Modelling the effects of dust on galactic SEDs from the UV to the millimeter band

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**ABSTRACT**

We present models of photometric evolution of galaxies in which the effects of a dusty interstellar medium have been included with particular care. A chemical evolution code follows the star formation rate, the gas fraction and the metallicity, basic ingredients for the stellar population synthesis. The latter is performed with a grid of integrated spectra of simple stellar populations (SSP) of different ages and metallicities, in which the effects of dusty envelopes around asymptotic giant branch (AGB) stars are included. The residual fraction of gas in the galaxy is divided into two phases: the star forming molecular clouds and the diffuse medium. The relative amount is a model parameter. The molecular gas is sub-divided into clouds of given mass and radius: it is supposed that each SSP is born within the cloud and progressively escapes it. The emitted spectrum of the star forming molecular clouds is computed with a radiative transfer code. The diffuse dust emission (cirrus) is derived by describing the galaxy as an axially symmetric system, in which the local dust emissivity is consistently calculated as a function of the local field intensity due to the stellar component. Effects of very small grains, subject to temperature fluctuations, as well as polycyclic aromatic hydrocarbons (PAH) are included.

The model is compared and calibrated with available data of normal and starburst galaxies in the local universe, in particular new broad-band and spectroscopic ISO observations. It will be a powerful tool to investigate the star formation, the initial mass function (IMF), supernovae rate (SNR) in nearby starbursts and normal galaxies, as well as to predict the evolution of luminosity functions of different types of galaxies at wavelengths covering four decades.

*Subject headings:* dust, extinction — galaxies: ISM — galaxies: spiral — galaxies: starburst — infrared: galaxies — radiative transfer
1. Introduction

Observations performed in the last decade or so, particularly in the IR regime, have clearly demonstrated that dust is one of the most important components of the interstellar medium (ISM), containing a large fraction of heavy elements ejected from stars. This paper is mainly concerned with the influence of dust grains on the transfer of radiation emitted by stellar systems. Basically dust absorbs and scatters photons, mostly at wavelengths $\lesssim 1 \mu m$ and returns to the radiation field the subtracted energy in the form of IR photons. The resulting spectral energy distribution (SED) is often substantially changed and in many relevant cases radically modified.

Not surprisingly, dust reprocessing of the optical–UV photons emitted by stars into the infrared regime turns out to be particularly severe in galaxies undergoing massive episodes of star formation, which preferentially occur within dense molecular clouds. Indeed dust could affect galaxy evolution because it modifies the physical and chemical conditions of the ISM. In particular star formation is at least favored by the presence of dust, which shields dense clouds from stellar UV radiation and keeps them to temperatures low enough to allow the onset of gravitational instability.

The SED of normal star–forming disk–like galaxies is also affected by dust, mainly associated with the diffuse ISM and with the envelopes of evolved asymptotic giant branch (AGB) stars. As for early type systems, it has been often suggested that the first episode of massive star–formation could be essentially hidden to optical searches due to dust reprocessing, since their ISM might have been metal enriched on a very short timescale, the lifetime of the first generation of massive stars (Franceschini et al. 1994 and references therein; Cimatti et al. 1997). Even local quiescent elliptical galaxies exhibit infrared emission (e.g. Jura 1986; Bally & Thronson 1989; Knapp et al. 1989; Roberts et al. 1991) and visual dust obscuration (e.g. Veron–Cetty & Veron 1988; Kim 1989; Goudfrooij et al. 1994), arising in part from dust grains continuously formed in dusty outflows from AGB stars (Tsai & Mathews 1996; Bressan, Granato, & Silva 1998), as well as molecular line emission (e.g. Gordon 1990; Roberts et al. 1991; Lees et al. 1991). Overall, a direct comparison of the luminosity functions of galaxies in the optical and in the far–IR shows that, locally, about 30% of starlight is dust–reprocessed.

At least three different dusty environments must be taken into account in order to properly understand the UV to sub–mm properties of galaxies: (i) dust in interstellar H I clouds heated by the general interstellar radiation field (ISRF) of the galaxy (the ‘cirrus’ component), (ii) dust associated with star forming molecular clouds and H II regions and (iii) circumstellar dust shells produced by the windy final stages of stellar evolution. These environments have different importance in different galactic systems at various evolutionary stages.

Despite this, in many papers dealing with the spectrophotometric evolution of galaxies the radiative processes occurring in a dusty interstellar medium were originally neglected (e.g. Bruzual & Charlot 1993 and Leitherer & Heckman 1995, the former the most adopted one to interpret data on different galaxy types, the latter appositely built for starburst galaxies). Indeed their codes are nowadays commonly used together with some prescription to approximate the effects of the ISM. In other cases (e.g. Guiderdoni & Rocca–Volmerange 1987; Mazzei, De Zotti, & Xu 1994; Lançon & Rocca–Volmerange 1996; Fioc & Rocca–Volmerange 1997), the effects of dust are included only partially and/or with substantial simplifications. For instance often extinction is considered but thermal reradiation is not, or scattering is neglected, or not all the relevant dusty environments are considered, or optically thin emission is assumed, or a unrealistic geometry is adopted. Those works facing a complete computation of the radiative transfer through a dusty medium, do not include it in the more general framework of galaxy evolution, but are instead interested either in the interpretation of single objects (e.g. Krügel & Siebenmorgen 1994) or in understanding the effects of dust geometry on the extinction of the emerging spectrum (e.g. Bruzual, Magris, & Calvet 1988; Witt, Thronson, & Capuano 1992; Cimatti et al. 1997; Wise & Silva 1996; Bianchi, Ferrara, & Giovanardi 1996; Gordon, Calzetti, & Witt 1997).

The inclusion of dust effects into spectrophotometric codes leads to many difficulties. While the integrated photometric properties of an hypothetical dust–free galaxy are geometry independent, dust introduces a strong dependence on the distribution of both stars and ISM. Moreover the optical properties of dust grains and their dependence on environmental conditions have not yet been fully explored and understood. The ensuing uncertainty may
only be parametrized to some extent. The effects of scattering, absorption and emission of grains, which may not be in radiative equilibrium with the radiation field, complicate the solution of the integro–differential transfer equation in a complex geometry.

Nonetheless a more realistic and complete computation of the spectrophotometric galaxy models including dust is required, since neglecting the complexity of the dust effects can lead to erroneous estimates of many interesting quantities such as the star formation rate (SFR). Also, the estimate of the age of a galaxy through the fit of its broadband SED is hampered by the degeneracy between the colors of an old galaxy and those of an extinguished young galaxy (e.g. Cimatti et al. 1997), further complicating the well known age–metallicity degeneracy.

We have therefore developed chemo–spectrophotometric self–consistent galactic models including dust. Three different dusty environments are considered: envelopes of AGB stars, molecular star–forming clouds and diffuse ISM; the dust model is comprehensive of normal big grains, small thermally fluctuating grains and polycyclic aromatic hydrocarbons (PAH) molecules; for each grain family, the appropriate computation of absorption and reemission is performed. The models are suited to simulate galaxies of any Hubble type, in different evolutionary stages, since we include the possibility of different geometrical distributions both for stars and gas. The complete radiative transfer equation is numerically solved whenever necessary.

The many parameters and uncertainties introduced by the presence of dust can be constrained only by means of the multiband approach pursued in this paper, where the spectrophotometric properties of galaxies are consistently reproduced from the UV to the sub–mm, i.e. taking into account extinction at short wavelengths and the consequent thermal emission in the IR regime. The combination of observations from HST, Keck, ISO and ground–based optical, IR and sub–mm telescopes already provided several objects at significant redshift with spectral information on this large λ range. Their number will increase after the completion of ISO surveys, and will burst when SIRFT, FIRST, Planck Surveyor and NGST will operate.

In this paper we present the model and we use it to study local galaxies. In a forthcoming paper we will exploit it to study the cosmic evolution of different types of galaxies.

### 2. Model description

We divide the problem of estimating the SED of a galaxy at age $t_G$, including dust effects, in two steps: (1) the history of the star formation rate $\Psi(t)$, of the initial mass function (IMF), of the metallicity $Z(t)$ and of the residual gas fraction $g(t)$ is determined and then (2) the integrated SED of the galaxy is predicted taking into account all the stars and the gas present at $t_G$. When the effects of dust are neglected, step (2) simply involves a sum of all the spectra of stars. In our case we have instead to introduce a specific geometry for gas and stars, and then to compute the radiative transfer of the radiation emitted by the stars and the dust.

The purpose of the present work is mainly to develop a general procedure for step (2). Step (1) includes a number of possible choices which can be easily interfaced to our code in order to describe the evolution of the SED.

#### 2.1. Chemical evolution

The chemical evolution is a preliminary process in our code. We summarize here the main aspects of the code, which basically follows the guidelines given by Tantalo et al. (1996).

The code describes one–zone open models including the infall of primordial gas ($\dot{M}(t) \propto \exp(-t/t_{inf})$), in order to simulate the collapse phase of galaxy formation and, when required by the astrophysical situation under study, galactic winds.

The adopted SFR is a Schmidt–type law, i.e. proportional to some power (between 1 and 2) of the available gas mass: $\Psi(t) = \nu M_g(t)^k$. For starburst galaxies we add to the general smooth SFR one or more bursts of star formation. As for the IMF we used the usual Salpeter law: $\Phi(M) \propto M^{-x}$, with $x = 2.35$. The upper limit of the mass range is fixed to $100 M_\odot$.

This kind of chemical evolution models has been successfully tested against nearby spheroidal galaxies, and also well reproduces the properties of different types of galaxies with appropriate choices of the parameters (e.g. a quiet spiral–type evolution is well mimicked with a low value of $\nu$ and/or a long infall time scale, see Matteucci 1996 for a thorough review).
2.2. Synthesis of starlight spectrum (including dusty envelopes of AGB stars)

The library of isochrones for the simple stellar populations (SSPs), the building-blocks of galaxy models, is based on the Padua stellar models (Bertelli et al. 1994), with a major difference, consisting in the computation of the effects of dusty envelopes around AGB stars. The SSPs span a wide range in age, from 1 Myr to 20 Gyr, and in metallicity, $Z = 0.004, 0.008, 0.02, 0.05, 0.1$, to realistically reproduce the mix of age and composition of the stellar content of galaxies. The inclusion of a wide range of metallicity is imposed by the aim of comparing model estimates to the excellent data available even for young high redshift galaxies.

The spectral synthesis technique, for the starlight alone, consists in summing up the spectra of each stellar generation, provided by the SSP of the appropriate age and metallicity, weighted by the SFR at time of the stars birth (e.g. Bressan, Chiosi, & Fagotto 1994).

Effects of dust in the envelopes of evolved stars are usually neglected in the synthesis of a composite population. This is not justified for intermediate age population clusters, whose brightest tracers are AGB stars, and/or in a wide-wavelength synthesis approach. To overcome this limitation, we computed new isochrones and SSPs in which, along the AGB, a suitable dusty envelope is assumed to surround the star. For this envelope the radiative transfer is solved by means of the code described by Granato & Danese (1994). The envelope parameters, in particular its optical thickness, which is straightforwardly linked to the mass-loss rate and to the expansion velocity, are derived as a function of basic stellar parameters (mass, luminosity, radius, and metallicity) combining hydrodynamic model results and empirical relations. A detailed description of the adopted procedure can be found in Bressan et al. (1998).

2.3. Geometry

As already pointed out, the dust effects on SEDs depend on the relative distribution of stars and dust. The assumed geometry is sketched in Fig. 1. The galaxy is approximated as a system having azimuthal symmetry as well as planar symmetry with respect to the equatorial plane. We take into account three components: i) star forming molecular clouds complexes, hereafter MCs, comprising dusty gas in a dense phase, H II regions and very young stars embedded in it (young stellar objects YSO); ii) stars already escaped from these dense clouds (henceforth free stars); iii) diffuse gas (cirrus).

We work in spherical coordinates $(r, \theta, \phi)$. The densities of the three components $\rho_{\text{MC}}$, $\rho_*$, and $\rho_c$ respectively, depend on $r$ and $\theta$ through analytical laws. In the following, unless otherwise explicitly stated, $\rho_{\text{MC}}$ and $\rho_*$ have identical spatial dependence. In order to describe disk–like galaxies, we use a double exponential of the distance from the polar axis $R = r \sin \theta$ and from the equatorial plane $z = r \cos \theta$:

$$\rho = \rho_0 \exp(-R/R_d) \exp(-|z|/z_d).$$

(1)

In the code the scale lengths $R_d$ and $z_d$ can be independently set for the three components, but in the models presented in this paper (Sec. 3) we simply adopt identical values for them. In other words we use two adjustable parameters when describing disk–like galaxies: $R_d^* = R_d^\text{MC} = R_d^\gamma$ and $z_d^* = z_d^\text{MC} = z_d^\gamma$. Observations within our Galaxy suggest $z_d^\gamma \sim 0.35$ kpc. As a reference the $e$-folding scale length is related to the absolute magnitude by

$$\log_{10}(R_d/\text{kpc}) \sim -0.2 M_B - 3.45,$$

(2)

(Im et al. 1995).

In the case of spheroidal systems we adopt for both stars and dust spherical symmetric distributions with King profile:

$$\rho = \rho_0 (1 + (r/r_c)^2)^{-\gamma},$$

(3)

extended up to the tidal radius $r_t$. This truncation radius is required in King models since $M(r)$, the mass contained within $r$, diverges as $r \to \infty$. Our results are not very sensitive to its precise choice, thus we simply adopted the standard value $\log(r_t/r_c) = 2.2$. As for the stellar component we simply set $\gamma = 3/2$. It has been suggested that the core radius $r_c$ correlates with the luminosity (Bingelli, Sandage, & Tarenghi 1984):

$$\log_{10} \left( \frac{r_c}{\text{kpc}} \right) \sim \begin{cases} -0.3 (M_B + 22.45) & \text{if } M_B \leq -20, \\ -0.1 (M_B + 27.34) & \text{if } M_B > -20. \end{cases}$$

(4)

The distribution of dust in spheroidal systems is poorly known, but it has been suggested that $\rho_{\text{dust}} \propto \rho_0^\text{stars}$ with $n \approx 1/2 \pm 1/3$ (Froehlich 1982; Witt et al. 1992; Wise & Silva 1996), i.e. $\gamma \approx 0.5 \div 0.75$. In other words the dust distribution seems to be less concentrated than that of stars. In particular an additional
cool component located in the outer parts has been invoked to explain IRAS observations (Tsai & Mathews 1996).

The volume emissivity (ergs cm\(^{-3}\) s\(^{-1}\) ster\(^{-1}\) Å\(^{-1}\)) of the galaxy at each point is the sum of three terms, arising respectively from the three components listed above:

\[
j_{\lambda} = j_{\lambda}^{\text{mc}} + j_{\lambda}^{\text{at}} + j_{\lambda}^{\text{d}}. \tag{5}
\]

In the following sections we will describe how these quantities, as well as the specific flux measured by an external observer, are computed. A preliminary stride is to define the optical properties of dust.

2.4. The dust model

Once the geometrical arrangement is specified, the effects of dust on radiative transfer depend on physical and chemical properties of grains, which affect the way they absorb and emit photons. It is expected and observationally well established that these properties are functions of the particular environment in which grains happen to live. Several populations may be distinguished (see Dorschner & Henning 1995 for a review): (i) stellar outflow dust (further subdivided into the two chemical subgroups of carbon rich and oxygen rich dust); (ii) dust in the diffuse ISM; (iii) dust in molecular clouds and dust around YSOs. As for stellar outflow dust, we refer to the treatment of Bressan et al. (1998) mentioned above. Here we discuss our choices for the other two dusty components of the model galaxy.

Although a lot of efforts have been devoted to derive a so called standard model for dust in the diffuse ISM, its precise composition remains controversial. Significant clues can be derived from observations. The prominent features observed in its spectrum at 9.7 and 18 µm indicate the presence of silicate grains. By converse, the origin of the 2175 Å feature is somewhat debated, though graphite still stands as the most attractive solution (see Mathis 1990). The emission bands in the 3–13 µm region indicate the presence of PAHs (Puget, Léger, & Boulanger 1985), which together with small thermally fluctuating grains contribute also to produce the warm mid–IR cirrus emission. Therefore we included these components in our diffuse dust model. We adopted the same mixture even for MCs, for which the information are scanty, only decreasing the fraction of PAH molecules (see below).

The optical properties of silicate and graphite grains have been computed by Laor & Draine (1993) for spherical shapes using Mie theory, the Rayleigh–Gans approximation and geometric optics. In particular we used the cross sections of graphite and silicate grains computed by B.T. Draine for 81 grain sizes from 0.001 to 10 µm in logarithmic steps \(\delta \log a = 0.05\), and made available via anonymous ftp at astro.princeton.edu.

In order to get the overall radiative properties of the dust mixture, the abundance and the size distribution of grains must be specified. We started from the distribution proposed by Draine & Lee (1984, henceforth DL), which is tuned on the optical–UV extinction law of the galactic diffuse ISM. On the other hand DL pointed out that their model displays significant discrepancies with extinction data above 2 µm, and that these discrepancies are not surprising, since observations at longer \(\lambda\) tend to sample lines of sight through denser clouds, where grain population may differ from that present in more diffuse regions.

A more severe limitation of DL model is that the mid–IR (MIR) cirrus emission at wavelengths \(\lambda \leq 60\) µm is not reproduced (Fig. 3), because grains are always large enough to maintain a low temperature thermal equilibrium in the general ISRF. This emission requires reprocessing of the field by particles, very small grains and/or PAH molecules, reaching temperatures higher than those attained with equilibrium heating (e.g. Puget et al. 1985; Draine & Anderson 1985; Dwek et al. 1997). This requirement can be matched by decreasing the lower limit of the graphite grain distribution. Since these grains must be more numerous than the simple extrapolation of the DL power law, a break to a steeper power law is introduced below \(a_h\). These adjustments to the DL model enhance the MIR cirrus emission, but tend to degrade the agreement with the observed extinction law in the optical–UV region. However a reasonable compromise can be found. For graphite grains we adopted the following size distribution:

\[
\frac{dn_i}{da} = \begin{cases} 
A_i n_H a^{\beta_i} & \text{if } a_h < a < a_{\text{max}}, \\
A_i n_H a_{\beta_i}^{\beta_2} & \text{if } a_{\text{min}} < a < a_h,
\end{cases} \tag{6}
\]

with \(a_{\text{min}} = 8\) Å, \(a_{\text{max}} = 0.25\) µm, \(a_h = 50\) Å, \(\beta_1 = -3.5\), \(\beta_2 = -4.0\) and \(A_i = 10^{-25.22} \text{ cm}^{2.5} / \text{H}\). As for silicate grains, we maintained the same size distribution as DL. As a result, 282 atoms per million H (ppM hereafter) of C are locked in dust grains.

In the code the size distributions have been discretized in 20 logarithmic bins following the prescriptions given by Draine & Malhotra (1993). Once the
bathing radiation field is specified, the emissivity of grains with radius $a > 100$ Å is computed assuming that they achieve thermal equilibrium, so that all grains of a given composition and radius emit as gray bodies at a single temperature. Below this limit a temperature distribution for each size bin and composition is computed following Guhathakurta & Draine (1989), and then the emissivity is obtained by integrating over this distribution.

To model the observed IR emission occurring in bands at 3.3, 6.2, 7.7, 8.6 and 11.3 μm we include also a population of planar PAHs. The optical–UV absorption cross-section $\sigma_{PAH}$ is reported in Fig. 2. This has been obtained by averaging the cross sections of 6 different PAH mixtures measured by Léger et al. (1989) above 1200 Å, and smoothly joining the resulting mean curve to the coronee cross section below this limit. The same cross section is used to take into account the effects of PAH on the extinction curve, assuming a vanishing albedo (Fig. 3). Désert, Boulanger, & Puget (1990) have proposed an analytical description of $\sigma_{PAH}$ derived from the observed interstellar extinction curve in the 1200–3300 Å range, under the assumption that these particles dominate its EUV rise. On the other hand the extreme UV (EUV) rise can be ascribed to small grains. Actually using DL optical efficiencies, the EUV part of the extinction curve is produced by small grains. Our $\sigma_{PAH}$ rests on laboratory measurements and predicts, in the local interstellar radiation field, a PAH absorption and subsequent IR emission lower by a factor $\sim 0.5$ with respect to the Désert et al. (1990) analytical approximation.

In order to compute the IR emission of PAHs, their heat capacity $C_{PAH}(T)$ must be specified. A numerically convenient and accurate enough representation of the estimate given by Léger, d’Hendecourt, & De Fourneau (1989) is:

$$C_{PAH}(T) = \begin{cases} 
9.25 \times 10^{-4} T & \text{if } T < 800 \text{ K}, \\
2 \times 10^{-4} T + .58 & \text{if } 800 \leq T < 2100 \text{ K}, \\
1 & \text{if } T \geq 2100 \text{ K},
\end{cases}$$

(7)

where $C_{max} = 3[N_t - 2]k$ and $N_t = N_C + N_H$ is the total number of atoms (carbon and hydrogen) in the molecule. We adopt a population of PAHs with a distribution $dn/dN_C \propto N_C^{-2.25}$ from $N_C = 20$ to $N_C = 280$. Smaller molecules are easily destroyed by UV photons (Omont 1986). This distribution is quite similar to those adopted by other authors (Dwek et al. 1997, Désert et al. 1990). Astrophysical PAHs are thought to be partially dehydrogenated: probably due to the large UV flux in the emission regions, some of the CH bonds, responsible for the 3.3, 8.6 and 11.3 μm bands, are broken. The number of H atoms in a molecule is thus written as $N_H = x_H N_{s,H}$, where $N_{s,H}$ is the number of hydrogen sites and $x_H$ is the H coverage. The relationship between $N_{s,H}$ and $N_C$ depends on the arrangements of hexagonal cycles in the molecule. The ratio $N_C/N_{s,H}$ is rather constant around 2 for laboratory PAH molecules, for which $N_C \lesssim 50$. However, the structure of typical interstellar PAHs is likely closer to that of catacondensed PAHs (Omont 1986), which are the most compact and stable ones and have the general formula $C_{bpz}H_{6p}$, i.e. $N_{s,H} = (6 N_C)^{0.5}$. For these quasi–circular molecules, usually assumed to represent the gross features of interstellar PAHs, the radius is given by $a = 0.9 \sqrt{N_C}$ Å if $N_C >> 1$. With the above relationship between $N_{s,H}$ and $N_C$ the typical flux ratios observed in the ISM between CH and CC bands (Mattila et al. 1996) is fairly well reproduced by our PAH model setting $x_H = 0.2$.

PAHs emissivity was then computed following substantially the guidelines given by Xu & De Zotti (1989). The adopted abundances of PAH molecules in the diffuse ISM and in the MCs implies that 18 and 1.8 ppM of C are locked in this component respectively. Indeed there are indications showing that in denser environments and/or in stronger UV radiation field the relative number of small particles is significantly diminished (Puget & Léger 1989; Kim & Martin 1996 and references therein). In particular Xu & De Zotti (1989) concluded that PAH molecules are less abundant by a factor ~10 in our galaxy star forming regions than in the diffuse gas.

As apparent from Fig. 3, this model reproduces reasonably well both the extinction from IR to UV and the whole cirrus emission. The model predicts an extinction below a few observational estimates at $\lambda \gtrsim 300\mu$m by a factor $\sim 10$. To account for this, Rowan–Robinson (1986, 1992) introduced ad hoc modifications of the grain optical properties in his discretized models. We avoid in general this ap-
approach (but see Sec. 3.1) mainly because these data have large uncertainties (DL), as it is apparent from their scatter. Moreover they refer to dusty environments for many respects different from the diffuse dust, which is instead the dominant contributor to the emission at \( \lambda \gtrsim 100 \mu m \) in our galaxy models. Also it has been suggested that the silicate grain absorption in the sub–mm wavelength range may decline less steeply than \( \lambda^{-2} \) (Agladze et al. 1996).

The adopted mixture, even taking into account the contribution of PAH emission features, tends to underpredict the MIR cirrus emission, in particular the shorter \( \lambda \) data. A larger quantity of small grains and/or PAH molecules would improve the match with DIRBE observations, but would also produce a large disagreement with observed UV–extinction (Dwek et al. 1997). We prefer to adopt a compromise more balanced toward the extinction law, since in our models and in most interesting cases the MIR emission is in general dominated by warm dust in MCs rather than thermally fluctuating grains in the cirrus, whilst a good specification of the extinction properties is crucial. Moreover, DIRBE cirrus data at short wavelength could be affected by significant systematic effects (Dwek et al. 1997).

The total (i.e. cirrus + MCs) dust content of a galaxy ISM depends on the residual gas and on dust–to–gas ratio \( \delta \). The residual gas mass is provided at each time step by the chemical evolution model (see above). Determinations of \( \delta \) in our Galaxy ISM and in nearby objects range typically from 1/100 to 1/400. For the purpose of this paper, where the model is compared only to galaxies in the local universe, we simply set \( \delta = 1/110 \), the standard value of DL model. However the code is thought to interpret data on objects in very different evolutionary stages, thus we need in general a recipe to scale \( \delta \) when the chemical conditions in the ISM where very different. We adopt the simplest assumption \( \delta \propto Z \), with the proportionality constant adjusted to have \( \delta = 1/110 \) for \( Z = Z_\odot \).

A recent difficulty for models relying on populations of carbon–based grains, the so-called carbon crisis, is connected with the quite uncertain determination of cosmic abundance of this element. Indeed these models were developed under the hypothesis that the measured solar system abundances (either in meteorites or solar photosphere) were also typical for the ISM. For instance, DL as well as our model, requires 282 ppM of C in grains, assuming a graphite density of 2.26 gr cm\(^{-3} \). This is 55 \% of the solar abundance which was adopted by DL as cosmic reference abundance (but \( \sim 80 \% \) of the more recent estimate in the solar system \( \sim 365 \) ppM quoted by Anders & Grevesse 1989). However in the last few years evidence has been accumulated that solar abundances may be not representative of the ISM. In particular in young star photospheres carbon is found to be only \( \sim 200 - 250 \) ppM (e.g. Snow & Witt 1995, 1996; Gies & Lambert 1992). This, if really representative of the ISM abundance, would put restrictions difficult to meet by carbon–based dust models (Sofia, Cardelli, & Savage 1994; Cardelli et al. 1996; Mathis 1996), especially when taking into account that about 140 ppM seem to be in gas phase (Cardelli et al. 1996), leaving for dust only about 1/3 of the C required by the DL model.

Possible ways out have been suggested: for instance big grains could be porous, likely because they are built up by sticking of smaller ones (Mathis & Whiffen 1989; Mathis 1996), or dust could be to some extent prevented to be incorporated into stars during their formation (Snow & Witt 1996). Also the introduction of carbonaceous grains in a form other than graphitic (amorphous carbon, possibly hydrogenated, or composite grains), the use of more complex size distribution than a simple power law, and an elongated grain shape tend to alleviate the C requirements (Mathis 1996; Kim & Martin, 1996).

Since these problems are still far from being clarified and our major concern is to obtain a good description of the absorption and emission properties of dust, we maintain by now a DL–type model, looking only for the minimum modifications required to obtain an acceptable overall match of the extinction curve from the UV to the far–IR and of the galactic cirrus emission. It is worth noticing that in the future this goal should be achieved with a more efficient use of the available cosmic carbon. The main effect of this on our spectrophotometric galaxy models will be a possible decrease of the required dust–to–gas ratio by a factor up to \( \sim 2 \).

### 2.5. The radiative transfer in dusty media

As already remarked, to get the SED from 0.1 to 1000 \( \mu m \), we have to solve the transfer equation for the radiation in presence of dust in the case of molecular clouds and diffuse ISM.
2.5.1. Radiation transfer in MCs and emerging spectra

In the Galaxy virtually all the star formation activity resides in molecular clouds. Maps of CO and other tracers, show that MCs are non-uniform, highly structured objects, containing density-enhanced regions, the cores, wherein star formation actually occurs. This implies the clustering of young stars at different locations inside giant molecular clouds, as confirmed by infrared imaging. The first evolutionary stages are hidden at optical wavelengths and a minor fraction being reradiated as recombination lines. The powerful stellar winds and outflows, and the ionizing flux from massive stars, all contribute to the destruction of the molecular clouds in a time scale comparable to the lifetime of OB stars, \( \sim 10^6 - 10^7 \) yr. Thus stars gradually get rid of their parent gas and become visible at optical wavelengths. The typical dust densities in these objects are so high that even IR photons are self absorbed, thus to compute the emitted SED the radiative transfer equation must be solved.

The complex evolution depicted above is simulated as follows. A fraction \( f_{mc} \) of the model gas mass \( M_{\text{gas}} \) at \( t_G \) is ascribed to the dense phase under discussion in this section. Recent estimates in our Galaxy suggest that half of the hydrogen mass is molecular \( \text{H}_2 \), mainly in clouds with diameters \( \gtrsim 10 \) pc. The molecular gas \( M_{mc} = f_{mc} M_{\text{gas}} \) is then sub-divided into spherical clouds of assigned mass and radius, \( m_{mc} \) and \( r_{mc} \), which may range in the typical observed intervals \( \sim 10^5 - 10^6 \) \( M_\odot \) and \( \sim 10 - 50 \) pc respectively. It is then supposed that each generation of stars, represented in our scheme by a SSP, is born within the cloud and progressively escapes it. This is mimicked by linearly decreasing the fraction \( f \) of SSP energy radiated inside the cloud with its age \( t \):

\[
f = \begin{cases} 
1 & \text{if } t \leq t_o, \\
2 - t/t_o & \text{if } t_o < t \leq 2 t_o, \\
0 & \text{if } t > 2 t_o. 
\end{cases}
\] (8)

The model parameter \( t_o \), introduced by this relation sets the fraction of starlight that can escape the star-bursting region. The starlight locked up inside the cloud is approximated as a single central source. The cloud optical depth is fixed by the cloud mass and radius and by the dust-to-gas ratio. The emerging spectrum is obtained by solving the radiative transfer through the cloud with the code described by Granato & Danese (1994).

The distribution of stars in real GMCs implies a dust temperature distribution with many hot spots and cooler regions randomly distributed. A complete discussion of the effects of different approximations in this complex geometrical situation, including the single central source adopted here, can be found in Krügel & Siebenmorgen (1994, see in particular their Fig. 1a). An obvious drawback of our approach is an overestimate of the amount of very hot dust around the source, with respect to the more realistic approximation in which the stars are split in many sources at different locations. On the other hand the approximation of a central point source is not much different from the IR spectrum predicted by a full treatment with hot spots, if the emission from the whole cloud is considered (Krügel & Siebenmorgen 1994).

Since the treatment of many hot spots in the cloud would introduce many other geometrical parameters and would slow down considerably our code due to the loss of symmetry, we simply treat the maximum temperature \( T_o \) of the grains at the inner edge as a parameter, summarizing in some way the geometrical parameters which would result in a lower ‘true’ maximum temperature: lowering the grain ‘sublimation’ temperature produces a lower average temperature with a less opaque cloud. This brings the overall spectrum very close to that predicted with a proper treatment of the hot spots. It is anyway interesting to note that Gordon et al. (1997) found that their shell geometry, similar to that adopted here, is suited to explain the observed optical and UV properties of starburst galaxies, while the dusty geometry, in which dust and stars share the same spatial distribution, is not, even allowing for clumpiness.

For typical values of the relevant parameters our model predicts IR spectra of star forming regions peaking around 40–60 \( \mu \)m (in a \( \nu L_\nu \) plot), depending on the optical depth, with a rather steep decrease at longer wavelengths. We found that this behavior reproduces quite well the typical range of IR spectra of galactic YSOs, H II, and star forming regions (e.g. Rowan–Robinson 1979; Ward-Thompson & Robson 1990; Men’shchikov & Henning 1996). For instance in Fig. 4 the observed SED of W49A, a huge star-forming region composed of H II regions and giant molecular clouds, is compared with the spectrum of the MC component we use in the fit of the overall
SED of Arp 220. Indeed we think that this ultraluminous infrared galaxy is a good benchmark for our MCs model, having an IR spectrum dominated by this component (see Section 3.1).

### 2.5.2. Propagation in the diffuse ISM and cirrus emission

Before escaping the galaxy the light arising from stellar populations and from molecular clouds interacts with the diffuse dust component.

We adopt a simplified treatment of radiative transfer in the diffuse gas which ignores dust self-absorption and approximates the effects of optical–UV scattering by means of an effective optical depth, given by the geometrical mean of the absorption and scattering efficiencies \( \tau_{\text{eff}, \lambda} = \tau_a(\tau_a + \tau_s) \) (Rybicky & Lightman 1979, p. 36). Indeed the relatively low opacity of dust in the IR regime, where the dust emission occurs, implies that in most cases of interest the diffuse ISM is transparent to its own photons. Our approximation for combined scattering and absorption processes is rigorously applicable only to an infinite homogeneous medium and isotropic scattering. However, we checked, by comparing our results with those obtained by Witt et al. (1992) by means of a Monte Carlo radiative transfer code including anisotropic scattering, that it is fairly good in most "real-world" geometrical arrangements (see Fig. 5).

The galaxy is subdivided into small volume elements \( V_i \). The local (angle averaged) radiation field in the \( i \)-th element due to the extinguished emissions of free stars and MCs from all the elements is computed from:

\[
J_{\lambda, i} = \sum_k V_k (j_{\lambda, k}^{\text{me}} + j_{\lambda, k}^{\text{MC}}) \exp \left( -\tau_{\text{eff}, \lambda}(i, k) \right) r^2(i, k), \tag{9}
\]

where \( \tau_{\text{eff}, \lambda}(i, k) \) and \( r(i, k) \) are the effective optical thickness and the distance between the elements \( i \) and \( k \) respectively. Then the local dust emissivity is calculated as described in section 2.4. Finally the specific flux measured by an external observer in a given direction \( \theta \) is derived as a sum over the galaxy of the extinguished emissivity of free stars, MCs, and diffuse dust:

\[
F_{\lambda}(\theta) = 4\pi \sum_k V_k j_{\lambda, k} \exp \left( -\tau_{\text{eff}, \lambda}(k, \theta) \right), \tag{10}
\]

where \( \tau_{\text{eff}, \lambda}(k, \theta) \) is the optical thickness from the element \( k \) to the outskirts of the galaxy along the direction \( \theta \).

In the code the spheroidal systems are assumed to extend up to the tidal radius \( r_t = 10^{2.2}r_c \) (of the star component), while exponential disks are truncated at \( 6r_d \), where \( r_d \) is the largest of the three components. Since more than 98% of the mass is included within these radii, adoption of larger cut off radii would not produce any significant difference. Deviations from the energy balance between dust emission and absorption, which mainly depend on the number of volume elements in which the galaxy is subdivided, are kept within \( < 2 - 5\% \).

### 3. Comparison with the data

A few examples, showing the capability of our model to reproduce the data on starbursting and normal galaxies in the local universe, are discussed below. We restrict ourselves to galaxies for which available photometric observations allow a precise evaluation of the SED for UV to far-IR. The fitting parameters are reported in Tables 1 and 2 for the chemical model (step 1) and for the photometric model (step 2) respectively. Table 3 summarizes a few relevant quantities derived from those parameters. Since the purpose of this paper is to present a procedure to take into account the radiative effects of the ISM, the parameters \( t_{\text{inj}} \) and \( \nu \) (Table 1), which rule the SF history of the galaxy, where set following the general results of papers dealing with the chemical evolution of different types of galaxies (see Matteucci 1996 for a review), under the major constraint to get a suitable amount of residual gas. The following parameters have been fixed to reasonable values: galactic age \( t_G = 13 \) Gyr; dust-to-gas mass ratio \( \delta = 9 \times 10^{-3} \); exponent of Schmidt SFR \( k = 1 \); maximum temperature of dust in MCs \( T_m = 400 \) K, mass of single MC \( m_{\text{mc}} = 10^6M_\odot \). Moreover the mass limits of the Salpeter IMF are the standard \( M_{\nu} = 100M_\odot \) and \( M_{\text{low}} = 0.1 \), but for starburst galaxies where the estimates of dynamical mass require \( M_{\text{low}} \gtrsim 0.2 \), as discussed below. We also remind that, in order to keep the number of free parameters to the minimum required by present quality data, we set the scale lengths of stars and gas distributions in spirals to the same values, i.e. \( R_d^c = R_d^c \) and \( z_d^c = z_d^c \).

As previously noticed, the SED of the MCs component is set mainly by its optical depth (Table 3) \( \propto m_{\text{mc}}/r_{\text{mc}}^2 \), which is in some sense the true "fitting parameter" for this component (together with \( t_o \)), rather than \( r_{\text{mc}} \) reported in Table 2. In other
words the values found for $r_{mc}$ depend on having set $m_{mc} = 10^6 M_\odot$, as typical for Giant Molecular Clouds in the Galaxy, and $r_{mc}$ could well be varied by a factor $\sim 2$ producing almost equivalent fits, provided $m_{mc}$ would be adjusted to keep $m_{mc}/r_{mc}^2$ constant.

### 3.1. Starburst galaxies

**M82**

In the prototype starburst galaxy M82 the burst was probably triggered by the interaction with M81, some $10^8$ yr ago (Solinger, Morrison, & Markert 1977). Thanks to the proximity of this system ($D = 3.25$ Mpc) a wealth of data do exist, providing a well sampled full coverage of the SED at different angular resolutions, as well as other observational constraints. The fit (Fig. 6) is obtained by evolving for lar resolutions, as well as other observational con-

samples full coverage of the SED at different angu-

3

in the burst, suggested by dynamical considerations

$3 \times \times 10^8 M_\odot$, a factor 6 less than the estimated total dynamical mass (Doane & Mathews 1993). We adopted $M_t = 0.2 M_\odot$ as lower limit of the Salpeter IMF. A lower value would require a baryonic mass closer to the dynamical mass. The assumed parameters provide a SFR raising from 0 to about $3 M_\odot/yr$ in the first 3 Gyr, then smoothly declining to 1.35 $M_\odot/yr$ at $t = 13$ Gyr. To this gentle star formation history, which leaves a gas fraction of 0.064, we have superposed an exponential burst processing 18% of the residual gas in the last $5 \times 10^7$ yr, with an e-folding time also of $5 \times 10^7$ yr (Figure 7). Note that our results are almost independent on the precise evolution of the SFR in the burst: even a constant burst yields very similar estimates of the relevant quantities. Also the duration of the burst could be doubled or halved with small adjustment of the other parameters without damaging the quality of the SED fit. Thus we end with a total gas mass of $8.6 \times 10^8 M_\odot$, 8% of which is ascribed to the molecular component, organized in clouds with $m_{mc} = 10^6 M_\odot$ and $r_{mc} = 16$ pc. These clouds reprocess almost completely the starlight due to the burst. The system is assumed to follow a King profile with $r_k^* = 150$ pc for stars and $r_k^* = 200$ for diffuse gas.

The masses we ascribe to the various components favorably compare with radio estimates of total gas masses $\sim 10^9 M_\odot$ (Solinger et al. 1977), with CO determinations of gas in molecular form $\sim 10^8 M_\odot$ (Lo et al. 1987; Wild et al. 1992), and with an upper limit $\lesssim 3 \times 10^8 M_\odot$ to the mass of stars formed in the burst, suggested by dynamical considerations (McLeod et al. 1993). Also, in our proposed model the predicted supernovae rate (SNR) is between 0.05 and 0.1 yr$^{-1}$, depending on the adopted lower limit of stellar mass yielding to supernovae explosion 9 or 6 $M_\odot$ respectively. Observational estimates suggest a SNR in the range 0.07–0.3 yr$^{-1}$ (McLeod et al. 1993; Doane & Mathews 1993). Increasing the lower limit of the IMF in the burst to, for instance, $M_t = 1.0 M_\odot$ would increase the SNR by a factor $\sim 2$. In conclusion the model required to nicely reproduce the observed SED turns out to be in agreement with independent estimates of masses and of SNR.

**NGC 6090**

This strongly interacting galaxy at 175 Mpc ($H_0 = 50$ km/s/Mpc) has been observed by ISO from 2.5 to 200 $\mu$m (Acosta-Pulido et al. 1996). The SED resulting from the combination of these data with previously published optical photometry is nicely re-

produced by our model (Fig. 8). The differences in the parameters with respect to M82, apart from an up-scale in involved baryonic mass ($4.1 \times 10^{11} M_\odot$), are aimed at enhancing the diffuse dust emission at $\lambda \gtrsim 100 \mu$m, which, as noticed by Acosta-Pulido et al., is not reproduced by published starburst models. Thus the pre-burst SFR has been adjusted to leave a larger gas fraction (0.127), 3.2 % of which is processed by the burst. The molecular star-forming clouds accounts only for 0.5 % of the gas left by the burst.

**Arp 220**

Arp 220 is an archetypal ultraluminous infrared galaxy (ULIRG), most likely the result of a recent merging between two gas-rich galaxies, for which ISO/PHOT data have been now published (Klaas et al. 1997), and whose K-band light profile resembles that of a typical elliptical galaxy. In this object there is evidence of both starburst as well as Seyfert activity, but ISO spectroscopy led to the conclusion that the IR luminosity is primarily ($\gtrsim 90$ %) powered by star-

burst (Sturm et al. 1996). The fitting model requires a strong burst, converting into stars $2.5 \times 10^9 M_\odot$, i.e. as much as 11% of the total baryonic mass, and a high fraction 50% of residual gas in star–forming clouds. The gas fraction before the burst is 0.25. As a result, the IR and sub–millimetric emission is everywhere dominated by dust associated with star forming regions. The mass in molecular gas is $\sim 1.6 \times 10^{10} M_\odot$, in agreement with CO estimates (Solomon et al. 1997;
Scoville, Yun, & Bryant 1997). From a determination of the CO rotation curve Scoville et al. (1997) infer a dynamical mass of \( \sim 3 - 6 \times 10^{10} M_\odot \) within \( r \sim 1.5 \) kpc (depending on the adopted potential), in agreement with the mass requested by our model within the same radius \( \sim 4.1 \times 10^{10} M_\odot \).

We find that the sub–millimeter data of Arp 220 are underpredicted by a factor \( \sim 2 - 3 \) by any model which successfully reproduces the remaining SED, unless the long wavelength decline of grain absorption efficiency is reduced, say from \( \propto \lambda^{-2} \) to \( \propto \lambda^{-1.6} \) above \( \sim 100 \mu m \) (see Agladze et al. 1996 for laboratory measurements supporting this possibility for silicate grains). In Fig. 9 we report fits obtained adopting either the modified as well as the standard DL cross–sections.

### 3.2. Normal galaxies

In the following we examine objects that do not show clear signs of enhanced SF or nuclear activities in the SED nor in the morphology, namely 3 late–type spirals and a giant elliptical template. Indeed elliptical galaxies form a relatively homogeneous class, while this is not the case for spirals. We fit spirals later than Sb, which are clearly disk–dominated, and we adopt for them an exponential geometry (see Sec. 2.3).

**M51**

In Fig. 10 we present a fit to the SED of the nearly face–on \( (i = 20^\circ \), Tully 1974) Sbc galaxy M51 (NGC 5194), taken at a distance \( D = 9.6 \) Mpc (Sandage & Tammann 1975). Since the discrepancy between ISO and IRAS data at 60 and 100 \( \mu m \) could be due to an excess of the ISO point spread function (Hippelein et al. 1996), we fit the IRAS data. The model has a baryonic mass of \( 1.55 \times 10^{11} M_\odot \), whose evolution leaves at 13 Gyr a gas fraction of 0.067, 70% of which in molecular form. The mass of ISM in the molecular and diffuse components, as well as their relative fraction is in agreement, within a factor \( \leq 2 \), with estimates by Scoville & Young (1983), Young et al. (1989), and Devereux & Young (1990). Gas and stars are exponentially distributed with the same scale–lengths, 4.7 and 0.4 kpc for the radial and vertical scales respectively. The former value is in good agreement with those estimated by Beckman et al. (1996) from observed brightness distributions in different optical bands. Due to the low energy output observed at \( \lambda \lesssim 0.2 \mu m \), stars born during the last \( 5 \times 10^6 \) yr are hidden inside molecular clouds.

The striking correspondence between the 15 \( \mu m \) emission mapped by ISO and the \( H_\alpha \) emission indicates that the MIR is powered by recent star–formation (Sauvage et al. 1996). As for the far–IR (FIR), somewhat contradictory claims have been reported: Devereux & Young (1992), comparing the radial distributions of FIR, \( H_\alpha \), \( H I \), and \( H_\beta \) emission, concluded that the same holds true in the range 40–1000 \( \mu m \), while Hippelein et al. (1996) found no obvious correlation between FIR ISO PHOT maps and \( H_\alpha \) fluxes. This apparently complex situation is not surprising, since according to the model the MIR emission is provided by the MCs component, while above \( \sim 60 \mu m \) the diffuse dust gives a comparable contribution, which however is in part powered by young stars.

**M100**

The Sbc galaxy M100 (NGC 4321) is the largest spiral in the Virgo Cluster. We adopt a distance \( D = 20 \) Mpc and an inclination angle \( i = 30^\circ \). The model in Fig. 11 has a baryonic mass of \( 2 \times 10^{11} M_\odot \), with a residual gas fraction of 0.048, 80% in molecular form. Indeed, according to the gas masses estimated by Young et al. (1989) and Devereux & Young (1990), larger than ours by a factor \( \sim 2 \), the ISM seems to be dominated by the molecular component. The location of M100 in the central regions of the Virgo Cluster could affect some of its properties, as the \( H \alpha \) distribution that shows a sharp edge in correspondence to the optical radius (Knapen et al. 1993). This could be the reason for the warm FIR SED observed in M100, as compared to M51 and NGC 6946, despite their morphological similarity. The steep decline of the spectrum in the sub–mm region has been interpreted by Stark et al. (1989) as indicating that the emitting grains are warm and small. In our model this is not required since the fit is obtained with standard diffuse dust. Stars and dust share the same radial and vertical scale–lengths, 5 and 0.4 kpc respectively, in agreement with the values derived by Beckman et al. (1996) for the stellar component and with the \( H \alpha \) distribution.

**NGC 6946**

The fit to this Scd galaxy at distance \( D = 6.72 \) Mpc (Rice et al. 1988) and inclination angle \( i = 34^\circ \)
(Considere & Athanassoula 1988), is shown in Fig. 12. The total gas mass in the model, \(1.04 \times 10^{10} \, M_\odot\) i.e. 8.3\% of the baryonic mass, agrees with the molecular plus neutral hydrogen mass given by Young et al. (1989) or Devereux & Young (1990) (reported at 6.72 Mpc), while the fraction we ascribe to the molecular component is a factor \(\approx 2\) higher.

The contribution of young and old stellar populations to dust heating in this object has been considered by several authors. Devereux & Young (1993), comparing the radial distributions of FIR, \(H_\alpha\), \(H\,I\), and \(H_2\), conclude that the 40 to 1000 \(\mu\)m luminosity is dominated by dust associated with molecular gas heated by young stars. However ISO data reported by Tuffs et al. (1996) reveal an extended FIR emission out to a radius of 8\', with a scale–length similar to the R–band one, while little \(H_\alpha\) emission has been detected beyond \(r \sim 6\'). This suggests that part of the observed cold FIR SED of NGC 6946 could be due to dust associated with a diffuse \(H\,I\) gas, which indeed extends out to \(r \sim 15\)' (Boulanger & Viallefond 1992), and heated mainly by old stellar populations. Malhotra et al. (1996) find that the radial scale–lengths at 7 and 15 \(\mu\)m are similar to those in \(H_\alpha\) and \(H_2\) but much shorter than those in R–band and \(H\,I\), consistent with a warm dust emission primarily heated by young massive stars. In the proposed fit the MIR emission arises from MCs dust heated by newly born stars. The SED above \(\sim 60 \mu \text{m}\) is almost equally contributed by MCs and diffuse dust, but, since \(t_o = 2.5\) Myr, even the latter is predominantly heated by young stars.

Tacconi & Young (1986) estimate a scale–length of 9.6 kpc for the cold ISM component, whilst for the star distribution their values range from 4 to 8 kpc, depending on the band and on the galactic component (disc or arms) considered. The model scale–lengths are set to 8 for both stars and the diffuse gas. The vertical scale–lengths are 1 kpc to keep the diffuse dust emission sufficiently cold.

**Giant Ellipticals**

Ellipticals constitute a class of objects with fairly homogeneous spectral properties. It is then interesting to test our model against an average SED of giant E galaxies, constructed combining the Arimoto’s template (1996) from 0.12 to 2.2 \(\mu\text{m}\) with the median IRAS over band fluxes of bright ellipticals estimated by Mazzei et al. (1994) and the average (K–L) color computed by Impey et al. (1986) (Fig. 13). The fit has been obtained with a ‘classical’ star formation history model for ellipticals: an open model with infall and galactic wind. The high efficiency \(\nu = 2\) causes a huge SFR in the first 1.2 Gyr interrupted by the onset of the galactic wind (see Tantalo et al. 1996 for a discussion of these values). The object is observed at 13 Gyr, when a comparatively very small fraction of galactic mass in a diffuse dusty component is sufficient to produce the observed IRAS emission. Note that this gas is not provided by the chemical model, according to which the bulk of the ISM is ejected by the galactic wind which stops the star formation. Thus in this case the mass in the diffuse dust 1.5 \(\times 10^7\) \(M_\odot\) is a fitting parameter of our photometric model. This dusty ISM could arise from evolved stars of the passively evolving galaxy, by cooling flows or by merging activity. It is also worth noticing that \(r_c\) needs to be much greater for the ISM than for stars (6 and 0.4 kpc respectively): for smaller values of \(r_c\) the cirrus emission would be too warm because dust would be more concentrated in the central regions where the radiation field is higher. Other authors already suggested that diffuse dust in elliptical galaxies needs to be less concentrated than stars, on the basis of either optical color gradients (e.g. Wise & Silva 1996) or IRAS colors (e.g. Tsai & Mathews 1996).

As discussed in section 2.5.2, an alternative proposed way to describe this lower concentration is to adopt the same \(r_c\) for both stars and diffuse dust, decreasing the exponent \(\gamma = 1.5\) in the King law of stars. However for this SED, adjusting \(\gamma = r_c^c\) and \(r_c\) with the constrain \(r_c^c = r_c^*\), we found only marginally acceptable fits in the IRAS regime, significantly worse than that presented in Fig. 13.

**4. Discussion**

When reproducing starburst galaxies, our model is characterized by the variations of 6 parameters related to the total mass and star formation history and of 5 geometrical parameters (Tables 1 and 2). For normal disc galaxies, the parameters become 3 and 5 respectively. In order to fit the elliptical galaxy template, 7 parameters have been adjusted, including the epoch at which the SF activity is stopped.

The masses reasonably constrained by matching the SED are the baryonic mass (though dependent on the IMF, particularly its lower limit) mostly from the energy emitted in the near–IR (NIR) by the old stellar component, and the mass of dust, from its MIR–FIR emission. Therefore the mass of gas present in
the galaxy is constrained from the fit, provided $\delta$ is known. Our assumption $\delta = 9 \times 10^{-3}$ is likely the best guess for our Galaxy, however in different systems and in the Galaxy itself, variations of a factor of a few are commonly quoted, e.g. Rand, Kulkarni, & Rice (1992) for M51 or Tuffs et al. (1996) for NGC 6946. As a consequence, our estimated gas masses suffer by a similar uncertainty. The SFR history of the old stellar component is constrained by the spectrum and, for starburst galaxies, also by the requirement that a certain amount of gas is available for the latest burst. The three analyzed starbursts exhibit rather different star formation histories, with the average SFR of the old component inversely proportional to the strength of the SFR in the burst. Estimates of masses in stars and gas, as well as of SF and SN rates from observations other than broad band spectra, discussed in the previous sections and below, nicely agree with those provided by our SED fitting.

4.1. Starbursts and ULIRGs

The SFR in a starbursting region can be estimated on the basis of the FIR luminosity, under the assumption that dust reradiates the overall bolometric luminosity and after calibration with stellar synthesis models. Kennicutt (1997) proposes $\text{SFR} = L_{\text{FIR}} / (2.2 \times 10^{43} \text{ergs s}^{-1})$, with calibration derived from models of Leitherer & Heckman (1995). This relationship properly applies to star forming regions, while the extension to a galaxy as a whole is dangerous, since a non negligible portion of the FIR luminosity may arise from cirrus emission powered also by relatively old stars. However our model accurately determines the warm component associated to the MCs where star formation is occurring ($L_{\text{mc}}$ in Table 3). For M82 our fit predicts an overall FIR luminosity associated to the MCs component of $1.1 \times 10^{44} \text{ergs s}^{-1}$, which following Kennicutt translates in SFR = $5.0 M_\odot \text{yr}^{-1}$. Similarly, the SFRs inferred from the luminosity of the warm component is $57 M_\odot \text{yr}^{-1}$ and $460 M_\odot \text{yr}^{-1}$ for NGC 6090 and Arp 220 respectively. These figures are in very good agreement with those derived by fitting the SEDs and reported in Table 3. Thus while Kennicutt’s calibration is confirmed, we stress that this refers only to the warm component, which contributes $\approx 50\%$ of $L_{\text{FIR}}$ in NGC 6090. This source of uncertainty adds to the obvious effect of the adopted IMF in the conversion from observed IR luminosity to SFRs.

Whilst the very recent (say in the last 10 Myr) SFR is relatively well constrained by the observed warm IR emission, the burst duration, and therefore the total mass converted into stars, can be varied within a factor $\sim 2$, still yielding the correct $L_{\text{FIR}}$ and spectra after readjustments of other parameters. However the supernovae rates deduced from observations put further constraints on the average SFR and duration of the burst. In the well studied case of M82 the model predicts a SN rate in the interval deduced by observations.

The SFR can also be inferred from the ionizing luminosity $L_{\text{Lyc}}$, which can be derived from recombination lines. With the adopted IMF we find $L_{\text{Lyc}}/10^{44} \text{ergs s}^{-1} \approx 0.017 \text{SFR}(M_\odot \text{yr}^{-1})$, which holds with very small deviations for the six studied star-forming galaxies (see Table 3). The uncertainties connected to extinction corrections of observed line fluxes are minimized employing transitions occurring in the IR regime, such as Br$\gamma$ line ($\lambda = 2.17 \mu$m). Calzetti (1997) and Kennicutt (1997), using Leitherer & Heckmann (1995) results, find $\text{SFR}(M_\odot \text{yr}^{-1}) = L(\text{Br}\gamma)/1.6 \times 10^{39} \text{ergs s}^{-1}$ adopting a Salpeter IMF within 0.1–100 $M_\odot$ or $\text{SFR}(M_\odot \text{yr}^{-1}) = L(\text{Br}\gamma)/3.7 \times 10^{38} \text{ergs s}^{-1}$ when the mass range is 0.1–30 $M_\odot$.

The $(\text{Br}\gamma)$ line luminosity $L(\text{Br}\gamma) = 9.2 \times 10^{40} \text{ergs s}^{-1}$ of NGC 6090 (Calzetti, Kinney, & Storchi–Bergmann 1996) corresponds to a SFR=56 $M_\odot \text{yr}^{-1}$ with the assumption of the 0.1–100 $M_\odot$ mass range, only 18% less than that used in our model, while the smaller range in the IMF would predict a SFR higher by a factor 4. Kennicutt (1997) has shown that there is a clear trend for SFRs derived from $L_{\text{FIR}}$ to be larger than those estimated from the $L(\text{Br}\gamma)$, suggesting that extinction is non negligible even at near–IR wavelengths.

Genzel et al. (1997) reported the ratio of the far–IR to Lyman continuum luminosity $L_{\text{FIR}}/L_{\text{Lyc}}$ of starbursts (including M82) and ULIRGs, derived from near and mid–IR recombination lines. For 12 starburst galaxies the median value is $L_{\text{FIR}}/L_{\text{Lyc}} \approx 16$. The model ratio depends on the adopted IMF. Our fit to M82 overall SED yields $L_{\text{FIR}}/L_{\text{Lyc}} \approx 12$, where $L_{\text{Lyc}}$ is the unextincted luminosity of the (young) stellar populations below 912 Å in very good agreement with the value found by Genzel et al. (1997). For NGC 6090 the fit predicts $L_{\text{FIR}}/L_{\text{Lyc}} \approx 10$, using $L_{\text{mc}}$ to evaluate the model $L_{\text{FIR}}$ powered by the burst, well within the range of the values inferred by the same authors. As for Arp 220, which properly belongs to the ULIRG class, higher values
15 \lesssim \frac{L_{\text{FIR}}}{L_{\text{LyC}}} \lesssim 112$ are inferred from IR recombination lines, whereas our model predicts \( \frac{L_{\text{FIR}}}{L_{\text{LyC}}} \approx 11 \). The discrepancy is likely due to the uncertain large correction for IR extinction in this object. Actually Genzel et al. (1997) use a screen obscuration with \( A_V = 45 \), while we find \( A_V \approx 150 \) in MCs of this object. Interestingly enough, the 15 ULIRGs (including Arp 220) studied by Genzel et al. (1997), exhibit a median \( \frac{L_{\text{FIR}}}{L_{\text{LyC}}} \approx 40 \), larger by a factor of \( \sim 2.5 \) than that inferred for starburst galaxies. This result can be explained by larger obscurations or by a softer intrinsic Lyman continuum, pointing to an IMF less rich in massive stars or to an older starburst. In the models we used bursts began 0.05 Gyr ago, but still rather active due to the large e–folding time \( t_\text{e} = 0.05 \) Gyr.

It is worth noticing that our model does not account for the ionizing radiation converted into recombination lines, which are much less absorbed by dust than the Lyman continuum. In the present version of the code the UV radiation can be only converted directly to IR photons through dust absorption. However the energy budget is not significantly affected, since the observed luminosity in recombination lines is only a few percent of the bolometric luminosity of starburst galaxies (e.g. Genzel et al. 1997).

The observed UV emission at \( \lambda \gtrsim 1000 \) \( \text{Å} \) is crucial in determining the fraction of the SSPs escaped from the parent molecular clouds. In our model the UV flux emerging from a single galaxy depends on the age \( t_o \) after which a SSP starts to get out from the molecular cloud. The UV photons are affected also by absorption in the diffuse ISM. In the case of M82 and Arp 220 the measured UV flux is a tiny fraction of the bolometric luminosity (see Figg. 6 and 9). This implies that the stars of the burst are still inside their parent clouds. Indeed in these two objects \( t_o \) is about equal to the time since burst ignition 0.05 Gyr. By converse for NGC 6090 the data show that the UV is not a negligible fraction of the total, implying for our model \( t_o - t_{\text{burst}} > t_o = 0.018 \) Gyr. As a result stars with lifetime \( \gtrsim 18 \) Myr (corresponding to \( M \lesssim 10 M_\odot \)) are no more embedded within the clouds and contribute significantly to the ISRF. Actually the luminosity we ascribe to the diffuse cold component equals the warm one in NGC 6090, whereas it is 25% and 9% for M82 and Arp 220 respectively.

Calzetti, Kinney, & Storchi-Bergmann (1994) computed the “intrinsic depth” of the 2175 \( \text{Å} \) dust absorption feature \( \eta \) (see their Eq. 23) in a number of starburst galaxies, finding that \( -0.15 < \eta < 0 \). For the three starbursts we find \( \eta \) ranging from -0.15 to -0.08. Since the dust properties we adopt follows very well those of our galaxy, at least in these objects the relative weakness of the 2175 \( \text{Å} \) feature can be ascribed to the adopted geometry, without invoking possible variations of extinction curve.

In conclusion for starbursts, the spectral coverage from UV to submillimeter wavelengths allows a robust evaluation of the luminosity of stars involved in the bursts and of the general interstellar radiation field. The latter is contributed by the long-lived stellar populations and by the stars produced in the burst but old enough to get out from the original MCs. Our model well describes the complexity of a starburst galaxy, and is flexible enough to reproduce the differences among them. It uses a reasonable number of parameters, which have a well defined physical meaning and compare favorably to values derived from observations other than broad band spectra.

### 4.2. Spirals

The SEDs of three spiral galaxies, namely M51, M100, and NGC 6946, have been well reproduced by our model. An interesting result is the significantly lower \( t_o \) in spirals with respect to starbursting objects. This derives from their smaller observed ratios \( \frac{L_{\text{FIR}}}{L_{\text{UV}}} \). In the three spirals analyzed here, the newly born SSPs quite soon get out from the parent clouds and significantly contribute to the heating of the diffuse dust. The expected contribution is larger for NGC 6946 and M100 than for M51. As a consequence, a significant portion of the far–IR luminosity emitted by the diffuse dust (almost all for NGC 6946 and M100) should be inserted in the budget to infer the SFR in spiral galaxies, in agreement with the findings of Devereux et al. (1994) and Buat & Xu (1996). Taking into account this, the SFRs derived from the FIR luminosities, through the conversion suggested by Kennicutt (1997), are in very good agreement with those used by the model.

The SFRs in our models, through the conversion of Kennicutt (1997) \( \frac{L(H_{\alpha})}{\text{ergs s}^{-1}} = 1.26 \times 10^{41} \times \text{SFR}(M_\odot \text{yr}^{-1}) \), yield \( H_{\alpha} \) luminosities of 7.6, 8.8, and 7.6\,10^{41} \text{ergs s}^{-1} \) for M51, M100, and NGC 6946 respectively, to be compared with observed values (Kennicutt, Tamblyn, & Congdon 1994, reported to our adopted distances) of 4.9, 5.0, and 2.2 \times 10^{41} \text{ergs s}^{-1}. These lower values would imply an internal H_{\alpha}}
extinction of $A_{H\alpha} = 0.5, 0.6, \text{and } 1.3$ magnitudes in the three spirals, consistent with the average value 1.1 adopted by Kennicutt (1997), based on a comparison of free–free radio and H$_\alpha$ fluxes.

It is also worth noticing that masses in stars, dust, and gas derived by the model, as well as geometric parameters such as the disc scale length are in good agreement with independent estimates. Our model includes the main physical aspects of star formation, stellar evolution, and dust absorption in spiral galaxies and allows a full exploitation of the broad band data in order to explain their present status and their past history.

4.3. Ellipticals

The model with a relatively small number of parameters is able to produce a very good fit to the template SED of giant elliptical galaxies (see Fig. 13). Most excitement about spheroidal galaxies is related to their evolution. Indeed it has been suggested that, during the initial phases of star formation, they might look very similar to local violent starbursts (such as Arp 220), since the chemical enrichment and, as a consequence, the dust formation are very quick processes when SFRs are very high (Mazzei et al. 1994; Franceschini et al. 1994). This initial phase, if confined to high enough redshifts $z \leq 2 \pm 2.5$, is the most natural way to produce the total energy and the shape of the Far–IR Background (Franceschini et al. 1991; Franceschini et al. 1994; Burigana et al. 1997), which has been tentatively detected by Puget et al. (1996) and recently confirmed by Hauser et al. (1998) and Fixsen et al. (1998). Also we expect that in the ISO extra deep surveys we may detect individual dusty spheroidal galaxies at substantial redshifts. Our model is able to describe in detail the evolution of elliptical galaxies in all the relevant range of frequencies, and will be exploited to a comprehensive discussion of galaxy counts, related statistics, and astrophysical backgrounds.

4.4. Conclusion

We showed that the model and the related numerical code are extremely efficient in deriving a wealth of information from broad band spectra of starburst and spiral galaxies. Indeed, when SEDs from the UV to the sub–mm range are available, we are able to quantify the effects of dust reprocessing on observations, gaining information on very substantial quantities such as SFR, the IMF and the past history of the galaxies. The model can be implemented in studies of local starburst and normal galaxies. It can also be used to trace back the history of the different classes of galaxies and, by confronting predictions and observations of number counts and redshift distributions in different bands, to understand their cosmological evolution. In particular we will use the model to investigate the role of dust during the early phase of galaxy formation, exploiting available and soon coming data on galaxy counts at wavelengths ranging from UV to radio bands.

Updated information on the code described in this study (GRASIL) can be found on the WEB at http://asterix.pd.astro.it/homepage/gian/.

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This 2-column preprint was prepared with the AAS \LaTeX\ macros v4.0.

Fig. 1.— Scheme of the components included in our model computations and their adopted geometry.

Fig. 2.— Solid line: cross-section of PAH per carbon atom, derived from laboratory measurements taken from Léger et al. (1989); dashed line: the analytical law assumed by Désert et al. (1990) for molecule with $N_C = 50$ C-atoms ($N_C$ controls the cut-off above 0.3 $\mu$m).
Fig. 3.— Upper panel: the extinction curves of the dust model we adopt for diffuse and molecular gas, and that by Draine & Lee (1984) are compared with available data. Lower panel: the predicted emissivity of grains (ergs s\(^{-1}\) cm\(^{-2}\) st\(^{-1}\) N\(_{\text{H}}^{-1}\)) in the local interstellar radiation field (Mathis, Mezger, & Panagia 1983) compared with observations toward the galactic pole. The horizontal line around 12µm marks the flux level obtained by convolving our expected SED with the 12µm IRAS passband. Triangles in the lower panel are data from Dwek et al. (1997), for references to other observations see Rowan–Robinson (1992, 1986).

Fig. 4.— The observed SED of W49A (Ward-Thompson & Robson 1990), a huge star–forming region composed of H II regions and GMCs, is compared with the spectrum of the MC component we use in the fit of the overall SED of Arp 220.
Fig. 5.— $F/F_0$ is the ratio between the dust extinguished flux and that expected if dust were not present. The points have been computed by Witt et al. (1992) with a Montecarlo radiative transfer code including anisotropic scattering, the dashed line represents the result of our code taking into account only absorption, whilst the solid line includes scattering with the effective optical depth $\tau_{eff}^2 = \tau_a (\tau_a + \tau_s)$. The adopted geometry is that defined by Witt et al. as elliptical galaxy.

Fig. 6.— Fit to the SED of M82. Data are from Code & Welch (1982), Soifer et al. (1987), Klein et al. (1988), Cohen & Volk (1989), Van Driel et al. (1993), Ichicawa et al. (1994,1995).
Fig. 7.— M82: SFR as a function of galactic time.

Fig. 8.— Fit to the SED of NGC 6090. Data are from Mazzarella & Boroson (1993), Acosta–Pulido et al. (1996), Gordon et al. (1997).

Fig. 9.— Arp 220: in this case the wavelength dependence of grain cross-section has been modified above 100 µm from $\propto \lambda^{-2}$ to $\propto \lambda^{-1.6}$. The dashed line above 100 µm represents the model prediction with standard $\lambda^{-2}$ decline. Data are from Carico et al. (1988), Sanders et al. (1988), Smith et al. (1989), Carico et al. (1990), Wynn–Williams & Becklin (1993), Rigopoulou et al. (1996), Klaas et al. (1997).
Table 1
SF history parameters

<table>
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<th>object</th>
<th>D [Mpc]</th>
<th>(M_G) [10^{10} M_\odot]</th>
<th>(\nu) [Gyr^{-1}]</th>
<th>(t_{inf}) [Gyr]</th>
<th>(M_{burst}) [10^{10} M_\odot]</th>
<th>(t_{burst}) [Gyr]</th>
<th>(t_e) [Gyr]</th>
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<td>12.95</td>
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<tr>
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<td>...</td>
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</table>

Note.—Parameters for the star formation history (Sec. 2.1): (2) adopted distance; (3) final baryonic galaxy mass; (4) SF efficiency; (5) infall timescale; (6) gas mass converted into stars during the burst; (7) galaxy age at beginning of the burst (when included); (8) e–folding time for SFR in the burst. All models have an age of 13 Gyr. In the case of gE the SF has been stopped at 1.15 Gyr.

Table 2
Geometric parameters

<table>
<thead>
<tr>
<th>object</th>
<th>(f_{mc})</th>
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<th>(t_o) [Myr]</th>
<th>(r_c^*) [kpc]</th>
<th>(R_d) [kpc]</th>
<th>(z_d) [kpc]</th>
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<tr>
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<td>5.0</td>
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<td>8.0</td>
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<tr>
<td>gE</td>
<td>...</td>
<td>...</td>
<td>...</td>
<td>0.4</td>
<td>6.0</td>
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</table>

Note.—Parameters for the photometric model estimated from SED fitting: (2) fraction of residual gas in MCs; (3) radius of MC; (4) parameter regulating the escape of young stars from MCs (Eq. 8); (5)–(8) parameters for the spatial distribution of stars, MCs, and cirrus (Eqs. 1 and 3). For disks the inclination angles have been taken from the literature (see text) and are \(i = 20^\circ\) (M51), \(i = 30^\circ\) (M100), and \(i = 34^\circ\) (NGC 6946).
### Table 3
**Derived quantities**

<table>
<thead>
<tr>
<th>object</th>
<th>(&lt; SFR &gt; ) ([M_\odot/yr])</th>
<th>(M_{dust} ) ([10^7M_\odot])</th>
<th>(\tau^{1\mu m}_{MC})</th>
<th>(\bar{\tau}_1)</th>
<th>(\tau_B)</th>
<th>(L_{MC} ) ([10^{44}\text{ergs/s}])</th>
<th>(L_C ) ([10^{44}\text{ergs/s}])</th>
<th>(L_{LyC} ) ([10^{44}\text{ergs/s}])</th>
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<td>0.06</td>
<td>0.28</td>
<td>1.01</td>
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<tr>
<td>M100</td>
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<td>0.12</td>
<td>0.62</td>
<td>0.53</td>
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<td>0.01</td>
<td>...</td>
<td>0.02</td>
<td>0.03</td>
</tr>
</tbody>
</table>

**Note.**—A few quantities derived from the models: (2) SFR averaged over the last \(5 \times 10^7\) yr, which is the time from burst onset for starburst models; (3) total mass in dust in the galaxy; (4) \(1\mu m\) optical thickness of the MCs from the centre; (5) \(1\mu m\) ‘average’ optical thickness of the model, defined such as \((\text{observed flux}) = (\text{dust–free flux} \times \exp(-\bar{\tau}))\) (6) same as (5) but at \(0.44\mu m\); (7) luminosities of the MCs, (8) of the diffuse dust and (10) in the Lyman continuum before dust absorption.

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**Fig. 11.**—Fit to the SED of the Sbc galaxy M100. Data are from Buat et al. (1989), Donas et al. (1987), De Jong et al. (1994), Stark et al. (1989), RC3, Devereux & Young (1990), Young et al. (1989), Helou et al. (1988), Knapp et al. (1987).
Fig. 12.— Fit to SED of the Scd galaxy NGC 6946. Data are from Rifatto et al. (1995), RC3, Engargiola (1991), Devereux & Young (1993), Rice et al. (1988), Tuffs et al. (1996).

Fig. 13.— A fit to a template SED of a giant elliptical galaxy.