HD 304373, the second case of 1O/2O double–mode Cepheid in the Galaxy

M. Beltrame¹, E. Poretti²

¹ Università degli Studi, Dipartimento di Fisica, Milano
² Osservatorio Astronomico di Brera, Via Bianchi 46, I-23807 Merate, Italy
e-mail: poretti@merate.mi.astro.it

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Abstract. We report on the discovery of the second case of a galactic Cepheid, ASAS 112843 –5925.7 ≡ HD 304373, pulsating in the the first (1O) and second (2O) radial overtones. The ratio between the periods (0.8058), the short value of the 1O period (0.922405 d) and the shape of the 1O light curve makes HD 304373 very similar to the 1O/2O Cepheids in the Magellanic Clouds. The implications of a so close similarity between a galactic 1O/2O pulsator and LMC ones are discussed in terms of importance of the metallicity effects.

Key words. Methods: data analysis - Stars: oscillations - Cepheids - Techniques: photometric - Stars: individual: HD 304373

1. Introduction

The All Sky Automated Survey (ASAS) is a project started at the beginning of 1996; its ultimate goal is to detect any kind of photometric variability present on a large area of the sky (Pojmański 1997). The aim has been pursued by means of an automated mount equipped with a 716x512 pixel MEADE CCD camera, a 135-mm f/1.8 lens and an I–band filter. The instrument is located at Las Campanas Observatory in Chile and in the first three years it surveyed fifty 2x3 deg² fields. Detailed descriptions of the project, the instrument, the data reduction and analysis can be found in three dedicated papers (Pojmański 1997, 1998 and 2000).

In 2001 we started a careful re-examination of the pulsating stars included in the ASAS catalogue, to find further confirmations of the characteristics of Cepheids with $P < 8$ d, RR Lyr stars and High Amplitude Delta Scuti stars. Such a re-examination can be useful to detect new double–mode radial pulsators, which are among the most elusive variable stars. Their discovery constitutes a continuous observational challenge in the study of stellar oscillations, especially in the Galaxy, where selection effects are very important. From a physical point of view, the period ratio directly allows us to identify the pulsation modes. In turn, the matching of the observed period ratios constitutes a powerful and practical tool to model the interior of stars. Pardo & Poretti (1997) provide a systematic frequency analysis of the available photometry of the galactic double–mode Cepheids. Thirteen stars show the fundamental ($F$) period ($P_0$) and the first overtone ($1O , P_1$) periods, ($P_1/P_0$ between 0.7127 and 0.6968), only one shows the 1O and second (2O, $P_2$) overtone periods (CO Aur, $P_2/P_1=0.8008$). Therefore, after the detection of a large number of double–mode Cepheids in the Magellanic Clouds, it is quite evident that the discovery of new double–mode Cepheids, and in particular new 1O/2O cases, can help to compare Cepheids of our Galaxy with those in other ones.

ASAS 112843 –5925.7 has been classified as a RR Lyr variable with $P=0.9220$ d (Pojmański 2000). The light curve has an amplitude of 0.22 mag in I–band. It looks scattered, but no second periodicity has been suspected during the automatic period search, performed by analysis of variance method (Pojmański 1998). The SIMBAD database identifies ASAS 112843 –5925.7 as HD 304373≡TYC 8629-00990-1 (spectral type F8). TYCHO photometry yields $B_T=11.22±0.06$ and $V_T=10.57±0.05$ (Høg et al. 2000).

2. Data analysis

The original dataset consists of 544 measurements in the I–band. They span about 1000 d, from 1997 April to 2000 January. The first 209 measurements were collected in 40 days in April and May 1997. Later, the survey started again in October 1998 and lasted until January 2000, only
or to characterize the relationship between the detected terms (i.e., \( 2f_1, f_1 + f_2, \ldots \)) locked.

A quick glance to the original dataset was enough to discover the double-mode nature of HD 304373: two terms at \( f_1 = 1.084 \text{ cd}^{-1} \) and \( f_2 = 1.345 \text{ cd}^{-1} \) clearly stand out, but a very high peak appeared at a very low frequency in the subsequent power spectrum. Therefore, we repeated the analysis by subdividing the original datasets into subsets (Tab. 1) as the low-frequency peak suggested the presence of systematic errors. In the first subset we detected not only the \( f_1 \) and \( f_2 \) term, but also \( 2f_1 \) and, more hidden in the noise, \( f_1 + f_2 \). In the second dataset we detected again the \( f_1, 2f_1 \) and \( f_2 \) terms, but also the \( f_1 + f_2 \) and \( 3f_1 \) ones, which are clearly over the noise. In the third dataset we only detected the \( f_1, 2f_1 \) and \( f_2 \) terms. The second and third subsets had the same mean magnitude, while the first one showed a remarkable systematic shift (Tab. 1). Therefore, we built up a homogenous dataset by shifting all the magnitudes of the first subset by \(-0.029 \) mag.

The results of the frequency analysis of such a dataset is shown in Fig. 1. The first power spectrum is dominated by the \( f_1 = 1.0842 \text{ cd}^{-1} \) term and its alias structure. This frequency is coincident with that reported in the ASAS database. The low peak at \( f_2 = 1.3454 \text{ cd}^{-1} \) becomes the highest in the second spectrum. The double-mode nature of HD 304373 is clearly established looking at these two panels. The subsequent analysis detected the \( 2f_1 \) term (left panel in the middle row) and the coupling term \( f_1 + f_2 \) (right panel in the middle row). The presence of the coupling term ruled out the possibility of a binary system composed of two pulsating stars. In the bottom row the signal detection is more complicated. If the \( 3f_1 \) term can be recognized in the fifth panel, the sixth one looks characterized by a bunch of frequencies around integer values of \( \text{cd}^{-1} \). One peak structure is at the sidereal month \( (f = 0.034 \text{ cd}^{-1}) \) and its aliases, reflecting the Full-Moon interference: this spurious peak is quoted by Pojmanski (1998) as a common result in his period search in the ASAS database. Another one is close to the \( f_1 \) value, just at the limit of the frequency resolution. Its presence can be explained pointing out that the amplitude of the \( f_1 \) term results smaller in the third dataset.

Fig. 1. Power spectra of all the ASAS measurements of HD 304373. Each panel shows the spectrum obtained by introducing all the previous identified frequencies as known constituents; this means that the frequency values are considered already determined, but their amplitude and phase values are worked out for each new trial frequency.

3. Least-squares fits and Fourier decomposition

Table 1 reports the parameters of the least-squares fits obtained by means of the formula

\[
I(t) = I_o + \sum A_z \cos[2\pi f_z(t - T_o) + \phi_z]
\]

where \( f_z \) is the generic frequency, which can be an independent frequency (\( f_1 \) and \( f_2 \)), a harmonic (\( 2f_1 \) and \( 3f_1 \)) or the cross coupling term \( f_1 + f_2 \). The fits of the three subsets are reported for comparison purposes: the procedure to identify the terms present in the light curve of HD 304373 is the same used by Pardo & Poretti (1997, see their Tab. 3), but here we failed to build a homogenous dataset owing to the differences in amplitudes. Indeed, the amplitude variation of \( f_1 \) looks big; its instrumental origin is not confirmed by the values of the \( f_2 \) term, which remains constant among the three subsets. Moreover, the amplitude ratio \( R_{21} \) \((0.18 \pm 0.02, 0.22 \pm 0.02\) and \(0.18 \pm 0.04)\) and the phase difference \( \phi_{21} \) \((3.89 \pm 0.20, 3.78 \pm 0.18, 3.62 \pm 0.33)\) rad) of the \( f_1 \) term remain constant. That does not support a beating modulation between two close frequencies as in this case the shape of the \( f_1 \) light curve should vary following the beat phase. Our analysis clearly indicates a sudden decrease of the \( f_1 \) amplitude, but it is not
able to point out the reason precisely. Therefore, we considered the 454 measurements between JD 2450546 and 2451402 as the final dataset, adjusted for the systematic differences.

In order to fit the $f_1$ curve three harmonics are necessary, while the $f_2$ curve does not require any harmonics. Therefore it is possible to calculate the Fourier parameters only in the former case. The values obtained from the final dataset are $\phi_{21} = 3.80 \pm 0.11$ rad, $\phi_{31} = 1.75 \pm 0.23$ rad and $R_{21} = 0.21 \pm 0.02$. Figure 2 shows the light curves of the two periods of HD 304373: the upper curve was obtained by subtracting the $f_2$ and $f_1+f_2$ terms from the measurements, the lower one by subtracting $f_1$, $2f_1$, $3f_1$, $f_1 + f_2$. Note also that the spurious term at $f = 0.034$ cd$^{-1}$ was not removed from the data. When considering it, the least-squares parameters don’t change in a significant way and the residual rms decreases just a little, to 0.019 mag.

4. The double-mode pulsation

Our analysis detected the simultaneous excitation of two modes in the light curve of HD 304373: $P_1 = 0.922405$ d and $P_2 = 0.743241$ d. The resulting ratio, $P_2/P_1 = 0.8058$, is that expected for Cepheids pulsating in the 1O and 2O radial modes. In the Galaxy there was only one similar star so far, i.e., CO Aur ($P_1 = 1.78303$ d, $P_2 = 1.42778$ d, $P_2/P_1 = 0.8008$; Mantegazza 1983).

Figure 3 shows the $P_2/P_1$ ratio as a function of log $P_1$ period (Petersen diagram) for 1O/2O pulsators in the Large (Alcock et al. 1999; Soszyński et al. 2000) and in the Small (Udalski et al. 1999) Magellanic Clouds. The parabolic fit of the LMC stars shown in Fig. 3 is after Soszyński et al. (2000), while the linear fit of the SMC stars has been worked out again. Figure 3 gives evidence that the $P_2/P_1$ values are not well separated in the Magellanic Clouds. It implies that the $P_2/P_1$ ratio is less sensitive than the $P_1/P_0$ ratio to the difference in metallicity between the Magellanic Clouds. Indeed, the $P_1/P_0$ ratio for each galaxy defines three well separated lines in the Petersen diagram (see Fig. 1 in Soszyński et al. 2000).

The $P_2/P_1$ value related to HD 304373 is quite normal for both samples and very similar to that of MACHO*0530:11.7 -69:52:02, a star belonging to the LMC (Fig. 3). Moreover, this ratio cannot be matched by the galactic composition models proposed by Morgan & Welch (1997), while it can be by the SMC and LMC ones. If HD 304373 is a normal Pop. I star, its $P_2/P_1$ value suggests a small dependence on metallicity, as it does not change in a environment as the Milky Way, which is more metallic than the Clouds.

We obtain $<I> = 16.51$ (standard deviation $\pm 0.12$ mag) considering the eleven 1O/2O Cepheids with $0.80 < P_1 < 1.00$ d in the LMC (see Tab. 2 in Soszyński et al. 2000). Assuming $M = 18.5$ for LMC stars, we get $<M_1> = -2.0$ for 1O/2O Cepheids. Therefore, $I = 9.70$ locates HD 304373 at 2.2 Kpc from the Sun. Taking into account the galactic coordinates ($l = 293^\circ$, $b = 2^\circ$), HD 304373 is 77 pc away from the galactic plane. These considerations support the hypothesis that HD 304373 is a disk Pop. I star. Christensen-Dalsgaard & Petersen (1995) pointed out that the matching between the F/1O ratios for galactic pulsators and the theoretical models occurs for metallicities smaller than the solar value of 0.017 - 0.020; if that applies for the 1O/2O pulsators too, a metallicity close to 0.010 allows the $P_2/P_1 = 0.8058$ and $P_1 = 0.922405$ d values to reasonably fit the theoretical models (Christensen-Dalsgaard & Petersen 1995; Morgan & Welch 1997).

Moreover, we notice that the scatter of the $P_2/P_1$ values observed in both Clouds is intrinsic, i.e., originated from slightly different physical conditions inside the stars (it is much larger than the error bars on the period ratios, typically a few units of $10^{-5}$, since the periods are known with high accuracy). Therefore, the weak effect of the metallicity can be masked by other reasons (see also Fig. 4 in Christensen-Dalsgaard & Petersen 1995).

As in the case of CO Aur, there is no significant contribution of the $2f_2$ harmonic in the light curve of HD 304373, i.e., it is perfectly sine-shaped within error bars. This is quite common among the 1O/2O pulsators. On the other hand, the $\phi_{21}$, $\phi_{31}$ and $R_{21}$ values found for the 1O light curve of HD 304373 are in excellent agreement with the values observed in the 1O light curves of 1O/2O pulsators in the Magellanic Clouds.

5. Conclusions

In each class (HADS, RR Lyr and Cepheids) the shortest period stars are typical of metal-poor environments. The more evident cases are the very-short period SX Phe stars observed in globular clusters. HD 304373 has a very
Table 1. Parameters of the least-squares fits of the ASAS measurements on HD 304373. They are divided into two subsets owing to the different mean magnitudes and to the change in the amplitude of the \( f_1 \) term. \( T_0 = \text{HJD} \, 2451026.2671 \)

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<td>( f_1 )</td>
<td>1.084123</td>
<td>0.089</td>
<td>5.82</td>
<td>0.090</td>
<td>5.84</td>
<td>0.067</td>
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<td>\pm 0.000007</td>
<td>± 0.002</td>
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<td>( f_2 )</td>
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<td>0.028</td>
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<td>± 0.000021</td>
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<td>2( f_1 )</td>
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<td>3( f_1 )</td>
<td>0.010</td>
<td>6.12</td>
<td>0.011</td>
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<td>–</td>
<td>0.010</td>
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<td>± 0.002</td>
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<td>( f_1 + f_2 )</td>
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<td>0.019</td>
<td>0.75</td>
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<td>0.008</td>
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<td>± 0.002</td>
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Mean I magnitude 9.734 ± 0.002 9.705 ± 0.001 9.704 ± 0.002 9.705 ± 0.002
Residual r.m.s. [mag] 0.022 0.019 0.019 0.020
N 209 245 90 454

Fig. 3. Period ratios among the 1O/2O pulsators in the Small (crosses) and Large (circles) Magellanic Clouds. Fits are also shown. The filled circles indicate the value observed for the galactic 1O/2O pulsators, HD 304373 and CO Aur.

short fundamental period for a classical Cepheid: assuming \( P_1/P_0 = 0.70 \), we obtain \( P_1 = 1.32 \) d. This result supports the previous discussion, suggesting a low metallicity for HD 304373 and explaining why its \( P_2/P_1 \) value is so similar to that of 1O/2O pulsators in the Magellanic Clouds.

From a methodological point of view, we identified the presence of a peak close to \( f_1 \) as the result of a smaller amplitude in the last observing season. No reasonable physical explanation has been found and its instrumental origin is likely. We also detected the influence of a non perfect sky subtraction or flat-fielding in presence of the Full Moon. It is interesting to note that this instrumental effect makes HD 304373 brighter at the New Moon and fainter at the Full Moon. We stress the importance of checking the homogeneity of the time-series on pulsating stars before processing them.

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