Charmonium suppression from purely geometrical effects

N. Hammon, L. Gerland, H. Stöcker, W. Greiner

Institut Für Theoretische Physik,
Robert-Mayer Str. 10,
Johann Wolfgang Goethe-Universität,
60054 Frankfurt am Main, Germany

Abstract

The extend to which geometrical effects contribute to the production and suppression of the $J/\psi$ and $q\bar{q}$ minijet pairs in general is investigated for high energy heavy ion collisions at SPS, RHIC and LHC energies. For the energy range under investigation, the geometrical effects referred to are shadowing and anti-shadowing, respectively. Due to those effects, the parton distributions in nuclei deviate from the naive extrapolation from the free nucleon result; $f_A \neq A f_N$. The strength of the shadowing/anti-shadowing effect increases with the mass number. Therefore it is interesting to see the difference between cross sections for e.g. $S+U$ vs. $Pb+Pb$ at SPS. The recent NA50 results for the survival probability of produced $J/\psi$'s has attracted great attention and are often interpreted as a signature of a quark gluon plasma. This publication will present a fresh look on hard QCD effects for the charmonium production level. It is shown that the apparent suppression of $J/\psi$'s must also be linked to the production process. Due to the uncertainty in the shadowing of gluons the suppression of charmonium states might not give reliable information on a created plasma phase at the collider energies soon available. The consequences of shadowing effects for the $x_F$ distribution of $J/\psi$'s at $\sqrt{s} = 20$ GeV, $\sqrt{s} = 200$ GeV and $\sqrt{s} = 6$ TeV are calculated for some relevant combinations of nuclei, as well as the $p_T$ distribution of minijets at midrapidity for $N_f = 4$ in the final state.

1Work supported by BMBF, DFG, GSI
1. Introduction

Since the advent of QCD in the 70’s great emphasis was laid on the existence of a phase transition of, yet unknown, order, being typical for non-abelian gauge field theories. From lattice calculations it was emphasized that, at zero chemical potential, a phase transition should show up at some temperature $T_c \approx 150 - 200$ MeV when explicitly taking quarks into account. The value for $T_c$ is slightly higher for a pure gauge theory. Also, at non-zero chemical potential, as suggested in the MIT bag model, one should access a phase transition due to the increasing outward pressure of the partons inside the bag finally leading to a deconfined phase. Due to the difficulties emerging when considering dynamical fermions the work on non-zero chemical potential has not yet reached the same level of success as that for $\mu = 0$ in lattice QCD.

Now, in actual high energy heavy ion collisions the following scenario can occur. Two streams of initially cold nuclear matter collide and may result in a plasma phase, which is created within the transverse dimension of approximately the size of the overlapping nuclei. The plasma cools down to form hadronic degrees of freedom in the subsequent expansion. If one has this phase transition in mind one also has to confront the question of its experimental detection. Typical signatures under discussion are leptonic (dilepton [1] and photon [2] production due to the interactions among the quasi free partons via the different QCD processes $q\bar{q} \rightarrow \gamma g$, $gq \rightarrow \gamma q$, ...) and hadronic ones, such as the suppression of $J/\psi$’s. Now, the QCD reactions in the plasma are not the only source for leptons. One expects a large background coming from the decay of $\pi^0$ and $\eta$ mesons. It therefore is necessary to carefully handle this background by experimental methods such as invariant mass analysis.

It is also obvious that the signatures have to give clear and powerful information on the plasma phase. Especially when looking at the hadronic signatures this does not have to be the case as emphasized in [3] where it was shown that gluon depletion due to DGLAP splitting in the colliding nuclei can lead to the same results as the current experiments at NA50 [4] show, which in turn implies that those experimental results probably have lost their
meaning as a plasma signature at SPS.

2. Production and suppression of the J/ψ

The J/ψ is a c–c̅ bound state interacting via two forces in a confined surrounding: a linear confining potential and a color-Coulomb interaction. In the plasma phase the linear potential is absent due to the high temperature leading to deconfinement. Every color-charge is Debye-screened by a cloud of surrounding quark-antiquark pairs which weaken the binding force between the c–c̅ pair, thus reducing the color charge seen by the other (anti)quark. Since the density of the screening pairs rises strongly with increasing temperature, the binding force gets weaker and weaker when the temperature rises above T_c. As a result, the charm quark and antiquark drift away from each other, so that finally no bound state formation is possible in a plasma phase of high enough temperature [5].

However, the plasma phase is not the only source of suppression [6]. One also has to take into account final state interactions for this hadronic degree of freedom that are absent for leptonic signatures. Because the J/ψ is a very weakly bound state, the interaction with nucleons and secondaries, that are always present in a heavy ion collision, in addition significantly lowers the survival probability for a J/ψ. It is obvious that such effects should increase with increasing mass number. One also expects the phase transition to happen for the heavier nuclei. Therefore one has two effects both increasing with the number of nucleons involved. This in turn implies that the experiments have to be done with very high precision to disentangle those effects.

At this point another source of suppression comes into play that also increases with the mass number and therefore has to be accounted for: nuclear shadowing. This effect already enters on the production level of the charmonium bound state. The former two effects, namely suppression by melting in the plasma phase and comover activity, enter only at a level when the J/ψ already exists at later proper times τ. Now the nuclear shadowing effect appears when the charmonium is produced via the various processes depicted in figure 1.

The total hidden charm cross section in pN collisions below the open charm
Figure 1: The various LO processes leading to the direct production of a $c\bar{c}$ pair.

The threshold is given by [7]

$$\sigma_{c\bar{c}}(s) = \int_{4m_c^2}^{4m_c^2} d\hat{s} \int dx_A dx_B f_i(x_A)f_j(x_B)\hat{\sigma}(\hat{s})\delta(\hat{s} - x_A x_B s)$$ (1)

Here, $f_i$ and $f_j$ denote the parton densities and $\hat{\sigma}$ is the cross section on the parton level, i.e. $q\bar{q} \rightarrow c\bar{c}$, $gg \rightarrow c\bar{c}$. The $c\bar{c}$ pair subsequently will turn into a color singlet by interaction with the color field, induced in the scattering, the so-called "color-evaporation" mechanism. In [7] the $J/\psi$ production in a proton nucleon reaction was parametrized as

$$\sigma_{pN \rightarrow J/\psi}(s) = f_{J/\psi}^p \sigma_{c\bar{c}}^{NLO}$$ (2)

with $f_{J/\psi}^p = 0.025$ from comparison with data [8]. Here the production of the $J/\psi$ is described as proceeding via the NLO production of a $c\bar{c}g$ state and a subsequent evaporation of the gluon. (For a more detailed model also including the non-relativistic quarkonium model in the quarkonium- and bottonium-nucleon cross section see [9]).

It is obvious that any changes in the parton densities will result in changes of the $c\bar{c}$ production cross section. Because we know since the EMC measurements [10] that $f_i^A \neq Af_i^N$ this demands for some further investigation.
Here we will investigate the influence of the nuclear gluon and quark distributions on the $J/\psi$ production cross section by using a modified version of a parametrization based on a (impact parameter averaged) data fit given in [11]. We will show the influence on the differential cross section $d\sigma^{AB}/dx_F$ for $gg$ fusion and $q\bar{q}$ annihilation [12] given by

$$
\frac{d\sigma^{AB}}{dx_F} = \int_{4m_c^2}^{4m_D^2} dQ^2 \frac{1}{Q^2} \frac{x_A x_B}{x_A + x_B} \hat{\sigma}^{gg\to c\bar{c}}(Q^2) \times g^A(x_A, Q^2) g^B(x_B, Q^2)
$$

(3)

and on the minijet cross section

$$
\frac{d\sigma^{AB}}{dx_F} = \sum_{q=u,d,s} \int_{4m_c^2}^{4m_D^2} dQ^2 \frac{1}{Q^2} \frac{x_A x_B}{x_A + x_B} \hat{\sigma}^{q\bar{q}\to c\bar{c}}(Q^2) \times \left[q^A(x_A, Q^2) q^B(x_B, Q^2) + q \leftrightarrow \bar{q}\right]
$$

(4)

and on the minijet cross section

$$
\frac{d\sigma}{p_Tdp_Tdy_1dy_2} = 2\pi x_A g^A(x_A, p_T^2) x_B g^B(x_B, p_T^2) \frac{d\hat{\sigma}^{gg\to q\bar{q}}}{dt}
$$

(5)

at midrapidity $y = y_1 = y_2 = 0$. We choose $m_c = 1.5$ GeV and $m_D = 1.85$ GeV. The momentum fractions are given as $x_{A,B} = 1/2[\pm x_F + (x_F^2 + 4Q^2/s)^{1/2}]$ for the $x_F$ distribution and $x = 2p_T/\sqrt{s}$ for the minijets at midrapidity. We take all cross sections in leading order and do not include any K factor for higher order contributions since we are mainly interested in relative effects. For the parton distributions we choose the CTEQ4L parametrization.

The reason for our investigation is the following: the recent NA50 data show a deviation from the tendency expected from earlier experiments when the mass number of the involved nuclei is increased. Now, in [3] it was shown that due to multiple scatterings between partons the uncertainty in the survival probability gets so large that one cannot distinguish whether the data found by NA50 is due to gluon splitting in the production phase or due to plasma absorption as claimed by several authors. Obviously, the originally good idea of $J/\psi$ suppression as a good tool for plasma investigation seems to have lost
its predictive power at the available energies. It is therefore interesting to see what one can expect at future colliders.

In the next part we will give some details of the parton densities in nuclei in the energy regimes of SPS, RHIC, and LHC.

3. Nuclear shadowing and the connection to the $J/\psi$

The history of the modification of nuclear structure functions, as compared to the free nucleon ones, is founded on the findings of the EMC group that lead to the so-called EMC effect \cite{10} (even though one should say that shadowing effects in principle have been known since the 70’s \cite{13}). This effect shows that $f_A \neq Af_N$, which implies that the parton density in the nucleus is not simply given by the nucleon number times the respective parton density in the nucleon. Depending on the frame (lab- or infinite momentum frame) one derives completely different interpretations for the nuclear structure functions and for the deviations from the naive $pp$-extrapolations. For typical values of the momentum transfer in a $pp$ reaction of $p_T = 1 - 6 \text{ GeV}$, where perturbation theory should be applicable, one is in the so-called anti-shadowing region for SPS and in the shadowing region for RHIC and LHC at midrapidity. In the following we will shortly review the interpretation of shadowing in the two relevant frames and will start with the lab frame description which is the natural frame for typical deep inelastic scattering measurements off nuclei (at least from the experimental setup point of view).

A. Lab frame description

In the lab frame the expression shadowing immediately seems to imply a geometrical effect. When one speaks of something lying in the shadow of another thing one means that the second body is not visible since the first body is placed nearer, e.g. to some source of light. A similar reasoning can be applied in the case when a lepton is scattered off a nucleus consisting of many nucleons. The exchanged virtual photon does not (in the relevant $x$ range) interact individually with each nucleon but coherently with all nucleons or at least with a major part of the nucleons inside the nucleus; some nucleons are therefore lying in the shadow of other (surface) nucleons. As we will
see later, this reasoning is linked to the momentum fraction of the struck parton inside the nucleon. Because the momentum fraction is bound from above this interpretation is limited to the explanation of shadowing and is not applicable for the reasoning of anti-shadowing, the EMC effect or the Fermi-motion effect. Unfortunately there is yet no single theory to understand the whole range of the momentum fraction from $0 \leq x_{Bj} \leq 1$. For an excellent review of different models and interpretations see [14].

For a deep inelastic scattering process there exist two possible time orderings for the interaction of a virtual photon with a nucleon or with a nucleus: either the photon hits a quark inside the target (the so-called hand-bag graph) or the photon creates a $q\bar{q}$ pair which then strongly interacts with the target. Those two possible processes are depicted in figure 2.

As can be seen from the ratio of the amplitudes of the two processes one realizes that the diagram on the right hand side only contributes at small enough $x$ ($x \ll 0.1$). At low $Q^2$ the interaction of the virtual photon with the nucleons inside the nucleus happens via the low mass vector mesons $\rho$, $\omega$ and $\phi$ as described in the vector meson dominance model (VMD) with the typical spectral ansatz for the description of the fluctuation spectrum [15].

The reduction in the quark density, manifesting itself in the shadowing ratio $R_{F_2} = F_2^A / A \cdot F_2^N$, can then be understood in terms of a multiple scattering series where the fluctuation interacts with more than one nucleon over a coherence length of $l_c \approx 1/(2mx)$. At higher $Q^2$ the partonic degrees of freedom are probed; nevertheless, shadowing is due to long distance effects.
and therefore always incorporates a strong non-perturbative component, even at large $Q^2$. Also, the $q\bar{q}$ continuum has to be taken in addition to the mesons giving rise to the generalized VMD model. The interaction of the virtual photon with a nucleon can essentially be split up into two parts: the virtual photon with its quark-antiquark fluctuation and the interaction of the fluctuation with the parton which happens via gluon exchange:

$$\sigma(\gamma^* N) = \int_0^1 dz \int d^2 r |\psi(z, r)|^2 \sigma_{q\bar{q}N}(r)$$

where the Sudakov variable $z$ gives the momentum fraction carried by the quark (or antiquark).

The cross section for the interaction of the fluctuation with the nucleon can be described in the DLA as

$$\sigma_{q\bar{q}N} = \frac{\pi^2}{3} r^2 \alpha_s(Q'^2) x' g(x', Q'^2)$$

where $x' = M_{q\bar{q}}^2/(2m\nu)$, $r$ is the transverse separation of the pair and $Q'^2 = 4/r^2$. Due to

$$|\psi(z, r)| \sim \frac{1}{r^2}$$

pairs with small transverse separation are favored. As can be seen from (7) this in turn implies a small cross section. This smallness is compensated by the strong scaling violation of the gluon distribution in the small $x$ region as $r$ ($Q'^2$) decreases (increases). In the Glauber eikonal approximation the interaction with the nucleus is expressed in terms of the nuclear thickness function $T_A(b)$ as

$$\sigma_{q\bar{q}A} = \int d^2 b \left(1 - e^{-\sigma_{q\bar{q}N}T_A(b)/2}\right)$$

When there is a longitudinal momentum transfer appropriate to the production of the hadronic fluctuation $h$ a phase shift behind the target results and the incident wave $\exp(ik_z^h z)$ is changed to $-\Gamma(b)\exp(ik_z^h z)$ with $k_z^h \neq k_z$ and the nucleus profile function $\Gamma(b)$. The phase shift $\Delta k_z = k_z^h - k_z$ in turn gives rise to the coherence length $l_c \approx 1/\Delta k_z$. When now $l_c \gg 2R_A$ (i.e. for small momentum transfers $\Delta k_z$), the hadronic fluctuation interacts coherently with
all nucleons inside the nucleus, Glauber theory is valid and a reduction in the cross section results (for further details we refer to [14, 15, 16, 17]). For an illustration of the effect see figure 3.

B. Infinite momentum frame description

In the infinite momentum frame a completely different mechanism is employed. The key idea here is the fusion of partons giving rise to a process that competes with parton splitting expressed in the DGLAP equations. This idea was first formulated in [17] and later proven in [18]. In the following we will give the main ideas and conclusions of the parton fusion model [19].

As is known, in the infinite momentum frame the Bjorken variable $x_{Bj}$ is interpreted as the momentum fraction of a parton with respect to the mother nucleon. When now, inside a nucleus, the longitudinal wavelength of a parton exceeds the Lorentz-contracted size of a nucleon or the inter-nucleon distance $2R_N$, then partons originating from different nucleons can "leak out" and fuse. This effect can be estimated from $1/(xP) \approx 2R_NM_N/P$ to show up at $x$ values smaller than $x \approx 0.1$. As a result of the parton-parton fusion partons are "taken away" at smaller values of $x$ and "shoveled" to larger
values of $x$ where anti-shadowing appears to guarantee momentum conservation. As a result of the parton fusion the $x$-range for the measured structure function is expanded to values $x > 1$. Hereby, an alternative description of Fermi-motion is achieved. In the lab frame interpretation the saturation of shadowing was interpreted in terms of a coherence length larger than the nucleus. Here, the saturation towards smaller $x$ values is interpreted in terms of the longitudinal parton wave length exceeding the size of the nucleus. In that sense the infinite momentum frame interpretation of shadowing is formulated in terms of variables that are inherent to the nucleus and there is no need for a scattered lepton or a collision.

In addition to the longitudinal shadowing one expects an additional shadowing effect from the transverse fusion of partons: for sufficiently small values of $x$ and/or $Q^2$ the total transverse occupied area of the partons becomes larger than the transverse area of the nucleon. This happens (e.g. for gluons) when $xg(x) \geq Q^2R^2$ where the transverse size of a parton is $1/Q^2$ and $R$ is the nucleon radius. The depletion in the gluon and sea-quark densities arising from that process are expected at values $x \leq 0.01$.

4. The used parametrization

In [11] a fit to the E772 [20], NMC [21] and SLAC [22] data was given as a parametrization for the ratio $R_{F_2} = F_2^A/A \cdot F_2^N$ (see figure 4). Now this parametrized ratio cannot simply be multiplied with all the individual parton distributions entering the formulas. One has to make a distinction between the valence and the sea quarks and also needs a different ratio for the gluons. Our results for $d\sigma_{AB}/dx_F$ are based on the shape of the ratio given in [11] at the initial momentum transfer $Q_0 = 2$ GeV. Up to now, the production processes were often calculated by using the measured shadowing ratio $R_{F_2}$. From the lab frame interpretation we know that the cross section for the interaction of a gluon pair is larger than the one for the interaction of the quark-antiquark pair ($\sigma_{qqN}^{pert} = 9/4\sigma_{ggN}^{pert}$). The same tendency can be found in the parton fusion model. In [23] calculations in the parton fusion model for $^{118}Sn$ showed an impact parameter averaged gluon shadowing that is as twice as strong ($R_G \approx 0.34$) as the sea quark shadowing at $x = 10^{-3}$ and $Q^2 = 5$ GeV$^2$ already for this light nucleus. To account for the much
stronger gluon shadowing we therefore modified the parametrization given in [11].

In the lab frame, the relevant range for the coherence length to produce the shadowing effect is \( l_0 = r_{NN} \approx 1.8 \text{ fm} \leq l_c = 1/(2m_x) \leq 2R_A \). For \( l_c \gg 2R_A \), corresponding to \( x \ll 0.1 \text{ fm}/1.1 \text{ fm}A^{1/3} \), the shadowing of gluons at some initial scale at fixed impact parameter behaves as [24, 25]

\[
\frac{A_{\text{eff}}}{A} = \frac{2 - 2(\exp - R/2)}{R} \quad (10)
\]

where \( R = T(b) \cdot \sigma_{\text{eff}} \). For the interaction of the \( q\bar{q} \) pair one finds \( \sigma_{\text{eff}, q\bar{q}} \approx 14 \text{ mb} \) which approximately corresponds to the \( pN \) cross section. We here assume that the perturbative factor \( 9/4 \) is valid also for the non-perturbative regime and therefore choose \( \sigma_{\text{eff}, gg} \approx 30 \text{ mb} \). At \( b = 0 \) and for \( Pb \) one therefore has a maximum amount of shadowing of \( A_{\text{eff}}/A \approx 0.39 \) which is approximately 15% smaller than the \( b \)-averaged result. Because the two dif-

Figure 4: Fit to the data for various nuclei at \( Q_0 = 2 \text{ GeV} \) as given by Eskola.
Figure 5: Initial gluon and quark shadowing parametrization at $Q^2 = 4 \text{ GeV}^2$ for $^{197}\text{Au}$ and $^{208}\text{Pb}$. 
Figure 6: Gluon shadowing ratio evolved to $Q^2 = 10$ GeV$^2$ with DGLAP without fusion terms. Due to the narrow range $4m_c^2 \leq Q^2 \leq 4m_D^2$ in the interpretation we use the ratio at some fixed intermediate scale $Q^2 = 10$ GeV$^2$. 
different scenarios (lab- or infinite momentum frame) give such different results, 

\[ R_G \approx 0.39 \] [24, 25] vs. \[ R_G \ll 0.3 \] for heavy nuclei at small \( x \), we decided to 
choose some intermediate value as a starting point for the DGLAP evolution. 
We therefore employ the curves shown in figure 5 to account for the large 
difference in the quark- and gluon shadowing ratios. Due to the large uncer-
tainty of the initial \( R_G \) we choose the same ratio for \( Au \) and \( Pb \) at \( Q^2 = 10 \) 
GeV\(^2\) as shown in figure 6. Also, we again want to emphasize that the com-
monly used shadowing ratios, only account for impact parameter averaged 
measurements in DIS reactions. Therefore our results should be seen as for 
central events only because the production mechanism in very peripheral 
collisions should produce significantly smaller rates with significantly smaller 
influences from shadowing effects [26]. 

For the minijet cross section we used a \( Q^2 \)-dependent parametrization given 
in [16] to account for the larger \( p_T \) region.

4. Results

We will first present the results for the minijet cross section including only 
processes \( i, j \rightarrow k, l \) with \( i, j = g \) and \( k, l = q\bar{q} \) with four flavors in the final 
channel (due to the dominance of the \( gg \) fusion process annihilation processes 
are neglected at RHIC and LHC at midrapidity). For the \( x_F \) distribution 
we used our modified version of the parametrization in [11] but for the mini-
jets we used an impact parameter dependent parametrization with \( b = 0 \) [16] 
shown in figure 7. This parametrization is applicable here since we are in the 
pure shadowing region where the generalized VMD approach used to derive 
it is applicable (even though one should say that the Glauber ansatz should 
only be valid up to values \( x \sim 10^{-2} \) as restricted by the eikonal approxima-
tion).

The regions of the momentum fractions corresponding to the momentum 
range \( 1 \text{ GeV} < p_T < 6 \text{ GeV} \) for RHIC (\( \sqrt{s} = 200 \text{ GeV} \)) and LHC (\( \sqrt{s} = 6 \) 
TeV) are represented in figure 7 as shaded areas. The results for the cross 
sections for RHIC and LHC are given in figure 8. In that calculation all 
quark antiquark pairs \( (k, l = q\bar{q}) \) up to the bottom threshold were taken 
to account, i.e. \( N_f = 4 \) in the final state. One clearly sees the deviation 
having its origin in the shadowing of the nuclear parton distribution. As ex-
Figure 7: Gluon ratios corresponding to the various energy and transverse momentum regimes.
pected, the shadowing effect decreases as $p_T$ increases due to the momentum fraction $x = 2p_T/\sqrt{s}$.

Next we will present the results for the $d\sigma^{AB}/dx_F$ cross sections. We first calculated the proton-proton cross sections to show the dominance of the $gg$ fusion process over the $q\bar{q}$ annihilation process at small $x_F$ (see figure 9): The results for the cross sections for $S + U$ and $Pb + Pb$ at SPS at $\sqrt{s} = 20$ GeV, $Au + Au$ at RHIC at $\sqrt{s} = 200$ GeV, and $Pb + Pb$ at LHC at $\sqrt{s} = 6$ TeV are presented in figure 10. In this case we were restricted to our modified version of the parametrization of [11] due to the integration reaching up to momentum fractions $x > 0.1$, not allowing us to use the same parametrization as for the minijet production. At SPS energies one clearly sees the different regions of the parametrization entering the cross section. At small $x_F$ one has the enhancement due to the antishadowing which is followed by the depletion due to the EMC region at larger $x$ and finally one can identify the Fermi motion effect as $x_F \to 1$. The effects are clearly stronger for $Pb + Pb$ than for $S + U$ (compare figure 4). To get an impression of the relative strength of the nuclear modifications in the respective nuclei we calculated the ratios of the shadowed to unshadowed cross sections in figure 11. The difference between $Pb + Pb$ and $S + U$ at SPS energies in principle is only small; in the relevant region of small $x_F$, where the cross section has not dropped yet too much, the charmonium production in $Pb + Pb$ is slightly larger than in $S + U$ ($\approx 8\%$). For RHIC one is in the shadowing region. The suppression strongly varies over the $x_F$ range between $\approx 0.6 - 0.35$. At LHC an even stronger suppression is found due to the smaller momentum fractions entering the shadowing ratios. Here the suppression is $\approx 0.3 - 0.5$.  

16
Figure 8: Minijet cross sections for creation of $q\overline{q}$ pairs for RHIC and LHC.
Figure 9: $d\sigma^{pp\rightarrow J/\psi}/dx_F$ for SPS, RHIC and LHC.
Figure 10: $d\sigma^{AB-\psi}/dx_F$ for SPS ($Pb + Pb, S + U$), RHIC ($Au + AU$) and LHC ($Pb + Pb$).
Figure 11: $\frac{d\sigma_{J/\psi}}{dxF} / \frac{d\sigma_{J/\psi}}{dxF}$ for SPS ($Pb + Pb, S + U$), RHIC ($Au + AU$) and LHC ($Pb + Pb$).
5. Conclusions

From the results shown above one now can draw the following conclusions for the consequences of the shadowing effects for charmonium production and suppression at SPS, RHIC and LHC.

First, one can conclude from figures 4 and 11 that an enhancement of charmonium states produced near midrapidity due to antishadowing at $\sqrt{s} = 20$ GeV is predicted (small $x_F$). For larger $x_F$, a clear suppression of the charm cross section to $\approx 70 - 80\%$ of the unshadowed result (figure 10) and again a rise at the largest $x_F$ values is predicted (the latter one due to the Fermi motion effect).

For RHIC energies of $\sqrt{s} = 200$ GeV the situation changes; for minijets with $1$ GeV $< p_T < 6$ GeV at midrapidity (or at small $x_F$, respectively) one is completely in the shadowing region. Here, the shadowed result are reduced by $\approx 45\%$. At LHC the situation is even more dramatic: the ratio of the shadowed cross section to the unshadowed cross section at $p_T = 1$ GeV is 0.22 which amounts to a suppression of a factor $\approx 4.6$.

Similar effects are observable for $d\sigma^{AB \rightarrow J/\psi}/dx_F$: at small $x_F \approx 0.05$ for RHIC the cross section is reduced by a factor $d\sigma^{\text{shad.}}/d\sigma^{\text{unshad.}} \approx 0.58$, and gets suppressed even more towards larger $x_F$ down to values $\approx 0.35$. At LHC one finds a less strong variation over the $x_F$ range with a mean value of $\approx 0.35$. In these results one problem is unveiled: the difference between the (not yet exactly known) gluon ratio $R_G$ and the quark ratio $R_{F_2}$ that, according to the calulations in [23] increases with increasing mass number. If, as it was recently done at CERN-SPS, the future experiments at RHIC and LHC compare different combinations of nuclei and derive results similar to the NA50 data one has to ask oneself whether one has detected the plasma or whether the detection is that the gluon ratio in not simply given by $R_{F_2}$, even at small $x$. To give clear predictions it is mandatory to control the value of $R_G$ at the typical semihard scale $Q_{SH} \approx 2$ GeV with high precision. Therefore charmonium and bottonium suppression effects can also be due to purely geometrical effects, i.e. shadowing.
Acknowledgements
We gratefully appreciated discussions with L. Frankfurt and M. Strikman.

References


