RACETRACK SHAPED MUON STORAGE RINGS FOR A NEUTRINO FACTORY *

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Abstract
20-GeV and 50-GeV lattices have been designed for muon storage rings at Brookhaven National Laboratory (BNL) and Fermi National Accelerator Laboratory (FNAL), respectively. Only recent work on the 20-GeV ring will be discussed in detail here as the 50-GeV ring has been well documented[1]. The 20-GeV designs presented in this paper supplement the lattice developed at BNL for the Feasibility II Study of a Neutrino Factory[2]. The principal difference between these designs is the use of an unconventional type of magnet in the Feasibility II Study design and of conventional magnets in the ones presented here.

1 INTRODUCTION
A planer racetrack geometry was chosen because it maximizes the production efficiency for neutrinos directed to a single detector site. (However, if it is necessary to preserve polarization and to service detectors at two distant sites, the ‘bowtie’ geometry is required.) With a racetrack layout, the entire ring is tilted with the production straight directed downward towards the neutrino detector. Site constraints limit the vertical drop of the ring at the FNAL site and the BNL site to 600’ and <40’, respectively. The tilt angle and the allowed vertical drop determine the length of the major axis of the ring, and, therefore, the relative length of the production straight. In the 50-GeV ring design, which assumes a neutrino source at Fermilab and a detector on the SLAC site, about 40% of the muons that decay produce neutrinos in the production straight. The 20-GeV ring at the Brookhaven Laboratory site, is directed to a detector located in Carlsbad, NM. In order to keep this ring above the water table, the length of the ring, and, likewise, that of the production straight, is limited, so the production efficiency is lower than that of the 50-GeV ring. In order to maximize its efficiency the arcs were made very compact, which motivated the initial adoption of an arc magnet design with skew-quadrupole focusing. As an alternative, the two designs discussed in this paper use conventional magnets, where the magnetic fields have mid-plane symmetry. One design uses combined-function magnets in the arcs, the other one uses separated-function magnets. The combined-function lattice is partly based on that of the 50 GeV Fermilab lattice (although the arcs of that design are separated function).

2 GENERAL
The racetrack design is simple and economical; it contains a downward straight, called the production straight, a return straight pointed towards the surface, and two arcs, together with dispersion suppressors and matching sections. The rings have periodicity one, but have reflection symmetry about the short axis.

The two lattices described in this paper are symmetric, in contrast to the antisymmetric lattice designed at BNL. We now proceed to a more detailed discussion of the two 20 GeV conventional-magnet lattices.

3 ARCS

2.1 Combined Function Ring Arc

The lattice of a full arc is shown in Figure 1. Both of the long straights have zero dispersion. The dispersion in the arcs is suppressed differently on the ends next to the production straight and those next to the return straight. On the return straight side, the two end arc cells have dipoles with half the normal bend angle. On the production straight side, the end cells are normal arc ones and the long matching drift is used to suppress dispersion by correctly positioning a normal-bend (0-gradient) dipole. In Figure 2, the left-hand side of the graph shows the return straight dispersion suppressor and the right-hand side the normal arc end before the combined matching and dispersion suppression section. The parameters of the arc cells are given in Table 1 together with those of the separated-function arc design discussed in the following section.

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2.2 Separated Function Ring Arc

The separated-function arc lattice, composed of sector-shaped, zero-gradient dipoles, is shown in Figure 2 with parameters listed in Table 1.

The dispersion is brought to zero at the ends of each arc by reducing both the length and the bending angle of the two cells at each end by an amount such that the product of length and angle is equal to half that of the central cells of the arc. This method, which was applied by one of the authors for the SSC collider lattice, is designed to suppress the dispersion at the arc ends without significantly reducing the dipole packing efficiency.

To improve the quality of the neutrino beam, a change of the above bending pattern has been included in the design. Specifically, high-divergence neutrinos generated in the upstream matching region of the production straight are diverted from reaching the detector by a bump magnet placed at each end of the production region. Then, in order to preserve zero dispersion in this region, it is necessary to shorten the 5th and 6th dipoles from the left of Figure 2, (2π in phase from the bump magnet).

Table 1. Parameters of the arc cells

<table>
<thead>
<tr>
<th>ARC CELLS</th>
<th>Unit</th>
<th>Combi. function</th>
<th>Separate function</th>
</tr>
</thead>
<tbody>
<tr>
<td>Number per arc</td>
<td>3.5 3</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Cell length</td>
<td>m 6.5</td>
<td>9.69</td>
<td></td>
</tr>
<tr>
<td>Guide Field</td>
<td>T 7.3</td>
<td>7.3</td>
<td></td>
</tr>
<tr>
<td>Intermagnet spacing</td>
<td>m 0.75</td>
<td>0.7</td>
<td></td>
</tr>
<tr>
<td>Dipoles</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Length</td>
<td>m 2.5</td>
<td>2.73</td>
<td></td>
</tr>
<tr>
<td>Strength (k1)</td>
<td>m⁻² 0.024</td>
<td>0</td>
<td></td>
</tr>
<tr>
<td>Quadrupoles</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Length QF / QD</td>
<td>m – 0.70 / 0.77</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Strength</td>
<td>m⁻² – 0.4</td>
<td></td>
<td></td>
</tr>
<tr>
<td>DISP. SUP. CELLS</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Number per arc</td>
<td>2 4</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Dipoles</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Length</td>
<td>m 2.5</td>
<td>1.69</td>
<td></td>
</tr>
<tr>
<td>Strength (k1)</td>
<td>m⁻² 0.024</td>
<td>0</td>
<td></td>
</tr>
<tr>
<td>Quadrupoles</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Length QF / QD</td>
<td>m – 0.97 / 1.01</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Strength</td>
<td>m⁻² – 0.4</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

3 PRODUCTION STRAIGHT SECTION

3.1 Combined Function Ring Production Straight

The straight section, shown in Figure 3, contains the high beta neutrino-production region and two matching regions with parameters described in Table 2.

3.2 Separated Function Ring Production Straight

In the separated-function design, the production region (Figure 4) is magnet free, and the matching sections each contain five quadrupoles. Parameters are given in Table 2.
4 RETURN STRAIGHT SECTION

4.2 Combined Function Ring Return Straight
The return straight shown in Figure 5, contains 20 90° cells. The parameters are shown in Table 2. The return straight section is used for beam injection and extraction, the rf system and phase adjustment. It is made up of periodic cells with quadrupoles and drifts.

4.3 Separated Function Ring Return Straight
Here, the return straight contains 14 90° cells, 9.14-m long. The parameters of these cells are shown in Table 5, and the lattice functions in Figure 4. Two cells at each end are used for matching from the arc cells, three cells on each side of the center of the straight for injection/extraction, and four cells in the center of the straight for a phase trombone.

Table 2. Parameters of the 20-GeV Storage Rings

<table>
<thead>
<tr>
<th>GENERAL</th>
<th>Unit</th>
<th>Comb. Function</th>
<th>Separate Function</th>
</tr>
</thead>
<tbody>
<tr>
<td>Circumference</td>
<td>m</td>
<td>377</td>
<td>376</td>
</tr>
<tr>
<td>Neut. decay fract.</td>
<td>%</td>
<td>28</td>
<td>25</td>
</tr>
<tr>
<td>Length / width</td>
<td>m</td>
<td>166 / 38</td>
<td>166 / 38</td>
</tr>
<tr>
<td>Declination</td>
<td>13°</td>
<td>13°</td>
<td></td>
</tr>
<tr>
<td>Vertical drop</td>
<td>m</td>
<td>38</td>
<td>37</td>
</tr>
<tr>
<td>Normalized emit. *a</td>
<td>m-rad</td>
<td>0.03</td>
<td>0.03</td>
</tr>
<tr>
<td>dp/p (rms) %</td>
<td>1.6</td>
<td>1.6</td>
<td></td>
</tr>
<tr>
<td>*x(max) / y(max)</td>
<td>250/366</td>
<td>125/181</td>
<td></td>
</tr>
<tr>
<td>x / y</td>
<td>6.34 / 6.30</td>
<td>8.18 / 7.28</td>
<td></td>
</tr>
<tr>
<td>x / y</td>
<td>-8/-8</td>
<td>-12/-12</td>
<td></td>
</tr>
</tbody>
</table>

PROD. INSERT

| Match region length | m | 32 | 17 |
| Prod. region length | m | 104 | 94 |
| - *x(max) | m | 250 | 125 |
| Beam Divergence | mr | 0.5 | 0.5 |

RETURN INSERT

| *x(max) / y(max) | m | 10 / 10 | 25 / 28 |

5 REFERENCES
