CCD drift-scan imaging lunar occultations: a feasible approach for sub-meter class telescopes

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Abstract. A CCD drift-scanning technique for lunar occultation (LO) observations is presented. While this approach has been addressed before by Sturmann (1994) for the case of large telescopes, the technical validity has never been discussed for sub-meter class telescopes. In contrast to Sturmann’s scheme, the proposed technique places the CCD in the image plane of the telescope. This does not represent a problem in the case of small telescopes, where the practical angular resolution attainable by LO is not limited by aperture smoothing. Photon-generated charge is read out at millisecond rate on a column-per-column basis, as the diffraction pattern of the occulted star is being tracked. Two LO events (SAO 79031 and SAO 77911) were observed to demonstrate the feasibility of the method. Data analysis was carried out and no angular diameter the observed stars were resolved. We show, however, that the technique could be useful for close binary detections with small telescopes. A discussion of the limiting resolution and magnitude imposed by our instrumentation is carried out, showing that drift-scanning technique could be extended to 1-2m telescopes for stellar diameter determination purposes. Finally, we point out that the technical demands required by this technique can be easily met by most small professional observatories and advanced amateurs.

Key words. Instrumentation: detectors - Techniques: high angular resolution - Occultations - Stars: fundamental parameters - (Stars:) binaries: general

1. Introduction

Along with eclipses, lunar occultations (hereafter LO) are the oldest astronomical phenomena ever recorded. Since the first high-speed photoelectric observations (Whitford 1939) LO have become one of the highest angular resolution techniques available in visible and infrared astronomy. It provides the opportunity of obtaining milliarcsecond resolution, far beyond the seeing and the diffraction limits of even the largest telescopes. Also note that optical LO is one of the few astronomical observations which can be successfully performed from light-polluted areas, since the natural background of the Moon overcomes any other background source. The purpose of observing such events has changed along centuries: geographical longitude calculation, Earth rotation studies, investigation of close binaries and stellar angular diameters. While timing applications have been largely overcome by atomic clocks and GPS, LO still plays an important role in the direct establishment of fundamental stellar quantities. Tests of stellar atmosphere models via the derived effective temperatures (Richichi et al. 1998) and studies of stellar pulsation and circumstellar shells (Richichi et al. 1988) are just a few examples of them.

In the 1970s, several intensive LO programs were started in the visible (Nather & Evans 1970, Ridgway et al. 1974). Later infrared programs were also initiated (Ridgway 1980, Richichi 1987). The usual detectors for all programs have been high speed photometers, with different photomultiplier technology depending on observing frequency (GaAs for visible and InSb for NIR). For the visible, we call such systems photoelectric photometers (PEP). PEP technical basis is widely documented in the literature (Henden & Kaitchuck 1990).

CCDs have never been used in a routine way for LO observational programs. During the last two decades, technical specifications of CCDs have been constantly improved. Despite this rapid development, most current research grade cameras are still not able to meet read out speed which LO work demands (1 ms sampling time), while operating at low read-out noise (RON) and high digitization resolution mode. The situation in the near-IR domain is
different, with panoramic arrays being used for LO observations thanks to the possibility of implementing fast read-out schemes on subarray sections. An example is the MAGIC camera (Herbst et al. 1993) at the Calar Alto observatory (Richichi 1996). Even in this successful case, the achieved sampling interval time is several times slower than the one achieved by photometers.

Recently, with the advent of adaptative optics (AO), a few expensive state-of-the-art frame transfer imagers have been released for being assembled in wavefront sensor systems (Ragazzoni 1998). These devices can operate above 3Mpixel/sec rates at moderate RON regime, meeting most of LO requirements. While they will play a key role in the near future as a medium-cost solution for fast photometry programs, their cost is currently too high for most professional and high-end amateur astronomers.

In this paper we show how low-cost full-frame CCDs can be considered as an alternative for LO detection, when operated in drift-scanning mode.

In Sect. 2 we state the main observational constraints when observing LO events. In Sect. 3 we compare the traditional observing method based on PEP systems, to the the drift-scan technique with CCDs that we propose. In Sect. 3.3, we present signal-to-noise ratio (hereafter SNR) constraints for LO as an indicator of data quality, and a theoretical estimation of lightcurve SNR for both detector systems is performed. In Sect. 4 we present in detail two observations by the drift-scanning technique. Finally, a brief description of the data analysis procedure is shown in Sect. 5. Results from fits with both an unresolved source and a binary source model are discussed.

2. Limiting angular resolution

As for every astronomical observation, a LO lightcurve is distorted by several non-ideal observing factors, each one having different characteristics. Typically, we can distinguish between two aspects which limit the data quality: instrumental effects and random errors. While the former are usually deterministic and can be removed a posteriori if we have an accurate calibration of our instrumental equipment, the latter is associated with stochastic processes with a (presumably) known noise distribution function.

We can also consider the SNR of the lightcurve as an indicator of achievable angular resolution. Actually, this is the key parameter when evaluating data quality, since it establishes how well deterministic distortions can be restored until their effects vanish into noise fluctuations.

In Sects. 2.1 and 2.2, we outline each one of the two mentioned limits on data quality.

2.1. Instrumental effects

When recording stellar interference fringes of an occulted star, the resolution limit, i.e. the minimum resolvable angle, $\phi_m$, is fixed by several instrumental parameters. In the nearly point-like source domain, three of them apply among others: aperture of the telescope $D$, filter bandwidth, $\Delta \lambda$, and integration time, $\tau$. From Fresnel diffraction pattern and geometry considerations all three effects can be expressed as (Sturmann 1997):

$$\phi_m \cong 0.54(D + v \tau)$$

$$\phi_m \cong 0.158(\Delta \lambda)^{1/2},$$

where $\phi_m$, $D$, $\Delta \lambda$ and $\tau$ are expressed in mas, m, Å and ms, respectively. Finally, $v$ represents the speed of the diffraction pattern in m ms$^{-1}$.

From Eq. 1 we see that large telescopes and long integration times, in spite of increasing SNR, blur high frequency information. This is one of the few cases in which the size of the telescope plays against the observer. On the other hand, with smaller $D$ and shorter $\tau$ the resolution is preserved, but the SNR is decreased, making more difficult the a posteriori removal of instrumental distortions, and restricting observations only to bright stars. For $m_V \leq 5$ stars, this trade-off relation balances to optimal SNR for about 1m telescope and 1ms integration time. For a typical value of $v$ of 0.5m ms$^{-1}$, the above relation yields $\phi_m=0.8$mas.

Since diffraction is a wavelength-dependent phenomenon, polychromatic observations introduce an additional distortion in the lightcurve. As seen in Eq. 2, the magnitude of this effect depends on filter bandwidth. Again, we find a trade-off between $\Delta \lambda$ and recorded SNR, which must be balanced properly. Considering, as in our case, a Johnson R filter ($\Delta \lambda \sim 580$Å) we obtain $\phi_m=3.8$mas.

As stated before, given sufficient SNR it is possible to deconvolve for these deterministic effects on the lightcurve, and achieve angular resolution much smaller than the formal limits of Eqs. 1 and 2.

2.2. Random errors

Depending on the detection technique and the temporal resolution, different noise sources appear. In the particular case of LO work, we should consider the following as dominant.

Firstly, in most astronomical situations, the detection process is Poisson distributed, i.e. the probability of obtaining a realization of intensity $k$ coming from a source of mean flux $\mu$ is given by the Poisson probability:

$$P(k|\mu) = e^{-\mu} \frac{(\mu)^k}{k!}$$

with an uncertainty over every realization $\sigma = \sqrt{\mu}$. It is important to note that Poisson noise, also known as shot noise, is inherent to light nature, and does not depend on detector used.

Secondly, in some detectors, as CCDs, the realization $k$ is read by the electronics of the detector, and a Gaussian RON of zero mean and standard deviation $\sigma_{CCD}$ is intro-
duced. The probability of obtaining a particular realization $m$ from $k$ is

$$P(m|k) = \frac{1}{\sqrt{2\pi}\sigma_{\text{CCD}}} \exp\left[-\frac{(m - k)^2}{2\sigma_{\text{CCD}}^2}\right]$$  

(4)

If, as in the case of CCDs, both processes in Eqs. 3 and 4 are at play, the Poisson+Gaussian compound probability of obtaining a realization $m$ given the mean $\mu$ and all its possible Poisson realizations $k$ is (Núñez & Llacer 1993):

$$P(m|\mu) = \sum_{k=0}^{\infty} \frac{1}{\sqrt{2\pi}\sigma_{\text{CCD}}} \exp\left[-\frac{(m - k)^2}{2\sigma_{\text{CCD}}^2}\right] e^{-\mu} \frac{(\mu)^k}{k!}$$  

(5)

Thirdly, the light wavefront is distorted due to inhomogeneities in the index of refraction $n$. This random fluctuation in $n$ makes recorded intensity vary temporally and spatially. This is normally referred to as scintillation noise. The intensity after scintillation can be approximated as a log-normal distribution:

$$P(m|k) = \frac{1}{\sqrt{2\pi}bm} \exp\left[-\frac{((\ln m - \frac{b^2}{2})^2)}{2b^2}\right]$$  

(6)

with $b = \sqrt{\ln(\sigma_{\text{sc}}^2 + 1)}$, where $\sigma_{\text{sc}}^2$ is the scintillation index, which characterizes the strength of the turbulence.

Likewise the former Poisson+Gaussian case in Eq. 5, the Poisson+Log-normal compound probability of obtaining a realization $m$ given the mean $\mu$ and all its possible Poisson realizations $k$ is:

$$P(m|\mu) = \sum_{k=0}^{\infty} \frac{1}{\sqrt{2\pi}bm} \exp\left[-\frac{((\ln m - \frac{b^2}{2})^2)}{2b^2}\right] e^{-\mu} \frac{(\mu)^k}{k!}$$  

(7)

which, as derived in Sturmann (1997), yields an uncertainty

$$\sigma_m^2 = \sigma_{\text{sc}}^2\bar{m}^2 + \bar{m} + \sigma_{\text{CCD}}^2$$  

(8)

where $\bar{m}$ is the mean number of photons detected in an integration time. We have included the Gaussian contribution from CCD RON accounted by $\sigma_{\text{CCD}}$ in [photons].

The right-hand terms in Eq. 8 are scintillation, Poisson and Gauss noise contributions, respectively. For usual intensity ranges in LO, lightcurve SNR will be marginally affected by CCD readout noise $\sigma_{\text{CCD}}$. If, as usual, turbulence is not negligible ($\sigma_{\text{sc}} \neq 0$), the scintillation factor must be taken into account, becoming dominant in the high intensity regime.

3. Possible approaches for recording LO

3.1. Traditional method - Photoelectric photometers (PEP)

Most LO work at visible wavelengths has been conducted by photoelectric instruments. These devices are usually based on a single thermoelectrically cooled GaAs cell detectors. They are placed at the telescope focal plane. The size of their field of view must be large enough to collect all photons from the seeing-affected stellar image, but at the same time small enough to include as less sky background as possible. One of the more remarkable features of PEP systems is their effective lack of read out noise: they are nearly pure photon counting devices.

3.2. Proposed method - CCD operating in drift scan mode

The conventional use of a CCD device is the operation in stare mode in which the CCD chip is read out at the end of the exposure. Once the shutter is closed, the charge generated by the incident light on the surface of the CCD is converted to digital numbers, in column per column basis, as the clocked charge moves through a serial register. This has been the usual operating mode in astronomy for years.

However, other modes can be considered since the clocking rate $\Delta$ can normally be specified by user. Typically, one has three options: $\Delta = \Delta_0$, $\Delta < \Delta_0$ or $\Delta > \Delta_0$, where $\Delta_0$ is the sidereal rate.

In the first case, the acquired data appear as point-like sources provided clocking charge direction coincides with star motion over chip and telescope tracking system is disconnected. In the second case, in order to record point-like images it is necessary to have the camera properly aligned and to slow down telescope tracking. These two variants in scanning mode are usually referred as drift-scanning and time delay integration (TDI). This is the way several meridian circles (e.g. Stone et al. 1996) and Schmidt cameras (e.g. Sabbey et al. 1998) observe for fast sky coverage at moderate limiting magnitude.

The third case is the one we adopt for observing LOs. $\Delta$ can be chosen according to rate and magnitude of the event to be recorded. The detector does not need to have a specific orientation thanks to the ability to track with the telescope. Thus, the stellar image remains stationary over the chip while photogenerated charge is clocked through the serial register at the desired rate $\Delta$. It is interesting to note that our technique is, in a sense, based on the same principle originally proposed by MacMahon (1908) to observe lunar occultations. In that case, a photographic plate on a revolving cylinder had been considered. Such an observation was performed later by Arnulf (1936).

It is worth noting that a measure of the star flux is actually obtained every time a column is read out. In standard full-frame CCDs this can be done typically at frequencies of 10 to 500kHz, fast enough for LO work. The fact that these CCDs can only readout one column at a time makes temporal sampling non-optimal, and introduces some smearing into LO lightcurve. However, this can be overcome by compressing the image scale in order to image the star over a few pixels.

In addition, as our technique makes use of a CCD, a flatfield calibration could be required. Also, residual image motion over several pixels due to atmospheric turbulence could in principle produce a smearing of the fringes. However, the compression of the image scale, plus the fact
that pixel sensitivity does not significantly change along a small CCD portion, minimize the incidence of this effect.

As SNR plays a key role in data analysis, the choice of a detector with both high QE and low RON is crucial for data quality. From this point of view, CCDs look very attractive in terms of QE compared to PEPs. We see, therefore, how a full-frame CCD could be used for recording a fast photometry event as LOs. This detector, far from being a specialized one, is very common among instrumentation available in all astronomical observatories. Moreover, it turns out to be a low-cost satisfactory solution for sub-meter class telescopes of low-end professional and high-end amateur profile.

3.3. Signal-to-noise ratio evaluation

Eq. 8 should be the expression to use when evaluating SNR for a given detector. However, as the purpose of this paper is to compare the performance of the technique with other classical detectors, we do not include scintillation noise the in SNR estimations described in Sect. 3. This will not bias our conclusions, as atmospheric turbulence affects in the same way both observing approaches.

The SNR for a pure-Poisson detector like PEPs placed in the image plane can be expressed as:

\[ SNR = \frac{N_\lambda}{(N'_\lambda + N_b)\frac{1}{2}} \]

where \( N_\lambda \) and \( N_b \) account for number of photon counts during integration time \( \tau \) due to the star and sky background, respectively. Eq. 9 can be reformulated as Sturrmann (1994):

\[ SNR = \frac{8.9\kappa^{1/2}F_\lambda D^2(D + \nu \tau)^\tau^{1/2}}{(F_bD^2 + F_bb^2)^{1/2}} \]

where \( F_\lambda = \frac{1.10 \times 10^7 \times 10^{-0.4m_\lambda}}{10^{-0.4m_\lambda}} \) and \( F_b = 9.95 \times 10^6 \times 10^{-0.4m_\lambda} \) are the extra-atmospheric average photon fluxes for a star of magnitude \( m_\lambda \) and sky background of magnitude \( m_b \). Both correspond to a temperature \( T = 6000K \) and all expressed in photons \( m^{-2}s^{-1}A^{-1} \) and photons \( s^{-1}A^{-1} \), respectively. The angular extension of the recorded scene projected over the image plane, measured in arcsec, is given by \( b \). Finally, \( \kappa \) stands for the product of detector quantum efficiency (QE) and a weighting function \( g(\lambda) \) correcting flux for atmospheric extinction and optical system absorption. A typical value for \( g \) at \( \lambda = 6500\AA \) is 0.6.

Eq. 10 for the case of CCD turns into:

\[ SNR_{CCD} = \frac{8.9\kappa^{1/2}F_\lambda D^2(D + \nu \tau)^\tau^{1/2}}{(F_bD^2 + F_bb^2 + \sigma_{CCD}^2)^{1/2}} \]

where \( \sigma_{CCD} \) is expressed in photons.

For assessing the theoretical SNR performance between PEPs and CCDs, we consider the following parameters to be input in Eqs. 10 and 11 for either case: \( m_\lambda \sim 4, \nu \sim 0.5m\text{ms}^{-1}, \tau \sim 1\text{ms}, D = 0.36\text{m}, \sigma_{CCD} = 5\text{counts}, b = 4\text{arcsec and } m_b \sim 10 \), which is typical during LO events just beside the Moon. This is close to the observational setting that we present in Sect. 4.

As for the \( QE \) of both detector systems, we adopt from Kristian & Blouke (1982) typical values: \( QE_{PEP} \sim 0.15 \) and \( QE_{CCD} \sim 0.70 \).

The gain \( \eta \) obtained by the use of a CCD is:

\[ \eta = \frac{SNR_{CCD}}{SNR_{PEP}} \sim 2.2 \]

Eq. 12 shows that, in the regime of a moderately bright star, CCDs with high \( QE \) and low \( \sigma \) can perform at least as well as PEPs in LO work. This is less true as we approach fainter stars, where \( \sigma \) is dominant with respect to Poisson noise. However, well before reaching this point the lightcurve SNR becomes so low that it is in any case impossible to deconvolve for instrumental effects (\( D, \Delta \lambda \) and \( \tau \)).

It is also worth remarking that in the case of our proposed technique, it is possible to adjust \textit{a posteriori} the size of the integrating aperture. In the data reduction stage, the user could adapt this size to obtain the optimum SNR depending on the actual image motion and on the brightness of the source. In the case of PEPs, the integrating aperture is fixed and in general this has the disadvantage, especially for faint sources and in the visual range, of introducing a large noise contribution from the background.

Thus, we cannot conclude that CCDs perform in general better LO SNR than PEPs. However, even with non-optimal temporal sampling inherent to the proposed CCD column shifting technique, it is reasonable to consider CCD as potential detector for LO work in moderately bright star regime.

4. Observations

The current paper examines the small-telescope regime. In particular, a Celestron 14 inches Schmidt-Cassegrain telescope (hereafter C14) was used to observe the occultation events reported below. The C14 tube was mounted parallel to the Mailhat double 38cm-astrograph at Fabra Observatory, Barcelona, Spain (see Docobo 1989 and Núñez et al. 1992 for a more specific description of the astrophograph).

Regarding the detector, we employed a Texas Instruments TC-211 CCD, set inside an SBIG ST8 camera as the tracking chip. This is a full-frame front-illuminated CCD with 13.75x16 pixels and a 192x164 pixel format. Being read out through a parallel port, its electronic module can operate at 30 kHz with 12 electrons rms RON. With these technical specifications and its high quantum efficiency (QE peak reaches 70% at both 650nm and 730nm), the TC-211 appears to be suitable for fast imaging purposes, such as tracking and millisecond photometry.

LO data has been acquired by the drift-scanning scheme described in Sect. 3.2. This technique demands
Table 1. Summary of observed occultation events, as reported in Dunham & Warren 1995

<table>
<thead>
<tr>
<th>Source</th>
<th>Date</th>
<th>Filter</th>
<th>(\lambda_0 \pm \Delta\lambda)</th>
<th>(\tau)</th>
<th>(m_V)</th>
<th>CA</th>
<th>PA</th>
<th>Limb vel.</th>
<th>System</th>
<th>Sep.</th>
<th>PA</th>
</tr>
</thead>
<tbody>
<tr>
<td>SAO 77911</td>
<td>13-03-00</td>
<td>R</td>
<td>641(\pm)58</td>
<td>2.344</td>
<td>4.6</td>
<td>34S</td>
<td>146</td>
<td>0.242</td>
<td>5.5</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td>6.3</td>
<td>0.02</td>
<td>178°</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td>6.3°</td>
<td>1.0°</td>
<td>335°</td>
</tr>
<tr>
<td>SAO 79031</td>
<td>14-03-00</td>
<td>R</td>
<td>641(\pm)58</td>
<td>2.067</td>
<td>4.0</td>
<td>63S</td>
<td>123</td>
<td>0.350</td>
<td>4.5</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td>4.5°</td>
<td>0.10°</td>
<td>90°</td>
</tr>
</tbody>
</table>

*a* Uncertain values: see text in Sect. 5.2.

![Fig. 1. Raw image of SAO 79031 occultation at Fabra Observatory. Strip patch spans for 1 second of data record, where every 20-pixel column corresponds to 2.067ms](image)

an accurate relative timing method while reading out on a column by column basis (absolute time reference is not a major concern for stellar diameter determination and binary detection). As the time sampling required for LO is about 1 ms, the timing accuracy should be far below this figure. Accuracies of 1 \(\mu\)s are usually achieved either by using specifically dedicated PC-boards or interrupting CPU internal clock cycle counter. In our case, the latter option was chosen. Both timing and reading out procedure was carried out by a DOS-based program called SCAN\(^1\).

Table 1 summarized the data for two observed occultation events. Columns (1) and (2) report source name and observation date. Columns (3) to (5) correspond to filter name, central wavelength and bandwidth and sampling time. Visual magnitude is detailed at column (6), while columns (7) to (9) report position angle (angle along Moon’s limb scans the star), contact angle (angle between lunar motion and scan direction) and angular rate of the event, respectively. All last three columns are predicted values. Columns (10) to (12) stands for binary system description: magnitudes of the components, angular separation and position angle. We have split the components into different lines.

As an example of strip obtained by the technique described in Sect. 3.2, we show in Fig. 1 the final part of the SAO 79031 occultation. In that case, a 20-pixel column is stored every 2.067 ms on average. It is important to note here that proposed drift-scanning scheme allows us to start observation far before predicted LO occultation time. This gives us more flexibility, since it prevents from eventual errors in such prediction.

In Sects. 5.2 and 5.3 we discuss our results separately for SAO 77911 and SAO 79031 events.

\(^1\) written by Christoph Flohr, available at http://home.t-online.de/home/christoph.flohr/tdi_1e.htm

5. Data analysis and results

5.1. Lightcurve model

The lightcurves were analyzed using a least squares method developed and implemented by Richichi et al. (1992). The complete function proposed in such approach is:

\[
I'(t) = F(t) + \left[ \beta(t) + [1 + \xi(t)] \int \int I^0(t, \bar{x}, \phi) T(\bar{x}) S(\phi) d\bar{x} d\phi \right]
\]

(13)

where \(I^0\) is the diffraction pattern of a point-like star, and \(S\) and \(T\) describe the instrumental effects discussed in Sect. 2.1. The background contribution is considered in \(\beta\). The signal can additionally fluctuate with different temporal frequencies: a low-frequency term is due to atmospheric turbulence and is represented by \(\xi\), and a high-frequency term is due to residual periodic components in the CCD power supply and cooler (hereafter pick-up noise), and is accounted by \(F(t)\).

We computed lightcurves from raw strip images by averaging central pixels of every column and subtracting the background estimated from the outer pixels. This represents an advantage of the proposed technique with respect to lightcurves derived from PEP systems, since it incorporates both source and background level in the recorded signal. In this way, \(\beta(t)\) can be discarded from Eq. 13.

5.2. SAO 77911

\(\chi^2\) Ori (HR 2135, BD+20 1233) is a B2 Ia emission line star. Its angular diameter has been determined by indirect methods three times, with all values smaller than 1mas (Pasinetti-Fracassini et al.2001). As stated in Table 1, this is suspected to be a close binary system, discovered by grazing LO (Reynolds & Povenmire 1975). There is great
uncertainty in the separation of the components derived from that graze, since there were only two rather widely spaced stations. In addition, a tertiary component is catalogued. However, serious doubts about its actual existence have been casted, since if it were really 1.0arcsec apart, it would have been resolved by Hipparcos (Dunham & Bulder 2001b).

The observation was conducted under partially cloudy conditions, and we are confident that the SNR of the resulting lightcurve could have been slightly higher under clear sky. Nevertheless, a visual inspection denotes a clear magnitude drop at the moment of occultation, and reveals at least the principal diffraction fringe. The same occultation event was also observed few minutes before by TIRGO telescope at $\lambda_0=2.2\mu$m.

We performed a binary fit of both Fabra and TIRGO lightcurves, and no evidence of binarity was found in any of them. In order to check the good degree of accordance of SAO 77911 Fabra lightcurve data with single point source model in Eq. 13, we show this in Fig. 2 along lightcurve data, fit and residuals.

5.3. SAO 79031

Mekbuda (HR 2650, zet Gem, BD+20 1687) is a Cepheid variable whose fundamental properties (angular diameter, absolute radius, etc.) have been studied by several authors (see Table 2). It is a multiple system. The brightest component is catalogued in Dunham & Warren (1995) as an occultation double separated by 0′′10. That was derived from a single visual observation made with nearly full Moon (Dunham 2001a). On the other hand, recent observations performed by modern optical interferometers clearly discard such duplicity (Nordgren et al. 2000). Therefore, hereafter we will consider SAO 79031 as a single object.

The data are shown in Fig. 3: at least two first diffraction fringes can be clearly seen. The lightcurve is significantly affected by both scintillation and pick-up noise. In particular, it has been proven that when scintillation is not taken into account in the lightcurve model, the derived angular diameters are biased towards larger values (Knoechel & von der Heide 1978). Our data analysis method, described by Eqn. 13, allowed us to account for both pick-up noise and scintillation. On the other hand, in our particular case with small telescope, stellar diameters could be confidently derived only for very bright and large stars. As shown in Table 2, SAO 79031 appears to have an angular diameter smaller than the limiting angular resolution imposed by our instrumentation ($\phi_m=4.0$ mas with R filter bandwidth). The lightcurve SNR appears to be insufficient to remove such smearing effect.

Thus, as shown in Fig. 3, we have fitted the lightcurve using a single point-source model. Superimposed over the theoretical diffraction curve we have included the 90Hz pick-up noise found in our electrical network. At the bottom, residuals give idea of the behaviour of scintillation component of noise. We consider that, taking into account the modest equipment being used, the fit is in good accordance with the data points.

6. Summary and final remarks

A new approach for observing LO has been described. We demonstrate that CCD drift-scanning at millisecond rate turns to be a viable alternative for LO observations. In our case, given the small telescope used, the SNR appears to be insufficient for deconvolving instrumental smearing at the level required for angular diameter studies, but we estimate that the technique yields enough spatial information for performing binary detection work.
Table 2. Measurements of stellar diameter for SAO 79031

<table>
<thead>
<tr>
<th>$\lambda$ (nm)</th>
<th>$\phi_{UD}$ (mas)</th>
<th>Observational technique</th>
<th>Ref.</th>
</tr>
</thead>
<tbody>
<tr>
<td>2200</td>
<td>1.6±0.5</td>
<td>Lunar occultation (1m telescope)</td>
<td>1</td>
</tr>
<tr>
<td>2170</td>
<td>1.81±0.31</td>
<td>Lunar occultation (4m telescope)</td>
<td>2</td>
</tr>
<tr>
<td>2170</td>
<td>1.66±0.16</td>
<td>Optical interferometry (38m baseline)</td>
<td>3</td>
</tr>
<tr>
<td>1670</td>
<td>1.88±0.86</td>
<td>Lunar occultation (4m telescope)</td>
<td>2</td>
</tr>
<tr>
<td>1650</td>
<td>1.65±0.30</td>
<td>Optical interferometry (104m baseline)</td>
<td>4</td>
</tr>
<tr>
<td>800</td>
<td>1.60±0.05</td>
<td>Optical interferometry (8-31m baseline)</td>
<td>5</td>
</tr>
<tr>
<td>735</td>
<td>1.48±0.08</td>
<td>Optical interferometry (37.5m baseline)</td>
<td>6</td>
</tr>
<tr>
<td>450</td>
<td>1.66±0.05</td>
<td>Optical interferometry (8-31m baseline)</td>
<td>5</td>
</tr>
</tbody>
</table>

1. Ashok et al. 1994
2. Ridgway et al. 1982
4. Lane et al. 2000
5. Mozurkewich et al. 1991

We remark that the proposed technique can be applied to any CCD which supports charge shifting at tunable rate. This can be done in nearly all CCDs of professional profile and in a large number on the amateur market.

In the visible domain, the same technique extended to observations performed with 1-2m telescopes would increase SNR and, therefore, enable to deconvolve most of the smearing caused by filter bandwidth and allow stellar diameter determination.

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