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in Deuteron Break-up Reactions
within the Bethe-Salpeter Formalism**

The Tensor Analyzing Power T_{20} in Deuteron Break-up Reactions within the Bethe-Salpeter Formalism

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Abstract

The deuteron tensor analyzing power T_{20} in the deuteron break-up reaction $Dp \rightarrow pX$ is calculated within a relativistic approach based on the Bethe-Salpeter equation with a realistic meson-exchange potential. Our results on T_{20} and the cross section are compared with experimental data and non-relativistic calculations and with the outcome of a relativization procedure of the deuteron wave function.

I. Introduction: Deuteron break-up reactions $A(D, p)X$ at medium and high energies are thought to serve as source of information on the high momentum components of the deuteron wave function. In the impulse approximation (IA) the differential cross section is proportional to the deuteron single-nucleon momentum density. This gives hope for the possibility of a direct extraction of the deuteron wave function from the experiment. Numerous experimental data from Dubna [1] and Saclay [2] have confirmed the IA picture for small internal momenta of nucleons in the deuteron, while a reasonable description of the data at higher momenta requires the incorporation of relativistic effects. It has been shown that even a minimal relativization procedure [3, 4] of the non-relativistic wave function is sufficient to describe fairly well the data in the kinematical region measured so far, except for a relatively broad shoulder around $p' \approx 0.3 \text{ GeV}/c$ (p' is the momentum of the final proton in the deuteron rest frame, see below). Some unconventional processes have been considered as small corrections to IA in attempts to explain this shoulder in the cross section [5]. The success of such a simple but descriptive interpretation of the data has allowed one to introduce a notion of an experimental deuteron wave function, often referred to as the Moscow wave function [1, 2], and to discuss different aspects of the deuteron structure in these experiments.

In the same experiments one measures the polarization characteristics of the deuteron, such as the tensor analyzing power T_{20} and the polarization transfer κ . These quantities are more sensitive to the reaction mechanism and to the internal structure of the colliding particles and give more detailed information. The first data on polarization phenomena has shown a discrepancy with theoretical predictions based on IA with Bonn or Paris light cone wave functions [4]. The main disappointing moment here is that, while the theoretical calculation predicts a change of the sign of T_{20} , the experimentally deduced values seem to remain negative in the whole interval of the measured momenta. Very recent, preliminary data [6] has confirmed that T_{20} is still negative, up to $p' \sim 0.5 \text{ GeV}/c$. In this case an interpretation of the data in terms of a direct extraction of the deuteron wave function becomes doubtful. Even the very notion of an experimental deuteron wave function has to put into question. This challenge stimulated investigations of other than IA mechanisms of interaction (c.f. [5] and references therein) and possible manifestations of non-nucleonic degrees of freedom in the deuteron. All these additional contributions have been investigated as corrections to minimal relativization, and conclusions about the role

of other mechanisms have been drawn relative to these results. Apart from the interest in other mechanisms, the investigation of relativistic effects in different approaches is still of importance. We would like to emphasize that the contributions of other (unconventional) mechanisms may be discussed only after a consistent relativistic calculation of the main process. Nowadays the most complete relativistic investigation of one-nucleon exchange diagrams has been performed in ref. [7] for backward elastic pD scattering by solving numerically the Bethe-Salpeter (BS) equation with a realistic interaction. Several authors [8] studied the relativistic effects in the deuteron by considering the $D \rightarrow NN$ vertex within different approximations of the exact BS equation and applying it to electromagnetic and hadron elastic scattering of the deuteron. Up to now a consistent relativistic calculations for the deuteron break-up reactions and polarization phenomena in these processes is still lacking.

In this paper we present a relativistic analysis of the deuteron tensor analyzing power T_{20} and cross section in forward break-up reactions. A fully covariant expression for both the cross section and T_{20} is obtained within the Bethe-Salpeter formalism. Results of numerical calculations, utilizing the recently obtained numerical solution of the BS equation with a realistic interaction, are compared with the available experimental data and with several theoretical approaches, such as nonrelativistic and light cone calculations.

II. The relativistic impulse approximation: We consider the inclusive break-up reaction of the type $\vec{D} + p \rightarrow p'(0^0) + X$, where the typical initial energy of the polarized deuteron is in the order of a few GeV, and one final proton is detected in the forward direction. In first approximation this reaction may be regarded as a process where one of the nucleons is removed from the deuteron by a small transferred momentum, while the other one continues to move nearly with the velocity it had before the collision. In this situation the cross section $D + A \rightarrow p'(0^0) + X$ is even expected to be independent of the target A and only the deuteron structure is relevant to describe the process. Such a simplified picture has been experimentally confirmed by detecting an almost target and energy independence of both the deuteron break-up cross sections and the tensor analyzing power T_{20} in a large interval of energies [1, 2, 6]. Therefore, the deuteron break-up may be represented by a Feynman diagram in IA as shown in Fig. 1a. Due to the target independence of the cross section it is clear that the vertices of the diagram should factorize and consequently, they may be computed separately. In the Fig. 1b the target part of the

cross section is depicted, and we begin our calculations with this subdiagram.

The corresponding amplitude is written in the form

$$A_{NN \rightarrow X} = (\bar{\mathcal{U}}_X \Gamma_{NN \rightarrow X})_{\alpha\beta} (u(p_p, s_p))_\alpha (u(p_n, s_n))_\beta, \quad (1)$$

where $(\bar{\mathcal{U}}_X \Gamma_{NN \rightarrow X})$ is the truncated $NN \rightarrow X$ vertex, and $u(p, s)$ are the Dirac spinors for the incident nucleons. Then the cross section is given by

$$d\sigma = \frac{1}{16\sqrt{\lambda(p_p, p_n)}} \Lambda_{\alpha\alpha'}(p_p) \Lambda_{\beta\beta'}(p_n) O_{\alpha\alpha'\beta\beta'}, \quad (2)$$

where $\lambda(p_1, p_2) = (p_1 p_2)^2 - m_1^2 m_2^2$ is the flux factor, and $\Lambda(p)$ stands for the projection operator of an on-shell nucleon. The operator O , acting in the nucleon spinor space, is defined as

$$O_{\alpha\alpha'\beta\beta'} = \sum_X (2\pi)^4 \delta^4(p_p + p_n - P_X) \left[(\bar{\Gamma}_{NN \rightarrow X} \mathcal{U}_X)_{\alpha'\beta'} (\bar{\mathcal{U}}_X \Gamma_{NN \rightarrow X})_{\alpha\beta} \right] \frac{d^3 P_X}{2E_X (2\pi)^3}. \quad (3)$$

To evaluate this operator one needs, in principle, an analysis of the $NN \rightarrow X$ vertices by expanding them in a basis of a complete set of (4×4) matrices in the spinor space and a further partial wave analysis of the corresponding coefficients. For the elastic NN scattering such a procedure has been realized in refs. [9, 10]. In our case, for the considered energies, one may neglect the spin structure of the NN vertices and take the operator (3) in its simplest form, i.e.,

$$O_{\alpha\alpha'\beta\beta'} \approx \delta_{\alpha\alpha'} \delta_{\beta\beta'} \cdot \mathcal{M}(p_p, p_n), \quad (4)$$

where $\mathcal{M}(p_p, p_n)$ is a scalar function depending only on the initial energy of the nucleons.

Then the expression for the total NN cross section takes the form

$$\sigma_{tot} = \frac{1}{16\sqrt{\lambda(p_p, p_n)}} \text{Tr}(\hat{p}_p + m) \text{Tr}(\hat{p}_n + m) \mathcal{M}(p_p, p_n) = \frac{m^2}{\sqrt{\lambda(p_p, p_n)}} \mathcal{M}(p_p, p_n). \quad (5)$$

The kinematics of the $Dp \rightarrow pX$ reaction is defined according to the graph in Fig. 1(a) by $p'_p = p_2$, $p_n = p_1$, $p_{1,2} = \frac{1}{2}P_D \pm p$, where p is the relative momentum and P_D is the total momentum of the deuteron. Then the amplitude of the basic process reads

$$A_{Dp \rightarrow pX} = (\bar{\mathcal{U}}_X \Gamma_{NN \rightarrow X})_{\alpha\beta} (\bar{u}(p_2, s_2))_\gamma \left(\frac{\hat{p}_1 + m}{p_1^2 - m^2} \right)_{\beta\delta} (u(p, s_p))_\alpha (\Gamma_{D \rightarrow NN})_{\delta\gamma}, \quad (6)$$

where the truncated $\Gamma_{D \rightarrow NN}$ vertex satisfies the BS equation. The cross section for the break-up of a polarized deuteron with a given spin projection M is

$$d\sigma_{Dp \rightarrow pX} = \sigma_{tot}(p_p, p_1) \frac{\sqrt{\lambda(p_p, p_n)}}{\sqrt{\lambda(p_p, P_D)}} \frac{1}{2m} \text{Tr} \left(\bar{\Psi}_M^D(p) \Psi_M^D(p) (\hat{p}_2 - m) \right) \frac{(p_2^2 - m^2)}{2E_2} \frac{d^3 p_2}{(2\pi)^3}. \quad (7)$$

In deriving eq. (7) we made use of eq. (4), and instead of the truncated $\Gamma_{D \rightarrow NN}$ vertex we introduced a modified BS amplitude, $\Psi_M^D(p)$, which includes the nucleon propagators in its definition [11]. As a consequence, in eq. (7) the term $(p_2^2 - m^2)$, which is zero when the nucleon is on mass shell, appears explicitly. It cancels singularities in the BS amplitude induced by the propagators and ensures the expression (7) to be finite. The trace in eq. (7) is evaluated by an algebraic formula manipulation code.

With this at hand it is easy to calculate the tensor analyzing power T_{20} in terms of cross sections (7) from the relation

$$\sqrt{2} T_{20} = \frac{d\sigma(M=1) + d\sigma(M=-1) - 2d\sigma(M=0)}{\sum_M d\sigma(M)} = 1 - \frac{d\sigma(M=0)}{\frac{1}{3} \sum_M d\sigma(M)} \quad (8)$$

III. Results and discussion: In the calculations we use our recent solutions [12] of the BS equation with a kernel with $\pi, \omega, \rho, \sigma, \eta, \delta$ exchanges (parameters as in Table 1 in ref. [12]). In obtaining numerical solutions of the BS equation we expanded the amplitude Ψ^D on the complete set of the Dirac γ matrices and solved a system of eight integral equations for partial amplitudes in the Wick-rotated system (for further details see ref. [11]). It is worth mentioning that our partial amplitudes depend on both $\vec{p}$ and ip_0 , whereas in the considered reactions with one nucleon on mass shell, the relative energy p_0 is fixed by kinematics and it is real. Hence, one needs a numerical recipe for an analytical continuation of the amplitudes from the imaginary to real axis of relative energy. This procedure has been investigated by Tjon [7] in studying diagrams similar to that in Fig. 1a with the result that there is a small difference (less than 5%) between the analytically continued partial amplitudes at the appropriate p_0 and simply putting $p_0 = 0$. In our calculation we follow the results of ref. [7] and choose the relative energy $p_0 = 0$.

In figs. 2 and 3 we present the results of our relativistic calculation of the cross section (7) and the deuteron tensor analyzing power T_{20} (8). A comparison is also given with nonrelativistic results which utilize the Bonn wave function [13] and with results of the minimal relativization of the Bonn and Paris wave functions within the light cone dynamics [3, 4]. Experimental data are from refs. [1, 2, 6]. It is seen that our calculated values of the cross section and T_{20} coincide with the nonrelativistic calculations up to $p' \sim 0.25$ GeV/c. Differences occur for larger proton momenta. For T_{20} these differences can be traced back to admixtures of negative energy states in the partial BS amplitudes, in particular the P -waves in the deuteron. The relative weight of the P -waves is rather small and in the unpolarized

case the contribution of these negative energy states is negligible [7, 8]. However, in the polarization case they play a more important role and lead to an improvement of the description of the data. As seen in fig. 3, even a consistent relativistic calculation does not yet describe satisfactorily the data in the region of the minimum of T_{20} at $p' \sim 0.3$ GeV/c. Note that in this region the unpolarized cross section has a broad shoulder, see fig. 2. As mentioned above, this shoulder may be reproduced by considering some other diagrams with final state interaction mediated by meson exchanges [5]. Other kinds of corrections, e.g., rescattering effects, have been computed in ref. [2]. Both these mechanisms, meson exchanges and rescattering effects, reduce the depth of the minimum in fig. 3 and lead to a shift of the sign change of T_{20} to larger values of p' . With this in mind one may expect that relativistic calculations, completed by corrections from the other mentioned mechanisms, describe both sets of experimental data in figs. 2 and 3. The present difference between relativistically calculated values of T_{20} and the experimental data may be referred to as a signal of manifesting some unconventional mechanisms (like meson exchange currents, Δ isobars, final state interaction, 3-body interaction etc.) in the deuteron break-up.

The approach based on the minimal relativization scheme describes also rather well the differential cross section (see fig. 2) but results in a more drastic disagreement with data for polarization observables (see fig. 3). The minimal relativization procedure [3, 4] consists of (i) a replacement of the argument of the nonrelativistic wave functions by a light cone variable $k^2 = m^2(1 - 2x)^2/4x(1 - x)$, where $x = (E_{p'} + p'_p)/(E_D + P_D)$ and (ii) multiplying the wave functions by a factor $\sim 1/(1 - x)$. As result the argument is shifted towards larger values and the wave function itself decreases more rapidly. This effect of suppressing the wave function is compensated by the kinematical factor $1/(1 - x)$. Hence, the minimal relativization leads to a rather good description of spin averaged observables in the deuteron. A different situation occurs in case of computing polarization observables which are proportional to the ratio of cross sections. In this case all the kinematical factors cancel out and the effect of relativization comes only from the shift in arguments of the S and D -waves in the deuteron. Clearly, this leads to a squeezing effect of T_{20} in comparison with the nonrelativistic values, as seen in fig. 3. In the BS amplitude the relativistic effects are of dynamical nature and are not reduced to a simple shift in arguments and, in addition to S and D -waves, it contains negative energy components, i.e., P -waves which allow for a more refined analysis of the data.

An analysis of polarization observables in two, at first glance, different processes, such as the deep-inelastic scattering of polarized leptons off polarized deuterons and the polarized deuteron break-up, persuades us to a tight relation between the deep-inelastic structure functions $b_{1,2}(x)$ (see ref. [14] for definition), and the tensor analyzing power T_{20} . In deep-inelastic processes one considers reactions of inclusive scattering similar to the break-up reaction; the deuteron structure functions $b_{1,2}(x)$ are related to the cross section by a relation similar to that in eq. (8), except that $d\sigma(M)$ is replaced by the deuteron structure function $F_2^D(x, M)$ and that $b_{1,2}(x)$ are not normalized to $\sum_M F_{1,2}^D(x, M)$. If we introduce new, normalized, deep-inelastic structure functions by

$$\tilde{b}_{1,2}(x) = \frac{F_{1,2}^D(x, M=1) + F_{1,2}^D(x, M=-1) - 2F_{1,2}^D(x, M=0)}{\sum_M F_{1,2}^D(x, M)}, \quad (9)$$

the correspondence between T_{20} and $\tilde{b}_{1,2}(x)$ will be almost one to one. Consequently, the relativistic effects in these two functions are expected to be very similar. This assertion is partially confirmed by the present work and by the calculations performed in ref. [12].

V. Summary: In summary we present an analysis of relativistic effects in the deuteron tensor analyzing power T_{20} within the Bethe-Salpeter formalism with realistic interaction. The minimal relativization scheme is discussed and a comparison of the results of two approaches, i.e., the relativization within the light-cone dynamics and covariant BS formalism, with experimental data is given. For a perfect description of the experimental data one needs obviously processes beyond the impulse approximation.

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Figure captions

Fig. 1 The Feynman graphs for the $Dp \rightarrow pX$ reaction (a) and for the elementary reaction $NN \rightarrow X$ (b).

Fig. 2 The differential break-up cross section as function of the final proton momentum p' in the deuteron rest frame (solid line - our relativistic calculation within the Bethe-Salpeter formalism, dotted line - non-relativistic calculation with the Bonn deuteron wave function, long-dashed (short-dashed) line - results of a minimal relativization within the light cone dynamics of the Bonn (Paris) wave functions). Experimental data from ref. [1].

Fig. 3 The tensor analyzing power as function of p' (the meaning of the curves is as in Fig. 2; experimental data: triangles - ref. [2]; open circles - ref. [6] open squares - ref. [6] (elastic backward pD-scattering); close circles - ref. [1] ($^{12}C(D, p)X$ reactions)).

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