MEASUREMENT OF SHORT BUNCHES

D.X. Wang
Thomas Jefferson National Accelerator Facility
12000 Jefferson Avenue
Newport News, VA 23602, USA

Abstract

In recent years, there has been increasing interest in short electron bunches for different applications such as short wavelength FELs, linear colliders, and advanced accelerators such as laser or plasma wakefield accelerators. One would like to meet various requirements such as high peak current, low momentum spread, high luminosity, small ratio of bunch length to plasma wavelength, and accurate timing. Meanwhile, recent development and advances in RF photoinjectors and various bunching schemes make it possible to generate very short electron bunches. Measuring the longitudinal profile and monitoring bunch length are critical to understand the bunching process and longitudinal beam dynamics, and to commission and operate such short bunch machines. In this paper, several commonly used measurement techniques for subpicosecond bunches and their relative advantages and disadvantages are discussed. As examples, bunch length related measurements at Jefferson Lab are presented. At Jefferson Lab, bunch lengths as short as 84 fs have been systematically measured using a zero-phasing technique. A highly sensitive Coherent Synchrotron Radiation (CSR) detector has been developed to noninvasively monitor bunch length for low charge bunches. Phase transfer function measurements provide a means of correcting RF phase drifts and reproducing RF phases to within a couple of tenths of a degree. The measurement results are in excellent agreement with simulations. A comprehensive bunch length control scheme is presented.

Measurement Techniques

One conventional technique uses transverse deflecting RF cavities or a streak camera to measure short bunches in the time domain [11]. This method provides bunch length and longitudinal profile information. Using dual sweeping options, bunch-to-bunch resolution can be achieved at the expense of single bunch resolution. Using a L-band RF deflecting cavity, a few tenths of a picosecond resolution has been reported by the LANL group [6]. High resolution is reported for commercially available streak cameras by the vendor specifications [11]. Though the resolution of streak cameras is continuously improving, their high cost is still a primary concern. Also, due to their operational complexity these devices require significant amount of experience and special equipment for calibrations.

Another recently developed method utilizes coherent radiation to determine the frequency components of the longitudinal profile. Though coherent radiation has long been studied theoretically [12-13], it was not until 1989 when CSR was first observed experimentally by Nakazato's group at Tohoku University with a linac machine [14]. Since then, coherent radiation has been extensively studied at Tohoku University University and Osaka University for various radiation mechanisms [15]. Meanwhile, Coherent Transition Radiation (CTR) was first measured by the Cornell group in 1991 [16].

In general, the total radiation power is the summation of the power from each individual electron with a phase factor, and is given in Eq. (1).

\[
P(\lambda) = P_{\text{inc}} \sum_{j=1}^{N} e^{\frac{2\pi i j}{\lambda}} F(\lambda), (1)
\]

where \( P_{\text{inc}} \) is the radiation power from an individual electron, \( N \) is the number electrons per bunch, and \( \lambda \) is the wavelength of the radiation. \( F(\lambda) \) is a bunch form factor given by

\[
F(\lambda) = \left| \int S(z) e^{-\frac{2\pi i z}{\lambda}} dz \right|^2
\]

where \( S(z) \) is the normalized longitudinal density distribution and the integral is over a single bunch. The first term on the right side of Eq (1) is the incoherent power proportional to the number of electrons and the second term is the coherent power proportional to the square of the number of electrons. The form factor is nearly zero in regions where the radiation wavelength is much shorter than the bunch length and becomes close to one when the wavelength is much longer than the bunch length. In between is a transition region. This is illustrated in Fig. 1, where the CSR power spectrum is plotted for bunches with a Gaussian distribution. The dashed line is the incoherent term. The coherent enhancement is clearly seen and the location of the transition region is determined by the bunch length.
Measurements at Jefferson Lab

A very stringent demand on final energy spread, with a design goal of $2.5 \times 10^{-4}$ (rms), requires short bunches at the Continuous Electron Beam Accelerator (CEBA) of Jefferson Lab [5, 20]. CEBA is routinely operated within its bunch length specification of 0.5 picosecond, and a bunch length as short as 84 fs has been achieved. Three bunch length related measurements have been performed and systematic studies of longitudinal bunching process have been carried out with the assistance of simulation tools. A block diagram of the CEBA injector layout is given in Fig. 2. A 0.1 MeV CW electron beam is chopped by a pair of RF chopper cavities into a bunch train with variable length from 0 to 100 ps separated by 2 ns. The beam is bunched and accelerated to 0.5 MeV by RF buncher and capture cavities. Then the beam is further bunched and accelerated to 5 MeV by the two Superconducting RF (SRF) cavities, followed by 16 SRF cavities to accelerate the beam to the final injection energy of 45 MeV.

A phase transfer function measurement has been proposed and utilized routinely over the last a few years [21-22]. A relatively narrow chopper slit is used and the phases of the chopper cavities are modulated, equivalent to sampling a small portion of the nominal bunch piece by piece. The arrival phases of the sampled beam are measured by two longitudinal pick up cavities at strategic locations downstream, operating at fourth harmonic of operating RF frequency of 1497 MHz. A particular measurement result of a phase transfer function at the first pick up cavity is shown in Fig. 3(a). Such measurements can give a time resolution to better than one tenth of a picosecond. However, since this measurement only quantifies phase compression, the effects of initial energy spread and space charge are not determined. Therefore, the profiles that can be obtained from projection of the phase measurement is only valid for bunches with small initial energy spread and low charge per bunch. PARMELA simulation results are in good agreement with the measurements (see Fig. 3(b)), where the initial energy spread and space charge were turned off. When a significant initial energy spread and both energy spread and space charge were turned on, the simulation results shows rather obvious effects (see Fig. 3(c) and (d), respectively). Nevertheless, the measured patterns of phase provide unique signatures of RF cavity parameters [22]. A distinguishable slope change of the measured pattern results from a four tenth of degree phase change of the capture cavity (see Fig. 3(e)) while a vertical slip of the pattern is displayed (see Fig. 3(f)) due to a two degree change of chopper gan phase. These pattern recognition techniques have been proven to be invaluable to operate the machine and are routinely used to correct RF

---

Fig. 1 Calculated CSR power spectrum with 20 % flat bandwidth for Gaussian beams with different bunch length.

Fig. 2 Block diagram of CEBA injector layout
phase drifts and reproduce RF phases to within a couple of tenths of a degree.

![Graphs showing phase transfer functions](image)

Fig. 3 Plots of phase transfer functions, a relation between modulating phase (input phase) and detected phase (output phase): (a) is measured phase pattern optimized at the first pick up cavity; (b) is simulation result with the initial energy spread and space charge off; (c) is simulation with a significant initial energy spread turned on; (d) is simulation with both energy spread and space charge turned on; (e) is measurement with 0.4 degree phase change of the capture cavity; (f) is measurement with 2 degree of chopper gang phase change.

A zero phasing measurement was employed to measure bunch length and obtain longitudinal profile information [23-24]. The measurement requires several RF cavities (zero-phasing cavities), a spectrometer, and a transverse profile measuring device. The RF cavities operated at zero-crossing of the accelerating gradient impart a time correlated momentum tilt along the beam bunch. Then the spectrometer translates the longitudinal momentum spread into a horizontal position spread. By measuring the horizontal profile, the bunch length and longitudinal profile can be determined. Namely, 16 SRF cavities in the first and second SRF modules are running on crest to achieve maximum energy gain and minimum energy spread. During the measurement, the last 8 SRF cavities are phased to 90 degree off crest. A wire scanner is used to measure horizontal profile at spectrometer. The relation between the bunch length and the transverse beam width at the scanner is given in Eq. (3),

$$\sigma (ps) = \frac{1.86 - \frac{1}{\pi} \sqrt{\frac{x_{rms}^2 - x_{0rms}^2}{D}}}{E} \Delta E$$  \hspace{1cm} (3)

where $\sigma$ is the rms bunch length, 1.86 is unit conversion factor between RF degrees and ps, $D$ is the dispersion of the spectrometer, $E$ is beam energy with the zero-crossing cavities off, $\Delta E$ is the energy gain at crest of the zero-crossing cavities, and $x_{rms}$ and $x_{0rms}$ are horizontal rms widths at the scanner with the zero-crossing cavities on and off, respectively. This relation and measurement procedure were tested using a simulation where the zero-phasing measurement is performed and compared to the actual bunch length. The results shows good agreement over bunch length of 0.1 to 0.4 ps range except a 10 fs offset.

The bunch length was systematically changed by varying the second SRF cavity phase, resulting in longitudinal phase space rotations. Excellent agreement has been achieved between the measurement and simulation, shown in Fig. 4. It was observed that plus and minus 90 degree off crest gave different measured bunch lengths, as shown in Fig. 5a and b, which is also consistent with the simulation results. The reason is that in general, the longitudinal phase space ellipse of the incident beam has a slope, $dE/dt$. The RF wave has slope of +/- 2πΔt at the zero-crossings. When these two slopes have the same sign, the measured horizontal profile will be wider, giving a longer bunch length. Therefore, the average bunch length of the two should be used. A relation between the phase space slope and measured bunch length is found to be

$$\frac{dE}{dt} = \frac{\sigma^2}{2\pi\Delta t}$$

where $\sigma^2$ are the measured bunch length with zero-phasing cavities at plus and minus 90 degree off crest, respectively, and $\sigma$ is the average. The left side of Eq (4) is plotted from simulation in the solid line while the right side of Eq (4) is displayed from measurement in circles in Fig. 6, as the phase of the second SRF bunching cavity is varied. They agree pretty well. It is noted that the zero value point represents the upright position of the ellipse in the phase space, where the shortest bunch was obtained in both experiment and simulation. There is a steep slope around the zero point where the slope of the ellipse changes sign, corresponding to the transition from under compression to over compression. The zero phasing measurement gives bunch length with high precision. The main shortcomings are that the measurement is destructive and time consuming.

![Graph showing bunch length versus phase change](image)

Fig. 4 Bunch lengths versus phase change of the bunching cavity, where circles are from measurement while solid curve is from simulation.

![Graph showing horizontal profile](image)

Fig. 5 Horizontal profile measured by wire scanner. (a) is for zero-phasing cavity minus 90 degree off crest, resulting a longer bunch length while (b) is plus 90 degree off crest, giving a shorter bunch length.
Fig. 6 Relation given by Eq. (4) is plotted for different bunching SRF phases, where the circles are the right side of the equation and from measured bunch lengths while the solid curve is the left side and from phase space of simulation.

Fig. 7 Schematic diagram of the whisker contacted GaAs Schottky diode assembly

To combat the shortcomings of the previous methods, a noninvasive CSR bunch length monitor has been developed [25-27]. Comparing two CSR power spectrum curves in Fig. 1, the spectrum for the shorter bunch length covers the spectrum for the longer bunch length at long wavelengths, but has extra power at short wavelengths. Therefore, the output signal from a CSR power detector with an arbitrary "bandpass" characteristic will always increase as the bunch length becomes shorter, until such power changes take place at wavelengths outside the range of the detector. Such a monitor was installed after the first chicane dipole. The key component of the detector is a state-of-the-art whisker contacted GaAs Schottky diode developed and fabricated at the Semiconductor Device Lab of the University of Virginia [28-30]. The diode assembly, shown in Fig. 7, consists of a 1/4 mm GaAs chip, a 90 degree polished corner reflector, and a 1 mil whisker wire. The whisker acts as a four wavelength traveling wave antenna with a 90 degree bend inductively cutting off the induced current to the open end. Its tip is etched to less than 1 μm and contacts one of thousands of 1 μm "honey-comb" Schottky diodes on the chip (see the right side of the drawing). The corner reflector is introduced to sharpen radiation pattern around the antenna. The radiation is focused on to the diode by a parabolic reflector following a single crystal quartz vacuum window. The diode is connected to a DC current supply providing a typical 1 μA operating current. Due to its nonlinear properties, a small voltage change, proportional to the incident radiation power, is generated and can be measured as the CSR signal. The diodes have high sensitivity. Unlike thermal detectors, due to its antenna structure the diode is insensitive to the background black body type radiation. The bandpass feature also makes it less responsive to background radiation outside of the interesting wavelengths. CSR signals were measured (see Fig. 8) and calibrated by the zero-phasing measurement shown above. The bunch length as short as 84 fs or 25 μm was achieved, and found simply by peaking the CSR signal (see Fig. 9). The measurement was done with a 513 μm diode plus a 20% bandpass mesh filter [31], for 3×10⁵ electrons per bunch. With 200 sample average, the CSR signals after amplification have a signal to noise ratio of 450 for the 84 fs bunch and 100 for a bunch length of 0.6 ps. The main limitation on the resolution in our experiment is due to a slow signal fluctuation of about 20 mV with a few minute time scale. At typical operating conditions, the CSR signal changed from 4 V to 2 V as the bunch length increased from 0.45 ps to 0.6 ps, so a bunch length change of a few fs may be resolved for Gaussian bunches. The monitor is noninvasive and has high resolution. It is also compact (3 cm in size), relatively inexpensive (a few thousand US dollars), and operates at room temperature. Potentially such a monitor can be integrated into a feedback of a control system to lock the operating bunch length. Its main shortcoming is that it cannot provide an absolute value of bunch length. Therefore, it needs to be calibrated with a precise bunch length measurement such as the zero-phasing [26-27].

Fig. 8 Experiment result of CSR power versus rms bunch length where CSR power was measured by the Schottky diode and bunch lengths were measured by zero-phasing technique.

Fig. 9 Measurement results of CSR power and bunch lengths versus relative SRF phase changes. As expected, the shortest bunch length corresponds to the highest CSR power signal.

The strategy of bunch length control at Jefferson Lab is: use zero-phasing measurements as the primary standard to
characterize the longitudinal beam dynamics and calibrate the CSR monitor with the assistance of PARMELA simulations as cross-checks, use the CSR detector to monitor bunch length during beam delivery, and when the CSR signal varies outside of acceptable bounds indicating the bunch length has changed, use the phase transfer function measurement to correct the RF phase drifts that have occurred.

Summary

Several bunch length related measurement in the subpicosecond parameter regime have been discussed. The conventional streak camera or fast deflecting cavity can be employed in the subpicosecond regime with some significant capital investment and operating expertise. Coherent radiation detection techniques offer a very attractive alternative, which is relatively easy to operate, much less expensive, and has excellent performance for shorter bunches. The uncertainty of extracting the longitudinal profile from measured power spectrum needs to be experimentally resolved.

At Jefferson Lab, a phase transfer function measurement is used to correct and reproduce RF phases to a couple tenths of degree, which is easy to implement and gives high sensitivity. The zero-phasing method was employed to characterize the bunching process; bunch lengths as short as 84 fs have been measured. Excellent agreement has been achieved between experiment and simulation, and simulation has been very helpful in understanding the measurement results. A noninvasive CSR bunch length monitor using a Schottky diode has been developed. The diode provides very high sensitivity, which means it is able to detect bunch length changes of order 1 fs and for charges as low as $10^5$ per bunch at a bunch length of 0.5 ps. It is compact, inexpensive, and operated at room temperature. The shortest bunch was found experimentally by peaking the CSR signal from the diode.

Acknowledgment

The author gratefully acknowledges G.A. Krafft, P. Wood, D. Porterfield, and T. Crowe for their contribution to the work done at Jefferson Lab. He would like to thank H. Nguyen, R. Abbott, and E. Feldt for their excellent technical support, and CEBA operations personnel for their help on the measurement. He wants to thank B. Dunham and H. Liu for their help on running PARMELA simulation code. He would also like to thank C. Sinclair for his constant encouragement and support. This work was supported by U.S. DOE under contract #DE-AC05-84ER40150.