The Epsilon Variables for Electroweak Precision Tests: A Reappraisal

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Abstract

We update the analysis of the precision electroweak tests in terms of the previously introduced epsilon parameters, by taking into account the new experimental information (i.e. the data presented at the Glasgow Conference) and some recent theoretical progress in the computation of radiative corrections in the Standard Model. At the same time we further clarify some important points, as, for example, the dependence of the analysis on the input values of $\alpha_s(m_Z)$ and $\alpha(m_Z)$.

Recently we have proposed [1] a general strategy for the analysis of precision electroweak tests in view of the search for new physics beyond the Standard Model. Our analysis is based on four parameters, ε_1 , ε_2 , ε_3 and ε_b . They represent an efficient parameterisation of the small deviations from what is solidly established in a way that is, in particular, unaffected by our relative ignorance of m_t . In fact, the extremely important new information on m_t from the CDF events [2] still leaves a considerable uncertainty on the value of m_t . Indeed the epsilons are defined in such a way that they are exactly zero in the Standard Model in the limit of neglecting all pure weak loop-corrections to a few especially relevant observables (i.e. when only the predictions from the tree level Standard Model plus pure QED and pure QCD corrections are taken into account). This very simple version of improved Born approximation - hereafter simply called Born approximation - is a good first approximation [3], according to the data. The main purpose of this letter is to update the epsilon analysis by taking into account the new experimental information (i.e. the data presented at the Glasgow Conference [4] and displayed in Table 1) and some recent theoretical progress in the computation of radiative corrections in the Standard Model. At the same time we further clarify some important points, as, for example, the dependence of the analysis on the input values of $\alpha_s(m_Z)$ and $\alpha(m_Z)$.

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In a completely model independent way we have defined [1] four variables, called* ε_1 , ε_2 , ε_3 and ε_b , that are precisely measured and can be compared with the predictions of different theories. The quantities ε_1 , ε_2 , ε_3 and ε_b are defined in ref.1 in one to one correspondence with the set of observables m_W/m_Z , Γ_l , A_{FB}^l and Γ_b . The relations between the basic observables and the epsilons can be linearised, leading to the formulae

$$\frac{m_W^2}{m_Z^2} = \frac{m_W^2}{m_Z^2} \Big|_B (1 + 1.43\varepsilon_1 - 1.00\varepsilon_2 - 0.86\varepsilon_3) \quad (1a)$$

$$\Gamma_l = \Gamma_l \Big|_B (1 + 1.20\varepsilon_1 - 0.26\varepsilon_3) \quad (1b)$$

$$A_{FB}^\mu = A_{FB}^\mu \Big|_B (1 + 34.72\varepsilon_1 - 45.15\varepsilon_3) \quad (1c)$$

$$\Gamma_b = \Gamma_b \Big|_B (1 + 1.42\varepsilon_1 - 0.54\varepsilon_3 + 2.29\varepsilon_b) \quad (1d)$$

The Born approximations, as defined above, of the corresponding quantities on the right hand side of eq. 1 depend on $\alpha_s(m_Z)$ and also on $\alpha(m_Z)$. Defining

$$\delta\alpha_s = [\alpha_s(m_Z) - 0.118]/\pi \quad ; \quad \delta\alpha = (\alpha(m_Z) - 1/128.87)/\alpha \quad (2)$$

* Here we resume the notation ε_i for exactly the same quantities as defined in ref.1, where they were denoted ε_{N_i} (the index N, for "new", had been inserted to signal some small differences with respect to the original definitions in refs.5,6).

we have

$$\left. \frac{m_W^2}{m_Z^2} \right|_B = 0.76883[1 - 0.40\delta\alpha] \quad (3a)$$

$$\Gamma_l|_B = 83.56[1 - 0.19\delta\alpha]MeV \quad (3b)$$

$$A_{FB}^\mu|_B = 0.01683(1 - 34\delta\alpha) \quad (3c)$$

$$\Gamma_b|_B = 379.6[1 + 1.0\delta\alpha_s - 0.42\delta\alpha]MeV \quad (3d)$$

Note that the dependence on $\delta\alpha_s$ for $\Gamma_b|_B$, shown in eq.3d, is not simply the one loop result for $m_b=0$ but a combined effective shift which takes into account both finite mass effects and the contribution of the known higher order terms.

The important property of the epsilons is that, in the Standard Model, for all observables at the Z pole, the whole dependence on m_t (and m_H) arising from one-loop diagrams only enters through the epsilons. The same is actually true, at the relevant level of precision, for all higher order m_t -dependent corrections. Recently, within the Standard Model, there has been some additional progress in the control of radiative corrections by new computations of some potentially dominant higher-loop effects: terms of order $(G_F m_t^2)^2$ in the $Z \rightarrow b\bar{b}$ vertex and in $\Delta\rho$, for all values of m_H [7]; terms of order $\alpha_s G_F m_t^2$ in the $Z \rightarrow b\bar{b}$ vertex [8] and, for some refinements, in Δr and $\Delta\rho$ [9]; terms of order $(\alpha_s m_b/m_Z)^2$ in $\Gamma(Z \rightarrow \text{hadrons})$ [10]. Very recently the $o(\alpha_s^2 G_F m_t^2)$ corrections to $\Delta\rho$ have also been computed [11]. We stress that since all of these improvements have to do with vacuum polarisation diagrams or with the $Z \rightarrow b\bar{b}$ vertex, the corresponding terms simply affect the theoretical predictions of the epsilons in the Standard Model but do not invalidate the basic property of the epsilons mentioned above. The improved theoretical values of the epsilons in the Standard Model are given in table 2. Actually, the only residual m_t dependence of the various observables not included in the epsilons is in the terms of order α_s^2 in the pure QCD correction factors to the hadronic widths [12]. But this one is quantitatively irrelevant, especially in view of the errors connected to the uncertainty on the value of α_s . It is important to remark that the theoretical values of the epsilons in the SM, as defined in eqs. 1 and given in table 2, are not affected, at the percent level or so, by reasonable variations of $\alpha_s(m_Z)$ and/or $\alpha(m_Z)$ around their central values. By our definitions, in fact, no terms of order $\alpha_s^n(m_Z)$ or $\alpha \log(m_Z/m)$ contribute to the epsilons.

In terms of the epsilons, the following expressions hold, within the SM, for the various precision observables

$$\Gamma_T = \Gamma_{T0}[1 + 1.35 \epsilon_1 - 0.46 \epsilon_3 + 0.35 \epsilon_b] \quad (4a)$$

$$R = R_0[1 + 0.28 \epsilon_1 - 0.36 \epsilon_3 + 0.50 \epsilon_b] \quad (4b)$$

$$\sigma_h = \sigma_{h0}[1 - 0.03 \epsilon_1 + 0.04 \epsilon_3 - 0.20 \epsilon_b] \quad (4c)$$

$$x = x_0[1 + 17.6 \epsilon_1 - 22.9 \epsilon_3] \quad (4d)$$

$$R_{bh} = R_{bh0}[1 - 0.06 \epsilon_1 + 0.07 \epsilon_3 + 1.79 \epsilon_b] \quad (4e)$$

where $x = g_V/g_A$ as obtained A_{FB}^μ . The quantities in eqs. 1 and 4 are clearly not independent and the redundant information is reported for convenience. By comparison with the code of Ref. 13 (we also checked the results with the programme of ref.14) we obtain

$$\Gamma_{T0} = 2488.88[1 + 0.73 \delta\alpha_s - 0.35 \delta\alpha] \text{ MeV} \quad (5a)$$

$$R_0 = 20.8177[1 + 1.05 \delta\alpha_s - 0.28 \delta\alpha] \quad (5b)$$

$$\sigma_{h0} = 41.4221[1 - 0.41 \delta\alpha_s + 0.03 \delta\alpha] \text{ nb} \quad (5c)$$

$$x_0 = 0.0753142 - 1.32 \delta\alpha \quad (5d)$$

$$R_{bh0} = 0.21823 \quad (5e)$$

Note that the quantities in eqs. 5 should not be confused, at least in principle, with the corresponding Born approximations, due to small "non universal" electroweak corrections. In practice, at the relevant level of approximation, the difference between the two corresponding quantities is in any case significantly smaller than the present experimental error, from a factor of 2 in the case of Γ_T up to a factor of 6 in R_{bh} .

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The properties of the epsilons, as precisely defined from eqs.1, make them suitable for a model independent analysis of the electroweak precision tests. In particular, the fact that, for all observables at the Z pole, the whole relevant dependence on m_t (and m_H) only enters through the epsilons, is true for any extension of the Standard Model with the property that all possible deviations only occur through vacuum polarisation diagrams and/or the $Z \rightarrow b\bar{b}$ vertex. In any such model, of course, the actual values of the epsilons will differ in general from the SM ones. As discussed in detail in ref.1, for this kind of models one can compare the theoretical predictions with the experimental determination of the epsilons as obtained from the whole set of LEP/SLC data. If a particular model does not satisfy this requirement, then the comparison is to be made with the epsilons determined from the defining variables only, eqs.1, or with some more limited enlargement of the same

set of data, depending on the particular case. For example, if lepton universality is maintained, then the data on A_{FB}^l can be replaced by the combined result on g_V/g_A from all lepton asymmetries.

In principle, any four observables could have been picked up as defining variables. In practice we choose those that have a more clear physical significance and are more effective in the determination of the epsilons. In fact, since Γ_b is actually measured by R_{bh} (which is nearly insensitive to α_s), it is preferable to use directly R_{bh} itself as defining variable, as we shall do hereafter. In practice, since R_{bh0} , eq.5e is practically indistinguishable from the Born approximation of R_{bh} , this determines no change in any of the equations given above but simply requires the replacement of eqs. 1d,3d with eqs.4e, 5e among the defining relations of the epsilons. In this way, the equations that have completely general validity are eqs.1a,b,c and 4e together with eqs.3a,b,c and 5e, whereas the remaining observables and the corresponding equations, among which eqs.1d and 3d can be included in the analysis only according to the progression of hypothesis that we shall discuss.

We hope to have made clear by now that our method of analysing the data is more complete and less model dependent than an alternative approach based on the variables S, T and U [15], which, from the start, necessarily assumes dominance of vacuum polarisation diagrams from new physics and truncation of the q^2 expansion of the corresponding amplitudes. Furthermore, the variables S, T, U depend on m_t and m_H , being defined as deviations from the complete Standard Model prediction for specified m_t (and m_H). Instead the epsilons are defined with respect to a reference approximation which does not depend on m_t .

By combining the value of m_W/m_Z [1] with the LEP results on the charged lepton partial width and the forward-backward asymmetry, all given in table 1, one obtains from eqs. 1a,b,c and 3a,b,c:

$$\begin{aligned}\epsilon_1 &= \Delta\rho = (4.7 \pm 2.2) 10^{-3} \\ \epsilon_2 &= (-3.2 \pm 5.0) 10^{-3} + 0.23 \delta\alpha \\ \epsilon_3 &= (3.4 \pm 3.0) 10^{-3} - 0.77 \delta\alpha\end{aligned}\tag{6}$$

Finally, by adding the value of R_{bh} listed in table 1 and using eqs. 4e, 5e one finds :

$$\epsilon_b = (2.5 \pm 4.6) 10^{-3}\tag{7}$$

The central values of the epsilons, as determined experimentally, depend on the chosen value $\alpha(m_Z)$, since the Born approximation of the defining variables does. As before, we have taken $\alpha(m_Z)=1/128.87$ [16] but, in eqs.6,7, we have given the variation induced on the epsilons by corresponding shifts $\alpha(m_Z)$. At present there is a lively debate in the

literature on the best value of $\alpha(m_Z)$ that can be extracted from the data on $e^+e^- \rightarrow \text{hadrons}$ and on the corresponding uncertainty [17]. By using eqs. 6,7 the reader can easily adapt the results to his/her preferred values.

In fig.1 the experimental 1σ ellipse in the ϵ_1 - ϵ_3 plane is shown and compared, as a particularly relevant example, with the Standard Model predictions for different m_t and m_H values. We recall that ϵ_1 and ϵ_3 are completely determined by Γ_1 and A_{FB}^1 . In fig.2 the experimental value of ϵ_2 is compared with the Standard Model prediction as a function of m_t . There is consistency at all practical values of m_t . Note that ϵ_2 also depends on m_W/m_Z and better measurements of this quantity are needed in order to make this test more stringent. Finally, in fig.3 we compare the experimental value of ϵ_b with the Standard Model prediction. Here we see that ϵ_b would prefer relatively small values of m_t . This result is a simple and direct consequence of the fact that the measured value of R_{bh} is a bit high (for $m_t \sim 170$ GeV, Γ_b is about 2σ larger than the Standard Model prediction).

To proceed further, and include other measured observables in the analysis we need to make some dynamical assumptions. The minimum amount of model dependence is introduced by including other purely leptonic quantities at the Z pole such as A_{pol}^τ , A_e (measured [4] from the angular dependence of the τ polarisation) and A_{LR} (measured by SLD [18]). At this stage, one is simply relying on lepton universality. With essentially the same assumptions one can also include the data on the b-quark forward backward asymmetry A_{FB}^b . In fact it turns out that A_{FB}^b is almost unaffected by the $Z \rightarrow b\bar{b}$ vertex correction.

As a result, we can combine the values of $x = g_V/g_A$ from the whole set of asymmetries measured at LEP (obtaining the value given in table 1) and we can include, in the fit of the epsilons, eqs. 4d, 5d, valid in a more general theory fulfilling the stated assumptions. At this stage, with the SLD result also taken into account, the best values of ϵ_1 , ϵ_2 and ϵ_3 are modified according to

$$\begin{aligned}\epsilon_1 &= \Delta\rho = (5.1 \pm 2.2) 10^{-3} \\ \epsilon_2 &= (-4.1 \pm 4.8) 10^{-3} \\ \epsilon_3 &= (5.1 \pm 2.0) 10^{-3} \\ \epsilon_b &= (2.4 \pm 4.6) 10^{-3}\end{aligned}\tag{8}$$

with a similar dependence on $\alpha(m_Z)$ as in eqs.6,7. In fig.4 we report the two ellipses in the ϵ_1 - ϵ_3 plane that correspond to the data with and without A_{LR} from SLD.

All observables measured on the Z peak at LEP can be included in the analysis provided that we assume that all deviations from the Standard Model are only contained in vacuum polarisation diagrams (without demanding a truncation of the q^2 dependence of the corresponding functions) and/or the $Z \rightarrow b\bar{b}$ vertex. Note that this is true for whatever partition of the new effect between g_{bV} and g_{bA} , because only one combination of them is measured in Γ_b , while, as already mentioned, A_{FB}^b is nearly independent of the $Z \rightarrow b\bar{b}$ vertex.

For a global fit of all high energy data we consider m_W/m_Z , Γ_T , R_h , σ_h , R_{bh} and $x=g_V/g_A$ given in table 1. The relations between these quantities and the epsilons, valid in any model of the assumed type, are given in eqs.1a,3a,4,5. For LEP data, we have taken the correlation matrix for Γ_T , R_h and σ_h given by the LEP experiments [4], while we have considered the additional information on R_{bh} and x as independent. We obtain (SLD is also included):

$$\begin{aligned}\varepsilon_1 &= \Delta\rho = (4.2 \pm 1.8) 10^{-3} - 0.27 \delta\alpha_s \\ \varepsilon_2 &= (-4.9 \pm 4.8) 10^{-3} - 0.24 \delta\alpha_s + 0.23 \delta\alpha \\ \varepsilon_3 &= (4.5 \pm 1.8) 10^{-3} - 0.17 \delta\alpha_s - 0.77 \delta\alpha \\ \varepsilon_b &= (-0.2 \pm 4.1) 10^{-3} - 1.23 \delta\alpha_s\end{aligned}\tag{9}$$

At this stage, the epsilons have acquired also a dependence on $\alpha_s(m_Z)$. We have taken $\alpha_s(m_Z) = 0.118$ [19] and we have given the variation induced on the epsilons by a shift of $\alpha_s(m_Z)$, as defined in eq.2. The comparison of theory (the SM) and experiment in the planes ε_1 - ε_3 , ε_b - ε_3 and ε_b - ε_1 is shown in fig.5,6 and 7, respectively. We see that the inclusion of all LEP quantities does not change the epsilons very much. The effect of a ± 0.007 uncertainty on $\alpha_s(m_Z)$ is included in the quoted error for ε_b . Note that ε_b moves in the direction of the Standard Model prediction. This is because Γ_T , σ_h and R_h (or equivalently the ratios of Γ_Z , Γ_h and Γ_1), which also depend on ε_b , are normal.

Because of the fact that Γ_T , σ_h , R_h depend on α_s much more than R_{bh} , the fitted value of ε_b in eq.9 depends on the assumed value of $\alpha_s(m_Z)$, that we have taken as in table 1. If we repeat the fit of high energy data with $\alpha_s(m_Z)$ free, ε_b moves up to $\varepsilon_b \cdot 10^3 = 2.6 \pm 4.8$ (to fix R_{bh} which is nearly independent of $\alpha_s(m_Z)$) while $\alpha_s(m_Z)$ goes down to $\alpha_s(m_Z) = 0.111 \pm 0.009$. Finally, ε_1 , ε_2 and ε_3 are quite insensitive to $\alpha_s(m_Z)$ and closely keep their values in eq.9.

To include in our analysis lower energy observables as well, a stronger hypothesis needs to be made: vacuum polarization diagrams are allowed to vary from the Standard Model only in their constant and first derivative terms in a q^2 -expansion. In such a case, one can, for example, add to the analysis the ratio R_V of neutral to charged current processes in deep inelastic neutrino scattering on nuclei [20], the "weak charge" Q_W measured in atomic parity violation experiments on Cs [21] and the measurement of g_V/g_A from $\nu_\mu e$ scattering [22]. The expressions of these quantities in terms of the epsilons are given in ref.1. In this way one obtains the global fit (also including SLD):

$$\begin{aligned}\varepsilon_1 &= \Delta\rho = (3.6 \pm 1.7) 10^{-3} \\ \varepsilon_2 &= (-5.3 \pm 4.7) 10^{-3} \\ \varepsilon_3 &= (4.0 \pm 1.7) 10^{-3} \\ \varepsilon_b &= (0.2 \pm 4.0) 10^{-3}\end{aligned}\tag{10}$$

with the same dependence on $\alpha_s(m_Z)$ and $\alpha(m_Z)$ as in eqs.9. With the progress of LEP the low energy data, while important as a check that no deviations from the expected q^2 dependence arise, play a lesser role in the global fit. The ε_1 - ε_3 plot for all data is shown in fig.8. We observe no drastic change in the epsilons and we take this fact as evidence that no exotic q^2 dependence is visible. The inclusion of more parameters to describe the possible departure from the q^2 behaviour predicted by the Standard Model was discussed in refs.

23,24. Their conclusion coincides with ours that no sign of special q^2 dependent non standard effects is observed. Any attempt of significantly constraining the additional parameters is frustrated by the limited precision of the low energy data.

Note that the present ambiguity on the value of $\alpha(m_Z) = (128.87 \pm 0.12)^{-1}$ [16] corresponds to an uncertainty on ϵ_3 (the other epsilons are not much affected) given by $\Delta\epsilon_3 \cdot 10^3 = \pm 0.7$. Thus the theoretical error is still comfortably less than the experimental error but the two will become close at the end of the LEP1 phase. The values of ϵ_2 and ϵ_b in eq.10 were compared with the Standard Model predictions in figs. 2 and 3.

* * *

Finally we would like to add some comments.

As is clearly indicated in figs.5-12 there is by now a solid evidence for departures from the "improved Born approximation", defined as including the predictions from the tree level Standard Model plus pure QED and pure QCD corrections only, where all the epsilons vanish. Such evidence comes from ϵ_1 and ϵ_3 , both measured with an absolute error below $2 \cdot 10^{-3}$ and shown to be different from zero at more than the 2σ level for each of them. In this way one has obtained a strong evidence for pure weak radiative corrections, thus fulfilling one of the explicit goals of the precision electroweak tests. LEP and SLC are now measuring the different components of the radiative corrections.

Of great significance is also the fact that both ϵ_1 and ϵ_3 are reproduced in the Standard Model with an appropriate choice of m_t and m_H . This can be interpreted as an indirect but nevertheless significant evidence for the description of the electroweak symmetry breaking sector of the theory in terms of fundamental Higgs(es), as in the Standard Model or its supersymmetric extension. This is true in spite of the fact that the dependence of ϵ_1 and ϵ_3 on the Higgs mass is rather weak. One should consider in fact that, in most examples of Higgs-less theories that can be found in the literature [25,26], ϵ_1 and ϵ_3 , when they can be computed [27], show relatively large deviations from the predictions of the Standard Model. In this respect a further reduction of the errors on ϵ_1 and ϵ_3 , together with an improved direct determination of m_t at the Tevatron, are extremely important. Similarly, it would also be interesting to have a clear evidence for a deviation from zero of the remaining parameters, ϵ_2 and ϵ_b . These important goals of the electroweak precision tests are indeed possible in a near future.

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$m_Z(\text{GeV})$	91.1888 ± 0.0044
$\Gamma_T(\text{MeV})$	2497.4 ± 3.8
$R=\Gamma_h/\Gamma_l$	20.795 ± 0.040
$\sigma_h=12\pi\Gamma_e\Gamma_h/m_Z^2\Gamma_T^2 \text{ (nb)}$	41.49 ± 0.12
$\Gamma_l(\text{MeV})$	83.96 ± 0.18
$\Gamma_h(\text{MeV})$	1745.9 ± 4.0
$\Gamma_b(\text{MeV})$	382.7 ± 3.1
$R_{bh}=\Gamma_b/\Gamma_h$	0.2192 ± 0.0018
A_{FB}^l	0.0170 ± 0.0016
A_{pol}^τ	0.143 ± 0.010
A^e	0.135 ± 0.01091
A_{FB}^b	0.0967 ± 0.0038
A_{FB}^c	0.0760 ± 0.0091
$g_v/g_a(\text{all asymmetries -LEP})$	0.0716 ± 0.0020
$A_{LR} \text{ (SLD)}$	0.1637 ± 0.0075
$g_v/g_a(\text{all asymmetries-LEP+SLD})$	0.0738 ± 0.0018
$m_W/m_Z \text{ (UA2+CDF+D0) [28]}$	0.8798 ± 0.0020
$\alpha_s(m_Z) \text{ [19]}$	0.118 ± 0.007

Table 1

Summary of the data [4] used in the present paper

m_t (GeV)	$m_H=$ 65 GeV	ϵ_1			ϵ_2			ϵ_3		ϵ_b
		300	1000	65	300	1000	65	300	1000	All m_H
120	1.51	0.888	-0.23	-5.72	-5.40	-5.25	5.04	6.4	7.07	-2.29
130	2.19	1.54	0.413	-6.10	-5.74	-5.56	4.96	6.3	6.96	-2.98
140	2.93	2.25	1.10	-6.46	-6.07	-5.86	4.88	6.21	6.85	-3.71
150	3.72	3.00	1.84	-6.80	-6.38	-6.15	4.81	6.12	6.75	-4.48
160	4.56	3.81	2.63	-7.13	-6.70	-6.45	4.74	6.03	6.65	-5.30
170	5.47	4.68	3.47	-7.48	-7.03	-6.76	4.68	5.95	6.57	-6.15
180	6.43	5.60	4.36	-7.84	-7.36	-7.07	4.63	5.88	6.49	-7.05
190	7.44	6.57	5.29	-8.23	-7.71	-7.39	4.58	5.81	6.41	-7.99
200	8.53	7.6	6.27	-8.64	-8.08	-7.72	4.54	5.76	6.35	-8.98
210	9.67	8.69	7.30	9.08	-8.47	-8.08	4.51	5.72	6.29	-10.0
220	10.9	9.83	8.37	9.55	-8.9	-8.45	4.49	5.69	6.23	-11.1
230	12.2	11.0	9.49	-10.0	-9.36	-8.85	4.49	5.67	6.18	-12.2

Table 2

Values of the epsilons in the Standard Model as functions of m_t and m_H as obtained from recent versions of ZFITTER [13] and TOPAZ0 [14]. These values are obtained for $\alpha_s(m_Z)=0.118$, $\alpha(m_Z)=1/128.87$ but are essentially independent of these input parameters.

Figure Captions.

1. The 1σ ellipse in the plane ε_1 - ε_3 obtained from the data on the defining variables Γ_1 and A_{FB}^1 compared with the Standard Model predictions for the indicated values of m_t and m_H .
2. The 1σ data on ε_2 obtained from the data on the defining variables Γ_1 , A_{FB}^1 and m_W/m_Z compared with the Standard Model predictions as functions of m_t for the indicated values of m_H . The arrows indicate the experimental 1σ band from the fit in eq.10 to all electroweak data.
3. The 1σ data on ε_b obtained from the data on the defining variables Γ_1 , A_{FB}^1 , m_W/m_Z and R_{bh} compared with the Standard Model predictions as functions of m_t . The arrows indicate the experimental 1σ band from the fit in eq.10 to all electroweak data.
4. The 1σ ellipses in the plane ε_1 - ε_3 obtained from the data on Γ_1 and g_V/g_A derived from all the asymmetries (see table 1), both with SLD included or not, compared with the Standard Model predictions for the indicated values of m_t and m_H .
5. The 1σ ellipses in the plane ε_1 - ε_3 obtained from the data on m_W/m_Z , Γ_T , σ_h , R_h , R_{bh} and g_V/g_A derived from all the asymmetries (see table 1), both with SLD included or not, compared with the Standard Model predictions for the indicated values of m_t and m_H .
6. The 1σ ellipses in the plane ε_b - ε_3 obtained from the data on m_W/m_Z , Γ_T , σ_h , R_h , R_{bh} and g_V/g_A derived from all the asymmetries (see table 1), both with SLD included or not, compared with the Standard Model predictions for the indicated values of m_t and m_H .
7. The 1σ ellipses in the plane ε_1 - ε_b obtained from the data on m_W/m_Z , Γ_T , σ_h , R_h , R_{bh} and g_V/g_A derived from all the asymmetries (see table 1), both with SLD included or not, compared with the Standard Model predictions for the indicated values of m_t and m_H .
8. The 1σ ellipse in the plane ε_1 - ε_3 obtained from all the data also including the low energy data compared with the Standard Model predictions for the indicated values of m_t and m_H .