Luminosity functions of galaxies in the Coma cluster
**U, B and r band luminosity functions of galaxies in the Coma cluster**

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**ABSTRACT**

We present a deep multi-colour CCD mosaic of the Coma cluster (Abell 1656), covering 5.2 deg² in the B and r bands, and 1.3 deg² in the U band. This large, homogeneous data set provides a valuable low redshift comparison sample for studies of galaxies in distant clusters. In this paper we present our survey, and study the dependence of the galaxy luminosity function (LF) on passband and radial distance from the cluster centre. The U, B and r band LFs of the complete sample cannot be represented by single Schechter functions. For the central area, \( r < 245 \, h^{-1}_{100} \) kpc, we find best-fitting Schechter parameters of \( M_U^* = -18.60^{+0.13}_{-0.18} \) and \( \alpha_U = -1.32^{+0.18}_{-0.28} \), \( M_B^* = -19.79^{+0.17}_{-0.17} \) and \( \alpha_B = -1.37^{+0.024}_{-0.016} \) and \( M_r^* = -20.87^{+0.12}_{-0.17} \) and \( \alpha_r = -1.16^{+0.012}_{-0.019} \). The LF becomes steeper at larger radial distance from the cluster centre. The effect is most pronounced in the \( U \) band. This result is consistent with the presence of a star forming dwarf population at large distance from the cluster centre, which may be in the process of being accreted by the cluster. The shapes of the LFs of the NGC 4839 group support a scenario in which the group has already passed through the centre.

**Key words:** Galaxies: clusters: individual: Coma (A1656) – Galaxies: luminosity function – Galaxies: evolution – Galaxies: formation.

1 INTRODUCTION

Clusters of galaxies are important laboratories for studies of galaxy evolution. The galaxy population in clusters is very different from the population in the field, suggesting that galaxy formation and evolution are a strong function of the environment.

The galaxy luminosity function (LF) should be an excellent tracer of environmental effects. Knowledge of the shape of the LF (in different bands) is a powerful tool for studies of galaxy evolution. Specifically, one can look for correlations between the shape of the general LF and environmental or cluster properties. In general, the LF drops steeply at bright magnitudes and rises gradually at fainter magnitudes as described by a Schechter function (Schechter 1976). Sometimes, however, features such as bumps and a steeply rising faint part are found, which cannot be adequately fitted by a single Schechter function. Galaxies in the cluster core region are expected to have a different merger history than the galaxies populating the cluster outskirts where it blends into the field. This should be reflected in differently shaped LFs for dense and less dense regions within a cluster. López-Cruz et al. (1997) propose that the flat faint end slopes found in rich clusters result from the disruption of dwarf galaxies. Biviano et al. (1995) report a dip in the bright part of the general LF for rich clusters which is not seen in LFs of poor clusters or in the field. Andreon (1998) verified the invariance of the shape of the bright part of the type-dependent LF in a large range of environments from the field to the cores of clusters several orders of magnitude denser. The determination of the exact shapes of LFs is difficult as the faint ends suffer from background contamination of field galaxies.

The Coma cluster (\( z = 0.023 \), richness class 2) is the richest of the nearby clusters and ideal to study environmental effects (for a detailed overview of research on the Coma cluster see Mazure et al. 1998). Previous large field studies of the photometric properties of the galaxies in the Coma cluster have been based on photographic plates (e.g. Godwin, Metcalfe & Peach 1983; Lugger 1989). CCD studies yield better photometric precision, but have hitherto been limited to relatively small areas, mainly focused on the central regions (e.g. Thompson & Gregory 1993; Biviano et al. 1995; Bernstein et al. 1995; López-Cruz et al. 1997; Secker et al.)
The prime focus of the INT. The sky coverage is in Fig. 1. It is designed to provide a large field survey capability for and a fifth CCD for autoguiding. The layout of the chips is shown

2 OBSERVATIONS

The data were collected during the nights of March 19–22 1999 with the Wide Field Camera (WFC) on the Isaac Newton Telescope (INT), on Roque de Los Muchachos on the island of La Palma (Spain). The WFC consists of four 2048 × 4100 pixels EEV CCDs and a fifth CCD for autoguiding. The layout of the chips is shown in Fig. 1. It is designed to provide a large field survey capability for the prime focus of the INT. The sky coverage is 4 × 2592 with a plate scale of 0.333 pixel−1. The camera covers 80 per cent of the unvignetted field of the INT.

We have imaged a mosaic of 25 overlapping pointings covering a total area of ~ 5.2 deg2 or 2.8 × 2.8 h−1 Mpc. Broadband filters RGO U, Harris B and Sloan r were used for the 6 pointings covering the core and the south-west group (containing NGC 4839). The other 19 pointings were observed with Harris B and Sloan r. For each pointing two exposures, offset by ~ 1, were taken. This ensured that we would be able to determine the relative zero point offsets between exposures and chips and there would be very few gaps in the final mosaic. Furthermore, galaxies in the overlapping regions give us good estimates of the errors due to photon noise and flatfielding. Integration times were 2 × 300 s in B, 2 × 600 s in r and 2 × 900 s in U. The layout of the field is shown in Fig. 2. Thick lines delineate pointings which were observed in the U band, as well as B and r. Pointing 11 served as reference field for the photometric calibration. The position of NGC 4839 is indicated by the square. Coordinates are given relative to α = 12h 59m 43s, δ = +27° 58′ 14″.

The overall weather was good with an average seeing during the first two nights of ~ 1.4 and ~ 1.9 during the last two nights in the r band. The strategy was to observe the central parts of the cluster in U, B and r under photometric conditions. During the first night the standard Landolt (1992) fields Sa107-602 and Sa101-427 were also observed at similar airmasses as the central fields. These standard fields contain many standard stars and give a good spread over the four CCD chips. This is important for the absolute calibration, since no two chips have exactly the same characteristics. In fact it is known that the WFC is non-linear.

The Coma fields were observed when the cluster had risen to an airmass < 1.8. At the start of nights 3 and 4 we took exposures of an empty field (no cluster). This field was later used to correct U band galaxy counts for foreground/background contamination.
3 INITIAL REDUCTION

3.1 Flatfielding

Prior to any reduction the images were inspected to judge their quality. For each chip the bias frames per night were checked for repeating structures and count levels. The bias-structures were also visible in the science images. We combined all bias frames to create an average master bias frame per night per chip. After several tests we decided that the bias subtraction had to be performed in two steps; we first subtracted the overscan level by fitting a second order polynomial to the columns and then subtracted the (overscan subtracted) master bias frames. The second step successfully removed the remaining bias structures for chips 1, 2 and 4. Chip 3 suffered from a few bad columns. These can be removed by interpolation or by aligning and combining the images taken with a small offset. The rms noise level in the master bias frame was negligible compared to the rms noise in the science frames.

Accurate flat field images were created from the science frames. We have obtained 52 science images of the Coma area per chip per band for the B and r bands. For the U band we have 23 science images, including the empty fields. We constructed a B and r band masterflat by scaling these images by the mode, rejecting the lowest 10 and highest 15 pixel values, followed by median filtering. The U band masterflats were constructed in the same way, but there we rejected the lowest 5 and highest 10 pixel values before median filtering.

As a test we compared our flatfields to the ones of the Wide Field Imaging Survey which are available from the WFC archive. Differences between the flat fields were at the level of at most 1 per cent. The flat fields of the WSC were scaled all pointings in such a way that the errors were spread over the whole area covered. We dedicated the photometric anchor object to determine the photometric offsets between neighbouring pointings. First, we made sky-images by filtering out all objects in the overlapping areas in order to guarantee a reliable determination. We found differences of a few hundredths of a magnitude between fields taken at significantly different times (airmasses, conditions) in B and r up to more than a tenth of a magnitude in U. We mapped all the photometric offsets per pointing per band and scaled all pointings in such a way that the errors were spread over the total observed region and did not accumulate towards the edges of the covered area. The final result is that all B and r band images have the same zero-point to $\sim 0.04$ mag and the U band images to $\sim 0.06$ mag.

The photometric calibration was done using Landolt (1992) standard stars. We did not have sufficient standard stars on all the chips to solve for the extinction coefficients so we set the extinction coefficients to constant values. We used average extinction coefficients at the effective wavelengths of the filter+CCD system, as listed in Table 2, to derive the colour terms and zero-points. The zero-points are listed in Table 3. The colour terms were found to be very small ($\sim 0.01$) and are neglected. Since Coma lies close to the galactic pole the extinction is insignificant for our purposes (0.043, 0.034 and 0.021 mag in the U, B and r bands respectively). Hence, we did not apply extinction corrections.

4 OBJECT CATALOGUES

The data volume is considerable and requires a fully automated pipeline for data handling. After the standard reduction steps the processed images were presented to software implemented at the Leiden Data Analysis Center (LDAC) for pipeline processing of overlapping images (Deul 1998). The processing software is a series of programmes that, when run in a chain, derive source parameters for any given set of input frames of a given passband. Only the

### Table 1. Photometric offsets relative to chip 4

<table>
<thead>
<tr>
<th>chip</th>
<th>U</th>
<th>B±σ</th>
<th>r±σ</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>+0.347±0.015</td>
<td>+0.337±0.013</td>
<td>+0.446±0.011</td>
</tr>
<tr>
<td>2</td>
<td>+0.170±0.015</td>
<td>+0.410±0.013</td>
<td>+0.501±0.017</td>
</tr>
<tr>
<td>3</td>
<td>+0.016±0.015</td>
<td>+0.325±0.014</td>
<td>+0.376±0.011</td>
</tr>
</tbody>
</table>

### Table 2. Average extinction coefficients for La Palma

<table>
<thead>
<tr>
<th>band</th>
<th>$\lambda_{\text{eff}}$ (Å)</th>
<th>extinction/airmass (mag/airmass)</th>
</tr>
</thead>
<tbody>
<tr>
<td>U</td>
<td>3610</td>
<td>0.45</td>
</tr>
<tr>
<td>B</td>
<td>4361</td>
<td>0.20</td>
</tr>
<tr>
<td>r</td>
<td>6216</td>
<td>0.08</td>
</tr>
</tbody>
</table>

### Table 3. Zero-points (ZP) of chip 4 for night 1

<table>
<thead>
<tr>
<th>ZP±σ</th>
</tr>
</thead>
<tbody>
<tr>
<td>U</td>
</tr>
<tr>
<td>B</td>
</tr>
<tr>
<td>r</td>
</tr>
</tbody>
</table>

5 http://archive.ast.cam.ac.uk/wfsurvey/wfsurvey.html
first step is an actual data reduction task in that it reduces the information to be processed from image data to catalogue data (an object list). All but the last of the following pipeline routines add information to the catalogue(s) increasing its size and information content. The final step merges the catalogues to create a multi-colour object catalogue with astronomically meaningful source information. The pipeline processing is performed on the full data set. Along the way we must decide on values for various parameters. We describe the pipeline steps in more detail below.

4.1 Detection of objects
We used SExtractor to automatically detect objects on each chip individually. The complete analysis of an image is done in six steps. First, a model of the sky background is built and parameters describing the global statistics are estimated. Then the image is background-subtracted, filtered and thresholded. Detections are then deblended, cleaned, photometered, classified and written to the final catalogue. For specific details of each of these steps the reader is referred to Bertin & Arnouts (1996) or the SExtractor user’s guide.

Objects were identified as the peaks in the (background subtracted) convolved images that were higher than a given threshold above the local background. We used most of the standard SExtractor settings except for the memory parameters which had to be increased in order to detect the large cD galaxies successfully. The seeing parameter had to be adjusted for each image individually for a good star/galaxy separation. For all objects positions, magnitudes, basic shape parameters and star/galaxy (S/G) classifiers were determined and written to a catalogue. SExtractor produced a catalogue for each image which was subsequently converted to a format suitable for pipeline reduction. As a first pipeline processing step, all information of the individual image source extractions plus all original FITS image header information is combined into one single output catalogue per band.

4.2 Astrometry
Astrometric calibration was performed by pairing the input position catalogue (USNO-A2) with the extracted object information. For multiple band processing intercolour pairing is done first and between frames in overlap, overlap pairing is performed as well. The derived astrometric solution is then applied to all the objects in the set of frames. Sky coordinates (RA and Dec), as well as corrected geometric parameters are calculated. The final precision of this calibration depends on the accuracy of the source extractions, input catalogue accuracies and the correctness of the functional description of the distortions. The pipeline documentation gives an estimate of $\sim 0.3$ rms.

4.3 Final object catalogue
The final step in creating a catalogue containing useful multi-colour astronomical data is to merge all catalogues to get one source per position on the sky. All information referring to the same astronomical object is gathered and merged. Position information is a weighted mean of all detections where the weighting is based on detection signal-to-noise and detection environment conditions. Details of the merging are configurable. When the brightness contrast between overlapping galaxies is too low the software is not able to deblend them correctly, resulting in an erroneous catalogue entry. On the other hand, setting the deblend contrast parameter too low causes SExtractor to consider bright star forming regions in a galaxy as separate objects. Then, there is the possibility that deblended objects are merged by the pipeline software when creating the final object catalogue. This can happen in cases where objects are small compared to the errors in position and shape parameters. We carefully inspected dense regions in our mosaic and conclude that erroneous catalogue entries are rare and consequently do not affect our results.

Star/galaxy separation was performed based on SExtractor’s stellarity index. For bright objects stars and galaxies are easily separated, but towards fainter magnitudes and for bad seeing the division is not so clear. For most purposes we consider the objects with a S/G classifier value smaller than 0.8 in the $r$ band (best seeing) to be galaxies. Bright (saturated) stars tend to have a S/G classifier smaller than this. We filtered these out by demanding a S/G classifier $< 0.1$ for the brightest magnitudes. We visually inspected all bright objects to conclude that there is no contamination by stars up to at least $m_r = 15$. Beyond $m_r \sim 19$ mag we probably still have a fraction of stars in the sample, but for most purposes it is better to be contaminated by a (small) fraction of stars than to reject compact galaxies. Histograms of the catalogue’s raw number counts are shown in the panels of Fig. 3. The final mosaic, composed of all pointings observed in the $B$ and $r$ bands, is shown in Fig. 4.

4.4 Control fields
For a survey as large and deep as ours, foreground/background subtraction can only be treated statistically, since only the brightest galaxies have measured redshifts. The main source of uncertainty in the determination of LFs comes from number statistics and background variance. Usually, flanking fields are used to get an estimate of the foreground/background correction and its variance. We expect that over the large area of the WFC the effects of cosmic variance are not important.

For the $U$ band we have used $4 \times 900$ s observations of an empty field located at $\alpha = 8^h 00^m 00^s$, $\delta = +500000$ spanning $\sim 980$ arcmin$^2$. For both the $B$ and $r$ bands we have made use of the Wide Field Survey (WFS) data archive to get images of random fields. The $B$ band control images are eight 600 s exposures, spanning $\sim 2000$ arcmin$^2$ and centered at $\alpha = 12^h 55^m 55^s$, $\delta = +270140$ and $\alpha = 12^h 53^m 40^s$, $\delta = +262000$. The $r$ band control images are four 600 s exposures, spanning $\sim 1000$ arcmin$^2$ centered at $\alpha = 16^h 04^m 26^s$, $\delta = +54059$. For the $B$ and $r$ band control fields we rely on the (photometric) reduction of the four chips by the WFS team.

All control images were pipeline reduced to give control catalogues which were filtered with the same criteria as the Coma fields. We applied relative extinction corrections (Schlegel, Finkbeiner & Davis 1998) to bring the extinction in the control fields into agreement with the Coma extinction, not zero extinction.

4.5 Completeness
The histograms shown in Fig. 3 suggest that the limiting magnitude is $\sim 22.5$ mag for all bands. However, due to less than perfect conditions in the last two nights this limit does not apply to the total observed area. To have uniform completeness for the total mosaic we compute LFs up to $m_{lim} = 21.73$. The positions of these objects,
Figure 3. Histograms of the normalized raw $r$, $B$ and $U$ band number counts. $N_{\text{total}}$ gives the total number of catalogue entries for each passband.

Figure 5. Distribution of objects with $m_B < 21.73$. Coordinates are given relative to $\alpha = 12^h 59^m 43^s, \delta = +27^\circ 58' 14"$.

relative to the cluster centre, are plotted in Fig. 5. The cluster is visible as a density enhancement on top of a uniform background. We have only considered clean detections (with good extraction flags) with more than 5 connected pixels above the background threshold.

Detection limits in general depend on the interplay between scale length/effective radius, magnitude and inclination, i.e. surface brightness. Edge-on galaxies of a certain magnitude are easier to detect than their face-on counterparts. Deep surveys have shown the existence of galaxies with surface brightnesses fainter than the night sky. These low surface brightness (LSB) galaxies are more likely to be missed at a given magnitude and inclination than their high surface brightness counterparts. Most of the LSB galaxies investigated in any detail are either late-type and disk dominated (de Blok et al. 1995; McGaugh & Bothun 1994), or giant, Malin-1-like galaxies (Sprayberry et al. 1995; Pickering et al. 1997).

In order to estimate these effects we generated artificial elliptical galaxies with de Vaucouleurs' law (de Vaucouleurs 1948) light profiles and spiral galaxies with exponential light profiles. We then added these galaxies into empty regions of our Coma images and verified whether SExtractor could recover these using the same selection criteria as for Coma fields. From our simulations we estimate that we are able to detect ellipticals with effective radii $r_e \sim 3 h_{100}^{-1}$ kpc or $r_e \sim 9$ down to $\sim 19.5$, $\sim 19.5$ and $\sim 19$ mag in the $U$, $B$ and $r$ band respectively. Furthermore, we are able to detect dwarf galaxies modelled as exponential disks with $h_d \sim 1$ kpc down to $\sim 19.5$, $\sim 20$ and $\sim 20$ mag or $\mu_0 = 23.8$, 24.3 and 24.3 mag arcsec$^{-2}$ in the $U$, $B$ and $r$ band respectively. At the distance of Coma, $m = 20$ corresponds to $M = -14.2$. Disk dominated LSB galaxies typically have $h_d \sim 3$ kpc and $\mu_{0,B} \sim 23.2$ mag arcsec$^{-2}$. Assuming typical colours as in the de Blok et al. (1995) sample, this corresponds to $\mu_{0,U} \sim 23.1$ and $\mu_{0,r} \sim 22.4$ mag arcsec$^{-2}$. Our simulations show that such LSB galaxies are within our detection limits.

5 TOTAL LUMINOSITY FUNCTIONS

We constructed foreground/background corrected LFs by subtracting counts in the control catalogues from the Coma counts. From Fig. 3 it is obvious that the number of foreground/background

<table>
<thead>
<tr>
<th>Filter</th>
<th>$M^*$</th>
<th>$\alpha$</th>
<th>$\phi^*[h_{100}^2 \text{Mpc}^{-2} \text{mag}^{-1}]$</th>
<th>$\chi^2$</th>
</tr>
</thead>
<tbody>
<tr>
<td>U</td>
<td>-19.39$^{+0.33}_{-0.40}$</td>
<td>-1.54$^{+0.036}_{-0.030}$</td>
<td>11.7 $\pm$ 1.05</td>
<td>27.8</td>
</tr>
<tr>
<td>B</td>
<td>-19.09$^{+0.36}_{-0.40}$</td>
<td>-1.32$^{+0.056}_{-0.049}$</td>
<td>13.7 $\pm$ 0.02</td>
<td>5.35</td>
</tr>
<tr>
<td>r</td>
<td>-20.63$^{+0.26}_{-0.34}$</td>
<td>-1.22$^{+0.034}_{-0.036}$</td>
<td>20.44 $\pm$ 0.48</td>
<td>2.87</td>
</tr>
</tbody>
</table>

Table 4. Best-fitting Schechter parameters for the luminosity functions of the complete sample
counts is a strongly varying function of magnitude. Especially the faintest points of the LFs are largely influenced by an inaccurate determination of the amount of contaminating galaxies. We used very large control fields, and large bin-widths compared to the photometric uncertainties. Therefore, effects caused by errors in the determination of foreground/background counts will be suppressed. Furthermore, we carefully calculated effective areas for all control fields and the Coma mosaic by counting unblotted pixels on each frame. Pixels which reduced the area for object detection, e.g. dead columns, saturated stars etc., were blotted prior to the pixelcounting.

In Fig. 6 the LFs for the complete data set are shown. Solid lines represent best-fitting Schechter functions with parameters as listed in Table 4. The faint end slopes increase towards shorter wavelengths. The best-fitting Schechter functions are rather poor representations of the data for all bands, with several points lying more than $1\sigma$ away from the best-fitting values. The $\chi^2$ statistic confirms the eye’s impression that the LFs for the complete data set cannot be represented by single Schechter functions. These are the first accurate determinations of LFs for such large areas of a cluster. Furthermore, to our knowledge the $U$ band LFs presented here are the first ever published for the Coma cluster.

6 DEPENDENCE OF LUMINOSITY FUNCTIONS ON RADIAL DISTANCE FROM THE CLUSTER CENTRE

In order to study the dependence of the LF on radial distance from the cluster centre we defined five areas as annuli with varying widths and radii projected on the cluster centre, as shown in Fig. 4.
Figure 6. LFs for the total area observed. The solid lines represent best-fitting Schechter functions with parameters as given in Table 4. The dashed lines correspond to the CNOC2 field LFs. $N_{\text{total}}$ gives the estimated number of Coma galaxies up to -15.2.

Figure 7. LFs for area I. Solid lines represent the best-fitting Schechter functions with parameters as listed in Table 5. The insets show the 1, 2 and 3σ contour levels of the best fitting Schechter function parameters. $N_{\text{total}}$ gives the estimated number of Coma galaxies up to -15.2.
Figure 8. LFs for the annuli of Fig. 4. In the top of each figure we indicate: filter, annulus number and estimated number of Coma galaxies up to -15.2.

Table 5. Schechter parameters for the central luminosity functions

<table>
<thead>
<tr>
<th>Filter</th>
<th>$M^*$</th>
<th>$\alpha$</th>
<th>$\phi^* [h_{100}^2 \text{Mpc}^{-2} \text{mag}^{-1}]$</th>
<th>$\chi^2_\nu$</th>
</tr>
</thead>
<tbody>
<tr>
<td>U</td>
<td>-18.60$^{+0.13}_{-0.18}$</td>
<td>-1.32$^{+0.018}_{-0.028}$</td>
<td>135.1 ± 4.3</td>
<td>1.78</td>
</tr>
<tr>
<td>B</td>
<td>-19.79$^{+0.18}_{-0.17}$</td>
<td>-1.37$^{+0.024}_{-0.016}$</td>
<td>61.7 ± 2.4</td>
<td>1.71</td>
</tr>
<tr>
<td>r</td>
<td>-20.87$^{+0.12}_{-0.17}$</td>
<td>-1.16$^{+0.012}_{-0.019}$</td>
<td>130.3 ± 11.6</td>
<td>1.34</td>
</tr>
</tbody>
</table>

For each of these areas we carefully determined the effective area for galaxy detection and constructed the corresponding LFs. The contamination by foreground/background galaxies becomes severe towards the outskirts of the cluster. Their numbers become equal or greater than the Coma counts at $r > 19$, $r > 18$ and $r > 17$ in annulus I, III and IV, respectively.

We arbitrarily defined the core of the Coma cluster as the area with $r < 245 h^{-1}_{100}$ kpc (area I). This is comparable in size to the total observed areas in previous studies. In Fig. 7 we show the central LFs with best-fitting Schechter functions overplotted as solid lines. The insets show the 68, 95 and 99 per cent confidence levels for the $M^*$ and $\alpha$ parameters resulting from the fit to the binned data. The best-fitting parameters are listed in Table 5. The bright end of the $B$ band central LF is not adequately represented by the Schechter function. The faint end, however, is well represented by the Schechter fit. We do not confirm the dip, located at $M_B \sim -17.2$, reported by Biviano et al. (1995). We stress that our LF has been determined with completely different data and methods, complicating any direct comparison of results. Their estimate of the faint end slope ($\alpha_B = -1.3 \pm 0.1$) is, however, in agreement...
with our result. Comparison of our $B$ band LF with the typical richness class 2 composite cluster LF (Trentham 1998b) shows that the faint ends are consistent up to the completeness limit. Beyond the completeness limit the composite LF rises more steeply than the LF we have derived. Our value of the faint end slope of the central $r$ band LF is in agreement with Lugger (1989) ($\alpha_R \sim -1.19 \pm 0.17$), but somewhat shallower than the slopes derived for Coma by e.g. Bernstein et al. (1995), López-Cruz et al. (1997) and Secker et al. (1997) who all find $\alpha_R \sim -1.4$. We stress that a direct comparison is hampered by the fact that these authors use different areas or composite LFs.

In general a single Schechter function is a reasonable representation of all the central LFs with 2 points lying 1σ or more from the best-fitting value for all bands. It is expected from LF studies of composite dense and loose clusters and of single rich and poor clusters that the LF shape depends on environment. Below, we study the change in the shape of the LF as function of position in the cluster. We will examine whether differences can be attributed to effects of the local environment.

In the panels of Fig. 8 the LFs corresponding to the annuli II to $V$ of Fig. 4 are shown for all bands. It is clear that these LFs are not simply scaled versions of the central LFs.

The $U$ band LFs are sensitive to star forming galaxies, and are therefore a poor indicator of the underlying mass distribution. They show significant curvature and at some radii dips, as reported for other bands (e.g. Biviano et al. 1995; Andreon & Pello 1999). Because of these dips these LFs cannot be adequately fitted by single Schechter functions.

The $B$ band LF of annulus II still resembles the central LF, but in annuli III and IV the faint end behaves differently. Even further out, in annulus $V$, the galaxies with $M_B \sim -19$ or brighter become very rare and the faint end seems to steepen again, but only marginally.

The $r$ band LF of annulus II is relatively flat. At larger radial distances from the cluster centre the LFs become much steeper.

We quantified these trends as follows. We fitted a power law function ($b 10^{aM}$) to the faint ends of the LFs in order to study their dependence on radial distance from the cluster centre. The LFs were fitted for $M_U > -18$, $M_B > -19$ and $M_r > -20$, respectively. In Fig. 9 we plot the power law slopes as function of cluster radius. We omitted the slope of the $B$ band LF for area IV: the value of the slope is extremely sensitive to the fitting region, and hence not well constrained. In general, the faint end slopes become steeper towards larger cluster radii.

7 COMPARISON WITH FIELD LUMINOSITY FUNCTIONS

In the field the galaxy density is orders of magnitudes lower than in the cores of clusters like Coma. Galaxies a dense cluster environment are likely to follow different evolutionary paths than galaxies in low density fields. It is therefore interesting to investigate whether this is reflected in their LF shapes. LFs of the field population have recently been measured by a number of surveys (e.g. Loveday et al. 1992; Lin et al. 1996; Lin et al. 1997; Geller et al. 1997; Marzke et al. 1998). Despite the large samples that were used to measure the LFs, controversy on the shape remains. The largest intermediate redshift sample at present is provided by the Canadian Network for Observational Cosmology (CNOC2) Field Galaxy Survey (Lin et al. 1999). The CNOC2 survey has multi-colour $UBVRI$ photometry, whereas most of the older surveys measure LFs only for the $B$ and $R$ bands. The CNOC2 LFs, renormalized and extrapolated to the limiting magnitude of the Coma data, are shown in Fig. 6. In contrast with the Coma LFs, the faint end slopes of the field LFs decrease towards shorter wavelengths. Especially in the $U$ band, this results in a significant excess of faint galaxies in Coma as compared to the field. One must, however, keep in mind that these field LFs have been derived with completely different data and methods. Specifically, the mean redshifts of the field galaxies are larger than the redshift of Coma, complicating the comparison of results.

8 GALAXY DISTRIBUTION

The best indicator of the underlying mass distribution in our data set is the $r$ band, since it is least influenced by episodic star formation. We use this band to investigate the projected galaxy density distributions. Following Driver et al. (1998) we separate our sample into giant and dwarf galaxies. We define giant galaxies as objects with $-23.5 < M_r < -19.5$ and dwarf galaxies as objects with $-19.5 < M_r < -16.5$. In Fig. 10 we plot the projected distributions of these two types on the sky. In panels (a) and (b) of Fig. 11 we plot their foreground/background corrected projected densities and in panel (c) their ratio as function of distance from the cluster centre. In panels (a) and (b) we also show isothermal profiles for comparison. The giant galaxies have a relatively small, sharply defined, area of high overdensity limited to the central cluster area. At a distance of $0.37 h^{-1}_{100}$ Mpc from the cluster centre their density abruptly drops by $\sim 70$ per cent and then decreases continuously. At distances from the cluster centre larger than $0.37 h^{-1}_{100}$ Mpc the dwarf-to-giant ratio (D/G) could become somewhat larger than in the core of the cluster, but this is not significant given the large uncertainties.
Figure 10. (a) Filled hexagons represent galaxies with $-23.5 < M_r < -19.5$ (giants). The 3 large hexagons represent NGC 4889, NGC 4874 and NGC 4839. (b) Crosses represent galaxies with $-19.5 < M_r < -16.5$ (dwarfs). Overplotted are annuli with radii: 0-0.2, 0.2-0.3, 0.3-0.42, 0.42-0.53, 0.53-0.74, 0.74-1.1 and 1.1-1.4 degrees ($1 = 1.22 h^{-1}_{100}$ Mpc at Coma distance).

Figure 11. (a) The number density of dwarf galaxies as function of distance from the cluster centre. (b) The number density of giant galaxies as function of distance from the cluster centre. (c) The dwarf-to-giant ratio (D/G) as function of distance from the cluster centre. The NGC 4839 group is indicated by a square. Dashed lines correspond to isothermal profiles. Horizontal errorbars indicate bin widths.

8.1 NGC 4839 group

It has long been known that at $\sim 40$ south-west of the cluster centre a secondary concentration of galaxies exists (e.g. Wolf 1901). This is the group associated with the cD galaxy NGC 4839. The presence of this group is clearly visible in Fig. 11: the group’s density lies well above the average density at that cluster radius and is comparable to the central densities. We used a circular area of 255 arcmin$^2$ centered on NGC 4839 (Fig. 4) to determine LFs. The LFs, shown in Fig. 12, are found to have different shapes than the central LFs (solid lines). Mobasher & Trentham (1998) have derived a $K$ band LF for the field around NGC 4839. However, due to a small field size (9.9 arcmin$^2$) and large uncertainties in background subtraction, their LF is essentially unconstrained. Lobo et al. (1997) have derived a $V$ band LF with a faint end slope comparable to their central LF, using an area of 117 arcmin$^2$. We find a $B$ band LF which is much shallower than the central LF. The faint end of the $U$ band LF is also flatter, except for the last point. In the $r$ band we have a lack of galaxies fainter than $M_r = -16$, but the faint end slope is comparable to the slope of the central LF.

9 DISCUSSION

In this paper we have used a statistical method to determine in $U$, $B$ and $r$ the LF of the galaxies in the Coma cluster and the dependence of the LF on projected distance from the cluster centre. We did find changes in shape as function of radius indicating changes in the galaxy population in the cluster. At the same time this implies that
comparison with other work is difficult as the LF shape depends critically on the area chosen for study. The changes in the LF shapes are very likely related to the local environment. We will accordingly discuss this possibility in more detail here.

The $\alpha$ parameter of the Schechter function measures effectively the faint end slope of the luminosity distribution and characterizes the intermediate and dwarf galaxy populations. A flat faint end slope implies a lack of these low luminosity galaxies. López-Cruz et al. (1997) observe the trend that steep faint end slopes are detected in poorer clusters and the flatter slopes are, on average, found in richer clusters. This suggests that environmental properties could dictate the faint galaxy population. In a scenario in which mergers, interactions, tidal stripping, destruction of dwarfs, infall etc. play a role we expect to see a lack of faint galaxies towards the regions of higher galaxy density. This then should be reflected in a flattening of the low luminosity end of the LF. We do observe this effect; e.g. the slope of the faint end of the $U$ band LF decreases from $\alpha = 0.20$ at $\sim 0.7 \, h_{100}^{-1}$ Mpc to $\alpha = 0.13$ in the centre. In terms of the slope of the Schechter function these values correspond to $\alpha = -1.5$ and $\alpha = -1.32$. The effect is also present in the $B$ and $r$ band LFs, and measured out to a larger radius of $r = 1.3 \, h_{100}^{-1}$ Mpc.

When comparing the faint end slopes of the Coma LFs with those from CNOC2 the most striking result is that the $r$ band slopes are very similar, while the $B$ and especially the $U$ band slopes of Coma are steeper than in the field. Apparently there is a relation between the relative increase in low luminosity systems in Coma and the colour of the band. A possible interpretation is that the (infalling?) dwarf galaxies in the outerparts of Coma are undergoing bursts of star formation triggered by interactions with neighbour galaxies and/or the intra-cluster medium. As a result the galaxies brighten, preferentially in the $U$ band and, albeit somewhat less, in the $B$ band causing a steepening of the faint end slopes of the LFs. If correct, this is a clear sign that the Coma cluster is not a relaxed system, but that, especially in its periphery, the cluster is still forming and inducing strong evolution to the galaxy population. The flattening of all Coma LFs towards the cluster centre hints that there the galaxies have already lost most of their gas and enhanced star formation has long ceased.

The group around NGC 4839 has been subject of debate in the literature, because it is not clear whether it is falling into the cluster for the first time or has already made one pass through (for scenarios see e.g. Colless & Dunn 1996; White et al. 1993; Burns et al. 1994). Bravo-Alfaro et al. (2000) have done H I imaging of the Coma cluster and the NGC 4839 group. From the nondetections in the close vicinity of NGC 4839 and the presence of several starbursts and post-starburst galaxies with very low H I content in that zone they conclude that it passed at least once through the core. The LF of the field around NGC 4839 has a different faint end slope than the central LFs which could be related to the dynamical history of this group. The observed shape differences could be explained if during the passage a large fraction of the dwarf galaxies has been stripped from the group and redistributed throughout the cluster potential.

To explain the dependence of the shape of the LF on projected distance from the cluster centre we would need much more information. Knowledge of the galaxy morphologies, redshifts, the morphology-density relation (Dressler 1980; Whitmore et al. 1983), the type-dependent LFs, H I observations etc. are necessary to derive a complete scenario in which mergers, tidal stripping, infall etc. play a role. For instance, the observed dips and increasing faint end slopes could be the combined result of Coma’s morphological composition together with the shapes of the type-dependent LFs.

10 SUMMARY AND CONCLUSIONS

We have presented the first results of a wide field photometric survey of the Coma cluster in the $U$, $B$ and $r$ bands. The derivation of the source catalogue, along with the steps concerning the pipeline reduction, have been discussed. Our high quality data provides a
valuable low $z$ comparison sample for studies of galaxy morphology, colour and luminosity at higher $z$.

In this paper we have used the data to study the dependence of the galaxy LF on passband and projected distance from the cluster centre. The LFs of the complete data set cannot be represented by single Schechter functions. The central $U$, $B$ and $r$ band LFs can be represented by Schechter functions with parameters as listed in Table 5. The expectation that the shape of the LF depends on environment is confirmed. The LFs as function of distance from the cluster centre have (very) different shapes than the central LFs and, therefore, no universal general LF exists. The faint ends of the LFs become steeper towards the outskirts of the cluster. A steepening of the faint ends of the LFs towards less dense regions clearly supports the existence of environmental effects. The difference in faint end slopes of the overall LFs and those of the field is colour dependent (strongest in $U$) and can be attributed to enhanced star formation in the dwarf galaxy population in the outer parts of Coma where evolution apparently is still very strong. The LFs of the field around NGC 4839 support the idea that this group has passed through the cluster centre at least once.

We are in the process of creating a catalogue of all spectroscopically confirmed cluster members. This will enable us to revise the Coma LFs and to check the quality of the statistical method to determine LFs. We have also obtained Westerbork Synthesis Radio Telescope (WSRT) H I mosaic data covering an total area of $2.64 \times 1.76$ in order to study the H I properties as function of environment and assess the importance of merging and stripping. Combined with our optical data set this will greatly enhance the ability to study the structure and dynamics of Coma, using a data set that is unrivalled by what is available for any other cluster.

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