O new physics, where art thou?
A global search in the top sector

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ABSTRACT: We provide a comprehensive global analysis of Run II top measurements at the LHC in terms of dimension-6 operators. A distinctive feature of the top sector as compared to the Higgs-electroweak sector is the large number of four-quark operators. We discuss in detail how they can be tested and how quadratic terms lead to a stable limit on each individual Wilson coefficient. Predictions for all observables are computed at NLO in QCD. Our SFitter analysis framework features a detailed error treatment and shows that theoretical uncertainties are a limiting factor.
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1 Introduction

Contemporary interpretation frameworks for LHC measurements are driven by the structural completeness of the Standard Model (SM) with a light observed Higgs boson and missing hints to the nature of physics beyond the SM. From a quantum field theory perspective the natural approach is therefore to consider the SM as an effective field theory (SMEFT). Here the effects of potential new particles can be systematically included in terms of higher-dimensional operators, suppressed by a sufficiently large matching scale. The framework relies on the idea that new physics affecting LHC measurements is too heavy to be produced and observed directly. This is a direct application of the general condition that an effective Lagrangian is applicable if the additional contributing degrees of freedom are kinematically decoupled.

Part of the SMEFT framework [1–5] was developed as a gauge-invariant description of anomalous gauge boson interactions at LEP [6, 7]. Its biggest success has been the application to Higgs and electroweak boson measurements at the LHC [8–13]. Most recently, the same approach [14–16] has been used to systematically analyze top quark measurements at the LHC [17–21] and at future colliders [22, 23] and their link to bottom sector [24]. These efforts pave the way towards a global SMEFT analysis at the LHC.

Searches for physics beyond the Standard Model in the top sector reflect three unique aspects of top physics: first, top physics at the LHC has entered a phase of precision predictions and measurements, a development which many of us would not have thought to be feasible before the start of the LHC; second, we might start to doubt available solutions of the hierarchy problem, but from a field theory perspective it has not lost its appeal and it singles out the top sector; third, many new physics scenarios, either weakly or strongly interacting at scales around a few TeV, predict deviations in the top couplings or new top interactions, such as new scalars coupled dominantly to the top quark [25].

In this paper we present a comprehensive analysis of the top sector in the framework of SMEFT, based on the data collected mostly during the LHC Run II. We consider measurements in top pair production, including associated $t\bar{t}W$ and $t\bar{t}Z$ production, as well as in single top final states. Since effective interactions typically have a sizeable impact on kinematic distributions we add a set of kinematic measurements with a focus on boosted top pair production [26, 27]. Finally, we include charge asymmetry [14, 28–30] and top decay measurements [31, 32] to shed light on specific sectors of the effective Lagrangian. To combine all of these measurements in a coherent picture of the top sector a global SMEFT analysis is without alternative. Our enlarged set of observables builds on earlier analyses by the TopFitter [18, 19] collaboration.

For our simulations we rely on next-to-leading order (NLO) QCD predictions obtained through FeynRules [33], Nloct [34] and Madgraph5_AMC@NLO [35]. NLO predictions allow us to better control the accuracy and theoretical precision of our predictions, i.e., the theoretical uncertainties in our fit. This is especially important in phase space regions where SMEFT contributions can be large, e.g., in tails of kinematic distributions. For
the global analysis we use the established SFitter framework [35, 36]. Our technical focus is on the consistent treatment of different types of uncertainties, including correlations of systematic and theoretical uncertainties. The specific error treatment, a detailed analysis of several physics aspects not considered before, as well as a slightly different data set complement other state-of-the-art analyses, such as that of the SMEFiT collaboration [21]. In particular, the SFitter technology allows us to easily study correlations between Wilson coefficients and to compare the impact of theoretical and experimental uncertainties.

The paper is organized as follows. We begin with an overview of the observables used in our fit in Sec. 2, where we derive analytic expressions for the operator contributions. After recapitulating the main aspects of the fitting approach in Sec. 3 we describe some of the unique aspects of a SMEFT analysis of top pair production in Sec. 4. They are related to the fact that many features of the set of four-quark operators are not immediately distinguishable in QCD processes. A crucial aspect is that while flat directions exist in this sector, the quadratic contributions from dimension-6 operators turn them into compact circular correlations. This in turn allows us to derive well-defined limits from profile likelihoods. Finally, we perform a global fit first of the single top sector in Sec. 5 and then of the entire top sector in Sec. 6. Details about our choice of operators and our numerical results are discussed in the Appendix.

2 Top-quark effective theory

In the absence of new resonances, effects of new physics can be described as effective interactions of SM particles at energies below a new physics matching scale Λ. Our goal is to probe effective interactions with top quarks in LHC observables [37]. The dominant effects are parametrized in terms of Wilson coefficients $C_k$ of dimension-6 operators $O_k$ in the effective Lagrangian

$$\mathcal{L}_{\text{eff}} = \sum_k \left( \frac{C_k}{\Lambda^2} \mathcal{O}_k + \text{h.c.} \right) + \sum_l \frac{C_l}{\Lambda^2} \mathcal{O}_l,$$

where the sum runs over all operators that involve top-quarks. Non-hermitian operators are denoted as $\mathcal{O}^\dagger$. We neglect operators of mass dimension seven and higher in the EFT expansion. We focus on CP-conserving extensions of the SM, assuming that all Wilson coefficients are real and therefore neglecting CP-violating interactions. Since top-quark observables at the LHC are largely blind to the flavor of light quarks with the same quantum numbers, we impose an $U(2)_q \times U(2)_u \times U(2)_d$ flavor symmetry among quarks of the first and second generation [37–39]. We use

$$q_i = (u_i^L, d_i^L), \quad u_i = u_i^R, \quad d_i = d_i^R, \quad i = 1, 2$$

$$Q = (t_L, b_L), \quad t = t_R, \quad b = b_R$$

(2.2)

to denote left- and right-handed quarks of the first two generations and the third generation, respectively. Within this framework, we consider 22 independent operators:
• 8 four-quark operators with $LL$ and $RR$ chiral structure

\[
O_{Qq}^{1,8} = (\bar{Q} \gamma_\mu T^A Q)(\bar{q} \gamma^\mu T^A q) \\
O_{Qq}^{2,8} = (\bar{Q} \gamma_\mu T^A \tau^I Q)(\bar{q} \gamma^\mu T^A \tau^I q) \\
O_{tu}^8 = (\bar{t} \gamma_\mu T^A t)(\bar{u} \gamma^\mu T^A u) \\
O_{td}^8 = (\bar{t} \gamma_\mu T^A t)(\bar{d} \gamma^\mu T^A d) ;
\]

(2.3)

• 6 four-quark operators with $LR$ and $RL$ chiral structure

\[
O_{Qu}^8 = (\bar{Q} \gamma_\mu T^A Q)(\bar{u} \gamma_\mu T^A u) \\
O_{Qd}^8 = (\bar{Q} \gamma_\mu T^A Q)(\bar{d} \gamma_\mu T^A d) \\
O_{tq}^8 = (\bar{t} \gamma_\mu T^A q)(\bar{t} \gamma_\mu T^A q) \\
O_{tb}^8 = (\bar{t} \gamma_\mu T^A b)(\bar{t} \gamma_\mu T^A b) ;
\]

(2.4)

• 8 operators with two heavy quarks and bosons [40]

\[
\begin{align*}
O_{\phi Q}^1 &= (\phi \stackrel{\leftarrow}{D}_\mu \phi)(\bar{Q} \gamma^{\mu} Q) \\
O_{\phi Q}^3 &= (\phi \stackrel{\leftarrow}{D}_\mu \phi)(\bar{Q} \gamma^{\mu} \tau^I Q) \\
O_{\phi t}^1 &= (\phi \stackrel{\leftarrow}{D}_\mu \phi)(\bar{t} \gamma^{\mu} t) \\
O_{\phi b}^1 &= (\phi \stackrel{\leftarrow}{D}_\mu \phi)(\bar{b} \gamma^{\mu} b) \\
O_{\phi t}^3 &= (\phi \stackrel{\leftarrow}{D}_\mu \phi)(\bar{t} \gamma^{\mu} \tau^I t) \\
O_{\phi b}^3 &= (\phi \stackrel{\leftarrow}{D}_\mu \phi)(\bar{b} \gamma^{\mu} \tau^I b) \\
O_{\phi t}^{1,3} &= (\phi \stackrel{\leftarrow}{D}_\mu \phi)(\bar{t} \gamma^{\mu} t) \\
O_{\phi b}^{1,3} &= (\phi \stackrel{\leftarrow}{D}_\mu \phi)(\bar{b} \gamma^{\mu} b) \\
\end{align*}
\]

(2.5)

The different color structures of the operators will eventually lead to different color factors in the LHC observables and different limits on the Wilson coefficients, as we will see later. In Appendix A, we list the relations between these operators and the operators in the Warsaw basis [41]. Gauge invariance imposes relations between effective top couplings to gauge bosons. We define

\[
C_{\phi Q}^+ \equiv C_{\phi Q}^3 - C_{\phi Q}^3 \\
C_{\phi Q}^- \equiv C_{\phi Q}^3 + C_{\phi Q}^3 = C_{\phi Q} + 2C_{\phi Q}^3 \\
C_{tQ}^+ \equiv C_{tQ}^3 + c_w C_{tW} - s_w C_{tW} \\
C_{tQ}^- \equiv C_{tQ}^3 - c_w C_{tW} + s_w C_{tW} = \frac{1}{s_w} (C_{tW} - c_w C_{tW}) \\
\]

(2.6)

We choose $C_{\phi Q}^3$, $C_{\phi Q}^-$, and $C_{tW}$, $C_{tZ}$ as degrees of freedom in our analysis. With this choice, $C_{\phi Q}^+$ and $C_{tQ}$ modify the $ttZ$ coupling, $C_{tW}$ modifies the $tbW$ vertex, while $C_{\phi Q}^-$ affects both.

The Wilson coefficients of the operators in Eqs. (2.3), (2.4), and (2.5) define the 22 parameters in our global analysis. Further operators either do not leave visible effects in the observables we have selected (like operators with four heavy quarks) or are strongly constrained by more sensitive observables (like the Yukawa operator at dimension six, which is constrained by Higgs measurements). We therefore do not include them in our analysis, but mention them whenever they are relevant.

Experimentally, we focus on observables in top pair and electroweak single top production at the LHC. These processes are precisely predicted and measured, both at the
level of total rates and kinematic distributions. We also include top pair production in
association with a W- or Z-boson, which is more sensitive to certain operators than top	pair or single top production and help distinguishing between operators. Table 1 shows
our set of Wilson coefficients and their contributions to the various processes.

<table>
<thead>
<tr>
<th>parameter</th>
<th>$t\bar{t}$</th>
<th>single $t$</th>
<th>$tW$</th>
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<th>$t\bar{t}Z$</th>
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Table 1. Wilson coefficients in our analysis and their contributions to top-quark observables via
SM-interference ($\Lambda^{-2}$) and via dimension-6 squared terms only ($\Lambda^{-4}$). A square bracket indicates
that the Wilson coefficient contributes via SM-interference at NLO QCD. All quark masses except
$m_t$ are assumed to be zero. ‘Single $t$’ stands for $s$– and $t$–channel electroweak top production.

In what follows, we describe in detail how the 22 top operators affect these processes.
We pay special attention to contributions of the dimension-6 squared terms, which will
be crucial for our global fit. Another important aspect in our discussion is the energy
dependence of operator contributions, which changes the top kinematics in distributions.
For top pair production, we present complete analytic expressions for four-quark operator
contributions at LO, including both SM-interference and dimension-6 squared terms. We
also derive the structure of operator contributions at NLO QCD.
2.1 Top pair production

Hadronic top pair production involves $gg \to t\bar{t}$ and $q\bar{q} \to t\bar{t}$ partonic processes. In SMEFT, effective operators contribute to both processes, as shown in Fig. 1. At the LHC, top pair production is dominated by incoming gluons. At leading order in QCD two operators contribute to this rate,

$$\hat{O}_{tG} = (\bar{Q} \sigma^{\mu\nu} T^{A}) \tilde{G}_{\mu
u}^{A} \quad \text{and} \quad O_{G} = f_{abc} G_{\mu}^{a} G_{\nu}^{b} G_{\rho}^{c}. \quad (2.7)$$

However, $O_{G}$ is strongly constrained by multi-jet production [42, 43],

$$\frac{\Lambda}{\sqrt{g_{s}|C_{G}|}} > 5.2 \text{ TeV}. \quad (2.8)$$

Since this sensitivity is beyond the reach of top pair production, we neglect $O_{G}$ in our analysis. Unfortunately, multi-jet features which lead to this reach in jet production do not help significantly in the top sector [43, 44].

The contribution of $O_{tG}$ to the partonic differential cross section is given by [15]*

$$\frac{d\sigma(gg \to t\bar{t})}{dc_{t}} = \frac{3\alpha_{s}^{2}}{16\sqrt{2}} \frac{\beta_{tt}}{s} \frac{m_{t}v}{\Lambda^{2}} \frac{7 + 9\beta_{tt}^{2}c_{t}^{2}}{1 - \beta_{tt}^{2}c_{t}^{2}} C_{tG} + \mathcal{O}\left(\frac{s v^{2}}{\Lambda^{4} C_{tG}^{2}}\right), \quad (2.9)$$

where $\beta_{tt} = \sqrt{1 - 4m_{t}^{2}}$, $m_{t} = m_{t}/\sqrt{s}$, and $c_{t} = \cos \theta_{t}$ with the scattering angle $\theta_{t}$ of the top against one of the incoming gluons in the partonic center-of-mass (CM) frame. Due to the large gluon luminosity, we expect a high sensitivity to $O_{tG}$ in inclusive top pair production. At high energies $\sqrt{s} \gg m_{t}$, the $O_{tG} - \text{QCD}$ and $O_{tG} - O_{tG}$ interferences scale as $m_{t}v/\Lambda^{2}$ and $v^{2}s/\Lambda^{4}$ relative to the QCD rate, respectively. In the collinear limit, $c_{t} \approx 1$, $O_{tG}$ contributions feature the same logarithmic enhancement as QCD. The kinematics of $O_{tG} - \text{QCD}$ interference is thus similar to QCD, while squared $O_{tG}$ contributions grow with energy relative to the SM. We will discuss the impact of $O_{tG}$ on kinematic distributions in detail in Sec. 4.1.

Compared to the $gg \to t\bar{t}$ contribution, $q\bar{q}$ scattering is suppressed by the parton luminosities. However, the quark-antiquark luminosity is enhanced in the production of boosted tops, where the partons carry a large fraction of the proton’s energy. In this regime,

*Notice that in Ref. [15] the top-gluon operator is defined as twice the $O_{tG}$ in Eq. (2.5).
top pair production is most sensitive to the four-quark operators introduced in Eqs. (2.3) and (2.4) and their interference with $O_{tG}$.

Contributions of four-quark operators are conveniently classified by their behavior under top charge conjugation. The vector current $V$ is odd under charge conjugation, while the axial-vector current $A$ is even. We define vector and axial-vector combinations of Wilson coefficients as

$$
4 C_{VV}^{u,s} = C_{Qq}^{1,s} + C_{Qq}^{3,s} + C_{tu}^{s} + C_{tq}^{s} + C_{Qu}^{s} \\
4 C_{AA}^{u,s} = C_{Qq}^{1,s} + C_{Qq}^{3,s} + C_{tu}^{s} - C_{tq}^{s} - C_{Qu}^{s} \\
4 C_{VA}^{u,s} = -(C_{Qq}^{1,s} + C_{Qq}^{3,s} + C_{tu}^{s} + C_{tq}^{s} - C_{Qu}^{s}) \\
4 C_{VA}^{d,s} = -(C_{Qq}^{1,s} + C_{Qq}^{3,s}) + C_{tu}^{s} - C_{tq}^{s} + C_{Qu}^{s}. 
$$

(2.10)

Pure $VV$, $AA$, $VA$, or $AV$ currents are obtained for

$$|C_{Qq}^{1,u} + C_{Qq}^{3,u}| = |C_{tu}^{u}| = |C_{tq}^{u}| = |C_{Qu}^{u}|. 
$$

(2.11)

The corresponding combinations of the down-type index $d$ can be derived by replacing the index $u \rightarrow d$ and $+C_{Qq}^{3,u} \rightarrow -C_{Qq}^{3,d}$ in Eqs. (2.10) and (2.11). For color-singlet coefficients, we define the same relations by changing all indices 8 → 1 in Eq. (2.10), yielding $C_{VV}^{u,1}$ etc. Neglecting electroweak contributions, the $q\bar{q} \rightarrow t\bar{t}$ partonic rate at LO is then given by $(q = u, d$; cf. Refs. [15] and [45])

$$
\frac{\mathrm{d}\sigma(q\bar{q}\rightarrow t\bar{t})}{\mathrm{d}c_t} = \frac{2\pi\alpha_s^2\beta_{tG}}{9\lambda^2} \left\{ (1 + \beta_{tG}^2/4m_t^2) + \frac{1}{\sqrt{4\pi\alpha_s}} \frac{m_t}{\Lambda} \frac{16}{\sqrt{2}} C_{tG} \\
+ \frac{1}{4\pi\alpha_s} \frac{2s}{\Lambda^2} \left[ (1 + \beta_{tG}^2/4m_t^2) C_{VV}^{q,s} + 2\beta_{tG} C_{AA}^{q,s} \right] \\
+ \frac{1}{4\pi\alpha_s} \frac{s^2}{\Lambda^4} \left[ 4\beta_{tG} C_{VA}^{q,s} \left( C_{VV}^{q,s} C_{AA}^{q,s} + C_{VA}^{q,s} C_{AV}^{q,s} + \frac{9}{2} \left( C_{VV}^{q,s} C_{AA}^{q,s} + C_{VA}^{q,s} C_{AV}^{q,s} \right) \right) \right] \\
+ \frac{1}{4\pi\alpha_s} \frac{m_t vs}{\Lambda^4} \frac{4}{\sqrt{2}} \left( C_{VV}^{q,s} + \beta_{tG} C_{AA}^{q,s} \right) C_{tG} + \mathcal{O}\left( \frac{\sqrt{s}}{\Lambda^4} C_{tG} \right) \right\}, 
$$

(2.12)

with the combinations of color-octet ($\alpha = 8$) and color-singlet ($\alpha = 1$) Wilson coefficients,

$$
|C_{V^+_A}^{q,s}|^2 = |C_{V^+_A}^{q,s}|^2 + |C_{V^+_A}^{q,s}|^2 + |C_{V^+_A}^{q,s}|^2 + |C_{V^+_A}^{q,s}|^2, \\
|C_{V^-_A}^{q,s}|^2 = |C_{V^-_A}^{q,s}|^2 + |C_{V^-_A}^{q,s}|^2 - |C_{V^-_A}^{q,s}|^2 - |C_{V^-_A}^{q,s}|^2 \\
q = u \left( |C_{Qq}^{1,s} + C_{Qq}^{3,s}|^2 + |C_{tu}^{s}|^2 + |C_{tq}^{s}|^2 + |C_{Qu}^{s}|^2 \right) / 4 
$$

(2.13)

$$
|C_{V^+_A}^{q,s}|^2 = |C_{V^+_A}^{q,s}|^2 - |C_{V^+_A}^{q,s}|^2 - |C_{V^+_A}^{q,s}|^2 + |C_{V^+_A}^{q,s}|^2 \\
q = u \left( (C_{Qq}^{1,s} + C_{Qq}^{3,s})C_{tu}^{s} + C_{tq}^{s}C_{Qu}^{s} \right) / 2. 
$$

(2.14)

To understand the operator effects in kinematic distributions, it is instructive to explore their behavior at high CM energies $\sqrt{s}$. The high-energy behavior of the various four-quark contributions and their interference with $O_{tG}$ is summarized in Tab. 2.
Table 2. Relative scaling of operator contributions with respect to QCD in top pair production \((q\bar{q} \rightarrow t\bar{t})\) at high energies \(\sqrt{s} \gg m_t\).

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<th></th>
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<td>(\frac{s^2}{\Lambda^4})</td>
<td>(c_t \frac{s^2}{\Lambda^4})</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>(C^{q,1}_{VV})</td>
<td>(\cdots)</td>
<td>(\cdots)</td>
<td>(\cdots)</td>
<td>(\frac{c_t s^2}{\Lambda^4})</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>(C^{q,1}_{AA})</td>
<td>(\cdots)</td>
<td>(\cdots)</td>
<td>(\cdots)</td>
<td>(\cdots)</td>
<td>(\frac{c_t s^2}{\Lambda^4})</td>
<td>(\cdots)</td>
</tr>
</tbody>
</table>

Dipole operators like \(O_{tG}\) flip the helicity of the top quark and require an insertion of the Higgs vacuum expectation value in the amplitude. Their interference with QCD scales as \(m_t v/\Lambda^2\) and does not feature an enhancement at high energies. Squared \(O_{tG}\) contributions, in turn, grow like \(s v^2/\Lambda^4\) as in the \(gg \rightarrow t\bar{t}\) process. Four-quark operator interferences with QCD and with \(C_{tG}\) grow as \(s/\Lambda^2\) and \(m_t v s/\Lambda^4\) relative to QCD, respectively. Squared terms in four-quark operators grow even stronger with energy, scaling as \(s^2/\Lambda^4\). The strong enhancement at high energies is typical of a four-quark contact interaction, compared to a short-distance interaction through gluon exchange. Top pair production is thus most sensitive to four-quark operators in the tails of kinematic distributions, due to both a kinematic enhancement and an increased quark-antiquark luminosity.

Among the four-quark interactions, only color-octet operators interfere with QCD and with \(C_{tG}\). Color-singlet operators contribute through interference among themselves. The relative factor of 9/2 between quadratic contributions of color-singlet and color-octet operators in Eq. (2.12) is due to the color structure. For color singlets, the rate is proportional to the number of colors \(N_c\) of each quark current, yielding \(N_c^2 = 9\). For color octets, it is proportional to \(\sum AB \text{Tr}(T^A T^B)^2 = (N_c^2 - 1)/4 = 2\).

The sensitivity of the \(q\bar{q} \rightarrow t\bar{t}\) process to the chirality of the top quarks is crucial to distinguish between different four-quark operators. Their interference with QCD or \(O_{tG}\) probes the two combinations \(C^{q,8}_{VV}\) and \(C^{q,8}_{AA}\), i.e., pure vector and axial-vector currents. Interference of two four-quark operators introduces the additional chirality structures from Eq. (2.14). The impact of chiral operators on kinematic distributions can be understood by considering charge-symmetric and -asymmetric differential cross sections

\[
\begin{align*}
\frac{d\sigma^S}{d\Omega} &= \frac{d\sigma(t(p_1)\bar{t}(p_2)) + d\sigma(t(p_2)\bar{t}(p_1))}{d\Omega} \\
\frac{d\sigma^A}{d\Omega} &= \frac{d\sigma(t(p_1)\bar{t}(p_2)) - d\sigma(t(p_2)\bar{t}(p_1))}{d\Omega}
\end{align*}
\]  

(2.15)
where $p_1$ and $p_2$ are the 4-momenta of of the two tops in the final state. In Tab. 3, we list the four-quark coefficients contributing to $\sigma^S$ and $\sigma^A$ in top pair production at LO in QCD. At leading order, 5 chiral combinations of Wilson coefficients per parton contribute. A priori, they can be distinguished by five measurements of different kinematic observables. Charge asymmetries play an important role in this endeavor, since they probe chiral structures that are not accessible in cross sections or other charge-symmetric observables [30]. These observations will be confronted with data in Sec. 4.3, where we show how to use cross sections and asymmetries to gain access to the chirality of the four-quark operators. At NLO, the chiral contributions to $t\bar{t}$ production are modified by QCD corrections, leading to additional kinematic degrees of freedom. In Sec. 4.4, we will elaborate more on NLO effects in kinematic distributions.

### 2.2 Single top production and top decay

Single top production and top decay are both sensitive to operators with weak gauge bosons and in this sense complementary to top pair production. We distinguish $t-$ and $s-$ channel production, as well as associated $tW$ and $tZ$ production. Examples of Feynman diagrams for these processes are shown in Fig. 2.

### Table 3. Four-quark contributions to $t\bar{t}$ production in SMEFT at LO QCD. We separate SM-interference, $\sigma^S,A$, and dimension-6 squared terms, $\sigma^S,A_{kl}$ for charge-symmetric and -asymmetric cross sections.

<table>
<thead>
<tr>
<th>$\sigma^S_k$</th>
<th>$C_{VV}^{q.8}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\sigma^S_{kl}$</td>
<td>$\left</td>
</tr>
<tr>
<td>$\sigma^A_k$</td>
<td>$C_{AA}^{q.8}$</td>
</tr>
<tr>
<td>$\sigma^A_{kl}$</td>
<td>$C_{VV}^{q.8}C_{AA}^{q.8} + C_{VA}^{q.8}C_{AV}^{q.8} + \frac{9}{2}(C_{VV}^{q.1}C_{AA}^{q.1} + C_{VA}^{q.1}C_{AV}^{q.1})$</td>
</tr>
</tbody>
</table>

2.2.1 $t-$ and $s-$channel production

Probe the same set of operators, because the underlying partonic processes $ub \to dt$ and $ud \to tb$ are related by a crossing symmetry. At the level of SM-interference three dimension-6 operators contribute,

\begin{equation}
O_{Q_q}^{3.1} = (\bar{Q}_\gamma \tau^I Q)(\bar{q}_\gamma \gamma^\mu \tau^I q_l)
\end{equation}

\begin{equation}
O_{\phi Q}^3 = (\phi^\dagger iD^\mu \phi)(\bar{Q}_\gamma \gamma^\mu \tau^I Q).
\end{equation}

Since the kinematics of the two channels is different, we also expect a different sensitivity to these operators. The dominant partonic cross sections for $t-$ and $s-$ channel production
are given by [15]

\[
\frac{d\sigma_t(ub \to dt)}{dc_{tu}} = \frac{G_F^2 m_W^4 \beta_t^2}{\pi s (2m_W^2 + \beta_t(1 + c_{tu}))^2} \left\{ 1 + 2 \frac{v^2}{\Lambda^2} C_{\phi Q}^3 + \sqrt{2} \frac{v^2}{\Lambda^2} C_{tW} \frac{m_t}{m_W} (1 + c_{tu}) \right. \\
- \frac{v^2}{\Lambda^2 m_W^2} C_{Qq}^{3,1} \left( 2m_W^2 + \beta_t(1 + c_{tu}) \right) \right\}
\]

\[
\frac{d\sigma_s(u\bar{d} \to \bar{t}b)}{dc_{tu}} = \frac{G_F^2 m_W^4 \beta_t^2}{16\pi s (1 - m_W^2)^2} (1 + c_{tu})(1 + \beta_t c_{tu} + \bar{m}_t^2) \left\{ 1 + 2 \frac{v^2}{\Lambda^2} C_{\phi Q}^3 \right. \\
+ 4\sqrt{2} \frac{v^2}{\Lambda^2} C_{tW} \frac{m_t}{m_W} \frac{1}{1 + \beta_t c_{tu} + \bar{m}_t^2} + \left. 2 \frac{v^2}{\Lambda^2 m_W^2} C_{Qq}^{3,1} (1 - \bar{m}_t^2) \right\}.
\]

Here \( \beta_t = 1 - \bar{m}_t^2, \bar{m}_W = m_W^2/s, \) and \( c_{tu} = \cos \theta_{tu} \) is the cosine of the angle between the top and the incoming up quark in the CM system. We set \( V_{tb} = 1 = V_{ud} \) and neglect all quark masses except \( m_t \). In \( t- \)channel production, the process \( \bar{d}b \to \bar{u}t \) also contributes, but is subdominant due to the smaller parton luminosity. We do not provide analytic expressions for this channel, but include it in the numerical analysis.

The operator \( O_{\phi Q}^2 \) has the same Lorentz structure as the \( tbW \) coupling in weak interactions, so its interference with the SM causes a constant shift in the rate. In turn, the contributions of \( O_{Qq}^{3,1} \) is logarithmically enhanced at high energies, while \( O_{tW} \) scales as \( \ln(s/m_W^2)/s \). In \( s- \)channel production the logarithmic enhancement is absent. In Tab. 4, we summarize the relative scaling of operators with respect to the SM for \( t- \) and \( s- \)channel production.

Once we include dimension-6 squared terms, three additional operators \( O_{Qq}^{3,8}, O_{\phi tb} \) and \( O_{bW} \) contribute to single top production. The operator \( O_{\phi tb} \) does not interfere because of its color structure. The interference of \( O_{\phi tb} \) and \( O_{bW} \) with the SM and all other operators is suppressed by the bottom mass \( m_b \), because \( O_{\phi tb} \) and \( O_{bW} \) involve right-handed bottom quarks. This means that their interference with left-handed currents is helicity-suppressed. The interference between \( O_{\phi tb} \) and \( O_{bW} \) are not \( m_b \)-suppressed and thus much larger than their interference with the SM amplitude.

**Top decay** is sensitive to the operators \( O_{Qq}^{3,1} \) (or operators with two heavy quarks and two leptons in semi-leptonic top decays), \( O_{\phi Q}^3 \) and \( O_{tW} \) in SM-interference. Since the \( W \)-boson in \( t \to bW \to bq\bar{q}' \) decays is on-shell in the observables we consider, the contribution
Associated $tW$ production probes $O_{\phi Q}^3$, $O_{tW}$ and $O_{tG}$ interfering with the SM amplitudes. Obviously, its sensitivity to $O_{tG}$ is much smaller than for top pair production. The operator $O_{\phi Q}^3$ is also probed in $t$-channel and $s$-channel production, and $O_{tW}$ is best probed in top decays. We therefore do not expect much additional information on SMEFT operators from $tW$ production.
**Associated $tZ$ production** is essentially $t-$channel single top production with an additional $Z$-boson in the final state. It probes all operators that contribute to $t-$channel production, as shown in Tab. 1. The contribution of an operator relative to the SM, however, is different for the two processes. In general, $tZ$ production probes operators at higher energies than $t-$channel production, leading to enhanced effects of operators that grow with energy [46]. A larger theoretical sensitivity in $tZ$ production can thus compensate for the lower experimental sensitivity.

In addition, $tZ$ production probes operators that modify the top coupling to the $Z$-boson, namely $O_{\phi Q}^-$, $O_{\phi t}$, and $O_{tZ}$. All three operators interfere with the SM. Their scaling at high energies depends on the polarization of the $Z$-boson and has been studied in detail in Refs. [5, 46]. The operators $O_{\phi Q}^-$ and $O_{\phi t}$ modify the SM $Z$ couplings with left- and right-handed tops, respectively. The main difference is observed in the longitudinal $Z$-mode. While the $O_{\phi Q}^-$–SM interference grows with energy, the $O_{\phi t}$–SM interference requires a helicity flip of the top quark and thus does not feature this growth. Similar considerations apply at the level of $O_{\phi Q}^-$ – $O_{\phi Q}^-$ and $O_{\phi t}$ – $O_{\phi t}$ interference. We therefore expect a higher sensitivity to $O_{\phi Q}^-$ than to $O_{\phi t}$, which we will confirm numerically in Sec. 5. The dipole operator $O_{tZ}$ features a similar energy growth in longitudinal $Z$-production as $O_{\phi Q}^-$, resulting in a sizeable contribution to $tZ$ production.

Associated single top production with a Higgs boson is an interesting channel that complements $tW$ and $tZ$ production [46]. In addition to the gauge operators $tH$ production probes modifications of the top Yukawa coupling. We do not consider $tH$ production in our fit here, but plan to include it in a combined analysis with Higgs observables.

NLO QCD corrections can modify the kinematics of operator contributions in single top production. However, the number of single top observables is large enough to distinguish between all contributing operators already at leading order. We therefore do not investigate NLO contributions in detail here, but include them in our numerical analysis. For $t-$channel single top production and top decay, NLO corrections in SMEFT have been calculated in Refs. [47, 48].

### 2.3 Associated $t\bar{t}W$ and $t\bar{t}Z$ production

Compared with top pair and single top production, associated $t\bar{t}W$ and $t\bar{t}Z$ production do not bring us sensitivity to new operators, but probe them in a different context. The main purpose of including these two processes in our global analysis is to resolve blind directions and to better probe operators that are difficult to access in other channels. Just as for the $tH$ production channel we leave $t\bar{t}H$ production [49] to a future combination with global Higgs analyses.

Associated $t\bar{t}W$ production is sensitive to a subset of the possible four-quark operators. Since the $W$ can only be radiated from the initial state in the SM, only operators with left-handed initial quarks contribute while $RR$ and $LR$ contributions are absent if we neglect light-quark masses. The non-trivial electroweak structure of $t\bar{t}W$ production affects the relative contributions of the weak singlet and triplet operators $O_{Qq}^{1,8}$ and $O_{Qq}^{3,8}$. We will use
this effect to distinguish between these two operators. In the SM, the total rate of $t\bar{t}W$ production is dominated by quark-antiquark interactions, while inclusive $t\bar{t}$ production is gluon-dominated. This means that relative to the SM contribution four-quark operators thus give sizeable effects in the $t\bar{t}W$ rate and we can hope for a good sensitivity to $LL$ and $RL$ operators.

Associated $t\bar{t}Z$ probes the same four-quark operators that enter $t\bar{t}$ production. Similarly to $t\bar{t}W$ production, the emission of the boson changes the relative contributions of four-quark operators with different weak gauge structure. In addition, $t\bar{t}Z$ is sensitive to operators with right-handed up versus down quarks, namely $O_{tu}^8$ and $O_{td}^8$ or $O_{Q_u}^8$ and $O_{Q_d}^8$. In Sec. 4.2, we will disentangle these operators by combining $t\bar{t}$ distributions with $t\bar{t}W$ and $t\bar{t}Z$ production in a global analysis. In addition, we use the $t\bar{t}Z$ process to probe $O_{\phi Q}^-, O_{\phi t}$ and $O_{tZ}$, which are so far constrained by $tZ$ production. In $t\bar{t}Z$ production, all three operators interfere with the SM. The contributions of $O_{\phi Q}^-$ and $O_{\phi t}$ re-scale the SM $Z$-couplings to left- and right-handed tops, but do not change the process kinematics. The dipole operator $O_{tZ}$ changes the kinematic distributions mildly, but its overall effect on the rate is modest [50].

Combining searches for $O_{tA}$ in $t\bar{t}\gamma$ and $O_{tW}$ in top decays is an alternative way to get access to $C_{tZ}$, see Eq. (2.6) and Ref. [51].

3 Global analysis setup

3.1 Data set

The key to any global analysis is the availability of enough measurements to constrain the model parameters. In case of the top sector we confront 22 dimension-6 operators with a much larger number of available measurements shown in Tabs. 5 and 6. The data forms two main parts, measurements of the leading top pair production process mediated by QCD couplings and measurements of processes including a weak coupling. The latter include single top production as well as associated top pair production with electroweak bosons. Because all our measurements are unfolded to the level of stable top quarks, and because there is essentially only one top decay channel leading to a universal branching ratio of one, we can assume SM-like top decays for all measurements except for the $W$ helicity fractions in top decays. Observables combining top production and decay play a special role in the SMEFT interpretation, because they probe features of operators not accessible in top production alone [31, 101–103]. In our analysis, the charge asymmetry described in Sec. 2.1 plays a similar role in probing operators, even though it is based on kinematics of fully reconstructed top quarks.

In terms of the Wilson coefficients of Sec. 2 all our rate observables have the form

$$\sigma = \sigma_{SM} + \sum_k \frac{C_k}{\Lambda^2} \sigma_k + \sum_{k,l} \frac{C_k C_l}{\Lambda^4} \sigma_{kl},$$

(3.1)

where $\sigma_{SM}$ is the SM prediction, $\sigma_k$ are contributions arising from the interference of a single dimension-6 operator with the SM, and $\sigma_{kl}$ arise from the interference of two
<table>
<thead>
<tr>
<th>experiment</th>
<th>$\sqrt{S}$ (TeV) $\mathcal{L}$ (fb$^{-1}$)</th>
<th>channel observable &amp; $K$-factor</th>
<th>#bins</th>
<th>R</th>
<th>M</th>
<th>D</th>
<th>A</th>
</tr>
</thead>
<tbody>
<tr>
<td>$pp \to \bar{t}t$</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>CMS [52]</td>
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<td>$e\mu$</td>
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<td>✓</td>
</tr>
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<td>$ll$</td>
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<td>[59–61]</td>
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<tr>
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<td>$lj$</td>
<td>$A_{\bar{C}C}$</td>
<td>[72]</td>
<td>.</td>
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</tr>
<tr>
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<td>$ll$</td>
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<td>[72]</td>
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<td>$ll$</td>
<td>$A_{\bar{C}C}$</td>
<td>[72]</td>
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<tr>
<td>ATLAS [76]</td>
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<td>139</td>
<td>$lj$</td>
<td>$A_{\bar{C}C}$</td>
<td>[72]</td>
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<tr>
<td>$pp \to \bar{t}tZ$</td>
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<td>77.5</td>
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<td>$\sigma_{\bar{t}tZ}$</td>
<td>[78]</td>
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<tr>
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<td>multi lept.</td>
<td>$\sigma_{\bar{t}tZ}$</td>
<td>[78]</td>
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</tr>
<tr>
<td>$pp \to \bar{t}tW$</td>
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<td>multi lept.</td>
<td>$\sigma_{\bar{t}tW}$</td>
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<td>multi lept.</td>
<td>$\sigma_{\bar{t}tW}$</td>
<td>[78]</td>
<td>.</td>
<td>.</td>
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</tbody>
</table>

**Table 5.** Top-pair observables included in our global analysis. The labels R, M, D, A define four different data sets with rates, rates and invariant mass distributions, distributions only, and asymmetries, used in the numerical analysis of Section 4.

Diagrams containing one operator each. Technically, $\sigma_k$ and $\sigma_{kl}$ are the theory input which Madgraph5_aMC@NLO [33] provides at NLO QCD accuracy.

The SMEFT Lagrangian leads to two main kinds of corrections, as illustrated for top pair production in Tab. 2: operators which change the high-energy behavior of the process through an additional energy dependence of the kind $s/\Lambda^2$ and those which scale merely like $v^2/\Lambda^2$ or $m_t v/\Lambda^2 \approx y_t v^2/\Lambda^2$ compared to the SM. For the latter the leading observables are
<table>
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<th>$\mathcal{L}$ (fb$^{-1}$)</th>
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<td>$\sigma_{tq+\bar{t}q}$</td>
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<tr>
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<td>$e + \mu$</td>
<td>$\sigma_{tq+\bar{t}q}$</td>
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<tr>
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<td>$e + \mu$</td>
<td>$\sigma_{tq}, \sigma_{\bar{t}q}$</td>
</tr>
<tr>
<td>CMS [84] 8</td>
<td>19.7</td>
<td>$e + \mu$</td>
<td>$\sigma_{tq}, \sigma_{\bar{t}q}$</td>
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<tr>
<td>ATLAS [85] 13</td>
<td>3.2</td>
<td>$e + \mu$</td>
<td>$\sigma_{tq}, \sigma_{\bar{t}q}$ [86]</td>
</tr>
<tr>
<td>CMS [87] 13</td>
<td>2.3</td>
<td>$\mu$</td>
<td>$\sigma_{tq}, \sigma_{\bar{t}q}$ [86]</td>
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<tr>
<td><strong>$s$-channel</strong></td>
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<tr>
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<td>5.1</td>
<td>$\mu$</td>
<td>$\sigma_{tb+\bar{t}b}$</td>
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<td>CMS [88] 8</td>
<td>19.7</td>
<td>$e + \mu$</td>
<td>$\sigma_{tb+\bar{t}b}$</td>
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<td>$e + \mu$</td>
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Table 6. Observables included in the single top fit, in analogy to Tab. 5.

rate measurements or the total cross section, because they offer the best statistics and often minimize theoretical uncertainties. From global Higgs-electroweak analyses we know that a modified momentum dependence can be constrained most efficiently by high-energy tails of kinematic distributions or simplified template cross sections [8–13]. Similarly, we know that for many kinematic distributions the few bins with the highest momentum transfer include the relevant information on individual operators, whereas for several operators with a different high-energy behavior there often exist several relevant regimes [104].

†Note that for a distribution to constrain a dimension-6 contribution in this phase space region it is not necessary that we actually observe the SM process in the same phase space region [12].
Unlike in the Higgs sector, cross section measurements in the top sector are reported such that we can easily compare them to parton-level predictions. Kinematic distributions are typically reported as normalized distributions, i.e. they integrate to one and can be combined with total rate measurements without double-counting information. A problem arises when we include operator contributions to the distribution in the numerator and to the rate in the denominator. In this case the normalized bin entries entering our fit become correlated and develop a distinct non-linear behavior.

3.2 SFitter analysis

For our global LHC analysis we use the SFitter framework [35, 36], which focuses on a proper treatment of uncertainties in a conservative frequentist approach. We extract the statistical uncertainties and a leading set of up to ~ 20 systematic uncertainties for each experiment and simulate a Gaussian shape of the completely exclusive likelihood for statistics and systematics. For the systematic uncertainties we also allow for correlations within the same experiment, collider energy scale, and top signature. This applies for example to jet uncertainties like the jet energy scale or the jet efficiencies. An exception is the uncertainty on the luminosity, which we correlate for all channels and both experiments. In order to simplify the treatment of uncertainty correlations, we fit only one observable from each experimental analysis, and we never take two measurements of the same observable at the same energy scale. Moreover, for total rates and charge asymmetries we fit only two observables, one for each collider energy, obtained with weighted averages of the measurements performed with different experiments and datasets.

In addition to the experimental sources of uncertainties, theoretical error bars reflect missing higher orders in the perturbative series. Precise predictions are crucial to extract any Lagrangian parameter from LHC rate measurements. We rely on NLO predictions for $t\bar{t}$ and single top observables in SMEFT using Madgraph5_aMC@NLO, while we use LO QCD predictions for the statistics-limited $t\bar{t}V$ rates. For the central values we add NNLO $K$-factors in the SM, whenever available, to account for the most precise predictions available (see Tabs. 5, 6). This means we assume that the operator contributions scale like the SM rate beyond NLO. The only exception is the charge asymmetry, that does not scale multiplicatively with higher-order corrections. In this case we fit the sum of the most precise available SM prediction and the new physics corrections at (N)LO from Madgraph5_aMC@NLO.

The theoretical uncertainties are obtained by varying the renormalization and factorization scales by a factor of two around the respective central scale choices. Since technically we cannot distinguish the uncertainties due to operator effects, we use the scale uncertainties on the SM prediction from our NLO simulations as an overall theory uncertainty on the observable. This gives for instance a 12% uncertainty for the combined SM and dimension-6 $t\bar{t}$ and $t\bar{t}V$ rates. Regarding higher-order corrections, our estimate based on the NLO scale dependence in the presence of dimension-6 effects is likely to be conservative for small new physics effects [105]. Since NLO corrections to the non-SM contributions are included in
our simulations, we generally expect QCD effects beyond NLO to be moderate. Exceptions occur in single top production, where SM QCD effects first occur beyond tree level, or in bins of kinematic distributions near the endpoints of the spectrum. Whenever the scale uncertainty in the NLO simulation for such rate measurements happens to be very small we replace it by a minimum of 10%. Similarly, when strong cancellations of scale uncertainties occur in normalized kinematic distributions, we replace the theoretical uncertainty in each bin by 2% whenever the scale variation drops below this level [106, 107].

In SFitter all theoretical uncertainties are modelled as a flat likelihood within the quoted error band. This applies to the theoretical uncertainties on the signal as well as the theoretical uncertainties on the background, quoted in the experimental analyses. If we combine them with Gaussian experimental uncertainties in a profile likelihood this leads to the RFit scheme [108]. Theoretical uncertainties are generally uncorrelated unless they describe the same fiducial volume at the same collider energy. This also includes the theoretical errors for individual bins in a kinematic distribution, which we assume to be uncorrelated. Uncertainties from the limited precision of parton densities are evaluated in analogy to the theoretical uncertainties reflecting the missing higher orders in the hard process. We evaluate them using a set of 209 predictions from the NNPDF3.0 NLO set with $\alpha_s(m_Z) = 0.118$ [109], the MMHT2014NLO set at 68% CL [110], and the CT14NLO set [111]. A typical error bar from the parton distribution functions (PDFs) is 6% for the $t\bar{t}$ or $t\bar{t}V$ rates. Because we assume a flat likelihood for these PDF uncertainties, the profile likelihood combination of higher-order and PDF uncertainties adds the two error bars linearly.

To probe the parameter space we rely on Markov chains, similar to Ref. [8], rather than the numerically more complex toy measurements used in Ref. [12]. To cover the full 22-dimensional parameter space we use up to 2000 Markov chains giving up to 400 million parameter points. This defines our fully exclusive likelihood which we then profile down to two and one relevant dimensions.

4 Top pair features

Before entering a global analysis of the top sector we study some of the underlying features in detail. This is essential for the top-pair side of the analysis. Its unique challenges are very different from the electroweak-Higgs sector [8, 10–12] and the single top sector discussed in Sec. 5.

In top pair production the operator $O_{tG}$ induces large corrections to the total and differential rates, as it is the only operator modifying the gluon-induced production process. We discuss its known and expected behavior in Sec. 4.1 and roughly estimate the expected sensitivity of our global fit.

The new feature in top pair production is the large set of four-quark operators affecting the partonic process $q\bar{q} \rightarrow t\bar{t}$. Fourteen such operators, different in their QCD and electroweak structure, contribute to one and the same process. Since top pair production
is a QCD process, most of its observables average or sum over the electroweak properties of the external particles. To distinguish these operators we rely on the observables
\[ \left\{ \sigma_{\text{tot}}, \frac{d\sigma}{dm_{\bar{t}t}}, \frac{d\sigma}{dp_{T,t}}, \frac{d\sigma}{d\Delta y_{t\bar{t}}}, A_C \right\} \] (4.1)
supplemented by \( p_{T,t} \) and \( m_{\bar{t}t} \) distributions in the boosted region. In Secs. 4.2 to 4.4 we will study how the gauge and chiral structure of four-quark operators can be resolved by dedicated \( t\bar{t} \) measurements. This allows us to break some of the flat directions in model space already at LO in the EFT analysis, where only the tree-level interference between the SM and the dimension-6 operators are considered.

Finally, in Sec. 4.5 we will study the effect of dimension-6-squared contributions on the sensitivity to operators. We will see that the flat directions turn into compact circles which allow us to derive more stringent limits on individual operators.

### 4.1 Event kinematics

Before we study the effects of specific dimension-6 operators on top pair production, we roughly estimate the reach of our analysis for operators affecting the total rate and for operators affecting the event kinematics. The top-gluon dipole operator \( O_{tG} \) is the only top EFT contribution to the leading partonic process \( gg \to t\bar{t} \). We therefore expect a high sensitivity to \( O_{tG} \) in inclusive top pair production. In contrast, four-quark operators contribute only to the \( q\bar{q} \to t\bar{t} \) process, which is subleading, but enhanced at high energies. We thus expect the best sensitivity to four-quark operators in tails of kinematic distributions.

In our analysis, all distributions are normalized to the total rate. These normalized distributions are direct probes of the dynamics of operator contributions relative to the SM. To illustrate this important point, we compare the event kinematics of the dipole operator \( O_{tG} \) with the four-quark operator \( O_{8tu} \). The normalized \( m_{\bar{t}t} \) distribution depends on these two operators as (neglecting \( O_{tG} - QCD \) interference)

\[
\frac{1}{\sigma} \frac{d\sigma}{dm_{\bar{t}t}} \approx \frac{\sigma_{\text{SM}}(m_{\bar{t}t})}{\sigma_{\text{SM}}(2m_t)} \left( 1 + \mathcal{O}(m_{t\bar{t}} - m_t) \frac{|C_{tG}|^2}{\Lambda^2} + \mathcal{O} \left( m_{\bar{t}t}^2 - (2m_t)^2 \right) \frac{|C_{8tu}|^2}{\Lambda^4} \right)
\]

(4.2)

Here \( 2m_t \) denotes the invariant mass close to the production threshold, which dominates in the total cross section, while \( m_{\bar{t}t} \) can be much higher in differential distributions. Since the \( O_{tG} - QCD \) interference does not feature an energy enhancement, it cancels almost completely in normalized distributions. Kinematic distributions are therefore expected to lead to relatively weak constraints driven by the \( |C_{tG}|^2 \) term. In contrast, the four-quark contribution of \( O_{8tu} \) features an energy enhancement already at \( \mathcal{O}(\Lambda^{-2}) \). This leads to a good sensitivity at high energies, despite the relative suppression by the parton luminosity. Total rates and distributions are thus complementary in probing dipole operators and
Figure 3. Contribution of $O_{tG}$ and $O_{8tu}^8$ to total $\bar{t}t$ rates (left) and the normalized $p_T$ distribution of a hadronically decaying top (right). The shaded regions correspond to the 68% CL from a simultaneous fit to the two rates and the distribution. The grey shaded regions show the contribution from $O_{tG}$ (rates) and $O_{8tu}^8$ (distribution) at order $\Lambda^{-2}$. The red and blue shaded regions show the contribution from $O_{tG}$ and $O_{8tu}^8$ to order $\Lambda^{-4}$, respectively.

four-quark operators. Notice that in our numerical analysis we keep the full operator contributions in the normalization of distributions.

The reach of measurements of total cross sections at 8 TeV and 13 TeV and a $p_T$ distribution at 13 TeV is estimated for $O_{tG}$ and $O_{8tu}^8$ in Fig. 3.

The upper-left panel shows the averaged cross section measurements with their combined uncertainties. Similarly, the upper-right panel shows the normalized $p_T$ distribution for the hadronically decaying top at 13 TeV from Ref [67] (see Tab. 5). The two lower panels show the relative deviations from the SM prediction and the 68% CL limits from a combined analysis of $C_{tG}$ and $C_{8tu}^8$ to the small data set consisting of only the observables shown in Fig. 3. The grey panels show the result from the new physics interference at order $\Lambda^{-2}$ for $C_{tG}$ in terms of the total rates and for $C_{8tu}^8$ in terms of the kinematic distribution, corresponding to the 68% CL ranges

$$C_{tG}/\Lambda^2 \in [-0.19, 0.78]/\text{TeV}^2 \quad C_{8tu}^8/\Lambda^2 \in [-6.77, -0.57]/\text{TeV}^2.$$  (4.3)

The limits are slightly asymmetric, because the top quarks in the normalized distribution are softer than in the SM expectation.

For the red ($O_{tG}$) and blue ($O_{8tu}^8$) shaded regions we also include the contributions to order $\Lambda^{-4}$ and find at 68% CL

$$C_{tG}/\Lambda^2 \in [-0.07, 0.58]/\text{TeV}^2 \quad C_{8tu}^8/\Lambda^2 \in [-1.72, 0.26]/\text{TeV}^2.$$  (4.4)

While these limits are just based on a small fit to three observables, they give us an intuition of what to expect from our fit. For $C_{tG}$ an expected range around $\Lambda/\sqrt{|C_{tG}|} = 1.3$ TeV
Figure 4. Normalized likelihood as a function of $C_{tG}$ (left) and a $C_{tu}^8$ (right) in individual fits at LO to order $\Lambda^{-2}$. We show fits to the R (blue) and D (yellow) observable sets of Tab. 5, and to all $t\bar{t}$ observables in Tab. 5 (red). In the right panel, we do not show the R likelihood, as it is 1 for all the values of $C_{tu}^8$ in the displayed range.

saturates the error bars of the leading total rate measurement, while for the four-quark operator $C_{tu}^8$ values around $\Lambda/\sqrt{|C_{tu}^8|} = 0.7$ TeV can be expected from this one kinematic distribution. Comparing these limits to the kinematic range probed by the $p_T$ distribution in Fig. 3, we see that the effective theory interpretation is valid for an underlying theory that does not predict propagating new states at the LHC and is not too strongly coupled.

In Fig. 4 we show how total rates and normalized kinematic distributions lead to very different likelihood distributions. First, rate measurements alone have a strong constraining power on $C_{tG}$ compared to four-quark operators, due to the SMEFT correction being relatively large. The likelihood from normalized distribution is strongly asymmetric: negative values of $C_{tG}$ are strongly limited by the physical requirement that the bin content of all the measured distributions remains positive. Positive values of $C_{tG}$, on the other hand, are less constrained as discussed in the previous section. More specifically, let $n_k$ be the number of entries in $k$-th bin of a normalized distribution. As a function of the SM ($n_k^{SM}$) and SM-$C_{tG}$ interference ($n_k^{int}$) contributions, it scales as

$$\frac{n_k^{SM} + n_k^{int}C_{tG}/\Lambda^2}{\sum_l (n_l^{SM} + n_l^{int}C_{tG}/\Lambda^2)} \xrightarrow{C_{tG} \to \infty} \frac{n_k^{int}}{\sum_l n_l^{int}}.$$  \hspace{1cm} (4.5)

For large values of $C_{tG}/\Lambda^2 \to \infty$ the normalized bin content becomes a constant. As noted in Eq. 4.2, $C_{tG}$ is characterized by a kinematic behavior very similar to that of the SM, which leads to values $n_k^{int}/\sum_l n_l^{int}$ generally compatible with $n_k^{SM}/\sum_l n_l^{SM}$. As a consequence the corresponding log-likelihood also converges to constant $> 0$. This asymptotic behavior is not observed once quadratic terms are included, because the sensitivity to $C_{tG}$ is enhanced by $sv^2/\Lambda^4$ in high-energy bins, see Eq. (4.2) and Tab. 2. Combining all $t\bar{t}$
measurements the likelihood recovers a fairly symmetric form, but with a distinct shift of the minimum towards small positive values of $C_{tG}$.

For comparison, the asymptotic behavior in the linear fit is not observed for an interfering four-quark operator like $C_{tu}^8$, because it induces a significantly different shape in the kinematic distributions compared to the SM, scaling as $s/\Lambda^2$. Large values of the Wilson coefficients are therefore strongly disfavored by at least one of the bin measurements that drive the log-likelihood towards zero. In the right panel of Fig. 4, we show that $C_{tu}^8$ is well constrained by measurements of normalized distributions. Total rates have little impact on the fit results.

4.2 Incoming up versus down quarks

The set of four-quark operators laid out in Eq. (2.3) and Eq. (2.4) span all possible assignments of the quark fields to representations the SM symmetry groups:

1. chirality of the light quark and top quark currents;
2. left-handed currents: singlet or triplet under $SU(2)_L$;
3. right-handed currents: up- or down-type light quarks;
4. singlet or octet color contraction of the currents.

Top pair production through strong interactions is not sensitive at parton level to the nature of the incoming quarks, i.e., questions 2 and 3. However, up-type and down-type quarks in the initial state are distinguished by the parton densities. The relative $u\bar{u}$ and $d\bar{d}$ contributions to the $t\bar{t}$ final state are determined by

$$r(x) = \frac{f_u(x)f_\bar{u}(s/(xS))}{f_d(x)f_\bar{d}(s/(xS))}. \quad (4.6)$$

Here $f_p(x, s)$ denotes the usual parton distribution of parton $p$ with momentum fraction $x$ of the energy $\sqrt{s}/2$ in the proton. $\sqrt{S}$ is the hadronic CM energy, and we suppressed the factorization scale choice. Around the valence quark maximum $x \approx 0.1$ the ratio becomes $r \approx 2$. For most observables used in our analysis, the ratio integrated over the relevant phase-space region varies roughly in the range

$$1.5 \lesssim r \lesssim 3. \quad (4.7)$$

In what follows we refer to $r$ as (roughly) the relative contribution up partonic up- and down-quark contributions to an observable. In what follows we discuss how the isospin of the incoming quarks can be disentangled in a minimal EFT analysis of $t\bar{t}$ production, neglecting quadratic EFT contributions and NLO QCD corrections.

Let us consider pairs of four-quark operators that are only distinguished by the nature of initial quarks: if the latter are right-handed, as in $O_{tu}^8$ and $O_{td}^8$, $t\bar{t}$ observables depend
Figure 5. Up-type versus down-type (left) and weak isospin (right) effects of four-quark operators from LO two-parameter fits to order $\Lambda^{-2}$. Solid and dashed lines mark the Gaussian equivalent of $\Delta \chi^2 = 1, 4$ from fits to: set $M$ of $t\bar{t}$ observables (red, see Tab. 5), highest-energy bins of a $t\bar{t}$ distribution in the boosted regime, $t\bar{t}Z$ rates (orange), $t\bar{t}W$ rates (blue). The shaded areas show the combined fit.

on the combination of Wilson coefficients

$$r C_{tu}^8 + C_{td}^8 \approx 2 C_{tu}^8 + C_{td}^8. \tag{4.8}$$

If the initial quarks are left-handed, their nature is only distinguished by a singlet versus triplet $SU(2)$ structure, as in $O_{Qq}^{1,8}$ and $O_{Qq}^{3,8}$. In this case the typical combination is

$$(r + 1) C_{Qq}^{1,8} + (r - 1) C_{Qq}^{3,8} \approx 3 C_{Qq}^{1,8} + C_{Qq}^{3,8}. \tag{4.9}$$

The numerical estimate $r \approx 2$ holds for the bulk of the phase space in top pair production. On the other hand, measurements that select highly boosted tops can probe higher parton momentum fractions $x$ and larger ratios $r$, thus constraining different directions in the EFT space.

To illustrate this effect, Figure 5 shows bounds on these two pairs of operators obtained from two-dimensional likelihood fit of top–anti-top observables to LHC data.

The red contours use set ‘$M$’ of Table 5, that contains rates and normalized $m_{t\bar{t}}$ distributions. These observables are most sensitive to quark-antiquark contributions around the maximum of the parton distributions in $x$, where $r \approx 2$. They leave the directions $(1, -2)$ for $(C_{tu}^8, C_{td}^8)$ and $(1, -3)$ for $(C_{Qq}^{1,8}, C_{Qq}^{3,8})$ essentially unbounded, as is expected from the relations in Eqs. (4.8) and (4.9).

Boosted top pair production [20] probes larger momentum fractions $x$ and hence larger ratios $r$. The black contours in Fig. 5 show the likelihood obtained by fitting the last bins of a $p_{T,t}$ distribution in the boosted regime, $p_{T,t} > 500$ GeV. The blind directions of this fit
are tilted compared to the previous analysis. They run roughly along \((1,-3)\) for \((C_{tu}^8, C_{td}^8)\) and along \((1,-2)\) for \((C_{Qq}^{1,8}, C_{Qq}^{3,8})\), which corresponds to \(r \approx 3\). Adding boosted top–anti-top observables thus breaks the blind directions in inclusive top–anti-top production, but only mildly.

To better resolve the weak gauge structure, we include \(t\bar{t}Z\) and \(t\bar{t}W\) production in the fit. As mentioned in Sec. 2.3, the radiation of the gauge boson changes the relative contributions of operators with different weak gauge structure. For operators with right-handed light quarks, only \(t\bar{t}Z\) production is relevant. At \(O(\Lambda^{-2})\), the contribution to the \(t\bar{t}Z\) rate depends on the Wilson coefficients as

\[
\sigma_{t\bar{t}Z}^{\text{int}} = \left( r C_{tu}^8 + C_{td}^8 \right) \sigma_{ff} + \left( r |g_{uZ}|^2 C_{tu}^8 + |g_{dZ}|^2 C_{td}^8 \right) \sigma_{ii} \quad (4.10)
\]

\[
+ \left( r g_{uZ}^R C_{tu}^8 + g_{dZ}^R C_{td}^8 \right) \sigma_{if} .
\]

The three terms correspond to final–state radiation (\(\sigma_{ff}\)), initial–state radiation (\(\sigma_{ii}\)), and interference between initial– and final–state radiation (\(\sigma_{if}\)) of the \(Z\)-boson. The quark couplings to the \(Z\)-boson are defined as \(g_{uZ}^R = -\frac{2}{3} s_w^2\), \(g_{dZ}^R = \frac{1}{3} s_w^2\), \(g_{uZ}^L = \frac{1}{2} - \frac{2}{3} s_w^2\), and \(g_{dZ}^L = -\frac{1}{2} + \frac{1}{3} s_w^2\). The term \(\sigma_{ff}\) includes contributions with \(Z\) couplings to left- and right-handed top quarks. By comparing with Eq. (4.8), we see that \(t\bar{t}Z\) production probes a different direction in the \(C_{tu}^8 - C_{td}^8\) parameter space than inclusive \(t\bar{t}\) production.

Operators with left-handed quarks and different weak isospin can be probed in both \(\bar{t}tZ\) and \(t\bar{t}W\) production. In \(t\bar{t}Z\) production, they contribute at \(O(\Lambda^{-2})\) as\(^4\)

\[
\sigma_{t\bar{t}Z}^{\text{int}} = \left( (r + 1) C_{Qq}^{1,8} + (r - 1) C_{Qq}^{3,8} \right) \sigma_{ff} \quad (4.11)
\]

\[
+ \left( (r |g_{uZ}^L|^2 + |g_{dZ}^L|^2) C_{Qq}^{1,8} + (r |g_{uZ}^L|^2 - |g_{dZ}^L|^2) C_{Qq}^{3,8} \right) \sigma_{ii}
\]

\[
+ \left( (r g_{uZ}^L + g_{dZ}^L) C_{Qq}^{1,8} + (r g_{uZ}^L - g_{dZ}^L) C_{Qq}^{3,8} \right) \sigma_{if} .
\]

In \(t\bar{t}W\) production, the parton luminosity for operators with different weak isospin structure is the same, since all operators with left-handed light quarks contribute to the same partonic processes, dominantly \(ud \rightarrow t\bar{t}W^+\) and \(d\bar{u} \rightarrow t\bar{t}W^-\), respectively. Associated \(t\bar{t}W^+\) production probes the following direction in the \(C_{Qq}^{1,8} - C_{Qq}^{3,8}\) plane at \(O(\Lambda^{-2})\),

\[
\sigma_{t\bar{t}W^+}^{\text{int}} = C_{Qq}^{1,8} C_{Qq}^{3,8} \sigma_{uu} + C_{Qq}^{1,8} C_{Qq}^{3,8} \sigma_{dd} + C_{Qq}^{1,8} C_{Qq}^{3,8} \sigma_{ud} \quad (4.12)
\]

\[
\approx C_{Qq}^{1,8} (\sigma_{uu} + \sigma_{dd}) + C_{Qq}^{3,8} \sigma_{ud} .
\]

Here \(\sigma_{uu}\) and \(\sigma_{dd}\) denote cross section contributions where the \(W^+\) boson is radiated off an incoming anti-down or up quark, which probes the operators \(O_{Qq}^{1,8}\) and \(O_{Qq}^{3,8}\) through their \((\bar{u}u)(\bar{t}t)\) and \((d\bar{d})(\bar{t}t)\) contributions, respectively. In \(\sigma_{ud}\) the \(W^+\) is radiated off an anti-bottom quark in the final state, probing \(O_{Qq}^{3,8}\) through its \((du)(\bar{t}b)\) contribution. The contribution of \(O_{Qq}^{3,8}\) largely cancels between \(\sigma_{uu}\) and \(\sigma_{dd}\), so that the total cross section is

\(^4\)Note that \(\sigma_{ff}, \sigma_{ii}\) and \(\sigma_{if}\) are generic symbols for the contributions to the total \(t\bar{t}Z\) cross section, so their meaning is different in Eq. 4.10 and in Eq. 4.11.
sensitive to $O^{3,8}_{Qq}$ mostly through final state radiation. Very similar considerations hold for $t\bar{t}W^-$ production. In summary, $t\bar{t}W$ production probes a third direction in the $C^{1,8}_{Qq} - C^{3,8}_{Qq}$ plane, in addition to $t\bar{t}$ and $t\bar{t}Z$ production.

In Fig. 5, we show the impact of cross section measurements at 13 TeV for $t\bar{t}Z$ (orange) and $t\bar{t}W$ (blue). For the $RR$ operators $C^8_{tu}$ and $C^8_{td}$ (left panel), $t\bar{t}Z$ production probes indeed a different direction than inclusive $t\bar{t}$ production, leaving a band along $(1, -0.8)$ unconstrained. However, the sensitivity of the $t\bar{t}Z$ cross section to $RR$ operators is much lower than in $t\bar{t}$ production. In the combined fit, shown as a blue area, the remaining blind direction is thus aligned with boosted top pair production. Differential $t\bar{t}Z$ distributions can help to resolve this direction, featuring a better sensitivity to four-quark operators at high energies, similar to $t\bar{t}$ production [77].

The situation is different for $LL$ operators, as we show in the right panel of Fig. 5. Associated $t\bar{t}Z$ and $t\bar{t}W$ production probe similar directions in $(C^{1,8}_{Qq}, C^{3,8}_{Qq})$, leaving blind directions along roughly $(1, 4.7)$ and $(1, 2.8)$ respectively. Remarkably, the sensitivity of $t\bar{t}Z$ and $t\bar{t}W$ cross sections to $LL$ operators is comparable to that of differential $t\bar{t}$ distributions. In $t\bar{t}W$ production, both SM and dimension-6 contributions are induced by quark-antiquark interactions. Compared to the SM rate, effects of $LL$ operators are thus larger than in $t\bar{t}$ production, which is dominated by gluon-gluon interactions. In $t\bar{t}Z$ production the sensitivity to $LL$ operators is much larger than for $RR$ operators. This is due to the different $Z$-couplings to left- and right-handed quarks, $|g^L_{uZ}|/|g^R_{uZ}| \approx 2.4$ and $|g^L_{dZ}|/|g^R_{dZ}| \approx 5.8$, which affect the operator contributions, see Eqs. (4.10) and (4.11). This makes $t\bar{t}W$ and $t\bar{t}Z$ production valuable probes of $LL$ four-quark operators, complementary to $t\bar{t}$ production.

### 4.3 Top chirality from charge asymmetry

One way to directly access the chiral structure of four-quark operators is through observables like charge asymmetries, as discussed in Sec. 2.1. At the LHC it has been measured in terms of absolute top and anti-top rapidities,

$$A_C = \frac{\sigma(\Delta|y| > 0) - \sigma(\Delta|y| < 0)}{\sigma(\Delta|y| > 0) + \sigma(\Delta|y| < 0)} \quad \text{with} \quad \Delta|y| = |y_t| - |y_{\bar{t}}|. \quad (4.13)$$

In QCD such an asymmetry arises only at NLO. In SMEFT, it is induced at LO by four-quark contributions. For illustration, we consider the two operators $O^1_{Qq}$ and $O^8_{tq}$ with a left-handed light-quark current and different chirality of the top current. Since both operators are weak singlets, there is no distinction between up and down quarks. Now the chiral coefficients from Eq. (2.10) are given by

$$4C^{q,8}_{VV} = C^{1,8}_{Qq} + C^8_{tq} = -4C^{q,8}_{VA}, \quad 4C^{q,8}_{AA} = C^{1,8}_{Qq} - C^8_{tq} = -4C^{q,8}_{AV}. \quad (4.14)$$

To leading order QCD, the charge asymmetry depends on the corresponding Wilson coefficients as

$$A_C = \frac{\sigma_{AA} (C^{1,8}_{Qq} - C^8_{tq})}{\sigma_{SM} + \sigma_{VV} (C^{1,8}_{Qq} + C^8_{tq})}, \quad (4.15)$$
Here \( \sigma_{\text{SM}} \) is the SM \( \tilde{t}\tilde{t} \) rate, \( \sigma_{VV} \) and \( \sigma_{AA} \) denote the contributions proportional to \( 4C_{VV} \) and \( 4C_{AA} \) (see Eq. (2.12)), and the sum over all \( q\bar{q} \) parton contributions is implicit. This expression is easily inferred from Eq. (2.12), observing that the charge asymmetry probes the linear terms in \( c_t \) in the partonic cross section. From the definition of \( C_{AA} \) in Eq. (2.10), we also see that \( A_C \) is sensitive to \( (LL - RL) + (RR - LR) \), thereby distinguishing between left- and right-handed top quarks.

For the operator pair we have chosen, charge-symmetric observables probe the \((1, 1)\) direction in \( (C_{Qq}^{1,8}, C_{tq}^{8}) \), which corresponds to a vector-like top coupling. The charge asymmetry is sensitive to the \((1, -1)\) direction, which corresponds to an axial-vector-like top coupling. The corresponding flat directions can be seen in the left panel of Fig. 6, where we show bounds on the Wilson coefficients \( (C_{Qq}^{1,8}, C_{tq}^{8}) \) from a fit to measurements of total cross sections and \( m_{t\bar{t}} \) distributions labelled ‘M’ in Tab. 5 (red lines) and of the charge asymmetries \( A_C \) (black lines). The shaded blue region shows the combined fit with both datasets, which probes both vector and axial-vector currents with top quarks and breaks the respective blind direction in \( \sigma \) or \( A_C \).

The same behavior applies to operators with right-handed initial quarks, like \( O_{tu}^8 \) and \( O_{Qq}^8 \). As shown in Fig. 6, right, their effects on \( \sigma \) and \( A_C \) at order \( \Lambda^{-2} \) are the same as in Eq. (4.14), just replacing \( C_{Qq}^{1,8} \rightarrow C_{tu}^{8}, C_{tq}^{8} \rightarrow C_{Qq}^{8} \).
Figure 7. Left: rapidity of top (plain curves) and anti-top (dashed curves) in $pp \rightarrow t\bar{t}$ for the SM-interference of the LR (green) and RR (purple) four-quark operators. Right: jet transverse momentum distribution in $pp \rightarrow t\bar{t}j$ for the SM-interference.

4.4 Top chirality from jet radiation

As an alternative to the asymmetry in the previous section we can also use patterns in QCD jet radiation to distinguish four-quark operators with different chirality structures. For instance the operators $O^8_{tu}$ (RR) and $O^8_{Qu}$ (LR) differ only in the chirality of the top quark. Their leading contribution to top pair production is the same for the inclusive rate and for any charge-symmetric observable, which probe $C_{VV}^{u,8} \propto C^8_{tu} + C^8_{Qu}$ and $|C_{VV+}^{u,8}|^2 \propto |C^8_{tu}|^2 + |C^8_{Qu}|^2$, cf. Eq. (2.10). However, the two operators are distinguishable in top rapidity distributions, as shown in the left panel of Fig. 7.

Here $O^8_{tu}$ gives more forward or backward tops, compared to $O^8_{Qu}$ which leads to more central tops. These different rapidity distributions are directly related to the angular distribution of the top quark in the CM frame of the collision (cf. Eq. (2.12)),

$$\frac{d\sigma(u\bar{u} \rightarrow t\bar{t})}{d\cos \theta_t} \propto (1 + 2\beta_{tt} \cos \theta_t + 4m^2 + \beta_{tt}^2 \cos^2 \theta_t) C^8_{tu} + (1 - 2\beta_{tt} \cos \theta_t + 4m^2 + \beta_{tt}^2 \cos^2 \theta_t) C^8_{Qu},$$

where $\theta_t$ is the angle between the incoming up quark and the top. In that sense the contribution of the RR operator is ‘forward’ whilst the LR operator contributes as ‘backward’.

Combined with the color structure this directionality implies that an additional jet can break the degeneracy of the two operators. In the hard process $q\bar{q} \rightarrow t\bar{t}$ the triplet color charge flows from the incoming quark to the top quark and from the anti-quark to the anti-top. This leads to a stronger acceleration of color, and consequently more QCD radiation, when the top is produced backwards compared to forwards in the $q\bar{q}$ frame. The same effect can be seen in the context of the top rapidity asymmetry [112]. The additional radiation when the top is backwards pushes the recoiling top–anti-top pair to higher transverse momentum. Indeed, in the right panel of Fig. 7 we find that $O^8_{Qu}$ gives a harder jet $p_T$ distribution than $O^8_{tu}$. The same effect can be seen in the invariant mass distribution, where $O^8_{Qu}$ gives a harder $m_{t\bar{t}}$ distribution.
Figure 8. Left: top pair invariant mass distribution in $pp \rightarrow t\bar{t}$ at NLO for the SM-interference of the RR and LR operators. Right: top pair invariant mass distribution in $p\bar{p} \rightarrow t\bar{t}$ at NLO in QCD. By ‘forward’ we denote events with $y_t > 0$ and by ‘backward’ events with $y_t < 0$.

The jet kinematics of the operator contributions illustrate the impact of NLO corrections in inclusive top–anti-top production. At NLO both the real and virtual corrections break the operator degeneracy in the $t\bar{t}$ distributions. The invariant mass distribution in $t\bar{t}$ production at NLO is shown in the left panel of Fig. 8. Now the RR operator $O_{tu}^8$ gives the harder distribution, implying that the virtual corrections have a large effect in the opposite direction of the real emission. The difference between the LR and RR operators at NLO reaches 20% in the distributions.

To clarify the interplay between virtual and real corrections, we perform a comparison between forward and backward tops in QCD. For a cleaner comparison, we use $p\bar{p}$ collisions that are dominated by the $q\bar{q}$ partonic initial state. We define forward top quarks as emitted in the direction of the proton and use positive and negative rapidities to define forward and backward tops. In the right panel of Fig. 8 we show the NLO distributions in $p\bar{p} \rightarrow t\bar{t}$ separately for forward and backward tops. The results confirm that real radiation behaves differently from the total rate at NLO, given by the sum of Born, virtual and real corrections. This means that NLO QCD corrections break the degeneracy of operators that occurs at LO. Our example demonstrates the potential of using NLO QCD corrections more generally to distinguish between operators.

4.5 Quadratic terms and flat directions

The dependence of the observables on effective operators changes significantly if we include contributions to order $\Lambda^{-4}$. This is particularly true for four-quark operators that do not interfere with the SM amplitude to leading order because of their color or helicity structure. For these operators, quadratic contributions can be the leading effect in an observable. For operators that interfere with the SM quadratic terms can change the bounds from LHC measurements significantly, for instance in case of strong cancellations between linear and quadratic contributions or in case of limited sensitivity. A dominance of quadratic terms is thus per se not a problem with the convergence of the effective theory, but can be due to a distinctive physics pattern which suppresses the naively leading contribution. In general,
an effective field theory approach is justified if a heavy particle can be decoupled for a given observable. This does not necessarily imply a fast convergence of the EFT expansion. Since the LHC covers a wide range of scales for a wide range of measurements, the justification of an EFT approach has to come from the decoupling pattern of the underlying theory. An illustrative extreme example is heavy quark effective theory which can be used in hadronization calculations for the LHC even though the LHC energy is clearly above the bottom mass. Another example are Higgs decays, for which the Higgs mass defines an upper limit on the energy scale independently of the Higgs production mode [113].

As an illustration we look again at the operators $O_{Qq}^{1,8}$ and $O_{Qq}^{3,8}$, for which the $t\bar{t}$ cross section and other charge-symmetric observables depend on the Wilson coefficients as

$$
\sigma_{t\bar{t}} = \sigma_{\text{SM}} + \sigma_{V}^{d} \left[ r(C_{Qq}^{1,8} + C_{Qq}^{3,8}) + (C_{Qq}^{1,8} - C_{Qq}^{3,8}) \right] + \sigma_{V+A}^{d} \left[ r(C_{Qq}^{1,8} + C_{Qq}^{3,8})^2 + (C_{Qq}^{1,8} - C_{Qq}^{3,8})^2 \right],
$$

where $\sigma_{V}^{d}$ and $\sigma_{V+A}^{d}$ are the contributions from the partonic $d\bar{d} \rightarrow t\bar{t}$ process. As discussed in Sec. 4.2, the linear terms to order $\Lambda^{-2}$ have a flat direction which can be resolved using the kinematic variation of the parton densities. From Fig. 5 we learn that the linear fit leaves certain directions in the parameter space basically unexplored. This is particularly true for $RR$ operators, where bounds only appear around values of $C/\Lambda^2 \approx \pm 10/\text{TeV}^2$. In this range contributions from the squared dimension-6 amplitudes, i.e., the terms in the second line of Eq. (4.17), are numerically dominant.

Due to the presence of quadratic terms of order $\Lambda^{-4}$ any rate prediction $d\sigma$ is positive even for large Wilson coefficients. This implies that in a fit of the two-dimensional parameter space $(C_{Qq}^{1,8}, C_{Qq}^{3,8})$, we can set an upper bound in any direction. From the second line of Eq. (4.17) we can immediately read off that there still exists a flat direction, where the cross section remains constant for varying Wilson coefficients. In contrast to the linearized case this flat direction forms an ellipse, which we can collapse into any direction and indeed derive a limit on the individual coefficients.

This argument also applies to more than two parameters. For rate observables that are positive-definite, the $n-1$-dimensional hyper-surface in the parameter space of $n$ Wilson coefficients is always a compact manifold, like a hyper-ellipsoid. Including the quadratic terms does not reduce the dimension of the parameter space, it merely changes the topology of the likelihood function describing the combinations of Wilson coefficients that provide a certain level of agreement between predictions and data. In particular, it does not break any blind directions in the parameter space.

In the left panel of Fig. 9 we show the same fit of $(C_{Qq}^{1,8}, C_{Qq}^{3,8})$ as in the right panel of Fig. 5, but including dimension-6 squared terms in the predictions. The elliptic shape of the bounds reflects the geometric dependence of the observables on the two Wilson coefficients. This is in contrast with the linear fit from Fig. 5, where the combined bound had a diamond shape. It is interesting to compare the respective sensitivity of the linear and quadratic fits. For $t\bar{t}$ production alone, quadratic contributions drastically increase the sensitivity to the individual operators. Including $ttZ$ and $ttW$ rates resolves the blind direction in top
Figure 9. Impact of the squared dimension-6 contribution on the fit result originally shown for the isospin distinction in Fig. 5 (right) and for the chirality distinction in Fig. 6 (left). The lines are based on the same $t\bar{t}$ data set as before, but the predictions now include SMEFT contributions to order $\Lambda^{-4}$ for $t\bar{t}$ (red), $t\bar{t}Z$ (orange) and $t\bar{t}W$ (blue). The black lines show the fit for symmetric observables in the boosted regime (left) and for the asymmetries $A_C$ (right) to order $\Lambda^{-4}$. Shaded areas show the combined fit to order $\Lambda^{-4}$. Solid and dashed lines mark the Gaussian equivalent of $\Delta\chi^2 = 1, 4$.

Pair production already at order $\Lambda^{-2}$. Quadratic terms from associated production (orange and blue ellipses) do not alter the fit results by much, since the combined fit result (blue area) is dominated by the quadratic contributions in boosted $t\bar{t}$ observables (black ellipse). This illustrates nicely the interplay of linear and quadratic contributions in a global fit. The bound on individual Wilson coefficients can be set either by quadratic terms in the dominant observable (for limited sensitivity) or by the interplay of linear terms in several observables that probe different directions of the parameter space (for high sensitivity). Which effect dominates depends on the overall sensitivity of the observables to operator contributions and on the precision of their measurement.

Beyond rates, quadratic terms do not necessarily lead to ellipses in a fit. The charge asymmetry in $t\bar{t}$ production is an example where quadratic terms modify the topology of the flat direction, but do not allow to set bounds in all directions of the parameter space. The reason is that $A_C$ is not defined to be positive, and therefore negative squared contributions can generally appear. For the chiral operators $O_{Qq}^{1,8}$ and $O_{tq}^{8}$, the cross section and the asymmetry read

$$\sigma_{t\bar{t}} = \sigma_{SM} + \sigma_V (C_{Qq}^{1,8} + C_{tq}^{8}) + \sigma_{V+A} (|C_{Qq}^{1,8}|^2 + |C_{tq}^{8}|^2) + \sigma_{V-A} C_{Qq}^{1,8} C_{tq}^{8},$$

$$A_C = \frac{\sigma_{SM} + \sigma_{AA} (C_{Qq}^{1,8} - C_{tq}^{8}) + \sigma_{VVAA} (|C_{Qq}^{1,8}|^2 - |C_{tq}^{8}|^2)}{\sigma_{t\bar{t}}}. \quad (4.18)$$
A fit of charge-symmetric observables leads to a spherical bound in \((C^{1,8}_{Qq}, C^{8}_{tq})\), shown as red curves in the right panel of Fig. 9. For the charge asymmetry the isocurves are hyperbolas with asymptotes along the directions \((1, 1)\) and \((1, -1)\). The fit results reflect this shape in the black curves. They leave the direction \((1, 1)\) unconstrained. The fact that the direction \((1, -1)\) is bounded is due to the combination of asymmetry measurements with different best-fit points.

5 Single top analysis

In addition to the top pair observables described in the previous section our global top analysis also includes single top production. Some Feynman diagrams for the different processes are shown in Fig. 2. The structure of the single top sector is very similar to classic global SMEFT analyses in that the operators listed in Tab. 1 have distinctive observable effects and can be probed with the sizeable number of different measurements listed in Tab. 6. Flat directions are not an issue in this sector, but it is interesting to test if there exist correlations in the bounds on the individual operators.

We evaluate all two-operator correlations based on two-dimensional profile likelihoods and find three distinct patterns shown in the upper row of Fig. 10. First, a box shape like for \(C_{tG}\) and \(C^{3,8}_{Qq}\) appears if two Wilson coefficients are bounded by two separate sets of observables. Next, an elliptic disk like the one between \(C_{bW}\) and \(C_{\phi tb}\) appears if two operators contribute quadratically to the same observable. Finally, a shifted circle like in the \(C^{3,1}_{Qq} - C^{3,8}_{Qq}\) plane appears if two operators contribute to the same observables, but one of them linearly \((C^{3,1}_{Qq})\) and the other one only quadratically \((C^{3,8}_{Qq})\). For this pattern the SM value cannot be at the center of the circle.

One of the few noteworthy correlations in the single top fit is the inverted heart shape in the \(C_{tG} - C^{3}_{\phi Q}\) plane shown in the lower left panel of Fig. 10. It can be understood as the interplay of the three operators \(C_{tG}, C^{3}_{\phi Q}, \) and \(C^{3,1}_{Qq}\) with at least two measurements. The only single top measurement sensitive to \(O_{tG}\) is \(tW\) production. Using its rate to constrain \(C_{tG}\) and \(C^{3}_{\phi Q}\) we find an elliptic correlation centered at negative values of \(C^{3}_{\phi Q}\). When we add the strong constraints on \(C^{3}_{\phi Q}\) from \(t\)-channel production the bottom part of the ellipsis gets removed. Finally, once we add \(C^{3,1}_{Qq}\) to the fit we find that \(O^{3}_{\phi Q}\) and \(O^{3,1}_{Qq}\) are slightly correlated and hence more negative values of \(O^{3}_{\phi Q}\) become consistent with data. In the lower panels of Fig. 10 we project the 3-dimensional profile likelihood from a 3-parameter fit along each of the three directions. In the left panel we see a very faint barrier for \(C^{3}_{\phi Q}/\Lambda^2 \approx 1.5\,\text{TeV}^{-2}\). It corresponds to the two disconnected regions, one for \(C^{3,1}_{Qq}/\Lambda^2 \approx 0\) and one for \(C^{3,1}_{Qq}/\Lambda^2 \approx 0.4\,\text{TeV}^{-2}\), which we see clearly in the central and right panels. In the global single top fit, once all observables are included, only the region for \(C^{3}_{\phi Q}/\Lambda^2 \approx 0\) remains, while the other region becomes disfavored.

Given the smooth behavior of the multi-dimensional likelihood we can perform a global fit of the single top sector, including the \(W\) helicity fractions in top decay and associated \(tV\) production. The one-dimensional profile likelihoods are shown in Fig. 11. The only
non-standard aspect in these results is that we cannot define meaningful 68% CL limits for some of the operators. This happens when a flat core of the profile likelihood covers more than 68% of the integral and there exists no unique definition of a range. We observe this for all operators except for \( O_{\phi tb} \), \( O_{tW} \), and \( O_{bW} \), implying that for all other operators the theory uncertainty is large compared to the experimental statistics and systematics.

One aspect which sticks out in the global fit is the low sensitivity to \( O^{3}_{3\phi Q} \), compared to \( O^{3}_{Qq} \) and \( O_{tW} \). All three operators interfere with the SM amplitude in \( t \)-channel single top production, but for \( O^{3}_{3\phi Q} \) the effect is numerically smaller by about a factor three. As discussed in Sec. 2.2, \( O^{3}_{3\phi Q} \) only rescales the SM contribution, while \( O^{3}_{Qq} \) changes the kinematics in \( t \)-channel production, see Tab 2. The operator \( O_{tW} \) is best constrained by the \( W \) helicity fractions in top decay, see Eq. (2.18), which are very sensitive to this operator.

The bounds on \( C^{3,8}_{Qq} \), \( C_{\phi tb} \) and \( C_{bW} \) are symmetric around zero, since the corresponding operators contribute to single top observables only at order \( \Lambda^{-4} \), cf. Tab 1. The coefficients \( C_{\phi Q}^{-}, C_{tZ} \) and \( C_{\phi t} \) are bound by \( tZ \) production. Due to the limited experimental precision, the bounds on these operators are very loose. Also here the SM-interference plays a role, leading to asymmetric bounds for \( C_{\phi Q}^{-} \) and \( C_{\phi t} \). The sensitivity to \( O_{\phi t} \) is especially poor because its contribution to \( tZ \) production is suppressed, see Sec. 2.2. This will change once we include the better-measured \( t\bar{t}Z \) channel in the global fit.

Figure 10. Upper: examples for correlated 2-dimensional profile likelihoods of operators in a global fit to the single top data. Lower: correlated profile likelihoods for a three-parameter fit of the same data.
Whenever the 68% CL is not shown it falls into the flat profile likelihood regime reflecting dominant theoretical uncertainties.

6 Global top analysis

In the final step we add all top pair measurements from Tab. 5 to our single top fit based on the measurements in Tab. 6 and presented in Sec. 5. On the parameter side we add the large number of four-quark operators, which roughly doubles the number of model parameters. For the measurements we not only include top pair production, but also associated $t\bar{t}W$ and $t\bar{t}Z$ rate measurements. They constrain some of the electroweak top operators in single top production and four-quark operators in top pair production, thus linking both sectors in the global fit.

First, we briefly comment on 2-dimensional correlations in the complete fit. The box-shaped correlations for separate operators and separate measurements, filled ellipses for more than one operator affecting a measurement, and shifted circles from linear contributions to compact flat directions which we observed in the single top fit (Fig. 10) also appear in the global fit.

Non-trivial correlations as between $C_{tG}$, $C^{3}_{Qq}$, and $C^{3,1}_{Qq}$ vanish once we include the full data set, see Fig. 12. The reason is that $C_{tG}$ and $C^{3,1}_{Qq}$ are strongly constrained individually by top pair production. For the weak-triplet operators $O^{3,1}_{Qq}$ and $O^{3,8}_{Qq}$ the bounds are the same in the single top fit and the global fit, see also Fig 14. Single top production is indeed more sensitive to these four-quark operators than top pair production.
In Fig. 13 we show the profile likelihoods for each of the top-related effective operators. On the x-axis we start with the diagonal $LL$ and $RR$ four-quark operators listed in Eq. (2.3), continue with the $LR$ and $RL$ four-quark operators from Eq. (2.4), and finally include the bosonic operators from Eq. (2.5). For each operator the red bars indicate the final result at 68% and 95% CL. These confidence levels are compact intervals defined by the area under the profile likelihood curve, where in addition we require the likelihood values on each side to be equal. For a Gaussian distribution we expect the 95% error bar to be symmetric around the best-fit value and twice as wide as the symmetric 68% error bar. For some of the Wilson coefficients, non-Gaussian effects occur, which are mainly due to theoretical uncertainties treated as flat likelihoods.

In general, the four-quark operators are extremely well constrained with limits in the range of $\Lambda/\sqrt{C} \approx 1 - 2$ TeV. For all weak-singlet four-quark operators, the sensitivity is dominated by high-energy bins in $t\bar{t}$ distributions. For $LL$ operators, we made this observation earlier in the left panel of Fig. 9. As discussed in Sec. 4.5, for most operators the well-defined limits on each of the four-quark operators rest entirely on the quadratic contributions to the observables. For color-singlet operators, which contribute to top pair production only at order $\Lambda^{-4}$, the bounds are fully determined by quadratic contributions and symmetric around zero. The only asymmetric limit on a color-singlet operator appears for $O_{31}^{\phi q}$ through a linear contribution to single top production.

Color-octet operators have asymmetric error bars due to their interference with QCD in top pair production. This interference is also the reason for the correlation patterns of shifted circles in Fig. 9. The bounds on color-octet operators thus rely on the interplay between contributions of order $\Lambda^{-2}$ and $\Lambda^{-4}$, where the inclusion of both terms is particularly important. In Fig. 13, the error bars for color-singlet operators appear much smaller than for color-octet operators. This is due to the fact that top–anti-top observables always probe the combination $(C^8)^2 + \frac{9}{2}(C^1)^2$ at order $\Lambda^{-4}$, see Eq. (2.12). Top–anti-top observables therefore constrain the quantities $C^8$ and $(C^8)^2 + \frac{9}{2}(C^1)^2$ at LO, which allows us to distinguish color-singlet from color-octet structures in kinematic distributions. The color combination is also changed at NLO in QCD, which offers the possibility to determine the
Figure 13. 95% and 68% CL bounds on top operators from a global fit to the full data set from Tabs. 5 and 6. We show the results including all uncertainties (red) and with theoretical uncertainties reduced by a factor of two, $\delta_{\text{th}}/2$ (blue).

color structure of operators from jet radiation.

Looking at the quark chirality, we observe that the bounds on operators with left- and right-handed tops are similar in strength. Charge-symmetric $t\bar{t}$ observables do not distinguish between these operators at high energies, see Eqs. (2.10) and (2.12). The charge asymmetry is sensitive to the top chirality, see Eq. (4.18), but still leads to equal bounds on the magnitude of $LL$ and $RL$ operators due to its small SM contribution.

Regarding different light quark flavors, operators with up quarks are better constrained than operators with down quarks. This reflects the parton content of the proton, which leads to an enhanced sensitivity of $t\bar{t}$ observables to up-quark operators over down-quark operators, see Eq. (4.8).

Let us now turn our attention to the bosonic operators. The strongest bounds are obtained for the dipole operators $O_{tG}$ and $O_{tW}$. For $O_{tW}$ the bound does not change compared to the single top fit (see also Fig 14), because it is dominated by the precise measurements of $W$ helicities in top decays. From our global fit, we obtain at 95% CL

$$\frac{\Lambda}{\sqrt{C_{tW}}} \in [-0.38, 0.47] \text{ TeV}.$$ (6.1)
For $O_{tG}$ the best global limit at 95% CL is obtained from top–anti-top production,

$$\frac{\Lambda}{\sqrt{C_{tG}}} \in [-0.02, 0.82] \text{ TeV}. \quad (6.2)$$

This bound is consistent with the estimate of Eq. (4.4) and much stronger than the bound from associated $tW$ production in Fig. 11. Most of the remaining bosonic operators are better constrained in the global fit than in the single top fit (see Fig 14). This shows the impact of the $t\bar{t}Z$ cross section measurements in the global fit. For the operator $O_{\phi t\bar{t}}$, which does not contribute to $t\bar{t}Z$ or $t\bar{t}W$ production, the sensitivity remains very low.

In our fit, theory uncertainties affect the relation between the (rate) measurements and the Wilson coefficients. Since we treat these uncertainties as flat errors in our statistical, they lead to plateaus in the center of the likelihood distributions and to some of the non-Gaussian effects. To study the relative impact of theoretical and experimental uncertainties on the fit results, we have performed a global fit with theory uncertainties divided by a factor of two. The 95% CL results are shown as blue bars in Fig. 13. We find that throughout the global analysis these theory uncertainties are limiting factors in interpreting Run-II results already now. Significant improvements are crucial to fully exploit the potential of Run-III measurements.

7 Conclusions

We have presented a comprehensive analysis of the LHC Run II data in the top sector. We use NLO simulations in *Madgraph5 aMC@NLO* and the *Sfitter* framework to constrain the Wilson coefficients of 22 dimension-6 operators. The bulk of the measurements involve final states with a top pair, including kinematic distributions, the charge asymmetry, and associated top pair production with a weak boson. In addition, we include different single top channels and $W$ helicity measurements in top decays. The measurements we use are based on up to 139 fb$^{-1}$ of integrated luminosity.

The main challenge of this global analysis is the large number of four-quark operators in top pair production, whose contribution to the QCD process are largely degenerate. We have discussed several ways of breaking this degeneracy, including parton luminosity effects, the charge asymmetry, jet radiation patterns, and associated production with weak bosons. We have also discussed the impact of dimension-6 squared terms on the fit results, and their role in lifting this degeneracy.

Altogether, we derive limits in the range of $\Lambda/\sqrt{C} = 0.35 - 2 \text{ TeV}$ for the different Wilson coefficients from a profile likelihood. The strongest limit is on the anomalous top coupling to the gluon, driven by the QCD production rate. Similarly strong limits apply to several four-quark operators, stemming mostly from normalized kinematic distributions. The top dipole interaction with the $W$ boson is also strongly constrained by the precisely known $W$ helicity fractions in top decays. Other operators with weak bosons are much less constrained, because they only occur in electroweak top processes with a limited sensitivity in total rates. Differential distributions in electroweak top production, as well as precision
observables in electroweak and flavor physics can help to increase the sensitivity. For all operators we find that the theory uncertainties linking measurements to Wilson coefficients in the Lagrangian are becoming the limiting factor in interpreting LHC results.

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A Operator relations

In this appendix we list the relations between the relevant operators in our analysis and the operators in the Warsaw basis, following the notation of Refs. [21, 41]. Using the \(SU(2)\) and \(SU(3)\) identities

\[
\begin{align*}
\tau^I_{ij} \tau^I_{kl} &= -\delta_{ij} \delta_{kl} + 2 \delta_{il} \delta_{jk}, \quad T^A_{ab} T^A_{cd} = -\frac{1}{6} \delta_{ab} \delta_{cd} + \frac{1}{2} \delta_{ad} \delta_{bc},
\end{align*}
\]

and the Fierz identities for anti-commutating fermion fields,

\[
(\bar{q} \gamma^\mu q)(\bar{Q} \gamma^\mu Q) = (\bar{q} \gamma^\mu q)(\bar{Q} \gamma^\mu Q), \quad (\bar{u} \gamma^\mu u)(\bar{t} \gamma^\mu t) = (\bar{u} \gamma^\mu u)(\bar{t} \gamma^\mu t),
\]

we derive the following relations:

- four-quark operators with \(LL\) and \(RR\) chiral structure \((i = 1, 2)\),

\[
\begin{align*}
O^{1,8}_{\bar{Q}q} &= (\bar{Q} \gamma^\mu T^A Q)(\bar{q} \gamma^\mu T^A q_i) \quad = -\frac{1}{6} O^{1(33)ii}_{qq} + \frac{1}{4} O^{(3)ii}_{qq} + \frac{1}{4} O^{3(3ii)ii}_{qq}, \\
O^{3,8}_{\bar{Q}q} &= (\bar{Q} \gamma^\mu T^A T^I Q)(\bar{q} \gamma^\mu T^A T^I q_i) \quad = -\frac{1}{6} O^{3(3ii)ii}_{qq} + \frac{3}{4} O^{1(3ii)ii}_{qq} - \frac{1}{4} O^{3(3ii)ii}_{qq}, \\
O^{1,1}_{\bar{Q}q} &= (\bar{Q} \gamma^\mu Q)(\bar{q} \gamma^\mu q_i) \quad = O^{1(3ii)ii}_{qq}, \\
O^{3,1}_{\bar{Q}q} &= (\bar{Q} \gamma^\mu T^A T^I Q)(\bar{q} \gamma^\mu T^A T^I q_i) \quad = O^{3(3ii)ii}_{qq}, \\
O^8_{\bar{t}u} &= (t \gamma^\mu T^A t)(\bar{u} \gamma^\mu U^A \bar{u}_i) \quad = -\frac{1}{6} O^{(3ii)}_{uu} + \frac{1}{2} O^{(3ii)ii}_{uu}, \\
O^1_{\bar{t}u} &= (t \gamma^\mu t)(\bar{u} \gamma^\mu U \bar{u}_i) \quad = O^{1(3ii)ii}_{uu}, \\
O^8_{\bar{t}d} &= (t \gamma^\mu T^A t)(\bar{d} \gamma^\mu T^A d_i) \quad = O^{8(3ii)ii}_{ud}, \\
O^1_{\bar{t}d} &= (t \gamma^\mu t)(\bar{d} \gamma^\mu d_i) \quad = O^{1(3ii)ii}_{ud},
\end{align*}
\]
• four-quark operators with $LR$ and $RL$ chiral structure

\[ O_{Qu}^8 \equiv (\bar{Q}\gamma^{\mu}T^A(Q)(\bar{u}_i\gamma_{\mu}T^A u_i) = O_{qu}^{8(iii)} \quad O_{Qu}^1 \equiv (\bar{Q}\gamma^{\mu}Q)(\bar{u}_i\gamma_{\mu}u_i) = O_{qu}^{1(iii)} \]

\[ O_{qd}^8 \equiv (\bar{Q}\gamma^{\mu}T^A(Q)(\bar{d}_i\gamma_{\mu}T^A d_i) = O_{qd}^{8(iii)} \quad O_{qd}^1 \equiv (\bar{Q}\gamma^{\mu}Q)(\bar{d}_i\gamma_{\mu}d_i) = O_{qd}^{1(iii)} \]

\[ O_{tq}^1 \equiv (\bar{q}_i\gamma^{\mu}T^A q_i)(\bar{t}\gamma_{\mu}T^A t) = O_{tq}^{1(iii)} \quad O_{tq}^1 \equiv (\bar{q}_i\gamma^{\mu}q_i)(\bar{t}\gamma_{\mu}t) = O_{tq}^{1(iii)} , \]

• operators with two heavy quarks and bosonic fields

\[ O_{\phi Q}^3 \equiv (\phi \leftrightarrow D_{\mu} \phi)(\bar{Q}\gamma^{\mu}Q) = O_{\phi Q}^{3(iii)} \quad \hat{O}_{tB} \equiv (\bar{Q}\sigma^{\mu\nu}t) \tilde{\phi} B_{\mu\nu} = \hat{O}_{tB}^{(iii)} \]

\[ O_{\phi \phi}^3 \equiv (\phi \leftrightarrow D_{\mu} \phi)(\bar{Q}\gamma^{\mu}t\phi) = O_{\phi \phi}^{3(iii)} \quad \hat{O}_{tW} \equiv (\bar{Q}\sigma^{\mu\nu}t) \tau^I \phi W_{\mu\nu}^I = \hat{O}_{tW}^{(iii)} \]

\[ O_{\phi t} \equiv (\phi \leftrightarrow D_{\mu} \phi)(\bar{t}\gamma^{\mu}t) = O_{\phi t}^{(iii)} \quad \hat{O}_{bW} \equiv (\bar{Q}\sigma^{\mu\nu}b) \tau^I \phi W_{\mu\nu}^I = \hat{O}_{bW}^{(iii)} \]

\[ \hat{O}_{\phi tb} \equiv (\phi \leftrightarrow D_{\mu} \phi)(\bar{t}\gamma^{\mu}b) = \hat{O}_{\phi tb}^{(iii)} \quad \hat{O}_{tG} \equiv (\bar{Q}\sigma^{\mu\nu}T^A t) \tilde{\phi} G_{\mu\nu}^A = \hat{O}_{tG}^{(iii)} \]

with the Higgs field $\phi = (0, \frac{1}{\sqrt{2}}(v + h))^T$ in unitary gauge, $\tilde{\phi} = i\sigma_2 \phi^*$ and the covariant derivative

\[ D_{\mu} = \partial_{\mu} - i \frac{e}{2s_W} A_{\mu}^I \tau^I - i \frac{e}{c_W} B_{\mu} Y, \quad D_{\mu}^I = \tau^I D_{\mu}, \quad \tau^I = \sigma_I. \] (A.1)

The relations between the corresponding Wilson coefficients $C_i$ and $\tilde{C}_i$ can be obtained by requiring that both bases lead to the same terms in the effective Lagrangian [37],

\[ \mathcal{L}_{\text{eff}} = \sum_a \left( \frac{C_a}{\Lambda^2} \hat{O}_a + \text{h.c.} \right) + \sum_b \frac{C_b}{\Lambda^2} O_b = \sum_c \left( \frac{C_c}{\Lambda^2} \hat{O}_c + \text{h.c.} \right) + \sum_d \frac{C_d}{\Lambda^2} O_d. \] (A.2)

After electroweak symmetry breaking, the effective interactions of the physical weak gauge bosons are described by linear combinations of the operators in the unbroken phase. In unitary gauge, the relations read

\[ \begin{pmatrix} O_{1\phi Q}^3 \\ O_{3\phi Q}^3 \end{pmatrix} = \begin{pmatrix} 1 & 1 & 0 & 0 \\ -1 & 1 & 1 & 1 \end{pmatrix} \begin{pmatrix} -\frac{e}{2s_Wc_W} (\bar{t}\gamma^{\mu}t L) Z_{\mu}(v + h)^2 \\ -\frac{e}{2s_Wc_W} (\bar{b}\gamma^{\mu}b L) Z_{\mu}(v + h)^2 \\ -\frac{e}{\sqrt{2}s_W} (\bar{t}\gamma^{\mu}b L) W_\mu^+(v + h)^2 \\ -\frac{e}{\sqrt{2}s_W} (\bar{b}\gamma^{\mu}t L) W_\mu^-(v + h)^2 \end{pmatrix}, \] (A.3)

\[ \begin{pmatrix} \hat{O}_{tB} \\ \hat{O}_{tW} \end{pmatrix} = \begin{pmatrix} c_W & -s_W & 0 \\ s_W & c_W & 1 \end{pmatrix} \begin{pmatrix} \frac{1}{\sqrt{2}} (\bar{t}\sigma^{\mu\nu}t R) A_{\mu\nu}(v + h) \\ \frac{1}{\sqrt{2}} (\bar{b}\sigma^{\mu\nu}b R) Z_{\mu\nu}(v + h) \\ \frac{1}{\sqrt{2}} (\bar{b}\sigma^{\mu\nu}t R) W_{\mu\nu}^+(v + h) \end{pmatrix}, \]

\[ \begin{pmatrix} \hat{O}_{bW} \end{pmatrix} = \left[ -\frac{1}{\sqrt{2}} \bar{b} \sigma^{\mu\nu}b R (c_W Z_{\mu\nu} + s_W A_{\mu\nu} + i \sigma^{\mu\nu}b R W_{\mu\nu}^+) \right] (v + h). \]

B Numerical bounds on operators

Here we list the limits on the 22 Wilson coefficients, obtained from fits to different data sets. Tab. 9 shows the results of our global fit, Tab. 7 corresponds to our single top fit, and Tab. 8 shows a fit of observables in top pair production only.
We also show a comparison of the bounds obtained from fits to top-pair production, single top production, and from the full global fit in Fig. 14.

<table>
<thead>
<tr>
<th>Operator</th>
<th>68% CL</th>
<th>95% CL</th>
</tr>
</thead>
<tbody>
<tr>
<td>$C_{tG}$</td>
<td>$-\infty$</td>
<td>$[5.68, 4.00]$</td>
</tr>
<tr>
<td>$C_{Qq}^{38}$</td>
<td>$-\infty$</td>
<td>$[-0.78, 0.74]$</td>
</tr>
<tr>
<td>$C_{Qq}^{31}$</td>
<td>$-\infty$</td>
<td>$[-0.49, 0.11]$</td>
</tr>
<tr>
<td>$C_{bW}$</td>
<td>$[-1.84, 1.68]$</td>
<td>$[-2.80, 2.80]$</td>
</tr>
<tr>
<td>$C_{tW}$</td>
<td>$[-0.32, 0.23]$</td>
<td>$[-0.47, 0.47]$</td>
</tr>
<tr>
<td>$C_{tZ}$</td>
<td>$-\infty$</td>
<td>$[-9.40, 9.40]$</td>
</tr>
<tr>
<td>$C_{qt}$</td>
<td>$-\infty$</td>
<td>$[-51.50, 22.50]$</td>
</tr>
<tr>
<td>$C_{qb}$</td>
<td>$[-5.94, 5.94]$</td>
<td>$[-9.18, 8.82]$</td>
</tr>
<tr>
<td>$C_{3\phi Q}$</td>
<td>$-\infty$</td>
<td>$[-4.70, 1.30]$</td>
</tr>
<tr>
<td>$C_{\phi tb}$</td>
<td>$-\infty$</td>
<td>$[-36.00, 12.00]$</td>
</tr>
</tbody>
</table>

Table 7. The 68% and 95% confidence levels for single top fit, corresponding to Fig. 11.

<table>
<thead>
<tr>
<th>Operator</th>
<th>68% CL</th>
<th>95% CL</th>
</tr>
</thead>
<tbody>
<tr>
<td>$C_{tG}$</td>
<td>$[0.30, 0.74]$</td>
<td>$[-0.03, 0.82]$</td>
</tr>
<tr>
<td>$C_{Qq}^{38}$</td>
<td>$[-0.79, 0.15]$</td>
<td>$[-1.11, 0.49]$</td>
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<tr>
<td>$C_{Qq}^{38}$</td>
<td>$[-0.49, 0.73]$</td>
<td>$[-0.84, 1.16]$</td>
</tr>
<tr>
<td>$C_{tq}^8$</td>
<td>$[-1.21, -0.09]$</td>
<td>$[-1.37, 0.47]$</td>
</tr>
<tr>
<td>$C_{Qu}^8$</td>
<td>$[-1.51, -0.09]$</td>
<td>$[-1.91, 0.44]$</td>
</tr>
<tr>
<td>$C_{Qd}^8$</td>
<td>$[-2.09, 0.15]$</td>
<td>$[-2.44, 1.24]$</td>
</tr>
<tr>
<td>$C_{tu}^8$</td>
<td>$[-1.16, 0.15]$</td>
<td>$[-1.48, 0.65]$</td>
</tr>
<tr>
<td>$C_{td}^8$</td>
<td>$[-1.40, 0.52]$</td>
<td>$[-1.93, 1.16]$</td>
</tr>
<tr>
<td>$C_{Qq}^{11}$</td>
<td>$[-0.38, 0.09]$</td>
<td>$[-0.47, 0.30]$</td>
</tr>
<tr>
<td>$C_{Qq}^{11}$</td>
<td>$[-0.18, 0.29]$</td>
<td>$[-0.34, 0.42]$</td>
</tr>
<tr>
<td>$C_{tq}^1$</td>
<td>$[-0.27, 0.21]$</td>
<td>$[-0.39, 0.37]$</td>
</tr>
<tr>
<td>$C_{Qu}^1$</td>
<td>$[-0.47, 0.09]$</td>
<td>$[-0.62, 0.27]$</td>
</tr>
<tr>
<td>$C_{Qd}^1$</td>
<td>$[-0.41, 0.37]$</td>
<td>$[-0.66, 0.58]$</td>
</tr>
<tr>
<td>$C_{tu}^1$</td>
<td>$[-0.35, 0.15]$</td>
<td>$[-0.47, 0.34]$</td>
</tr>
<tr>
<td>$C_{td}^1$</td>
<td>$[-0.41, 0.35]$</td>
<td>$[-0.58, 0.63]$</td>
</tr>
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Table 8. The 68% and 95% confidence levels for the top pair production fit.
<table>
<thead>
<tr>
<th>Operator</th>
<th>68% CL</th>
<th>95% CL</th>
<th>95% CL, $\delta_{th}/2$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$C_{1G}$</td>
<td>[0.30, 0.74]</td>
<td>[-0.02, 0.82]</td>
<td>[0.24, 0.57]</td>
</tr>
<tr>
<td>$C_{1Q}^{8}$</td>
<td>[-0.68, 0.20]</td>
<td>[-1.00, 0.52]</td>
<td>[-0.76, 0.12]</td>
</tr>
<tr>
<td>$C_{2Q}^{8}$</td>
<td>[-0.26, 0.58]</td>
<td>[-0.62, 0.74]</td>
<td>[-0.42, 0.54]</td>
</tr>
<tr>
<td>$C_{3Q}^{8}$</td>
<td>[-1.00, 0.04]</td>
<td>[-1.32, 0.44]</td>
<td>[-1.08, 0.04]</td>
</tr>
<tr>
<td>$C_{Qu}^{8}$</td>
<td>[-1.40, -0.12]</td>
<td>[-1.72, 0.52]</td>
<td>[-1.32, -0.04]</td>
</tr>
<tr>
<td>$C_{Qd}^{8}$</td>
<td>[-1.88, 0.12]</td>
<td>[-2.20, 1.08]</td>
<td>[-1.72, 0.04]</td>
</tr>
<tr>
<td>$C_{Q}^{1}$</td>
<td>[-1.16, 0.04]</td>
<td>[-1.48, 0.52]</td>
<td>[-1.16, 0.04]</td>
</tr>
<tr>
<td>$C_{Qd}^{1}$</td>
<td>[-1.40, 0.36]</td>
<td>[-1.88, 1.00]</td>
<td>[-1.48, 0.28]</td>
</tr>
<tr>
<td>$C_{Q}^{1}$</td>
<td>[-0.22, 0.26]</td>
<td>[-0.38, 0.42]</td>
<td>[-0.22, 0.22]</td>
</tr>
<tr>
<td>$C_{Qu}^{1}$</td>
<td>[-0.25, 0.05]</td>
<td>[-0.39, 0.11]</td>
<td>[-0.23, 0.09]</td>
</tr>
<tr>
<td>$C_{tG}^{1}$</td>
<td>[-0.22, 0.22]</td>
<td>[-0.38, 0.38]</td>
<td>[-0.22, 0.22]</td>
</tr>
<tr>
<td>$C_{tQ}^{1}$</td>
<td>[-0.26, 0.26]</td>
<td>[-0.42, 0.42]</td>
<td>[-0.30, 0.22]</td>
</tr>
<tr>
<td>$C_{tQ}^{1}$</td>
<td>[-0.38, 0.38]</td>
<td>[-0.62, 0.62]</td>
<td>[-0.34, 0.38]</td>
</tr>
<tr>
<td>$C_{t}^{1}$</td>
<td>[-0.26, 0.26]</td>
<td>[-0.42, 0.42]</td>
<td>[-0.26, 0.30]</td>
</tr>
<tr>
<td>$C_{td}^{1}$</td>
<td>[-0.34, 0.38]</td>
<td>[-0.62, 0.58]</td>
<td>[-0.30, 0.38]</td>
</tr>
<tr>
<td>$C_{BW}$</td>
<td>[-1.68, 1.68]</td>
<td>[-2.80, 2.64]</td>
<td>[-2.16, 2.32]</td>
</tr>
<tr>
<td>$C_{W}$</td>
<td>[-0.23, 0.26]</td>
<td>[-0.38, 0.47]</td>
<td>[-0.26, 0.38]</td>
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<tr>
<td>$C_{LZ}$</td>
<td>[-2.30, 2.30]</td>
<td>[-3.10, 3.30]</td>
<td>[-2.90, 2.50]$^{*}$</td>
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<tr>
<td>$C_{tb}$</td>
<td>[-5.58, 5.58]</td>
<td>[-8.46, 8.82]</td>
<td>[-7.02, 6.66]</td>
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<tr>
<td>$C_{eQ}^{3}$</td>
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<tr>
<td>$C_{eQ}$</td>
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<td>[-5.78, 13.12]</td>
<td>[-4.80, 8.80]</td>
</tr>
</tbody>
</table>

Table 9. The 68% and 95% confidence levels for the full global fit, corresponding to Fig. 13. The asterisk marks non-Gaussian effects for which we quote conservative envelopes of the likelihood. The label $\delta_{th}/2$ stands for the fit with halved theoretical uncertainties.

References


Figure 14. 95% and 68% CL bounds on top operators global fits to top pair production measurements (blue), single top (green) and to the full data set from Tabs. 5 and 6 (red).


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