Broad emission lines from opaque electron-scattering environment of SN 1998S
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ABSTRACT

I propose that broad narrow-topped emission lines with full width at zero intensity > 20000 km s\(^{-1}\) revealed by early-time spectra of SN 1998S originate from a dense circumstellar (CS) shell with the outer radius \(R \approx 10^{15}\) cm. The tremendous line width is the result of multiple scattering of photons of the narrow line by thermal electrons of the opaque CS gas. The H\(\alpha\) line on 1998 March 6 is reproduced by Monte Carlo simulations provided the Thomson optical depth of the CS shell is 3–4 at this epoch. The high density of CS shell implies that a cool dense shell (CDS), which forms at the ejecta-wind interface, is opaque in the Paschen continuum for about 40–50 days after the explosion. This explains, why strong lines from the supernova ejecta were not seen during an initial period of about 40 days after the discovery. The Thomson optical depth recovered from the electron-scattering wings is consistent with observational constraints imposed by the bolometric luminosity, photospheric radius and expansion velocity of the CDS.

Key words: supernovae – circumstellar matter – : stars.

1 INTRODUCTION

Supernova SN 1998S discovered on March 2.68 UT (Li & Wan 1998) belongs to a diverse family of SN IIn, which are generally believed to interact with a dense presupernova wind (Filippenko 1991, 1997; Chugai 1990). Of particular interest are the earliest spectra of SN 1998S, taken before 1998 March 12, with strong Balmer emission lines and Wolf-Rayet (WR) features, N III 4640 Å, He II 4686 Å on a smooth black-body continuum (Leonard et al. 2000; Liu et al. 2000; Fassia et al. 2001). The lines have similar profiles, composed of an unresolved line with full width at half maximum (FWHM) < 300 km s\(^{-1}\) and a broad line with full width near zero intensity ≥ 20000 km s\(^{-1}\) (Leonard et al. 2000). The narrow component is identified with the CS gas, while the broad line is attributed to the SN ejecta (Leonard et al. 2000), in accord with a picture generic to SN IIn.

I will present quite different view on the origin of the broad component. It will be explained as a result of broadening of the narrow line due to multiple scattering by thermal electrons in the opaque CS gas. I will show that this conjecture is consistent with observational constraints imposed by the bolometric light curve, photospheric radius and velocity of the ejecta-wind interface. I first outline the phenomenological picture, which will hint, why the CS gas and not SN ejecta is an appropriate site for the early-time broad emission (section 2), then calculate simple models of the ejecta deceleration and bolometric light curve (section 3). In section 4 the line profile will be simulated using Monte Carlo technique.

Henceforth the distance 17 Mpc, the extinction \(A(V) = 0.68\) (Fassia et al. 2000), and the redshift 850 km s\(^{-1}\) (Fassia et al. 2001) are assumed.

2 THE PHENOMENOLOGICAL MODEL

Below we outline the qualitative physical picture of the spectrum formation in the early-time SN 1998S using arguments based upon the available observational data and results obtained in other papers.

2.1 Why CS Thomson scattering?

SN 1998S exploded after 1998 February 23.7 (Leonard et al. 2000), which suggests that on March 6 SN was less than ten days old. At this age SN ejecta is essentially opaque, and the emission lines from SN ejecta must be affected by the occultation, i.e. they must show strong line asymmetry with the suppressed red part. The early emission lines, on the contrary, are symmetric (Leonard et al. 2000), and their origin from SN 1998S ejecta is, therefore, unlikely.

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The alternative explanation for the broad lines, we propose, is that they are the result of narrow line broadening
due to electron scattering in an opaque CS shell outside the SN photosphere. The following simple arguments give an order of magnitude estimate of the required Thomson optical depth of the CS shell to produce the broadening effect.

Let the Hα emissivity and scattering electrons be homogeneously distributed in a spherical layer with the Thomson optical depth \( \tau_T \). The expected ratio of the unscattered, i.e. narrow component, to the total emergent line flux is then \( U \approx [1 - \exp(-\tau_T)]/\tau_T \). On the other hand, assuming that the CS shell velocity is about \( 10^3 \) km s\(^{-1}\), which is hinted by the UV lines in HST spectra on March 16 (Lentz et al. 2001), we obtain that the narrow component (or unscattered emission) of Hα in the spectrum on March 6 (Fassia et al. 2001) comprises roughly 20 – 25% of the overall line emission, which suggests \( U(\tau_T) \approx 0.2 - 0.25 \). With this value the above expression for \( U(\tau_T) \) implies the optical depth of the CS gas \( \tau_T \approx 4 \). More precise value of \( \tau_T \) will be obtained in Section 4.

### 2.2 The distribution of the CS matter

The abrupt disappearance of the early-time emission lines after March 12 means that a dense CS shell, responsible for these lines, was overtaken by the SN ejecta to this moment. This argument was used by Fassia et al. (2001) to estimate the outer radius of the CS shell, \( R_{\text{c,1}} \approx 10^{15} \) cm. Note, the radius of the photosphere on March 6 estimated by the extrapolation of empirical data provided by Fassia et al. (2000) is \( R_P \approx 5 \times 10^{14} \) cm < \( R_{\text{c,1}} \).

Apart from this inner CS shell, there is also the CS matter in the outer region \( r > R_{\text{c,1}} \), which is revealed by narrow absorption and emission lines in spectra seen after March 12 and by the emergence at \( t > 50 \) d of the 'boxy' components of Hα and He I 10830 Å caused by the interaction (Fassia et al. 2001). The modeling of UV lines in the HST spectrum on March 16 (Lentz et al. 2001) indicates that the Thomson optical depth of the CS gas in the region \( r > 10^{15} \) cm is only \( \tau_T \approx 0.2 \). Therefore, practically all the optical depth \( \tau_T \approx 4 \) should be accumulated in the range of \( R_P < r < R_{\text{c,1}} \) with a linear density \( w = 4\pi r^2 \rho = 4\pi R_P^3 \tau_T/k_T/(1 - R_P/R_{\text{c,1}}) \approx 2 \times 10^{17} \) g cm\(^{-3}\), where we assume \( \rho \propto r^{-2} \), and \( k_T = 0.3 \) cm\(^2\) g\(^{-1}\).

The estimated value of \( w \) is tremendous, but yet is in line with the similar records in other SN IIn (Chugai 1992). As to the outer CS gas, the value \( \tau_T \approx 0.2 \) in the range \( r > R_{\text{c,1}} \) suggests that \( w = 4\pi R_{\text{c,1}}^3 \tau_T/k_T \approx 10^{16} \) g cm\(^{-3}\), which is consistent with the wind density required by the late-time (\( t > 1 \) yr) radio and X-ray emission (Pooley et al. 2001).

The above analysis implies that the CS environment has a 'dense core plus rarefied halo' morphology. This structure will be described here as a superposition of two components (\( j = 1, 2 \)), each described by the expression

\[
\rho_j = \rho_\infty (r/R_{\text{c,j}})^{s_j}[1 + (r/R_{\text{c,j}})^{p_j}]^{-1}.
\]

For the template model of the CS gas distribution (Fig. 1), which meets above requirements and will be used below for the light curve and line profile models, we adopt \( s_1 = -2, p_1 = 10, R_{\text{c,1}} = 8 \times 10^{14} \) cm, \( s_2 = 0, p_2 = 2, \) and \( R_{\text{c,2}} = 5 \times 10^{15} \) cm with the linear density in the steady-state wind zones \( w_1 = 2.1 \times 10^{17} \) g cm\(^{-3}\) and \( w_2 = 2 \times 10^{16} \) g cm\(^{-3}\). In addition, we plot the Thomson optical depth (Fig. 1) assuming full ionisation of the CS gas and the hydrogen abundance \( X = 0.4 \). The latter is estimated from the fact that the flux ratio of He II 4686 Å to Hα in the spectrum on 1998 March 6 is about unity (Fassia et al. 2001) and assuming recombination case B. (The low hydrogen abundance may reflect mixing and mass loss). Note, at \( r = 10^{15} \) cm the model yields the Thomson optical depth \( \tau_T \approx 0.3 \) (Fig. 1), which is in a qualitative agreement with \( \tau_T \approx 0.2 \) derived by Lentz et al. (2001).

### 2.3 The opaque cool dense shell

The interaction of the freely expanding SN ejecta with the CS environment produces a double shock structure with the outer (direct) shock, running in the wind and the inner (or reverse) shock propagating inward the SN ejecta (Nadyozhin 1981, 1985; Chevalier 1982). If the CS wind is dense enough \( (w \geq 3 \times 10^{15} \) g cm\(^{-3}\)\), a cool dense shell (CDS) forms at the ejecta-wind interface due to the cooling and compression of the shocked ejecta in the inner shock (Chevalier & Fransson 1985, 1994). In case of a very dense wind \( (w \geq 10^{17} \) g cm\(^{-3}\)) the outer shock during the initial epoch of about one month may be radiative as well and contribute to the CDS formation. The evidence for the CDS in SN 1998S is hinted by the 'boxy' Hα emission at the late epoch (Leonard et al. 2000; Gerardy 2000; Fassia et al. 2001). The blue slope of the Hα boxy component, when approximated by the emission from a spherical shell, suggests the average CDS velocity \( 5600 \pm 500 \) km s\(^{-1}\) and \( 5500 \pm 500 \) km s\(^{-1}\) according to spectra on day 92 (Fassia et al. 2001) and on day 140 (Leonard et al. 2000) respectively.

Remarkably, the CDS turns out opaque in the Paschen continuum for about 40–50 days. This claim is supported by...
the following arguments. The mass of the CS shell in the range of $10^{15}$ cm for the template wind model is $\sim 0.1 M_\odot$. After the CS shell is swept up by the SN ejecta with the density in outer layers $\rho \propto v^{-2}$ one expects that the mass of the CDS should be $(\omega - 4)/2$ times larger (Chevalier 1982) or $M_\text{CDS} \sim 0.2 - 0.8 M_\odot$ depending on $\omega$, which lies in the range 8–20 (Chevalier & Fransson 1994). We assume that the excitation temperature is equal to the effective temperature $T_{\text{eff}}$ and approximate the bolometric luminosity evolution by the power law $L = L_0(t_0/t)^2$, where $L_0 = 10^{43}$ erg s$^{-1}$ and $t_0 = 40$ d, which is compatible with the observed luminosity during the period of 15–80 d after the discovery (Fassia et al. 2000). With these remarks, the condition $\tau_3(0.65 \mu \text{m}) = 1$ at Ho or $\tau_3 = 2$ at the Paschen edge results in the following expression for the time of the CDS transparency $t_1$ in the Ho band

$$t_1 = 44 \left( \frac{t_0}{40 \text{ d}} \right)^{0.5} \left( \frac{v}{6000 \text{ km/s}} \right)^{-0.5} \left( \frac{L_0}{10^{43} \text{ erg/s}} \right)^{0.25} \times (1 + 0.05 \ln \phi) \text{ days,} \quad (2)$$

where $v$ is the CDS average expansion velocity, $\phi \propto M_\odot X (1 - x)t_1^{-2} v^{-2}$ and the numerical prefactor in Eq. (2) is obtained for $M_\odot = 0.5 M_\odot$, $X = 0.4$, H ionisation degree $x = 0$, $t_1 = 44$ d, and $v = 6000$ km s$^{-1}$, which implies $\phi = 1$. According to Eq. (2), the value of $t_1$ weakly depends on parameters, which gives us a confidence that the CDS is actually opaque during initial 40–50 days.

Two important consequences follow from the fact that SN ejecta is enshrouded in the opaque CDS. First, the SN photosphere should reside in CDS at the epoch $t < t_1$, which matters to the observational test of the deceleration dynamics (section 3). Notably, the optically thick electron-scattering gas does not affect the photospheric continuum, because CDS shell is effectively thin, i.e. the scattering is conservative. Actually, for the typical density of the CS shell $n_e \sim 10^{19}$ cm$^{-3}$ and temperature $T_e \sim (2 - 3) \times 10^4$ K the ratio of the absorption to the extinction coefficient is $\epsilon \sim 10^{-3}$, so the thermalization length $1/\sqrt{\tau} \gg \tau_3$.

The second point, but of a primary significance, is that the opaque CDS prevents the emergence of strong emission lines from the SN ejecta. Moreover, strong emission lines are not expected from the opaque CDS either. To clarify the latter point, note that the pressure equilibrium and the mass conservation result in a small width of the CDS (Chevalier & Fransson 1994), $\Delta R/R \ll 1$, which leads to the small width of the SN atmosphere residing in the CDS, $\Delta R_{\text{atm}}/R < \Delta R/R \ll 1$. Since the early-time continuum is nearly black-body, $I_\nu \approx B_\nu(T)$, and the line source function in the CDS is limited by the inequality $S_\nu \leq B_\nu(T)$, we conclude immediately that the expected contrast of emission lines formed in the opaque CDS is very small, $\Delta F/F \approx (S_{\nu}/B_\nu)(2\Delta R_{\text{atm}}/R) \ll 1$. It becomes thus clear, why strong emission and absorption lines of SN 1998S ejecta were not seen during the period 10–40 days after the discovery, the observational fact emphasised by Fassia et al. (2001). On the other hand, the opaque CDS does not preclude the emergence of the strong emission lines from the extended CS shell.

To summarize, the qualitative model for the early-time spectrum of SN 1998S may be portrayed as a sharp black-body photosphere embedded into the opaque electron-scattering CS shell, which is responsible for the emission lines observed before March 12.

3 THE INTERACTION AND LIGHT CURVE MODEL

Given the similarity of SN 1998S and SN 1979C photometric and spectral properties (Liu et al. 2000), the light curve of SN 1998S is likely of the same nature as that of SN 1979C. In line with the hydrodynamical model of the SN 1979C (Blinnikov & Bartunov 1993) we suggest that the light curve of SN 1998S is the result of an explosion of a red supergiant with an extended envelope, $R \sim (1 - 10) \times 10^3 R_\odot$, and a moderate mass of ejecta $\sim 5 M_\odot$. The radioactivity as well as the ejecta-wind interaction are likely responsible for the late-time SN 1998S luminosity. One cannot rule out that the ejecta-wind interaction may contribute to the initial phase of the light curve as well.

The bolometric light curve will be simulated using a linear composition of the analytical bolometric light curve of 'bare' (i.e. without wind) SN II (Arnett 1980, 1982) and the

![Figure 2. Bolometric light curve of SN 1998S, radius and velocity of the thin shell.](image)
light curve powered by the ejecta-wind interaction (Chugai 1992). The latter model computes the optical luminosity, produced as a result of reprocessing of the X-ray radiation from the outer and inner shocks. This model is upgraded here to include the Compton cooling of the postshock gas (Fransson 1982) and the reprocessing of the X-ray radiation by the wind material as well. The dynamics of the ejecta deceleration in a thin shell approximation (Chevalier 1982) is solved numerically, which yields the thin shell radius \( R(t) \) and its velocity \( v(t) \). The light curve computed in an approximation of the instant radiation escape from the CS shell, is corrected for the diffusion delay in the CS medium using Sobolev (1980) analytical formula for the escaping luminosity.

The density profile of a freely expanding SN envelope is insensitive to the outer wind density unless \( \rho \times v \) affects the very early phase of the model and the empirical light curve is not dramatic. Note, the factor of two increase in the luminosity corresponds to 20\% higher value of \( T_{\text{eff}} \).

The CDS is opaque during initial \( \approx 47 \) days in agreement with the previous estimates (section 2). Taking into account the six days lag between the explosion and the discovery we conclude that the opaque CDS gets transparent at \( \approx 40 \) d after the discovery. This is consistent with the observational fact that strong broad emission and absorption lines from SN ejecta appear only about day 40 after the discovery (Fassia et al. 2001). Remarkably, the outer shock is radiative in both models for \( \approx 20 \) days. As a result on March 6 with \( \approx 9 \) days passed after the explosion the outer postshock gas should cool very quickly resulting in a very thin outer postshock region, \( i.e. \Delta R/R < 0.1 \).

### Table 1. Parameters of light curve models

<table>
<thead>
<tr>
<th>Model</th>
<th>( M )</th>
<th>( E )</th>
<th>( R_0 )</th>
<th>( R_{c1} )</th>
<th>( w_1 )</th>
<th>( w_2 )</th>
<th>( t_1 )</th>
<th>( t_c )</th>
<th>( R_s )</th>
<th>( T_{\text{eff}} )</th>
<th>( \tau_T )</th>
</tr>
</thead>
<tbody>
<tr>
<td>A</td>
<td>5</td>
<td>1.1</td>
<td>2.4</td>
<td>21</td>
<td>2</td>
<td>47</td>
<td>19</td>
<td>5.0</td>
<td>21700</td>
<td>3.4</td>
<td></td>
</tr>
<tr>
<td>B</td>
<td>5</td>
<td>1.1</td>
<td>2.4</td>
<td>10</td>
<td>18</td>
<td>47</td>
<td>22</td>
<td>5.0</td>
<td>21500</td>
<td>3.8</td>
<td></td>
</tr>
</tbody>
</table>

procedure. Derived values shown in Table 1 include the moment \( t_1 \), when the optical depth of the CDS in the Paschen continuum at H\( \alpha \) wavelength \( \tau(0.65\mu m) = 1 \), the time \( t_c \), when the outer shock becomes adiabatic, and three important values on March 6: the radius of the thin shell \( (R_s) \), which coincides with the CDS, effective temperature \( (T_{\text{eff}}) \), and Thomson optical depth \( (\tau_T) \) of the wind. The optical depth of the CDS in the Paschen continuum is calculated assuming LTE for \( T = T_{\text{eff}} \) and the number density of the CDS defined by the isobaric condition, \( i.e. \) with the thermal pressure equal to the dynamical pressure \( \rho v^2 \), where \( \rho \) is the preshock wind density and \( v \) is the thin shell velocity. Models A and B produce similar results being consistent with the empirical light curve, photospheric radii and CDS velocity. Some luminosity deficit before day 30 might be related to the mentioned fact that in the analytical light curve the initial luminosity peak is underproduced (Arnett 1980). Yet, given large uncertainties of data, the difference between the model and the empirical light curve is not dramatic.

### 4 LINE PROFILE CALCULATIONS

We consider only the H\( \alpha \) line, although a similar approach may be applied to any other line, including WR lines, observed in early-time spectra of SN 1998S. The model suggests a sharp photosphere with a radius \( R_0 = R_s \) in a fully ionised isothermal CS gas \( (r > R_p) \) with an electron temperature \( T_e = T_{\text{eff}} \) (Table 1). Any effects related to the outer shock are omitted; they are of a minor importance for the line profile. The wind velocity law \( v = v_{\text{max}}(R_p/r)^2 + v_{\text{min}} \) is taken to mimic a radiative acceleration of the wind by the SN radiation. We adopt \( v_{\text{min}} = 40 \) km s\(^{-1} \) for the distant wind (Fassia et al. 2001) and \( v_{\text{max}} = 1000 \) km s\(^{-1} \) at the photosphere, a rough guess based upon the extrapolated behavior of the maximal velocities of the fast CS gas on March 20 and April 8 (Fassia et al. 2001). The result, actually, is not very much sensitive to \( v_{\text{max}} \) unless it significantly exceeds 1000 km s\(^{-1} \). The wind emissivity in H\( \alpha \) is assumed to scale as a recombination emissivity \( j = C_{\text{rec}}(h\nu/4\pi)\alpha_{32}n_e n(H^+) \)
Table 2. Parameters of demonstration models for line profile

<table>
<thead>
<tr>
<th>Model</th>
<th>$T_e$ K</th>
<th>$w_1$</th>
<th>$\tau_T$</th>
</tr>
</thead>
<tbody>
<tr>
<td>D1</td>
<td>25000</td>
<td>13</td>
<td>4.0</td>
</tr>
<tr>
<td>D2</td>
<td>25000</td>
<td>1.3</td>
<td>0.4</td>
</tr>
<tr>
<td>D3</td>
<td>25000</td>
<td>16.2</td>
<td>5.0</td>
</tr>
<tr>
<td>D4</td>
<td>30000</td>
<td>13</td>
<td>4.0</td>
</tr>
</tbody>
</table>

($\text{erg s}^{-1} \text{ cm}^{-3} \text{ ster}^{-1}$), where $\alpha_{2}^{}$ is the effective recombination coefficient for the H$\alpha$ emission (case B), while $C_{\text{em}}$ is an emission correction factor, which allows for uncertainties in the distance, extinction, electron temperature, hydrogen abundance, as well as for a wind clumpiness and a possible deviation from the recombination case B. The scattering in the wind is essentially conservative, but the photons struck the photosphere will be considered lost. The resonance scattering is neglected. This approximation is justified by our simulations, which do not show a dependence on the resonance scattering at the considered epoch.

The emergent line spectrum is computed using the Monte Carlo technique. The photon frequency at each scattering is randomly chosen adopting the symmetric angle-averaged frequency redistribution function (cf. Mihalas 1978). Note, computations with both angle-averaged and angle-dependent frequency redistribution functions are mutually consistent with a high precision even in the case of $\tau_T \approx 1$ as Hillier (1991) has shown in his study of electron-scattering effects in WR stars. The relativistic correction to the Doppler effect and Compton recoil produce a net blue shift $\Delta \nu/\nu = N_e (3kT_e - h\nu)/m_e c^2$ (Weymann 1970), where $N_e$ is the average number of scatterings. This effect, although small, is included in the profile modeling.

The H$\alpha$ line broadening effect in the case of the high Thomson optical depth is illustrated in Fig. 3 with model parameters given in Table 2, which presents the electron temperature, the linear wind density $w_1$, and the Thomson optical depth. In all the cases the photospheric radius is $R_p = 4 \times 10^{14}$ cm, the wind velocity is $u = 40 + 1000 (R_p/r)^2$ km s$^{-1}$ and the CS density distribution is defined by Eq. (1) with $w_2 = 0$, $R_{c1} = 9 \times 10^{14}$ cm, $s_1 = -2$, $p_1 = 10$. All the profiles are normalized to unity at maximum. A gaussian smoothing with FWHM=6.7 Å is applied henceforth to the computed profile to allow for the finite resolution in the spectrum on 1998 March 6 (Fassia et al. 2001).

Results show that the template model D1 with the Thomson optical depth $\tau_T = 4$ produces strong nearly symmetric electron-scattering wings. It should be emphasised that the line profile from the expanding electron scattering wind with the opaque core is the result of the combination of several factors including, (i) single scattering broadening related to the outmost layers with $\tau_T \leq 1$; (ii) broadening due to multiple scattering, which may be interpreted as a diffusion in the frequency space; (iii) the redshift acquired in the course of multiple scattering in the expanding medium; (iv) the photon absorption by the opaque photosphere. It should be emphasised that the resulting redshift essentially depends on the wind expansion kinematics. The model D2 with ten times lower optical depth compared to the model D1 clearly shows the blue shift due to the occultation of the wind by the photosphere and the enhanced red wing due to the expansion effect. A primary reason, why the expansion effect is not so apparent in the model D1 relates to the adopted wind kinematics with the velocity dropping outward. In the optically thick situation the contribution of the outer slow expanding gas dominates, which thus accounts for the small expansion effect in the model D1. Obviously, this effect does not operate in the transparent case D2, where fast inner scattering wind essentially contributes in the line profile. Note, the mentioned bias to the red wing in the model D2 very much resembles the appearance of electron-scattering wings in WR stars (Auer & van Blerkom 1972; Hillier 1991). The model D3 with $\tau_T = 5$ has markedly stronger wings compared to the model D1 in a wide range of velocities. The 20% higher electron temperature (model D4) slightly increases high velocity wings. Such an effect is practically on the verge of detectability. In this regard we note, that the uncertainty of $T_{\text{eff}}$ in the light curve model is of $\approx 20\%$, which is thus insignificant for the line modeling.

The spectrum of H$\alpha$ on 1998 March 6 (Fassia et al. 2001) with two 'best' fit versions of the line profile based upon models A and B are shown in Fig. 4. To make the plot the emission lines are placed upon the appropriate continuum. As noted before (section 3), parameters of models A and B are found using iterative procedure to fit simultaneously the light curve, photospheric radius, expansion velocity and the line profile. Both models reproduce the observed profile with the emission correction factor $C_{\text{em}}$ being close to unity (1.36 and 1.13 for model A and B respectively).

![Figure 3. The line broadening effect for different parameter sets (see Table 2). Shown are the template model D1 (thick solid line), model D2 with small Thomson optical depth (thin line), model D3 with higher optical depth (dot-dashed line), and model D4 with higher electron temperature (dotted line).](image-url)
Surprisingly enough that the model A, which only slightly differs from the model B, shows a noticeable blue shift. This is related to the smaller ratio \( R_{c,1}/R_p \), i.e. higher compactness of the CS shell. Note, the higher blue shift would be inconsistent with the observed profile, which implies that \( R_{c,1} \geq 8 \times 10^{14} \text{ cm} \). On the other hand with the Thomson optical depth of CS gas at the radii \( r > 10^{15} \text{ cm} \) as low as \( \tau_T \sim 0.2 \) (Lentz et al. 2001) the outer boundary of the CS shell cannot significantly exceed \( 10^{15} \text{ cm} \). Therefore we conclude that \( R_{c,1} \approx 10^{15} \text{ cm} \) is an optimal estimate for the cutoff radius of the inner CS shell.

With the single studied epoch we cannot rule out that the density distribution at \( r < R_{c,1} \) may deviate from the law \( s_1 = -2 \). For instance, the profile may be fitted assuming \( s_1 = -2.5 \) and \( R_{c,1} = 10^{15} \text{ cm} \) with similar value of the optical depth, \( \tau_T \approx 3.5 \). Other uncertainties of the model include the clumpiness, and asymmetry of CS gas. The clumpiness would result in the decrease of the Thomson optical depth compared to the smooth distribution. The global asymmetry of the CS environment (if any) would suggest that our results must be refereed to some equivalent spherical model. At any case, uncertainties are not able to change the major result, that the broad line wings on March 6 require the Thomson optical depth of the CS shell in the range of 3–4.

5 DISCUSSION

I have argued that the broad narrow-topped emission lines in the early-time spectra of SN 1998S are the result of the emission and Thomson scattering of line photons in the opaque CS shell with the outer radius of \( \approx 10^{15} \text{ cm} \). It was demonstrated that the CS density distribution appropriate to the line broadening is consistent also with the constraints imposed by the light curve, photospheric radius and velocity of the CDS. It was shown that the CDS is opaque in the Paschen continuum during about 40–50 days after the SN explosion. The absence of strong emission and absorption lines from SN ejecta during 40 days after the SN discovery (Fassia et al. 2001) is explained as a direct consequence of the opaque CDS. Both the electron-scattering CS environment and the opaque CDS, thus, may produce pronounced observational effects in SN IIn.

Despite an obvious success in explaining the spectral evolution of SN 1998S, the concept of the opaque CDS faces a problem in accounting for the weak broad absorptions of H, HeI and Si II, which are noticeable in SN 1998S spectra before day 40 (Fassia et al. 2001). A plausible explanation for these lines might be that the CDS is not a perfect sphere, but is instead ‘punched’ i.e. has ‘holes’. In such a case the absorbing gas may be identified with the unshocked gas of SN ejecta seen through the holes in the opaque CDS. A punched structure of the CDS might be caused by the Rayleigh-Taylor instability or by a global wind asymmetry. The latter is implied by the detection of the intrinsic polarization of SN 1998S on 1998 March 7 (Leonard et al. 2000).

For instance, the asymmetric opaque CDS might have an appearance of a wide equatorial belt with two transparent poles, one of them lying in the near hemisphere.

In regard to the ambiguous interpretation of the spectropolarimetric data (Leonard et al. 2000) the following property of our model may be relevant. Specifically, the model predicts that the narrow component in the early-time spectrum must consist mostly of the non-scattered radiation, while the broad wings are the result of multiple scattering. With this property more consistent is the interpretation II (polarized broad lines and unpolarized narrow lines) suggested by Leonard et al. (2000).

The origin of the inner CS shell with the outer radius of \( \approx 10^{15} \text{ cm} \) is intriguing. If it was created by the slow red supergiant wind with the velocity \( u = 10 \text{ km s}^{-1} \), then the age of this CS shell was 30 yr at the explosion, which cannot be readily associated with any specific time scale of the presupernova. On the other hand, the velocity of the matter ejection might be as high as 100 km s\(^{-1}\), which is still tolerared by the spectral resolution of the narrow component (Fassia et al. 2001). In that case the age of the CS shell was only 3 yr, which reminds the time scale 1–10 yrs for the Ne and O burning in cores of 12–20 \( M_\odot \) stars (Heger 1998).

Woosley (1986) noted that the Ne burning in degenerate cores of \( \sim 11 M_\odot \) stars may result in the violent mass loss roughly 1 yr prior to core collapse. Remarkably, the dense shell of a similar size (\( \sim 10^{15} \text{ cm} \)) has been invoked to account for the early-time line behavior in SN 1983K (Niemela et al. 1985), which is another SN II with WR features, and in type IIn SN 1994W (Sollerman et al. 1998).

It would be interesting to search for signatures of broadening of CS lines due to scattering by thermal electrons in other SN IIn spectra. To distinguish between the case of narrow lines on top of the broad lines emitted by SN ejecta, likewise in e.g. SN 1988Z (Filippenko 1991; Stathakis & Sadler 1991) and the case of narrow lines with CS electron-scattering wings, the following properties of the early-time...
spectra of SN 1998S must be stressed: (i) the broad wings
are smooth; (ii) strong emission lines have similar profiles;
(iii) the continuum is smooth and close to black-body. We
deliberately do not emphasize the wing symmetry, since
in the case of a low Thomson optical depth and a high
wind velocity the red wing may become stronger due to
the CS expansion effect and the resonance scattering. In
this regard of particular interest are SN 1994Y, SN 1994W,
and SN 1994ak, reviewed by Filippenko (1997). Their early-
time spectra show narrow lines with smooth broad wings on
smooth continua. These properties are very suggestive of the
CS electron-scattering origin of line wings and the presence
of the opaque CDS in these supernovae.

Acknowledgments

I am grateful to Peter Lundqvist, Peter Meikle and Alexand-
dra Fassia for discussions of different issues of SN 1998S
and for a creative aura during my visit to Saltsjöbaden and
Imperial Colledge.

The study was supported by RFBR grant 01-02-16295.

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