_0$ of tungsten absorber.

12.6 Conclusion

The best time resolution of 23 ps for a silicon sensor was achieved with a 32 GeV beam and with the silicon sensor placed after 6 radiation lengths of tungsten absorber. Based on the calibration data for the response of the silicon sensor to MIPs, this measurement corresponds roughly to an average of 54 secondary particles registered from the electromagnetic shower. This results provide a solid ground and further encouragement to use silicon as the sensitive medium in sampling calorimeters, as is planned for example for the CMS Phase 2 upgrade [72], and explicitly demonstrates the opportunity to use silicon for timing measurements in future calorimeters. Further measurements include more realistic prototypes covering larger transverse and longitudinal regions of the electromagnetic shower and increasing the transverse granularity.
CMS HIGH-GRANULARITY CALORIMETER TIMING LAYER

13.1 Introduction

Recent advances in silicon sensors in terms of radiation tolerance, highly granular designs [28], and cost per unit area offers the possibility of their use as the sensitive media in a sampling calorimeter at the HL-LHC. An important example of such a device is the forward calorimeter proposed for the CMS Phase 2 Upgrade [72], where high-granularity silicon sensors and tungsten/copper absorber layers are interleaved. As described in Chapter 12, silicon-based shower maximum detectors have extremely good precision timing capabilities – achieving a TOF resolution of 25 ps for 32 GeV electron induced shower – which could be use to reduce the detrimental effects of the high pileup environment foreseen for the HL-LHC. This chapter presents recent studies on the intrinsic timing properties of the silicon sensors to be used by the proposed CMS high-granularity calorimeter (HGC).

This chapter is organized as follows. General properties of the HGC silicon sensor are described in Section 13.2. The test beam setup and experimental apparatus are presented in Section 13.3. The results of the test beam measurements are presented in Section 13.4. Finally, Section 13.5 is devoted to discussion and conclusions.

13.2 General Properties of Silicon Timing and Bench Test Studies

All measurements presented in this chapter were carried out using a silicon sensor identical to that of the CMS HGC. The silicon sensor thickness is 300 µm and it is comprised of 128 hexagonal pixels with 1 cm maximal diameter. The left and right panels of Figure 13.1 show an schematic with 7 pixels and a full CAD schematic of the sensor, respectively. The silicon sensor was wire-bonded to a printed circuit board (PCB) where 25 pixels were implemented with an independent analog readout. The PCB provided amplification for all the 25 implemented pixels and was optimized for timing measurement; this final HGC timing layer is shown in Figure 13.2. The silicon sensor was operated with a bias voltage of −300 V and the measured total current was 170 µA.
Figure 13.1: An HGC sensor schematic geometry with 7 pixels (left), and a CAD schematic of the entire sensor (right) are shown.

Figure 13.2: The implemented HGC timing layer is shown. 25 pixels with full analog electronics were implemented. The silicon sensor is at the back of the PCB.

13.3 Test-beam Setup and Experimental Apparatus

Test-beam measurements were carried out at the FTBF which provided a 120 GeV proton beam from the Fermilab Main Injector accelerator, and secondary beams composed of electrons, pions, and muons of energies ranging from 4 GeV to 32 GeV. A simple schematic diagram of the experimental setup is shown in Figure 13.3. A small plastic scintillator of transverse dimensions 1.7 mm×2 mm is used as a trigger counter to initiate the read out of the DAQ system and to select incident beam particles from a small geometric area, allowing us to center the beam particles on the HGC timing layer. Next, we place a stack of either tungsten or lead absorbers
of various thicknesses for measurements of the longitudinal profile of the electromagnetic shower. The HGC timing layer is located immediately downstream of the absorber plates. Finally, a Photek 240 MCP-PMT detector [211, 225, 228, 226] is placed furthest downstream, and serves to provide a very precise reference timestamp; Its precision has been previously measured to be less than 10 ps [228]. A photograph showing the various detector components is presented in Figure 13.4. More details of the experimental setup are described in our previous studies using the same experimental facility in references [211, 225, 228, 226] as well as in Chapters 10 and 11. The DAQ system is based on a CAEN V1742 digitizer board [5],

![Diagram](image.png)

Figure 13.3: A schematic diagram of the test-beam setup is shown. The \( t_0 \) and \( t_1 \) are defined in Section B.7.

which provides digitized waveforms sampled at 5 GS/s. The HGC timing layer was not electromagnetically shielded and therefore some electronic pickup noise was detected and accounted for during the offline analysis. A nominal bias voltage of \( \sim 300 \) V was applied to deplete the silicon sensor in all of the studies shown below.

### 13.4 Test Beam Measurement, Data Analysis, and Results

Measurements were performed in June 2016, using the primary 120 GeV proton beam, and secondary electron beam provided for the FTBF. Secondary beams with energies ranging from 4 GeV to 32 GeV were used. As discussed in Chapter 12, the electron purity for those beams ranges between 70% at the lowest energy to about 10% at the highest energy. Stacks of either tungsten or lead plates with varying thicknesses were placed immediately upstream of the HGC timing layer in order to measure the response along the longitudinal direction of the electromagnetic shower, although most of the results presented below correspond to \( 6X_0 \) of lead.
Signals from the HGC timing layer (25 pixels were implemented and read out) and the Photek 240 MCP-PMT are read out and digitized by the CAEN V1742 digitizer; representative signal waveforms for one of the 25 silicon pixels and the Photek 240 are shown in the left and right panel of Figure 13.5, respectively. The silicon signal pulse has a rise time of about 2 ns, and a full pulse width of around 7 ns. This rise time is consistent with a time constant of a silicon sensor coupled to a 50 Ohm amplifier.

The CAEN digitizer is voltage and time calibrated using the procedure described in Ref. [185]. The total collected charge for each signal pulse is computed by integrating a 10 ns window around the peak of the pulse. The time for the reference
Photek 240 MCP-PMT detector is obtained by fitting the peak region of the pulse to a Gaussian function and the mean parameter of the Gaussian is assigned as the timestamp $t_0$, see the right panel of Figure 13.6. The time for signals from each pixel in the HGC layer is obtained by performing a linear fit to the rising edge of the pulse and the time at which the pulse reaches 45% of the maximum amplitude is assigned as its timestamp $t_1$; see the left panel of Figure 13.6. The electronic time resolution of the CAEN V1742 digitizer was measured to be $\sim 4$ ps and neglected on the timing measurements described below.

![Figure 13.6: Examples of the timestamps extraction for a pulse waveform in one the pixels of the HGC timing layer (left) and the Photek 240 MCP-PMT (right) digitized by CAEN V1742 digitizer board. The timestamp on the HGC pixel is extracted by intersecting the linear fit (solid red line) with the horizontal line corresponding to 45% of the pulse maximum. The timestamp for the Photek 240 is the mean parameter of the Gaussian fit (solid blue line).](image)

Electrons were identified by requiring that the signal amplitude of the Photek 240 MCP-PMT detector, located downstream of the HGC timing layer, exceeds certain thresholds because electromagnetic showers induced by electrons produce significantly larger signals, while pions produce much smaller signals. This procedure has been measured to provide electron purities between 80% and 90% for all beam conditions; see Chapter 12.

**Intrinsic HGC TOF resolution**

Let’s now examine the intrinsic timing capabilities of the HGC layer. The HGC timing layer was positioned just downstream of $6X_0$ of lead and showering electrons were selected by requiring the signal amplitude and integrated charge in the Photek 240 MCP-PMT to be above a certain threshold. Figure 13.7 shows two examples of transverse shower profile measured by the HGC layer, where the color palette represents the integrated charge in each pixel. As observed in Figure 13.7 most of the activity is concentrated in the central and the 6 neighboring pixels – these 7 pixel are
more clearly represented in the left panel of Figure 13.1 – and therefore the studies in this chapter just include these pixels. It is of note that the central pixel could fluctuate in an event-by-event basis. The TOF for each of the considered pixels in the

Figure 13.7: Examples of the shower transverse profile sampled by the HGC layer for a 32 GeV (left) and 16 GeV (right) electron beam. There is $6X_0$ of tungsten right upstream of the HGC layer.

HGC layer with respect to the Photek 240 MCP-PMT, i.e. $\Delta t = t_1 - t_0$, is calculated. Subsequently, the information from all the pixels is combined by weighting the individual times with the corresponding charge deposited in the following fashion:

$$\Delta t_{HGC} = \frac{\sum_{i=0}^{6} \text{charge}_i \times \Delta t_i}{\sum_{i=0}^{6} \text{charge}_i},$$

(13.1)

where $\Delta t_{HGC}$ is the combined HGC layer TOF, charge$_i$ is the charge deposited in the $i$-th pixel, and $\Delta t_i$ is the $i$-th pixel TOF. The TOF distributions for the pixels with highest and second highest charge are shown in the left and right panel of Figure 13.8, respectively. The TOF distributions of the HGC layer ($\Delta t_{HGC}$) is shown in the left panel of Figure 13.9, while an alternative method for combining the HGC pixels – using the most probable value (mpv) of the deposited charge distribution in each pixel as the weight, see Eq. 13.1. These weights are constant throughout an entire run. – is shown in the right panel of Figure 13.9. It is of note that the default and the alternative (mpv) algorithms yield very similar results with an outstanding time resolution of about 15 ps for an electron beam of 32 GeV.

Comparing Figure 13.8 (left panel) and Figure 13.9, it is observed that the TOF resolution of the central pixel is already close to the final time resolution of the entire
Figure 13.8: TOF distributions for (left) the pixel with the highest and (right) the the pixel with the second highest charge in the HGC layer using a 32 GeV electron beam and 6X₀ of tungsten. The TOF resolutions are estimated by the standard deviation parameter of the Gaussian fit (red solid curve) to the TOF distribution.

Figure 13.9: TOF distributions of the HGC layer using a 32 GeV electron beam and 6X₀ of tungsten, where the pixels are combined with (left) the default algorithm and (right) the mpv of the charge distribution as the weight. The TOF resolutions are estimated by the standard deviation parameter of the Gaussian fit (red solid curve) to the TOF distribution.

HGC layer. This suggests that pixels combination does not provide a significant improvement to the overall TOF resolution. Figure 13.10 shows the HGC TOF resolution as a function of the pixels combined at different separations between the tungsten absorber and the HGC layer, where it is observed that the TOF resolution is not significantly improved as a function of the added pixels for any of the separations. Despite the small improvement, it is observed that the larger the distance between the absorber and the HGC layer, the larger the relative improvement in the time resolution as more pixels are added; this is consistent with the fact that showers are more spread for the runs with more separation. Thus, it is convenient to define a quantity related to the transverse shower spread, and to achieve this we use the ratio of the charge in the central pixel and the total charge in the 7 pixels as proxy to the transverse shower profile:
\[ R_7 = \frac{\text{charge}_0}{\sum_{i=0}^{6} \text{charge}_i}, \quad (13.2) \]

where \( \text{charge}_i \) is the charge deposited in the \( i \)-th pixel, with the zeroth being the central pixel. The \( R_7 \) distribution is shown in Figure 13.11.

Figure 13.10: HGC layer TOF resolution as a function of the number of pixels combined. The distance between the absorber and the HGC layer was varied to sample the shower at different location.

Figure 13.11: \( R_7 \) distribution for different separations between the HGC layer and the \( 6X_0 \) of tungsten.

Finally, the dependence of the time resolution as a function of the beam energy is studied. Electron beams with energies of 8, 16, and 32 GeV were used, the separation between the absorber and the HGC layer was 1 mm. The results are summarized in Figure 13.12, the functional form \( A/\sqrt{E} + B \) was used to fit the data points. It is observed that the functional form does not fit the data well and thus
more beam energy points are needed to better constrain the floating parameters. Nevertheless, the best time resolution measured was found to be around 15 ps for a 32 GeV electron beam.

![Beam Energy vs. Time Resolution (all pixels, charge weighting)](image)

Figure 13.12: HGC layer TOF resolution as a function of the beam energy using 6$X_0$ of tungsten. The functional form $A/\sqrt{E} + B$ was fitted to the data points (red solid curve).

**Combining Two Timing Layers**

Combining the timing information of multiple HGC layers could improve the final TOF resolution of the calorimeter to em showers. The measurements presented in this chapter lack of an identical second HGC layer, but as shown in Chapter 11 the Photonics MCP-PMT located downstream of the HGC layer could be use as an additional timing measurement. To obtain the final TOF measurement (two-layer combination) the HGC layer and the Photonis MCP-PMT are combined with an equal weigh. Figure 13.13 shows the TOF distribution for the Photonis MCP-PMT and the final two-layer combination in the left and right panels, respectively.

**Emulation of SKIROC2 Readout**

The HGC proposed for the Phase 2 Upgrade of the CMS electromagnetic calorimeter uses a front-end electronics readout based on the *SKIROC2* chip, which has been preliminarily shown to have around 50 ps jitter[72]. In order to simulate the effect of having a *SKIROC2* readout, the studies just presented above are now repeated with all the measured timestamps randomly smeared by 50 ps. Each timestamp – this includes all the HGC layer pixels, the Photonis MCP-PMT, and the reference
Photek 240 MCP-PMT. – is smeared by adding a random number drawn from a Gaussian p.d.f with a mean and a width of 0 and 50 ps, respectively.

Figure 13.14 shows the TOF distributions after smearing for the pixels with highest and second highest charge in the left and right panel, respectively. The $\Delta t_{HGC}$ distribution and the two-layer combination TOF distribution are shown in the left and right panel of Figure 13.15. Here, pixels and layer are all combined with the same weight. The HGC time resolution improves from that of the central pixel only, and this could be explain since the dominance of the central pixels has been diluted by the 50 ps Gaussian smearing. The HGC time resolution as a function of the number of pixels combined is shown in Figure 13.16.

Figure 13.14: TOF distributions after a 50 ps Gaussian smearing for (left) the pixel with the highest and (right) the the pixel with the second highest charge in the HGC layer using a 32 GeV electron beam and 6$X_0$ of tungsten. The TOF resolutions are estimated by the standard deviation parameter of the Gaussian fit (red solid curve) to the TOF distribution.
Figure 13.15: TOF distributions after a 50 ps Gaussian smearing for (left) the HGC layer and (right) the final two-layer combination using a 32 GeV electron beam and 6$X_0$ of tungsten. The TOF resolutions are estimated by the standard deviation parameter of the Gaussian fit (red solid curve) to the TOF distribution.

Figure 13.16: HGC layer TOF resolution after a 50 ps Gaussian smearing as a function of the number of pixels combined.

Finally, the dependence of the TOF resolution is studied after the 50 ps smearing was applied. The results are summarized in Figure 13.17. It is of note that the final two-layer combination time resolution for a 32 GeV electron beam is around 30 ps and meets the requirements needed to reject pileup at the HL-LHC (30 ps is equivalent to 1 cm resolution in the collision axis).

13.5 Conclusions
The first timing studies on the HGC were carried out; the studies were done on a single HGC layer implemented with 25 pixels, each with an independent analog readout and then digitized by the the CAEN V1742 digitizer. The HGC layer was placed right downstream of 6$X_0$ of tungsten absorber. The selected em shower
Figure 13.17: TOF distributions as a function of the beam energy after a 50 ps Gaussian smearing for the HGC layer using $6X_0$ of tungsten. The functional form $A/\sqrt{E} + B$ was fitted to the data points (red solid curve).

Events showed a transverse spread that was contained in the inner most pixels with the central pixel containing most of the energy of the shower. As expected, the total charge deposited in the 7 HGC pixels showed a linear relationship with respect to the electron beam energy. The HGC time-of-flight resolution was obtained by combining the 7 inner pixels and found to be around 15 ps, which was close to that of the central pixel alone; suggesting, that sampling the shower at place with more transverse spread could improve the timing performance, provided large signal to noise ratios in the 7 inner pixels. The combination of two timing layers was also studied, and the results suggest that adding additional timing layers improves the timing performance as expected from two uncorrelated measurements. Finally, the effect of the SKIROC2 readout was studied by smearing each timestamp measurement by a Gaussian with 50 ps width. The HGC layer time resolution and the final two-layer combination were measured to be about 45 ps and 30 ps, respectively. These studies suggest that the desirable time-of-flight resolution for the proposed CMS high-granularity calorimeter are in principle well within reach.
Part V

Summary and Conclusions
CONCLUSION AND DISCUSSION

We presented a summary of the SM most important ingredients, we also outlined some of the issues with this theory, such as the hierarchy problem, the non-unification of the gauge coupling at the Planck scale, and the lack of a suitable dark matter candidate, among others. We also presented a review of the astronomical and astrophysical evidence for dark matter as well as the status of searches for WIMP dark matter. The problems with the SM, the evidence for dark matter, and its possible production in particle colliders motivated the searches for beyond the standard model physics presented in this thesis.

We review the most important aspects of the LHC machine and the different detectors operating at the Compact Muon Solenoid experiment, these include, the CERN accelerator facility, the LHC superconducting magnets, the tracker pixel and strip detectors, the electromagnetic calorimeter, the hadronic calorimeter, the muon system, the superconducting solenoid, and the trigger system. All of these ingredients are essential for carrying out the searches for beyond the standard model physics presented in this thesis. We also presented a review of the properties of the razor variables for discovering new physics.

We presented a search for particle dark matter in events with two or more jets using 20fb$^{-1}$ of $\sqrt{s} = 8\text{ TeV}$ data. This search used the razor kinematic variable to discriminate signal from background events. We observed good agreement between the observations and the estimated background yield, therefore we set 90% CL. limits in the cutoff scale ($\Lambda$) of the vector and axial vector effective field theory operators considered. We found that the sensitivity of the search was very competitive with respect to that of the standard monojet searches, setting a limit on $\Lambda \sim 1\text{ TeV}$, and using a phase space not yet explored thus improving the CMS sensitivity for particle dark matter production. The final results were interpreted as a DM-nucleon cross-section limit as a function of the DM candidate mass and compared to the 90% CL. from direct detection experiments. The LHC results are very competitive in the spin-dependent case and at masses below a few GeV.

We also presented a search for anomalous Higgs boson production using 15.3fb$^{-1}$ of $\sqrt{s} = 13\text{ TeV}$ data. This analysis selects events with a Higgs boson in association
with jets, where the Higgs candidate decays into two photons in the central region of the CMS detector. This analysis uses the razor variables to discriminate between signal and background. There are a total of 14 $M_R - R^2$ search regions and we observed a $2.4\sigma$ excess in one of the bins with the highest values of $M_R - R^2$ and where the Higgs candidate has a transverse momentum larger than 110 GeV. Another excess of events was observed in the 8 TeV analog of this analysis but in a different $M_R - R^2$. Nevertheless, this excess has to be followed closely and confirmed or disproved with a larger integrated luminosity.

We dedicated an entire part of this thesis to present the detector research and develop towards a precision timing calorimeter. This work was carried out with Fermilab and Caltech collaborators where we studied different calorimeter prototypes equipped with precision timing capabilities. We studied LYSO-based sampling calorimeters, “shashlik” sampling calorimeters, multichannel plates as the active element of a sampling calorimeter, silicon detectors as the active element of a sampling calorimeter, and finally we studied one of the modules proposed to be used in the Phase-II upgrade of the CMS electromagnetic calorimeter. The prototypes were tested at the Fermilab Test Beam Facility and at CERN with electron and proton beam. We found time resolution of the order of 10-50 ps depending on the calorimetric device. These results are very encouraging, particularly in light of its application to alleviate the detrimental effects of pileup on particle reconstruction and identification at the High Luminosity LHC.

We have also presented in the appendices a search for beyond the standard model physics in high-mass diphoton resonances. This search observed a $2.9\sigma$ excess at an invariant mass of about 750 GeV in the data collected during 2015 and drew significant attention from the community. We presented in this thesis an update of this analysis with approximately 5 times the integrated luminosity, where the 750 GeV excess was found to be greatly disfavored. The CMS collaboration decided that an independent analysis should be carried out given the importance of this analysis. This second parallel analysis was carried out in an independent fashion and the two analyses were found to be compatible, thus providing confidence in the observed results. No significant excess of events over the SM background was found and 95% CL limits were placed in the context of a massive spin-0 and a spin-2 Randall-Sundrum resonance with various experimental widths. Also in the appendices is a reinterpretation of the search for anomalous Higgs boson production using razor variables carried out by CMS at 8 TeV. The reinterpretation includes two model of
bottom squark pair production that decays into neutralinos and the Higgs boson. The search studied seems to have a good sensitivity for this particular supersymmetric scenario excluding the bottom squark up to a mass of about 350 GeV. It is also of note that this event topology seems to be consistent with the excess of events reported by the CMS analysis where the preferred bottom squark mass was found to be around 500 GeV.

Despite the null results regarding the discovery of new physics, the LHC experiments have covered a large amount of well motivated searches for BSM physics with a few interesting excesses to be followed closely. In particular this thesis presented a pioneer effort to search for particle dark matter production at the LHC, which has now become one of the most widely covered topic at the LHC experiments, including final state with a lepton, photons, W/Z boson, and recently Higgs boson. Another direction that we have studied is the more model independent search for anomalous Higgs production, which has been enabled by the measurements of the SM Higgs properties. This search is very relevant since the Higgs is most likely involved in beyond the SM process that could enhance its production or decay rate. A possible extension of this analysis is to add searches targeting different Higgs final states as well as to search for associated production of HW, HZ, and HH. The later, will be realized by the large integrated luminosities to be collected in the high luminosity run of the LHC. We also presented a very model independent search for high-mass diphoton resonances which will remain very important for the LHC program as well as other resonance searches that will become feasible, again, as more integrated luminosity is collected.

We want to emphasize the importance of developing new detector technologies that will enable us to answer the most important puzzles in nature today. In particular the pursuit of sub-10 ps precision timing devices, including calorimeters, is an area that shows a lot of potential applications for particle collider experiments and that has been proven to be readily available.

Finally, with larger integrated luminosities and possible increases in beam energies – either by an upgrade of the LHC magnets or by the construction of new particle colliders – we will continue search for new phenomena by probing rare processes and exploring new phase space.
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Appendix A

SEARCH FOR MASSIVE RESONANCES DECAYING INTO TWO PHOTONS

A.1 Introduction
The standard model (SM) of particle physics has been highly successful in describing physical phenomena but it is widely considered to be an incomplete theory because of various shortcomings. In particular, the SM suffers from the so-called hierarchy problem [53], which refers to the large difference between the Higgs boson mass of 125 GeV [15] and the highest energy scale up to which the SM must be valid. Many extensions to the SM have been proposed to address the hierarchy problem, including theories with additional space-like dimensions [220] and models with extended Higgs boson sectors [67]. Some of these extensions predict new resonances that decay to a diphoton final state. For example, the Randall–Sundrum (RS) approach [220, 221] to extra dimensions postulates massive excitations of spin-2 gravitons that can decay to two photons. The simplest extension of the SM Higgs boson sector consists of the addition of a doublet of complex scalar fields. In such models [115], some of these additional scalar resonances can decay to a photon pair [62]. According to the Landau–Yang theorem, the spin of a resonance decaying to two photons can only be zero or an integer larger than one [196, 258].

Recently, the ATLAS and CMS Collaborations at the CERN LHC presented results on searches for high-mass diphoton resonances in proton-proton (pp) collisions at a center-of-mass energy of 13 TeV [6, 182]. The results were based on data collected in 2015, corresponding to integrated luminosities of approximately 3 fb$^{-1}$ per experiment. The CMS results included a combined analysis with pp collision data at √s = 8 TeV collected in 2012 [167] corresponding to an integrated luminosity of 19.7 fb$^{-1}$. Both collaborations reported the observation of a moderate excess of events compared to SM expectations, compatible with the production of a new resonance with a mass around 750 GeV.

In this appendix, we report on an updated search for spin-0 resonances and RS gravitons produced in pp collisions and decaying to two photons. The data were collected in 2016 with the CMS detector at √s = 13 TeV and correspond to an integrated luminosity of 12.9 fb$^{-1}$. The analysis procedures are very similar to those
presented in Ref. [182] for the 2015 data. A combined analysis of the 8 TeV data set of Ref. [167], the 13 TeV data set of Ref. [182], and the 13 TeV data set examined here is performed to improve the sensitivity of the results. Earlier LHC searches for RS gravitons are presented in Refs. [11, 9, 10, 8, 12, 13, 167, 87, 171, 85, 170, 86, 179, 172, 168, 84, 83], and for spin-0 particles decaying to two photons in Refs. [14, 167]. These earlier searches are based on $pp$ collisions at either $\sqrt{s} = 7$ or 8 TeV.

A.2 Event simulation

The \texttt{pythia} 8.2 [242] event generator with NNPDF2.3 [50] parton distribution functions (PDFs) is used to produce simulated signal samples of spin-0 and spin-2 resonances decaying to two photons. The samples are generated at leading order (LO), with values of the resonance mass $m_X$ in the range $0.5 < m_X < 4.5$ TeV. Three values of the relative width $\Gamma_X/m_X$ are used as benchmarks: $1.4 \times 10^{-4}$, $1.4 \times 10^{-2}$, and $5.6 \times 10^{-2}$, where $\Gamma_X$ is the width of the resonance. These relative widths correspond, respectively, to resonances much narrower than, comparable to, and significantly wider than the detector resolution. In the context of the RS graviton model, for which $\Gamma_X/m_X = 1.4 \tilde{k}^2$ [121], the relative widths correspond to the dimensionless coupling parameter $\tilde{k} = 0.01$, 0.1, and 0.2. The scalar resonances are produced through gluon-gluon fusion, and RS graviton resonances through both gluon-gluon fusion and quark-antiquark annihilation. In the RS model, the first mechanism accounts for approximately 90% of the production cross section.

The SM background mostly arises from the direct production of two photons, the production of $\gamma$+jets events in which jet fragments are misidentified as photons, and the production of multijet events with misidentified jet fragments. These backgrounds are simulated with the \texttt{sherpa} 2.1 [142], \texttt{MadGraph5_aMC@NLO} 2.2 [41] (interfaced with \texttt{pythia} 8.2 for parton showering and hadronization), and \texttt{pythia} 8.2 generators, respectively, using the CT10NLO [195], NNPDF3.0 [51], and NNPDF2.3 PDF sets, again respectively. The \texttt{pythia} tune CUETP8M1 [173] is used.

For both the signal and background samples, the detector response is simulated using the \texttt{Geant4} package [30]. The simulated samples incorporate additional $pp$ interactions within the same or a nearby bunch crossing (pileup) and are weighted to reproduce the measured distribution of the number of interactions per bunch crossing.
A.3 Event selection and diphoton mass spectrum

The trigger requirements, photon identification criteria, and event selection procedures are described in Ref. [182]. Some details are given below. Energy deposits in the ECAL compatible with the shower shape expected for a photon are clustered together to define a photon candidate. Variations in the crystal transparency during the data collection period are corrected for using a dedicated monitoring system, and the single-channel response is equalized based on collision data [166]. A multivariate regression technique [166] is used to correct the photon energy for the incomplete containment of the shower in the clustered crystals, the shower losses for photons that convert before reaching the calorimeter, and the effects of pileup. The interaction vertex is selected using the algorithm described in Ref. [174], which combines information on the correlation between the diphoton system and the recoiling tracks, the average transverse momentum ($p_T$) of the recoiling tracks, and, when available, directional information from reconstructed photon conversions. For resonances with a mass above 500 GeV, the fraction of events in which the interaction vertex is correctly assigned is approximately 90%. For each photon candidate, the transverse size of the electromagnetic cluster in the $\eta$ coordinate must be compatible with that expected for a photon from a hard interaction, and the ratio of the associated energy in the HCAL to the photon energy must be less than 0.05.

Photon candidates are required to have $p_T > 75$ GeV and to appear within $|\eta| < 2.5$. Candidates in the transition region between the barrel and endcap detectors ($1.44 < |\eta| < 1.57$), where the acceptance is difficult to model, are rejected. Photon candidates associated with electron tracks that are incompatible with conversion tracks are rejected. Photon candidates are required to be isolated. There are two isolation criteria, both of which are imposed: i) the sum of the scalar $p_T$ of charged hadron candidates from the interaction vertex that lie within a cone of radius $R = \sqrt{(\Delta \eta)^2 + (\Delta \phi)^2} = 0.3$ around the photon candidate must be less than 5 GeV, where charged hadrons identified as conversion tracks associated with the photon candidate are excluded; ii) the pileup-corrected sum of the scalar $p_T$ of additional photon candidates within this same cone must be less than 2.5 GeV.

The identification and trigger efficiencies are measured as functions of photon $p_T$ using data events containing a Z boson decaying to a $\mu^+ \mu^-$ pair in association with a photon, or to an $e^+ e^-$ pair [166]. The efficiency of the photon selection procedure in the kinematic range considered in the analysis is above 90 and 85% for candidates in the barrel and endcap regions, respectively. The ratio between the efficiencies
measured in data and simulation is found to be lower than 1 by 3.5% for photons in the barrel region and by 6.5% for photons in the endcap region. No significant \( p_T \) dependence of the efficiency ratios is observed, and a \( p_T \)-independent correction is applied to the normalization of the simulated event samples to account for this difference.

The photon candidates in an event are grouped into all possible pairs. At least one photon candidate in the pair must have \( |\eta| < 1.44 \), i.e., lie in the barrel. Photon pairs are divided into two categories. The first category, denoted “EBEB”, contains pairs for which both candidates lie in the barrel. For the second category, denoted “EBEE”, one candidate lies in the barrel and the other in an endcap. The invariant mass \( m_{\gamma\gamma} \) of the pair must satisfy \( m_{\gamma\gamma} > 230 \text{ GeV} \) for EBEB candidates and \( m_{\gamma\gamma} > 330 \text{ GeV} \) for EBEE candidates. The fraction of events in which more than one photon pair satisfies the selection criteria is approximately 1%. In these cases, only the pair with the largest scalar sum of photon \( p_T \) is retained.

The selection efficiency for signal events varies between 50 and 70%, depending on the signal hypothesis. Because of the different angular distribution of the decay products, the kinematic acceptance for the RS graviton resonances is lower than for scalar resonances. For \( m_X < 1 \text{ TeV} \) the difference is approximately 20%. The two acceptances are similar for \( m_X > 3 \text{ TeV} \).

The event selection procedure described above was finalized on the basis of studies with simulated signal and background event samples prior to inspection of the data in the search region of the diphoton invariant mass distribution, which is defined as \( m_{\gamma\gamma} > 500 \text{ GeV} \).

A total of 6284 (2791) photon pairs are selected in the EBEB (EBEE) category. Of these, 461 (800) pairs have an invariant mass above 500 GeV. According to simulation, the direct production of two photons accounts, respectively, for 90 and 80% of the background events selected in the EBEB and EBEE categories. This prediction is tested in data using the method described in Ref. [81].

The diphoton invariant mass distribution of the selected events is shown in Fig. A.1, for both the EBEB and EBEE categories. We perform an independent maximum likelihood fit to the data in each category using the function

\[
  f(m_{\gamma\gamma}) = m_{\gamma\gamma}^{a+b \log(m_{\gamma\gamma})}. \tag{A.1}
\]

This parametric form is chosen to model the background in the hypothesis tests discussed below. The results of the fits are shown in Fig. A.1.
Figure A.1: The observed invariant mass spectra $m_{\gamma\gamma}$ for selected events in the (left) EBEB and (right) EBEE categories. There are no selected events with $m_{\gamma\gamma} > 2000$ GeV. The solid lines and the shaded bands show the results of likelihood fits to the data together with the associated 1 and 2 standard deviation uncertainty bands. The ratio of the difference between the data and the fit to the statistical uncertainty in the data is given in the lower plots.

A.4 Likelihood fit

A simultaneous fit to the invariant mass spectra of events in the EBEB and EBEE event categories is performed to determine the compatibility of the data with the background-only and the signal+background hypotheses. The test statistic is based on the profile likelihood ratio:

$$q(\mu) = -2 \log \frac{L(\mu S + B|\hat{\theta}_\mu)}{L(\hat{\mu} S + B|\hat{\theta})},$$

(A.2)

where $S$ and $B$ represent the probability density functions for resonant diphoton production and for the SM background, respectively. The parameter $\mu$ is the so-called signal strength, while $\hat{\theta}$ represents the nuisance parameters of the model, used to account for systematic uncertainties. The $\hat{x}$ notation indicates the best fit value of the parameter $x$ for any $y$ value, while $\hat{x}_y$ denotes the best fit value of $x$ for a fixed value $y$.

To set upper limits on the rate of resonant diphoton production, the modified frequentist method known as CL$_s$ [165, 222] is used, following the prescription described in Ref. [197]. The compatibility of the observation with the background-only hypothesis is evaluated by computing the background-only $p$-value. The latter is defined...
as the probability, in the background-only hypothesis, for \( q(0) \) to exceed the value observed in data. This quantity, the “local \( p \)-value” \( p_0 \), does not take into account the fact that many signal hypotheses are tested.

Asymptotic formulas [114] are used in the calculations of exclusion limits and local \( p \)-values. The accuracy of the asymptotic approximation in the estimation of exclusion limits and significance is studied, using pseudo-experiments, for a subset of the hypothesis tests and is found to be about 10%.

The signal shape in \( m_{\gamma\gamma} \) is determined from the convolution of the intrinsic shape of the resonance and the CMS detector response to photons. The intrinsic shape is taken from the \textsc{pythia} 8.2 generator. A grid of mass points with 125 GeV spacing, in the range 500–4500 GeV, is used. The resulting shapes are interpolated to intermediate points using a parametric description of the distribution. The detector response is determined using fully simulated signal samples of small intrinsic width, corrected through Gaussian smearing to agree with measurements based on \( Z \rightarrow e^+e^- \) data. Nine uniformly spaced mass hypotheses in the range 500–4500 GeV are employed. The signal mass resolution, quantified through the ratio of the full width at half maximum of the distribution, divided by 2.35, to the peak position, is approximately 1.0 and 1.5% for the EBEB and EBEE categories, respectively. The signal normalization coefficients are proportional to the product of the kinematic acceptance and the signal efficiency within the acceptance region. These are computed, for each category, in simulated samples and interpolated to intermediate points using quadratic functions of \( m_X \) and \( \Gamma_X/m_X \).

The background shape in \( m_{\gamma\gamma} \) is described by the parametric function given by Eq. (A.1). The values of the parameters \( a \) and \( b \) are determined in the fit to data, with separate values for the EBEB and EBEE categories, and are treated as unconstrained nuisance parameters in the hypothesis tests.

The accuracy of the background parameterization is assessed using simulation and is quantified by studying the difference between the true and predicted numbers of background events in several \( m_{\gamma\gamma} \) intervals in the search region. The relative widths of the intervals, defined by \( 2(x_1 - x_2)/(x_1 + x_2) \) with \( x_1 \) and \( x_2 \) the lower and upper bin edges, range between 2 and 15%. Pseudo-experiments are drawn from the mass spectrum predicted by the simulation and are fit with the chosen background model. The total number of events in each pseudo-experiment is taken from a Poisson distribution whose mean is set equal to the observation in data. For each interval, the distribution of the pull variable, defined as the difference between the
true and predicted numbers of events divided by the estimated statistical uncertainty, is constructed. If the absolute value of the median of this distribution is found to be above 0.5 in an interval, an additional uncertainty is assigned to the background parametrization. A modified pull distribution is then constructed, increasing the statistical uncertainty in the fit by an extra term, denoted the “bias term”. The bias term is parametrized as a smooth function of $m_{\gamma\gamma}$, which is tuned in such a manner that the absolute value of the median of the modified pull distribution is less than 0.5 in all intervals. The amplitude of the bias term function is comparable to that of the 1 standard deviation bands in Fig. A.1. This additional uncertainty is included in the likelihood function by adding to the background model a component having the same shape as the signal. The normalization coefficient of this component is constrained to have a Gaussian distribution of mean zero, with a width equal to the integral of the bias term function over the full width at half maximum of the tested signal shape. The inclusion of this additional component has the effect of avoiding falsely positive or falsely negative tests that could be induced by a mismodeling of the background shape, and it reduces the sensitivity of the analysis by at most 10%.

A.5 Systematic uncertainties

The impact of systematic uncertainties in this analysis is smaller than that of the statistical uncertainties. The parametric background model has no associated systematic uncertainties except for the bias term uncertainty described in the previous section. Since the background shape coefficients $a$ and $b$ [Eq. (A.1)] are treated as unconstrained nuisance parameters, the associated uncertainties are statistical in nature.

The systematic uncertainties in the signal normalization associated with the integrated luminosity, the selection efficiency, and the PDFs are 6.2, 6.0, and 6.0%, respectively. The uncertainty in the integrated luminosity is estimated from beam scans performed in August 2016, utilizing the methods of Ref. [108]. The uncertainty associated with the PDFs is evaluated by comparing the overall selection efficiency obtained with the CT10 [195], MSTW08 [199], and NNPDF2.3 [50] PDF sets and taking the largest deviation over all tested signal hypotheses. A 1% uncertainty is associated with the level of knowledge of the energy scale and accounts for the uncertainty in the energy scale at the $Z$ boson peak and its extrapolation to higher masses. A 10% uncertainty is assigned to the knowledge of the photon energy resolution, corresponding to the uncertainty in the estimated additional Gaussian smearing determined at the $Z$ boson peak.
A.6 Results for the 2016 data

Figure A.2: The 95% CL upper limits on the production of diphoton resonances as a function of the resonance mass $m_X$, from the analysis of data collected in 2016. Exclusion limits for the scalar and RS graviton signals are given by the grey (darker) and green (lighter) curves, respectively. The observed limits are shown by the solid lines, while the median expected limits are given by the dashed lines together with their associated 1 standard deviation uncertainty bands. The leading-order production cross section for diphoton resonances in the RS graviton model is shown for three values of the dimensionless coupling parameter $\tilde{k}$ together with the exclusion upper limits calculated for the corresponding three values of the width relative to the mass, $\Gamma_X/m_X$. Shown are the results for (upper) a narrow width, (middle) an intermediate-width, and (lower) a broad resonance.

The observed and expected 95% confidence level (CL) upper limits on the product of the production cross section ($\sigma_X^{13\text{ TeV}}$) and branching fraction to two photons ($B_{\gamma\gamma}$) for scalar and RS graviton resonances are shown in Fig. A.13. Using the LO cross sections from PYTHIA 8.2, RS gravitons with masses below 1.75, 3.75, and 4.35 TeV are excluded for $\tilde{k} = 0.01$, 0.1, and 0.2, respectively, corresponding to $\Gamma_X/m_X = 1.4 \times 10^{-4}$, $1.4 \times 10^{-2}$, and $5.6 \times 10^{-2}$.

The value of $p_0$ for different signal hypotheses is shown in Fig. A.3. The largest excess is observed for $m_X \approx 620$ GeV, and has a local significance of approximately
Figure A.3: Observed background-only $p$-values for resonances with (upper left) $\Gamma_X/m_X = 1.4 \times 10^{-4}$, (upper right) $1.4 \times 10^{-2}$, and (bottom) $5.6 \times 10^{-2}$ as a function of the resonance mass $m_X$, from the analysis of data collected in 2016. The solid black and dashed blue lines correspond to spin-0 and spin-2 resonances, respectively.

2.4 and 2.7 standard deviations for narrow spin-0 and RS graviton signal hypotheses, respectively. After taking into account the effect of searching for several signal hypotheses, i.e., searching over a range of widths and masses, the significance of the excess is reduced to less than one standard deviation. No excess is observed in the proximity of $m_X = 750$ GeV.

A.7 Combination with the 2012 and 2015 data

The results obtained for the 2016 data are combined statistically with those obtained for the data discussed in Ref. [182], namely 19.7 fb$^{-1}$ of proton-proton collisions recorded at $\sqrt{s} = 8$ TeV in 2012 [167] and 3.3 fb$^{-1}$ recorded at $\sqrt{s} = 13$ TeV in 2015. For a portion of the 2015 data (0.6 fb$^{-1}$), the CMS magnet was off (0 T), while for the rest of the 2015 data and for all of the 2012 and 2016 data, the magnet was at its operational field strength (3.8 T). The analysis of the 0 T data from 2015 is described in Ref. [182].

The procedure followed for the combined analysis of 8 and 13 TeV data is the same as in Ref. [182]. The ratio of the 8 to the 13 TeV production cross section
is computed using **Pythia** 8.2, for the two types of signal hypotheses considered: scalar resonances and RS graviton resonances. The cross section ratio decreases from 0.27 and 0.29 at \( m_X = 500 \text{ GeV} \) to 0.03 and 0.04 at \( m_X = 4 \text{ TeV} \), for the scalar and RS graviton resonance hypotheses, respectively.

Exclusion limits are set on the 13 TeV production cross section for both models, and background-only \( p \)-values are computed for the signal hypotheses.

The correlation model between the systematic uncertainties associated with 8 and 13 TeV data is described in Ref. [182]. It assumes all uncertainties to be uncorrelated except for those related to the knowledge of the photon energy scale, which are taken to have a linear correlation of 0.5, and those related to the knowledge of the PDFs, which are taken to be fully correlated. For the combination of the two 13 TeV data sets, the background shape and the associated bias term uncertainties are assumed to be fully correlated between the corresponding categories of the 2015 (3.8 T) and 2016 data. Independent background normalization coefficients are used for the two data sets. The uncertainty in the signal selection efficiency is taken to be uncorrelated between the 2015 and 2016 data. The uncertainty in the knowledge of the integrated luminosity is treated as follows: a 2.3% uncertainty, corresponding to the knowledge of the absolute luminosity scale calibration determined with beam scans, is taken to be fully correlated between the 2015 (3.8 T) and 2016 data, and additional uncertainties of 1.5 and 5.8%, corresponding to the uncertainty in extrapolating the scale calibration to the data collection conditions, are applied, again respectively. Finally, the photon energy scale uncertainties are taken to be fully correlated between the two data sets.

Figure A.4 shows the observed and expected 95% CL upper limits on the 13 TeV production cross section of the different signal hypotheses obtained with the combined analysis of the 13 TeV data recorded in 2015 and 2016. The upper limits on the production of scalar resonances decaying to two photons range from about 10 to 0.2 fb, for resonance masses between 0.5 and 4.5 TeV. Compared to the 2016 data alone, the sensitivity is improved by approximately 10 and 20% at the high and low end of the \( m_X \) search region, respectively. Using the LO cross sections from **Pythia** 8.2, RS gravitons with masses below 3.85 and 4.45 TeV are excluded for \( \bar{k} = 0.1 \) and 0.2, respectively. For \( \bar{k} = 0.01 \), graviton masses below 1.95 TeV are excluded, except for the region between 1.75 and 1.85 TeV.

The observed \( p_0 \) for \( \Gamma_X/m_X = 1.4 \times 10^{-4} \) and \( 5.6 \times 10^{-2} \) obtained with the combined analysis of the 2015 and 2016 data is shown in Fig. A.5. The largest excess is
observed for $m_X \approx 1.3$ TeV and has a local significance of about 2.2 standard deviations, corresponding to less than 1 standard deviation after accounting for the effect of searching for several signal hypotheses. For $m_X = 750$ GeV, the 2.9 standard deviation local significance excess observed in the 2015 data is reduced to 0.8 standard deviations.

Figure A.4: The 95% CL upper limits on the production of diphoton resonances as a function of the resonance mass $m_X$, from the combined analysis of data collected in 2015 and in 2016. Exclusion limits for the scalar and RS graviton signals are given by the grey (darker) and green (lighter) curves, respectively. The observed limits are shown by the solid lines, while the median expected limits are given by the dashed lines together with their associated 1 standard deviation uncertainty bands. The leading-order production cross section for diphoton resonances in the RS graviton model is shown for three values of the dimensionless coupling parameter $\tilde{k}$ together with the exclusion upper limits calculated for the corresponding three values of the width relative to the mass, $\Gamma_X / m_X$. Shown are the results for (upper) a narrow width, (middle) an intermediate-width, and (lower) a broad resonance.

The observed and expected 95% CL upper limits on the 13 TeV signal production cross sections obtained through a combined analysis of the 8 TeV data from 2012 and the 13 TeV data from 2015 and 2016 are shown in Fig. A.6. Compared to the combined 13 TeV data, the analysis sensitivity improves by about 10% at the low
The analysis is completely independent and branches off from the analysis just presented above at the point where the basic reconstructed objects are available. A completely independent analysis was put in place in order to be in a position to confirm or disprove the excess observed – at about 750 GeV – in the 2015 analysis. The results obtained for the two individual data sets are also shown. The curves corresponding to the scalar and RS graviton hypotheses are shown in left and right columns, respectively. The insets show an expanded region around $m_X = 750$ GeV.

end of the $m_X$ range, while the improvement is negligible at the higher end of the range. Thus the lower limits on the mass of RS gravitons obtained by combining the 8 and 13 TeV data coincide with those obtained with the 13 TeV data alone.

The observed $p_0$ for $\Gamma_X/m_X = 1.4 \times 10^{-4}$ and $5.6 \times 10^{-2}$ obtained with the combined 8 and 13 TeV analysis is shown in Fig. A.7. The largest excess, observed for $m_X \approx 0.9$ TeV, has a local significance of about 2.2 standard deviations, corresponding to less than 1 standard deviation overall. For $m_X = 750$ GeV, the 3.4 standard deviation local significance excess reported in Ref. [182] is reduced to about 1.9 standard deviations.

A.8 Alternative analysis

A completely independent analysis was put in place in order to be in a position to confirm or disprove the excess observed – at about 750 GeV – in the 2015 analysis. The analysis is completely independent and branches off from the analysis just presented above at the point where the basic reconstructed objects are available.
Figure A.6: The 95% CL upper limits on the production of diphoton resonances as a function of the resonance mass $m_X$, from the combined analysis of the 8 and 13 TeV data. The 8 TeV results are scaled by the ratio of the 8 to 13 TeV cross sections. Exclusion limits for the scalar and RS graviton signals are given by the grey (darker) and green (lighter) curves, respectively. The observed limits are shown by the solid lines, while the median expected limits are given by the dashed lines together with their associated 1 standard deviation uncertainty bands. The leading-order production cross section for diphoton resonances in the RS graviton model is shown for three values of the dimensionless coupling parameter $k$ together with the exclusion upper limits calculated for the corresponding three values of the width relative to the mass, $\Gamma_X/m_X$. Shown are the results for (upper) a narrow width, (middle) an intermediate-width, and (lower) a broad resonance.

The event selection was synchronized using the 2015 dataset. The comparison of the diphoton invariant mass distribution between the two analyses is presented in Figure A.8, where it can be seen that the two analyses select mostly the same events with same distribution. The efficiency times acceptance ($\epsilon \times A$) for the spin-0 and spin-2 signal sample with $\Gamma_X/m_X = 1.4 \times 10^{-4}$ are shown in Figure A.9.

The background modeling in the alternative (cross-check) analysis is the one presented in Equation A.1. The background only hypothesis is done by performing an unbinned maximum likelihood to the diphoton invariant mass distribution in the
Figure A.7: Observed background-only $p$-values for resonances with (upper) $\Gamma_X/m_X = 1.4 \times 10^{-4}$ and (lower) $5.6 \times 10^{-2}$ as a function of the resonance mass $m_X$, from the combined analysis of the 8 and 13 TeV data. The results obtained for the two individual center-of-mass energies are also shown. The curves corresponding to the scalar and RS graviton hypotheses are shown in left and right columns, respectively. The insets show an expanded region around $m_X = 750$ GeV.

EBEB and EBEE categories. The results of these fits are shown in Figure A.10.

The signal modeled using a double-sided crystal-ball function. An unbinned maximum likelihood fit is performed to the available signal samples with different masses. Figure A.11 shows the result of two signal fits for $m_X = 750$ GeV and $m_X = 1000$ GeV in the left and right panels, respectively. This is repeated for all the available mass points and the final continues signal model is obtained by using a piece-wise linear interpolation for the parameter of the signal model. The results is a smooth signal model that is parametrized only by the nominal resonance mass ($m_X$), as result is illustrated by Figure A.12.

The final results is obtained by doing a simultaneous fit to the invariant mass spectra in the EEBB and EEDE to determined the compatibility of the data with the background-only or the signal-plus-background hypotheses, as discusses in section A.4. Given that the selected data events between the two analyses – the main and alternative – are already compatible, one should expect the exclusion limits to be compatible as well, provided that all operations carried out in the analyses performed...
Figure A.8: The comparison of the diphoton invariant mass distributions for the two independent analysis. The two events categories are shown, (left) EBEB, and (right) EBEE.

Figure A.9: The efficiency times acceptance ($\epsilon \times A$) for the (red) spin-0 and (blue) spin-2 signal sample with $\Gamma_X/m_X = 1.4 \times 10^{-4}$. The EBEB categories are represented by solid curves while the EBEE categories by dashed curves.

as expected. The alternative analysis 95% CL. limits and significance for the spin-0 with $\Gamma_X/m_X = 1.4 \times 10^{-4}$ are shown in the left and right panel of Figure A.13, respectively. The comparison of the two analyses is presented in Figure A.14, where it can be clearly seen that the two analyses are very much compatible. The effort to carry out a totally independent analyses builds confidence in the final result of this important search for new resonances.

A.9 Summary
A search for the resonant production of high-mass photon pairs has been presented. The analysis is based on a sample of proton-proton collisions collected by the CMS
Figure A.10: The non-resonant background fits for the (left) EBEB and (right) EBEE categories for events selected by the alternative analysis. The background functional form is presented in Equation A.1.

Figure A.11: The signal fits in the EBEB category for (left) $m_X = 750$ GeV and (right) $m_X = 1000$ GeV.

experiment in 2016 at $\sqrt{s} = 13$ TeV, corresponding to an integrated luminosity of 12.9 fb$^{-1}$. Events containing two photon candidates with transverse momenta above 75 GeV are selected. The diphoton mass spectrum above 500 GeV is examined for evidence of the production of high-mass spin-0 and spin-2 resonances.

Limits on the production of scalar resonances and Randall–Sundrum gravitons in the range $0.5 < m_X < 4.5$ TeV and $1.4 \times 10^{-4} < \Gamma_X/m_X < 5.6 \times 10^{-2}$ are determined using the modified frequentist approach, where $m_X$ and $\Gamma_X$ are the resonance mass and width, respectively. The results obtained with the 2016 data set are combined statistically with those obtained in 2012 and 2015, corresponding to integrated luminosities of 19.7 and 3.3 fb$^{-1}$ of data recorded at $\sqrt{s} = 8$ and 13 TeV, respectively.

An independent analysis was carried out in parallel in order to confirm the results obtained by the analysis just described. The final comparison shows that the two
Figure A.12: An illustration of the result of the piece-wise interpolation for the signal model. The curves shown with different colors are the interpolated shapes for different masses not present in the nominal signal samples.

Figure A.13: The (left) 95% CL. limits and (right) significance for the spin-0 with $\Gamma_X/m_X = 1.4 \times 10^{-4}$ interpretation in the case of the alternative analysis.

analyses yield very similar results, thus providing extra assurance in the presented results.

No significant excess is observed above the predictions of the standard model. Using the leading-order cross sections, Randall–Sundrum gravitons with masses below 3.85 and 4.45 TeV are excluded for values of the dimensionless coupling parameter $\tilde{k} = 0.1$ and 0.2, respectively. For $\tilde{k} = 0.01$, graviton masses below 1.95 TeV are excluded, except for the region between 1.75 and 1.85 TeV. These are the most stringent limits on Randall–Sundrum graviton production to date.
Figure A.14: Comparison of the two analyses presented in this chapter. The comparison shows the (left) 95% CL. limits and (right) significances for the spin-0 with $\Gamma_X/m_X = 1.4 \times 10^{-4}$ interpretation.
Appendix B

PHENOMENOLOGY OF ANOMALOUS HIGGS PRODUCTION IN SUPERSYMMETRIC MODELS

B.1 Introduction

The ATLAS and CMS collaborations intensively searched for SUSY production in the data collected at a center-of-mass energy $\sqrt{s} = 8$ TeV in 2012. A large part of the searches focused on SUSY models with conserved R-parity, for which the lightest SUSY particle (LSP) is stable. The LHC is particularly sensitive to the production of SUSY partners charged under QCD (squarks and gluinos), given the large production cross section in proton collisions. Given the strong bounds on generic SUSY models derived with $\sqrt{s} = 7$ TeV data, ATLAS and CMS moved the focus of their SUSY searches to the so-called natural SUSY models [208]. In its minimal realization, a natural SUSY spectrum is composed of the minimum set of SUSY partners needed to protect the mass of the Higgs (H) boson from quantum corrections: a gluino, one bottom squark, two top squarks, and three higgsinos (two neutral and one charged). This SUSY scenario results in events with multiple top and bottom quarks, produced in association with missing transverse energy $E_T^{\text{miss}}$. No evidence for the production of such particles was found, pushing the allowed mass range for gluinos and top squarks above $\sim 1600$ GeV and $\sim 700$ GeV, respectively, for a low-mass neutralino LSP and largely independent of the top squark and gluino branching ratios (see for instance Ref. [183, 160]).

In a few cases, a data yield above the expected background was observed for certain signal regions, for example, in the case of the edge dilepton analysis by CMS [233] and the SUSY search in $Z$+jets events by ATLAS [25]. These excesses correspond to, respectively, $\sim 2.4\sigma$ and $\sim 3.0\sigma$ of local significance, which are reduced after accounting for the look-elsewhere effect (LEE). Several interpretations of these results were given in the literature [157, 38, 39, 75, 126, 186], mainly related to the electroweak production of SUSY particles with long decay chains.

Here we discuss another interesting excess, observed in a search for electroweak SUSY partners in $H(\gamma\gamma)^+ \geq 1$ jet events by the CMS collaboration performed at 8 TeV [237]. The analysis uses the diphoton invariant mass $m_{\gamma\gamma}$ to select events with a H-like candidate. The nonresonant (mostly QCD diphoton production) and
resonant (standard model $H(\gamma\gamma)$ production) backgrounds are estimated using the $m_{\gamma\gamma}$ sidebands in data and the Monte Carlo simulation, respectively. The background prediction is performed as a function of the razor variables $M_R$ and $R^2$ in five mutually exclusive boxes, targeting different final states: high-$p_T$ $H(\gamma\gamma)$ (HighPt box), $H(\gamma\gamma) + H(b\bar{b})$ (Hbb box), $H(\gamma\gamma) + Z(b\bar{b})$ (Zbb box), and low-$p_T$ $H(\gamma\gamma)$ with high- and low-resolution photons (HighRes and LowRes boxes, respectively). Five events are observed in one ($M_R$, $R^2$) bin of the HighRes box, compared to less than one expected background event. This corresponds to a local significance of 2.9σ, reduced to 1.6σ after the LEE.

In this paper, we discuss a possible interpretation of this search in terms of SUSY models with light quarks. We emulate this CMS analysis to derive bounds on squark production. Since the analysis does not require or veto jets originating from b-quarks (b-jets), the results apply to bottom-squark production in natural SUSY models.

Recently, an updated search was performed with data collected at 13 TeV [235], which exhibits a similar excess of 2.5σ local significance, reduced to 1.4σ after the LEE. Model B proposed in this paper was also used for the interpretation of the results.

### B.2 Benchmark signal models

We consider two simplified models with bottom squark pair production, both resulting in a H+jets final state.

In the first model, hereafter referred to as model A, we consider the asymmetric production of a $\tilde{b}_2\tilde{b}_1$ pair, where $\tilde{b}_2$ and $\tilde{b}_1$ are the heaviest and the lightest bottom squarks, respectively. The $\tilde{b}_2$ decays to $b\tilde{\chi}_2^0$, with $\tilde{\chi}_2^0 \rightarrow H\tilde{\chi}_1^0$. The lightest neutralino $\tilde{\chi}_1^0$ is assumed to be the LSP. The $\tilde{b}_1$, close in mass to the LSP, decays to $b\tilde{\chi}_1^0$. All the other SUSY partners are assumed to be too heavy to be produced at the LHC and are ignored in this analysis. This model represents a new mechanism for the production of $H + 2b$-jets + invisible, with one of the associated b-jets typically having low momentum.

In the second model, hereafter referred to as model B [250], two bottom squarks $\tilde{b}_1\tilde{b}_1$ are produced, each decaying as $\tilde{b}_1 \rightarrow b\tilde{\chi}_2^0$. The $\tilde{\chi}_2^0$ then decays to $H\tilde{\chi}_1^0$, the $\tilde{\chi}_1^0$ being the LSP. As for model A, the other SUSY partners are assumed to be too heavy to be produced at the LHC and are ignored in this analysis. This simplified model corresponds to a final state consisting of $2H + 2b$-jets + invisible.

The mass spectrum for each model is shown in Fig. B.1. We fix the $\tilde{\chi}_2^0$ and $\tilde{\chi}_1^0$ masses to 230 GeV and 100 GeV, respectively. In model A, we fix the $\tilde{b}_1$ mass to
130 GeV as varying its mass in between the limits of the $\tilde{\chi}_1^0$ and $\tilde{\chi}_2^0$ masses has little effect. Finally, we scan the $\tilde{b}_2$ ($\tilde{b}_1$) mass between 250 GeV and 800 GeV for model A (B). These assumptions do not limit the conclusions derived on the squark production cross section. In fact, the analysis is sensitive to mass differences and not to the absolute mass of SUSY partners. On the other hand, the chosen LSP and NLSP masses does play a role when the cross section limits are translated in terms of mass exclusion bounds.

Figure B.1: Pictorial representation of the decay chains and event topologies associated with model A (left) and model B (right), as described in the text.

B.3 Event generation and detector simulation

The study is performed using samples of Monte Carlo events. The event generation is performed in PYTHIA 8.210 [239, 241]. The default parton density function set is NNPDF 2.3 QCD+QED LO (with $\alpha_s(m_Z) = 0.130$) [52, 78, 77]. Fast simulation of the CMS detector is performed in DELPHES 3.3.2 [129]. The default description of CMS as provided in the release is used, except for a modification to the photon isolation and efficiency, described in the next section. Jet clustering is performed using FASTJET 3.1.3 [73]. As in CMS, the anti-$k_T$ jet clustering algorithm is used with jet-size parameter $R = 0.5$ [74].

B.4 Emulation of the CMS search

The emulated event selection is summarized as follows,

- Events with two isolated photons with $p_T > 25$ GeV and $|\eta| < 1.44$ are selected. As in Ref. [178], the photon isolation variables, $I_\gamma$, $I_n$, and $I_\pi$, are computed by summing the transverse momenta of photons, neutral hadrons, and charged hadrons, respectively, inside an isolation cone of radius $\Delta R = 0.3$ around the selected photon. The photon isolation requirements on these variables are shown in Tab B.1. An additional photon selection efficiency
Table B.1: Photon isolation requirements, as in Ref [178]. The photon isolation variables, $I_\gamma$, $I_n$, and $I_\pi$, are computed by summing the transverse momenta of photons, neutral hadrons, and charged hadrons, respectively, inside an isolation cone of radius $\Delta R = 0.3$ around the selected photon.

<table>
<thead>
<tr>
<th></th>
<th>barrel</th>
<th>endcap</th>
</tr>
</thead>
<tbody>
<tr>
<td>$I_\gamma$</td>
<td>$1.3 \text{ GeV} + 0.005 p_T$</td>
<td>$-$</td>
</tr>
<tr>
<td>$I_n$</td>
<td>$3.5 \text{ GeV} + 0.04 p_T$</td>
<td>$2.9 \text{ GeV} + 0.04 p_T$</td>
</tr>
<tr>
<td>$I_\pi$</td>
<td>$2.6 \text{ GeV}$</td>
<td>$2.3 \text{ GeV}$</td>
</tr>
</tbody>
</table>

is applied in DelPHES such that isolated photons with $p_T < 10 \text{ GeV}$ ($p_T \geq 10 \text{ GeV}$) are randomly selected with 94% (98%) efficiency.

- Events with one H candidate with $p_T > 20 \text{ GeV}$ are selected. A pair of selected photons is considered an H candidate if at least one photon has $p_T > 40 \text{ GeV}$ and the diphoton mass $m_{\gamma\gamma} > 100 \text{ GeV}$. If the event contains more than one H candidate, the one with the highest scalar sum $p_T$ of the two photons is selected.

- Jets are reconstructed using the FastJet [73] implementation of the anti-$k_T$ [74] algorithm with jet radius parameter $R = 0.5$.

- Events with at least one jet with $p_T > 30 \text{ GeV}$ and $|\eta| < 3.0$ are selected.

- An emulation of the “medium” requirement (mistag probability of 1% and b-tag efficiency of $\sim 68\%$) of the combined secondary vertex (CSV) b-tagging algorithm is used to identify b-jets [212].

- A $b\bar{b}$ candidate pair is identified if both jets satisfy the medium requirement of the b-tagging algorithm (note: the CMS analysis requires only one to satisfy the medium requirement, while both are required to satisfy the loose requirement).

- The $b\bar{b}$ candidate pair with the mass closest to 125 GeV or 91.2 GeV is chosen as the $H \to b\bar{b}$ or $Z \to b\bar{b}$ candidate, respectively.

- The razor variable $M_R$, calculated from two megajets [99] is required to be greater than 150 GeV. All possible combinations of the reconstructed jets and the $H(\gamma\gamma)$ candidate are clustered to form megajets. The pair of megajets that
minimizes the sum in quadrature of the invariant masses of the two megajets is selected.

After this baseline selection, events are categorized according to the following requirements,

- **HighPt**: all events with an $H \rightarrow \gamma\gamma$ candidate with $p_T > 110$ GeV.
- **Hbb**: remaining events with a $H \rightarrow b\bar{b}$ candidate with mass $110 \geq m_{bb} \geq 140$ GeV.
- **Zbb**: remaining events with a $Z \rightarrow b\bar{b}$ candidate with mass $76 \geq m_{bb} \geq 106$ GeV.
- **HighRes**: 70% of remaining events after the Zbb selection (emulating the efficiency of the “high-resolution photon” selection).
- **LowRes**: all remaining events.

We assume the breakdown of events between the HighRes box and LowRes box is 70%-to-30% after the Zbb selection. This is based on the following observations: (i) CMS categorizes events in the HighRes box if both photons in the event satisfy $\sigma_E/E < 0.015$, where $\sigma_E/E$ is the estimated relative energy resolution, and categorizes events in the LowRes box otherwise, (ii) CMS observes a similar 70%-to-30% breakdown for both SM Higgs production and electroweak SUSY processes in Monte Carlo simulation [237], and (iii) we expect this breakdown to be model-independent assuming both photons are real and come from the decay of a Higgs boson, as it is based on the properties of such photons detected in CMS and not on the details of the model.

Finally, the search region selection is as follows,

- The search region in the $m_{\gamma\gamma}$ distribution is defined by $(125-2\sigma_{\text{eff}}, 126+2\sigma_{\text{eff}})$ in each event category, where $\sigma_{\text{eff}}$ is defined such that $\sim 68\%$ of Higgs boson events fall in an interval of $\pm \sigma_{\text{eff}}$ around the nominal $m_H$ value. Following this procedure using our generated and simulated signal samples, we derive $\sigma_{\text{eff}}$ to be 3.8 GeV in the HighPt box and 2.2 GeV in the HighRes and LowRes boxes. For the Hbb and Zbb boxes, due to the low number of selected signal events, we use the overall average value of 2.8 GeV.
We note that these $\sigma_{\text{eff}}$ values are larger than the corresponding ones in Ref. [237]. This is due to the larger width observed for the diphoton mass distribution in Higgs boson events simulated and reconstructed with DELPHES, compared to official CMS software. This implies the effective diphoton mass resolution when using DELPHES is larger than in the real CMS detector. We attempt to account for this with a modification explained in Sec. B.6.

B.5 Bayesian Statistical Interpretation

We model the likelihood according to a Poisson density, considering the expected background yield (with associated uncertainty), the expected signal yield (for a given signal cross section), and the observed yield. The background uncertainty is modeled with a gamma density. The background yields and the corresponding uncertainties are taken from the tables provided in Ref. [237]. To take into account systematic uncertainties on the signal, we assign a 30% uncertainty (assuming a log-normal density) on the signal strength, a multiplicative factor modifying the signal cross section. We then derive the posterior density for the signal cross section $\sigma$ as:

$$p(\sigma|\text{data}) \propto \mathcal{L}(\text{data}|\sigma)p_0(\sigma), \quad (B.1)$$

where $\mathcal{L}(\text{data}|\sigma)$ is the likelihood and $p_0(\sigma)$ is the prior density taken to be uniform. The likelihood is then

$$\mathcal{L}(\text{data}|\sigma) = \int_0^\infty d\mu \ln(\mu|\bar{\mu}, \delta \mu) \quad (B.2)$$

$$\times \prod_{i=0}^{n_{\text{bins}}} \int_0^\infty db_i \text{Poisson}(n_i|L\mu\sigma \epsilon_i + b_i)$$

$$\times \Gamma(b_i|\bar{b}_i, \delta b_i), \quad (B.3)$$

where the product runs over the number of bins $n_{\text{bins}}$; $n_i$ is the observed yield in the $i^{\text{th}}$ bin, $L$ is the integrated luminosity, $b_i$ is the assumed value of the background yield in the $i^{\text{th}}$ bin and $\bar{b}_i \pm \delta b_i$ is its expected value and the associated uncertainty; $\epsilon_i$ is the nominal value of the signal efficiency times acceptance in the $i^{\text{th}}$ bin; $\mu$ is the signal strength, a nuisance parameter modifying the signal cross section (nominally equal to $\bar{\mu} = 1$ with a $\delta \mu = 30\%$ uncertainty); $\ln(x|m, \delta)$ is the log-normal distribution for $x$, parameterized such that $\log(m)$ is the mean and $\log(1 + m\delta)$ is the standard deviation of the log of the distribution; $\Gamma(x|m, \delta)$ is the gamma distribution for $x$, parameterized such that $m$ is the mode and $\delta^2$ is the variance of the distribution. The 95% credibility level (CL) upper limit on the signal cross section $\sigma_{\text{up}}$ is obtained
from the posterior, such that

\[
\frac{\int_0^\sigma_{\text{up}} d\sigma \ p(\sigma|\text{data})}{\int_0^\infty d\sigma \ p(\sigma|\text{data})} = 0.95 .
\]  

(B.4)

We also utilize a signal significance measure defined by

\[
Z(\sigma) = \text{sign} [\log B_{10}(\text{data}, \sigma)] \sqrt{2} |\log B_{10}(\text{data}, \sigma)| ,
\]  

(B.5)

where

\[
B_{10}(\text{data}, \sigma) = \frac{\mathcal{L}(\text{data}|\sigma, H_1)}{\mathcal{L}(\text{data}|H_0)}
\]  

(B.6)

is the local Bayes factor for the data for a given signal cross section \( \sigma \), and \( \mathcal{L}(\text{data}|\sigma, H_1) \) and \( \mathcal{L}(\text{data}|H_0) \) are the likelihoods for the signal-plus-background (\( H_1 \)) and background-only (\( H_0 \)) hypotheses, respectively. As described in Ref. [214], this measure is a signed Bayesian analog of the frequentist “n-sigma.” For each signal model with specified masses, we scan the signal cross section \( \sigma \) to find the maximum significance, which occurs at the mode of the posterior.

B.6 Correction and Validation

As explained above, we find differences in the performance of the emulated CMS detector and the real CMS detector, e.g. the larger diphoton mass resolution. To take into account this and other differences in the detector simulation and reconstruction performed by Delphes and official CMS software, we conservatively double the background uncertainties in each bin reported by CMS in Ref. [237] when evaluating the likelihood in Eqn. B.3. We find this conservative approach better reproduces the observed and expected limits on a benchmark simplified model.

To validate our emulation result, we produced 95% CL limits on the production cross section of an electroweak simplified model of \( \tilde{\chi}_1^\pm \tilde{\chi}_2^0 \) production, followed by the decays \( \tilde{\chi}_1^\pm \rightarrow W^\pm \tilde{\chi}_1^0 \), \( \tilde{\chi}_2^0 \rightarrow H_1 \tilde{\chi}_1^0 \). For this model, CMS provided the 95% confidence level upper limits on the cross section assuming an LSP mass of \( m_{\tilde{\chi}_1^0} = 1 \text{ GeV} \) and equal chargino and second neutralino masses, \( m_{\tilde{\chi}_1^+} = m_{\tilde{\chi}_2^0} \).

The comparison between our result and the CMS result for this model is shown in figure B.2 as a function of \( m_{\tilde{\chi}_1^+} \).

B.7 Results

Figures B.3-B.5 contain the results of the reinterpretation of the CMS data for both models. To show how well signal model A agrees with the excess observed
Figure B.2: Comparison between the CMS result (red) and our emulation (black). Note, this scan assumes $m_{\tilde{\chi}_1^0} = 1$ GeV and $m_{\tilde{\chi}_2^0} = m_{\tilde{\chi}_1^0}$.

by CMS, Fig. B.3 (top) displays the expected SM background distribution and uncertainty taken from the CMS result compared to the distribution of the signal events for $m_{b_2} = 500$ GeV and $m_{b_2} = 800$ GeV, with other mass parameters set as $m_{b_2} = 130$ GeV, $m_{\tilde{\chi}_2^0} = 230$ GeV, and $m_{\tilde{\chi}_1^0} = 100$ GeV. The bin numbers correspond to the order of the signal regions in the yield tables in Ref. [237] and are reproduced in Tab. B.2. The normalization for each signal model is taken from the mode (i.e.

Table B.2: HighRes bin numbering scheme as in Ref. [237].

<table>
<thead>
<tr>
<th>Bin</th>
<th>$M_R$ range</th>
<th>$R^2$ range</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
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<td>[0.00, 0.05]</td>
</tr>
<tr>
<td>1</td>
<td>[150, 250]</td>
<td>[0.05, 0.10]</td>
</tr>
<tr>
<td>2</td>
<td>[150, 250]</td>
<td>[0.10, 0.15]</td>
</tr>
<tr>
<td>3</td>
<td>[150, 250]</td>
<td>[0.15, 1.00]</td>
</tr>
<tr>
<td>4</td>
<td>[250, 400]</td>
<td>[0.00, 0.05]</td>
</tr>
<tr>
<td>5</td>
<td>[250, 400]</td>
<td>[0.05, 0.10]</td>
</tr>
<tr>
<td>6</td>
<td>[250, 400]</td>
<td>[0.10, 1.00]</td>
</tr>
<tr>
<td>7</td>
<td>[400, 1400]</td>
<td>[0.00, 0.05]</td>
</tr>
<tr>
<td>8</td>
<td>[400, 1400]</td>
<td>[0.05, 1.00]</td>
</tr>
<tr>
<td>9</td>
<td>[1400, 3000]</td>
<td>[0.00, 1.00]</td>
</tr>
</tbody>
</table>

“best-fit”) signal cross section of the posterior density in the HighRes box. Fig. B.4 (top), shows the 95% CL combined upper limit on the cross section for model A. Finally, Fig. B.5 (top) shows the maximum significance $Z$ as well as the best fit signal cross section for model A as a function of $m_{b_2}$.

The bottom of Fig. B.3-B.5 are the analogous results for model B. The chosen model B mass points in Fig. B.3 are $m_{b_1} = 500$ GeV or $m_{b_1} = 800$ GeV, $m_{\tilde{\chi}_2^0} = 230$ GeV, and $m_{\tilde{\chi}_1^0} = 100$ GeV. The limit and significance scans in Fig. B.4 and B.5 are performed as a function of the $b_1$ mass. For model B, we also compare both the
excluded cross section at 95% CL and the best-fit cross section as a function of the \( \tilde{b}_1 \) mass to the NLO+NLL predicted cross section at \( \sqrt{s} = 8 \) TeV [57, 189, 188, 55, 56, 64]. We find the 8 TeV data excludes bottom squark pair production below \( m_{\tilde{b}_1} = 330 \) GeV for the chosen neutralino masses of \( m_{\tilde{\chi}^0_2} = 230 \) GeV and \( m_{\tilde{\chi}^0_1} = 100 \) GeV. More interestingly, the largest combined significance is 1.8\( \sigma \) for \( m_{\tilde{b}_1} = 500 \) GeV and the best-fit cross section is 0.4 pb, which is of the same order of magnitude as the predicted cross section.

![Figure B.3](image)

Figure B.3: (Top) The expected background and uncertainty (multiplied by a factor of two as explained in the text) compared to the best-fit signal distribution in the HighRes box for two particular mass points, \( m_{\tilde{b}_2} = 500 \) GeV and \( m_{\tilde{b}_2} = 800 \) GeV, in model A. (Bottom) The expected background and uncertainty (multiplied by a factor of two as explained in the text) compared to the best-fit signal distribution in the HighRes box for two particular mass points, \( m_{\tilde{b}_1} = 500 \) GeV and \( m_{\tilde{b}_1} = 800 \) GeV, in model B. The bin numbers correspond to the order of the signal regions in the yield tables in Ref. [237] and are reproduced in Tab. B.2.

### B.8 Discussion and summary

In this paper, we proposed two simplified models of bottom squark pair production for use in the interpretation of an excess observed by CMS in a search for SUSY in H+jets events using razor variables at \( \sqrt{s} = 8 \) TeV [237]. In model A, we considered the asymmetric production of a \( \tilde{b}_2\tilde{b}_1 \) pair, with the \( \tilde{b}_1 \rightarrow \tilde{\chi}^0_1, \tilde{b}_2 \rightarrow b\tilde{\chi}^0_2 \).
Figure B.4: (Top) The 95% CL upper limit on the cross section on $b_1\bar{b}_2$ production in model A as a function of $m_{b_2}$ (black). (Bottom) The 95% CL upper limit on the cross section on $b_1\bar{b}_1$ production in model B as a function of $m_{b_1}$ (black) compared to the NLO+NLL predicted cross section (yellow). Note, these scans assume $m_{\chi_1^0} = 100 \text{ GeV}, m_{\chi_2^0} = 230 \text{ GeV}$, and for model A $m_{b_1} = 130 \text{ GeV}$.

and $\chi_2^0 \rightarrow H\chi_1^0$, where $\chi_1^0$ is a neutralino LSP and we fix the mass splitting $m_{\chi_2^0} - m_{\chi_1^0} = 130 \text{ GeV}$. In model B, we considered the symmetric production of a $b_1\bar{b}_1$ pair, with $b_1 \rightarrow b\chi_2^0, \chi_2^0 \rightarrow H\chi_1^0$, and $m_{\chi_2^0} - m_{\chi_1^0} = 130 \text{ GeV}$.

We scanned the bottom squark masses for a fixed LSP mass of $m_{\chi_1^0} = 100 \text{ GeV}$ for both models and quantified the agreement with the data. We found the excess observed in data is broadly consistent with both models, with the largest signal significance being 1.8$\sigma$ corresponding to model B with $m_{b_1} = 500 \text{ GeV}, m_{\chi_2^0} = 230 \text{ GeV}$, and $m_{\chi_1^0} = 100 \text{ GeV}$. Following this study, model B used by the CMS collaboration to interpret the results of the updated 13 TeV search for SUSY in the same channel [235], which also exhibits an excess possibly consistent with the model.
Figure B.5: (Top) The maximum significance $Z(\sigma)$ for a given $m_{\tilde{b}_2}$ in the top panel and the “best fit” signal cross section $\sigma$ in the bottom panel for model A. (Bottom) The maximum significance $Z(\sigma)$ for a given $m_{\tilde{b}_1}$ in the top panel and the “best fit” signal cross section $\sigma$ in the bottom panel for model B. Note, these scans assume $m_{\chi_1^0} = 100$ GeV, $m_{\chi_2^0} = 230$ GeV, and for model A $m_{\tilde{b}_1} = 130$ GeV.