2 Dynamics and Break Time

Dynamics were investigated in (e.g., papers for the 2002 problem solved in the model). The question is now, however, the discussion led (e.g., for instance, for events that bridge the gap between the model and the problem solved). We consider that the limit of the diagram of the evolution is not reached for a given value of the parameter $\theta > 0$. The parameter $\theta$ is defined as range and determines the set of plane points in the plane. The range's different angles vary, and the parameter $\theta$ is defined as range and determines the set of plane points in the plane. The range's different angles vary, and the parameter $\theta$ is defined as range and determines the set of plane points in the plane. The range's different angles vary, and the parameter $\theta$ is defined as range and determines the set of plane points in the plane. The range's different angles vary, and the parameter $\theta$ is defined as range and determines the set of plane points in the plane.
and
\[
\Gamma = \begin{cases} 
\Gamma_0 \left( \frac{\theta}{\theta_0} \right)^{-3/2}, & 0 \leq \theta \leq \theta_0 \\
\Gamma_0 \left( \frac{\theta}{\theta_0} \right)^{-3/8}, & \theta_0 \leq \theta \leq \theta_j, 
\end{cases}
\]
(2)
where \( \theta_0 \) is introduced just for formal reasons to avoid a divergence at \( \theta = 0 \), but can be taken to be smaller than any other angle of interest. A lower limit to this angle is \( \theta_c \geq 1/\Gamma_{\max} \sim 30^\circ \), whereas \( \Gamma_{\max} \sim 30^\circ \) is the maximum value to which the fireball can be accelerated (Piran 1999). The power law index of \( \Gamma, \alpha_\rho \), is not important for the dynamics of the fireball and the computation of the light curve as long as \( \Gamma(t=0, \theta) \equiv \Gamma_0(\theta) > \theta^{-1} \) and \( \Gamma_0(\theta) \gg 1, \theta \). Nevertheless, it plays a role when we want to calculate the fraction of GRBs-afterglow without prompt \( \gamma \)-ray emission, as we discuss in \( \S 6 \).

Consider an observer at the angle \( \theta_j \leq \theta_j \) with respect to the axis of the jet. He measures an isotropic equivalent energy \( E_{\text{iso}} = 4\pi\epsilon(\theta_j) \) from the \( \gamma \)-ray fluence. If also the afterglow emission is dominated by the component pointing the earth, he will infer \( \theta_j = \theta_{\text{obs}} \), the half-opening angle of the jet by means of the break time in the light curve, \( t_b \) (Sari, Piran & Halpern 1999) \( \theta_j \propto t_b^{1/8} (E_{\text{iso}}/n)^{-1/8} \), where \( n \) is the external medium density. Since the total energy inferred from all viewing angles is \( E_{\text{iso}} \approx 2\pi \theta^2 \epsilon = \text{const.} \), the observer will derive the same conclusions obtained by F01 and Panaiteu & Kumar (2001, hereafter PK01) of GRBs as fireballs with the same total kinetic energy but very different jet apertures.

To evaluate how the contributions of the components add to the light curve from the zone with \( \theta \geq \theta_j \) we calculate when their beamed emission include the observer direction, (when \( \theta > \theta_j \leq \theta_\text{obs} \)) and which energy per unit solid angle they have at that time compared to \( \epsilon(\theta_j) \equiv \epsilon_\text{iso} \). We show that under the assumptions of Eq. 1 the afterglow light curve is indeed dominated by the fireball element along the line of sight: neither the "core" of the jet with \( \theta \leq \theta_j \) nor the regions with \( \theta \geq \theta_j \) make substantial contributions.

For an effective though simplified discussion we consider only three components of the jet corresponding to \( \theta = \theta_c < \theta_j \leq \theta_\text{obs} \), \( \theta = \theta_j \leq \theta_\text{obs} \), and \( \theta = \theta_j \gg \theta_\text{obs} \). We call them "core", \( \theta_c \), \( \theta_j \), respectively. This approach is justified by the fact that only the inner parts of the jet with \( \epsilon > \epsilon_\text{iso} \) and the much wider (bil \( \theta_\text{obs} > \theta_j \)) outer parts could contribute and substantially modify the light curve of cone 0. We approximate cone 1 as a relativistic source moving at an angle \( \theta_j \) with respect to the observer, while the observer is approximately considered on the symmetry axis for cones 0 and 3. The cones, that are not causally connected (\( \Gamma_\text{obs} > \theta^{-1} \)), evolve independently and adiabatically in a constant density medium and spread sideways when \( \Gamma \), drops below \( \theta^{-1} \) (Rhoades 1997). We consider relativistic lateral expansion of the cones so that their geometrical angles \( \theta \) grow as \( \theta \sim \theta_j (t = 0) + \frac{t^i}{\theta_j} \). Since the dynamics of the fireball components changes at \( t_b \), also \( \Gamma \) decreases with time differently before and after the break time. For \( t < t_b \)
\[
\Gamma = \begin{cases} 
\Gamma_0 \left( \frac{t_b}{t_b} \right)^{-3/2}, & \text{for } \theta_j \\
\Gamma_0 \left( \frac{t_b}{t_b} \right)^{-3/8}, & \text{for } \theta_j, \text{ and } \theta_j,
\end{cases}
\]
(3)
where \( t_b \) is the deceleration time at which \( \Gamma = \Gamma_0/2 \) and the jet begins to decelerate significantly. From Eq. 3 to Eq. 8 we drop the subscript \( i \) for an easier reading. For \( t > t_b \)
\[
\Gamma = \theta^{-1} \left( \frac{1}{\theta_0} \right)^{-1/2}.
\]
(4)
This on-axis calculation is valid for all \( \theta_j \), because \( \Gamma_j \sim 1/\theta_j \), soon after the break time and the emitting plasma enters the line of sight: from this moment we can consider the observer to be on the cone axis. The lateral expansion starts at a time
\[
t_b = \begin{cases} 
\theta_j^{2/3} t_0^{1/3} t_0^{1/3}, & \text{for } \theta_j \leq \theta_j, \\
\theta_j^{2/3} t_0^{1/3} t_0^{1/3}, & \text{for } \theta_j, \text{ and } \theta_j,
\end{cases}
\]
(5)
where the deceleration time, \( t_d \), depends on
\[
t_d \propto \left\{ \begin{array}{ll}
\epsilon_1 \theta^{-1/3} (1 - \beta \cos \theta_j) & \text{for } \theta_j \\
\epsilon_1 \theta^{2/3} \theta_j^{2/3} \theta_j^{2/3} & \text{for } \theta_j, \text{ and } \theta_j,
\end{array} \right.
\]
(6)
and consequently
\[
R_b \propto \theta^{2/3} \theta_j^{1/3}.
\]
(7)
Therefore from Eq. 1 it follows that \( R_b = \text{constant} \) and
\[
t_b \propto \left\{ \begin{array}{ll}
\theta_j^{2/3} \theta_j^{2/3} \theta_j^{2/3} \theta_j^{2/3} & \text{for } \theta_j \\
\theta_j^{2/3} \theta_j^{2/3} \theta_j^{2/3} \theta_j^{2/3} & \text{for } \theta_j, \text{ and } \theta_j,
\end{array} \right.
\]
(8)
Cones 0 and 3 are hollow but they spread only outwards because the inner components which have already expanded (for cone 3) or are about to do so (for cone 0) have higher pressure. Eq. 8 shows also that when \( \Gamma_j \sim 1/\theta^{-1} \), and the part of the blast generated by the core of the jet becomes visible to the observer, cone 0 has just started spreading. The contribution of region 1 to the light curve of the cone with \( \theta_j \) is not dominant because when \( \Gamma_j \sim \theta_j^{-1} \), the energy per unit solid angle is comparable to \( \epsilon_\text{iso} \).

The regions with \( \theta \gg \theta_j \), spread at later time, so when \( \Gamma_j \sim \theta_j^{-1} \), the energy per solid angle of cone 0 has already decreased with time but it remains always comparable to \( \epsilon_\text{iso} \).

\[
e_j(t_b) = \epsilon_\text{iso} \Gamma_j^2(t_b) = \epsilon_\text{iso} \left( \frac{t_b}{t_{b_0}} \right)^{-1} \epsilon_\text{iso} \left( \frac{t_b}{t_{b_0}} \right)^{-1} = \epsilon_3 \epsilon_0 \)
\]
(9)
where \( t_b_0 \) is the break time for cones \( i \) and we used Eq. 4 and Eq. 8.

Therefore the regions with \( \theta \ll \theta_j \) (or those with \( \theta \) substantially above \( \theta_j \)), don’t determine the overall shape of the light curve, because they are hidden by the dominant emission from the component along the line of sight. In principle, the superposition of many components of energy given by Eq. 9 and 10 may give rise to a sizable contribution. As shown by the more detailed calculation of \( \S 3.2 \) (see Fig 2), this is not the case and the only effect is to delay by a factor of 2 the time of the break. Consequently the energy per unit solid angle that is measured modeling the afterglow is \( \epsilon_\text{iso} \) and the time break depends only on the viewing angle \( \theta_j \).

3 LIGHT CURVE CALCULATION

In order to compute a reasonably accurate light curve in our model, we adopt the following approach. We divide the inhomogeneous jet in \( N \) hollow cones (all but the very central one), each characterized by energy per unit solid angle and Lorentz factor given by Eq. 1. We compute an approximate light curve for each sub-jet using three asymptotic behaviors.
For the cones with $\theta < \theta_0$ and $\theta > \theta_0$, we adopt the $\theta = \theta_0$ and $\theta > \theta_0$ approximations described in § 2. For the cones defined by $\theta_0 - 1/\Gamma < \theta < \theta_0 + 1/\Gamma$ which point towards the observer since the beginning, we again consider the observer along the symmetry axis, but the emission is calculated in a filled cone geometry, instead of the hollow cone adopted for the other cases. For $\theta > \theta_0 - 1/\Gamma$ we use the usual afterglow theory to perform the lightcurve calculations, while for $\theta < \theta_0$ we generalize it for an off-axis observer as explained in the following section.

### 3.1 Radiation from an off-axis homogeneous fireball

Consider a uniform jet with Lorentz factor $\Gamma$ and initial half-aperture $\theta_0$. The radiative process is synchrotron emission (Meszaros & Rees 1997) and we concentrate on the power law branch of the spectrum between the peak, $\nu_\nu$, and the cooling, $\nu_c$, frequencies. The observed flux at a frequency $\nu$, time $t$, and viewing angle $\theta_v$ is

$$F(\nu, t, \theta_v) \propto A_v \Gamma^4 \nu^{-\alpha} \left( \frac{\nu}{\nu_c} \right)^{-\alpha} \delta^3(\Gamma, \theta_v),$$  \hspace{1cm} (11)

where $A_v$ is the emitting area and $\delta = (1 - \beta \cos \theta) \Gamma^{-1}$ is the relativistic Doppler factor, $l'$ is the comoving intensity at the comoving frequency $\nu' = \nu/\delta$ and at the comoving time $t' = \delta t$.

$$l' = l'(\nu'_v, t') \left( \frac{\nu'_v}{\nu_c} \right)^{-\alpha} \Gamma^{4(3-\alpha)} \delta^{(1-\alpha)} \nu^\alpha. \hspace{1cm} (12)$$

Due to the relativistic beaming, the observed flux depends on the observer angle. In particular, if $\theta_v \approx 0$

$$F = F_{\nu0} \simeq \pi \left( \frac{R}{\nu} \right)^2 \nu \left( \frac{\nu}{\nu_c} \right)^{-\alpha} \Gamma^2 \delta^3 (2 \Gamma)^3, \quad \forall \ t \hspace{1cm} (13)$$

while for $\theta_v > \theta_0$

$$F = F_{\nu0} \simeq \left\{ \begin{array}{ll} \pi \left( \frac{R \theta_0}{\nu} \right)^2 \nu \left( \frac{\nu}{\nu_c} \right)^{-\alpha} \Gamma^2 \delta^3 (2 \Gamma)^3 & t < t_h \\ \pi \left( \frac{R \theta_0}{\nu} \right)^2 l' \left( \frac{\nu}{\nu_c} \right)^{-\alpha} \Gamma^2 \delta^3 (2 \Gamma)^3 & t > t_h. \end{array} \right. \hspace{1cm} (14)$$

In this case the jet is initially a source moving at an angle $\theta_0$ with the observer. At the break time $\Gamma \sim \theta_0^{-1}$ and then it starts decreasing very fast (Eq. 3) until $\theta_0 - \theta_0' < \Gamma$ and we can again use the approximation that the jet is viewed on-axis. In the intensity, the change in the slope and the break time of the afterglow depend on the observer viewing angle. In Fig. 1 we show the resulting off-axis lightcurve for a jet with opening angle $\theta_0 = 1^\circ$ as viewed with off-axis angles $\theta_0 = 0, 2, 4$ and 8 degrees. The flat part of the lightcurves corresponds to the time interval between the beginning of the jet spreading and the time in which the jet enters the line of sight. In this time interval our approximations are no longer valid and we simply model the lightcurve with a flat component connecting earlier and later times. This crude approximations is likely responsible for the slight flattening of the final lightcurves (see below and Fig. 2) just before the break.

### 3.2 Inhomogeneous jet

Using Eq. 13 and Eq. 14 we can compute the total light curve as a sum over the fireball components according to the scheme described at the beginning of this section.

$$F(t, \theta_0) = \sum_{\phi} F_{\nu0}(\phi) + \sum_{\phi} F_{\nu0}(\phi) \left[ F_{\nu0}(\phi) - F_{\nu0}(\phi) \right], \hspace{1cm} (15)$$

where $\phi_{\nu0}$ is the inner edge of the cone and $F_{\nu0}(\phi)$ is the light curve for a jet with $\phi(\theta), \Gamma(\theta)$ half-opening angle.
\( \theta_{in} \). N is the number of jet components that are oriented around the line of sight at small times.

The results of this calculation are shown in Fig. 2 for different viewing angles. On top of the solid lines we plot with a dashed line the lightcurve of a homogeneous fireball with \( \epsilon = \epsilon_0 \) and \( \theta_1 = \theta_0 \). This shows that, for \( \theta_1 < \theta_0 \), the lightcurve of an inhomogeneous jet can be successfully modelled with the lightcurve expected for a homogeneous jet: \( F \propto t^{2-2(1-\beta)/3} \) for \( t < t_1 \) and \( F \propto t^{-\beta} \) for \( t > t_1 \).

One of the main simplifications that we made in Eq. 15 is to assume that the observer is on the jet axis of the cones with \( \theta \geq \theta_1 \). The main consequence is to predict a transition between the two power-law branches sharper than what we expect from the exact integration. This is due to the fact that, even in a uniform jet, off-axis observers see smoother transitions (see Fig. 4 of Ghisellini & Lazzati 1999).

4 TIME BREAK-END RELATION

Recently an important observational result on the energetic content of GRBs was published by PK01 and F01. They found an anti-correlation between the isotropic equivalent energy, \( E_{iso} \), and the break time in the afterglow lightcurves. F01 in particular derived \( E_{iso} \) from gamma ray fluences, \( F_\gamma \propto E_{iso} \), and their data are consistent with \( F_\gamma \propto t^{-1} \). They explain it in the framework of collimated, uniform, lateral spreading jets interacting with a constant, low density (0.1 cm\(^{-3}\)) external medium. The observer is postulated to be along the jet axis. They argue that the afterglow emission steepens because at that time the Lorentz factor has dropped to \( \Gamma \sim \theta^{-\gamma} \), so that the on-axis observer sees the edge of the jet and the lateral jet spreading becomes important. In this case \( E_{iso} \propto t^{-1} \) is predicted, which matches observation. They convert the observed break times in jet opening angles through the formulation of Sarı et al. (1999). The \( \gamma \)-ray energy measured and corrected for the inferred geometry of the jet is clustered around \( 5 \times 10^{50} \) erg. They concluded that GRBs central engines release the same amount of energy through jets with very different opening angles. In this framework, then, the wide distributions in kinetic energy per unit solid angle, which spans 3 orders of magnitude, is due only to the distribution of jet solid angles. PK01 obtained the same results, modeling a subset of multivariate afterglows from which they could assign an external density, a time break and an equivalent isotropic energy for the fireball. Both F01 and PK01 found geometric angles that span an order of magnitude but strongly concentrate around \( 2^{\circ} - 4^{\circ} \). In the framework of our model an alternative explanation of the observed relation between \( E_{iso} \) and \( t_1 \) can be found. As discussed in §2 and shown in Fig. 2, we can infer from observations only the properties of the cone pointing towards the observer and not those of the whole jet. So \( E_{iso} = 4 \pi \epsilon_0 \) and using Eq. 8 and Eq. 1 we obtain

\[ E_{iso} \propto \theta^{-2} \propto t_1^{-1}. \]  

Then, the observed distribution of \( E_{iso} \) and its relation with \( t_1 \) is due to an inhomogeneous jet and the possibility to view it from different angles.

5 LUMINOSITY FUNCTION

Under our assumptions, each \( \gamma \)-ray luminosity corresponds to a particular viewing angle. The probability to see a jet between \( \theta \) and \( \theta + d\theta \) is given by

\[ P(\theta)d\theta \propto \sin \theta d\theta \ 0 \leq \theta \leq \theta_1, \]  

(17)

\[ \langle \theta \rangle \approx 0.7 \]  

and the highest probability is for \( \theta = \theta_1 \). Therefore it is highly improbable to see a jet on axis. Consequently we expect more faint GRBs then very luminous ones according to a luminosity function

\[ L(\gamma) \propto 10^{-\gamma}, \]  

(18)

where \( y = \log \epsilon \).

Since there are only a small number of GRBs with observed redshift, the comparison of our predicted luminosity function with data is far from being definitive. Recently Bloom et al. (2001) published an histogram of the bolometric corrected prompt energies for 17 GRBs. The distribution is roughly flat from \( 6 \times 10^{51} \) to \( 2 \times 10^{54} \) erg but as the authors emphasize this analysis applies only to observed GRBs with redshifts and several observational biases obscure the true underlying energy distribution. The main bias that overcasts faint GRBs is the detection threshold of the instruments: this sample is thus flux and not volume limited. Moreover redshift determination encounters more problem for faint GRBs. Based on \( \langle V/V_{\text{max}} \rangle \)-hardness correlation, Schmidt (2001) derived a luminosity function without using any redshift. They had to assume how the comoving GRBs rate varies with redshift and they based their calculations on three star forming rate models. In this case a power-law luminosity function was derived, but flatter than the \( n(L) \propto L^{-2} \) predicted in the simplest version of our model. A luminosity function not based on assumed burst rate evolution can be derived by measuring the burst distance scale through the recently discovered variability-luminosity relation (Fenimore & Ramirez-Ruiz 2000, Reichart et al. 2001). A cumulative analysis of a sample of 239 bursts (Fenimore & Ramirez-Ruiz 2000) yielded a power-law luminosity function \( n(L) \propto L^{-2.5} \), which compare more favorably with our prediction. More recently, Lloyd-Ronning, Fryer & Ramirez-Ruiz (2001) find that the typical luminosity of GRBs evolves with redshift. As a consequence, a flatter power-law index \( n(L) \propto L^{-2.2} \) is obtained. We stress, however, that our deduced luminosity function can be altered by distributions in total energy or geometric angles or by luminosity evolution with redshift. Given the somewhat contradictory observational results discussed above, we conclude that more accurate spectral and fluence measures and a larger sample of bursts are needed for a proper comparison.

6 DISCUSSION AND CONCLUSIONS

We considered inhomogeneous GRB jets with a standard total energy, opening angle and local energy distribution, \( \epsilon \propto \theta^{-2} \). We show that this jet structure can reproduce the observed correlation between isotropic energy and break time. In this model both measurements depend only on the viewing angle because the \( \gamma \)-ray fluence and the afterglow emission are dominated by the components of the jet pointing towards the observer at small times. Since all cones have
the same total energy $E_{\text{tot}} = 2 \pi \theta^2 \epsilon = \text{const}$, we recover the results of F01 and PK01 but the constrains on the geometrical beaming can be relaxed and an appealing more standard structure for all GRBs can be adopted. The jet total energy can be calculated from Eq. 1

$$E_{\text{total}} = 2 \pi \theta^2 \left(1 + 2 \ln \frac{\theta_0}{\theta_0'} \right) = E_{\text{tot}} \left(1 + 2 \ln \frac{\theta_0}{\theta_0'} \right) \quad (10)$$

and compared to $E_{\text{tot}} = 2 \pi \theta^2 \epsilon = 2 \pi \epsilon \theta^2$, the total energy inferred from observation, $E_{\text{tot}} \leq E_{\text{total}}$. To give an example, for a fireball with $\theta_0 = 1^\circ$ and $\theta_0' = 20^\circ$, we have $E_{\text{total}} / E_{\text{tot}} \approx 6$, i.e. the true energy of the fireball can be one order of magnitude larger than what inferred with the models of F01 and PK01.

In addition (§ 5) we can derive the GRBs luminosity function from the probability distribution of the viewing angle and compare it to data. The comparison is, at this stage, still uncertain because more accurate spectral and fluence measures are required to build a volume limited sample and confirm (or rule out) this model.

In any fireball model considering a jet-like GRB structure, a certain number of afterglows without $\gamma$-ray emission (orphan afterglows) is expected. For an homogeneous jet, orphan afterglows are possible only for viewing angles greater than $\theta_0 + 1/\Gamma$. In our jet configuration a fraction of the total area could have a Lorentz factor lower than the minimum $\Gamma$ necessary for $\gamma$-ray radiation. Consequently, considering the same opening angle, an inhomogeneous jet could produce a higher fraction of orphan afterglows than an homogeneous one. This intrinsic fraction depends above all on the $\Gamma$ distribution within the jet (in Eq 2) and on the minimum Lorentz factors to produce $\gamma$-ray radiation and afterglow emission. The observed number of orphan afterglows depends also on flux detection limits, GRB explosion rates with redshift and cosmology. An accurate calculation of the expected orphan afterglow rates is therefore beyond the scope of this paper.

We emphasize that we implicitly assumed the radiation efficiency of the fireball to be weakly dependent on $\Gamma$ or $\epsilon$. This is a plausible assumption in internal-shocks scenario. If it was not the case and the efficiency grew with $\epsilon$, a different relation between $\epsilon$ and $\theta$ should be postulated in order to reproduce observations. In this paper we concentrated for simplicity on a beam profile $\epsilon \propto \theta^{-2}$ which is consistent observational results but it is interesting to briefly discuss other power-law relations $\epsilon \propto \theta^{-\alpha}$ (see Fig. 3). A decay flatter then 2 would cause two breaks in the light curve: the first due to the cone pointing the observer when $\Gamma (\theta_i') = \theta_0^{-1}$ and the second, at later times, when the observer sees the edge of the jet and $\Gamma (\theta_i') = \theta_0^{-1}$. The power law index after the first break is flatter then $t^{-\alpha}$ because the cones with $\theta_i' < \theta < \theta_i$ enter the line of sight with $\epsilon \geq \epsilon_i$ and substantially modify the light curve shape. With a steeper decay in the distribution of $\epsilon$ the time break and the emission after that break would be dominated by the jet along the axis rather then by the very much weaker part directed to the observer. The jet break would then be preceded by a prominent flattening in the lightcurve, especially for $\alpha_i > 3$, difficult to reconcile with observations. In this case we would have $\gamma$-ray emission only for very small angles and the number of orphan afterglows would be much greater then expected from the $\alpha_i = 2$ model. From Eq. 8 we can derive the relation between the index $\alpha_i$ and $\alpha$ (where $E_{\text{tot}} \propto T_{\text{dec}}^{\alpha_i}$). We obtain $\alpha_i = \alpha_i / 2$ for $\alpha_i \geq 2$ and $\alpha_i = 3 \alpha_i / (8 - \alpha_i)$ for $\alpha_i < 2$, when the first break is considered. In Fig. 4 we plot this relation overlaid on the interval in $\alpha_i$ allowed by observations (we used F01 data). We derive $1.5 \lesssim \alpha_i \lesssim 2.2$, at the 1$\sigma$ level. Further $\gamma$-ray and afterglow observations will allow to constrain this parameter much better in the future.

Besides the luminosity function discussed in § 5, there are several ways in which this model can be proved or disproved. First, we have shown that the real total energy of the fireball can easily be an order of magnitude larger than what estimated by PK01 and F01. In this case, after the fireball has slowed down to mild-relativistic and sub-relativistic speed, radio calorimetry (Frail, Waxman & Kulkarni 2000) should allow us to detect the excess energy. In addition, in this model we naturally predict that the more luminous part of the fireball have higher Lorentz factors. This may help
explaining the detected luminosity-variability (Fenimore & Ramirez-Ruiz 2000) and luminosity-lag (Norris, Marani & Bonnell 2000) correlations (Salmonson 2000, Kobayashi, Ryde & MacFadyen 2001; Ramirez-Ruiz & Lloyd-Ronning 2002). Another constraint is given by polarization. Since fireball anisotropy is a basic ingredient of this model, inducing polarization (Ghisellini & Lazzati 1999; see also Sari 1999 and Gruzinov & Waxman 1999). The time evolution of the polarized fraction and of the position angle are however different from a uniform jet (Rossi et al. in preparation). Finally, the properties of the bursts should not depend on the location of the progenitor in the host galaxy, and therefore this model can accommodate the marginal detection of an $F_\nu$-offset relation (Ramirez-Ruiz, Lazzati & Blain 2001) only if a distribution of $\theta_j$ is considered.

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