PSR B 1706−44 and the SNR G 343.1−2.3 as the remnants of a cavity supernova explosion

D.C.-J. Bock and V.V. Gvaramadze

1 Radio Astronomy Laboratory, University of California, Berkeley, CA 94720, USA
2 Sternberg State Astronomical Institute, Moscow State University, Universitetskij Pr. 13, Moscow, 119992, Russia
3 E.K.Kharadze Abastumani Astrophysical Observatory, Georgian Academy of Sciences, A.Kazbegi ave. 2-a, Tbilisi, 380060, Georgia
4 Abdus Salam International Centre for Theoretical Physics, Strada Costiera 11, P.O. Box 586, 34100 Trieste, Italy

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Abstract. The possible association of the supernova remnant (SNR) G 343.1−2.3 with the pulsar PSR B 1706−44 (superposed on the arclike “shell” of the SNR) has been questioned by some authors on the basis of an inconsistency between the implied and measured (scintillation) transverse velocities of the pulsar, the absence of any apparent interaction between the pulsar and the SNR’s “shell”, and some other indirect arguments. We suggest, however, that this association could be real if both objects are the remnants of a supernova (SN) which exploded within a mushroom-like cavity (created by the SN progenitor wind breaking out of the parent molecular cloud). This suggestion implies that the actual shape of the SNR’s shell is similar to that of the well-known SNR VRO 42.05.01 and that the observed bright arc corresponds to the “half” of the SNR located inside the cloud. We report the discovery in archival radio data of an extended ragged radio arc to the southeast of the bright arc which we interpret as the “half” of the SN blast wave expanding in the intercloud medium.


1. Introduction

The pulsar PSR B1706−44 (Johnston et al. 1992) is superposed on an incomplete arc of radio emission (McAdam et al. 1993). McAdam et al. interpreted this arc as a shell-type supernova remnant (SNR), named G 343.1−2.3, and suggested that the SNR is physically associated with PSR B 1706−44. This suggestion was questioned by Frail et al. (1994a) and Nicastro et al. (1996; see, however, Dodson et al. 2001). Usually, a particular claimed pulsar/SNR association is considered reliable if the following five criteria are fulfilled (e.g. Kaspi 1996):

1. agreement of independent distance estimates for pulsar and SNR;
2. agreement of independent age estimates for pulsar and SNR;
3. consistence of the implied pulsar transverse velocity (i.e. the velocity inferred by the displacement of the pulsar from the geometrical centre of the associated SNR) with the measured (proper motion and/or scintillation) velocity;
4. existence of any sign of interaction between the pulsar and the SNR;
5. “correct” (inferred or measured) orientation of the vector of pulsar transverse velocity (it is assumed that this vector should be pointed away from the geometrical centre of the associated SNR).

Although the distance and age estimates for PSR B1706−44 and G 343.1−2.3 are in reasonable agreement, the implied transverse velocity is at least an order of magnitude larger than the scintillation velocity calculated by Nicastro et al. (1996). This inconsistency along with the absence of any apparent interaction between the pulsar and the SNR constitute the two main arguments against the physical association between these two objects (Frail et al. 1994a, Nicastro et al. 1996). The fifth criterion is not applied to the system, since the direction of the pulsar proper motion is still unknown (cf. Giacani et al. 2001 with Frail et al. 1994a; see also Sect. 3.5). Additional (indirect) arguments against the association are based on
We speculate that the wind-blown cavity formed inside the cloud was surrounded by a shell of mass less than some critical value (for spherically-symmetric shells this value is about 50 times the mass of the SN ejecta; e.g. Franco et al. 1991), so that the SN blast wave was able to overrun the shell to propagate further into the unperturbed gas of the cloud, leaving behind the reaccelerated and gradually broadening turbulent shell (Franco et al. 1991). We suggest that the bright arc discovered by McAdam et al. corresponds to the shocked former wind-driven shell and that the diffuse radio emission seen by Frail et al. and Dodson et al. comes from the “half” of the SN blast wave propagating into the cloud (see Fig. 1). These two components correspond to the bright arclike structure in the low resolution image of G 343.1−2.3 (Fig. 2). Under this scenario a more extended component of the SNR should exist to the southeast of the known bright structure. This would correspond to the “half” of the SN blast wave expanding in the inter-cloud medium.

We have found such a feature in the 2.4 GHz Parkes Survey of the Galactic Plane (Duncan et al. 1995; Fig. 2) – an extended arc of diffuse emission stretched from \((l = 345, b = -2.5)\) to \((l = 342, b = -4.5)\). Its location in the “proper” place and its symmetry with respect to the bright arc of G 343.1−2.3 suggest that it could be physically related to this SNR. We note that the ragged appearance of the extended component could result from the development of a Rayleigh-Taylor instability caused by the impact of the SN blast wave with the wall of the

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1 It is believed that the unusual appearance of VRO 42.05.01 is due to the breaking out of the SN blast wave into a hot, low-density tunnel, whose origin is the result of an amalgamation of cavities created by one or more SN explosions or stellar winds (e.g. Pineault et al. 1987). We suggest that an alternative explanation of the origin of SNRs of this type (another example is the SNR G 350.0−3.0) is a SN explosion inside a (mushroom-like) wind-driven cavity created near the edge of a molecular cloud. Numerical simulations of this situation would be highly desirable.
Fig. 1. Schematic of the proposed origin of G 343.1−2.3 (not to scale).

Fig. 2. 2.4 GHz image of G 343.1−2.3 (Duncan et al. 1995). A cross marks the position of the pulsar.

low-density cavity created in the inter-cloud medium by the SN progenitor wind breaking out of the cloud (cf. Gvaramadze 1999a). Note however that Duncan et al. consider this feature to be a part of a larger complex of filaments. The association between the extended arc and the SNR G 343.1−2.3 may be further investigated by detailed Hi mapping in the vicinity of the arc or by combining new continuum interferometric observations with the existing single dish maps of the region.

3. Reliability of the association between the pulsar PSR B 1706−44 and the SNR G 343.1−2.3

We now discuss the criteria for evaluating the reliability of pulsar/SNR associations (Sect. 1) as applied to the system PSR B 1706−44/G 343.1−2.3. It is obvious that the first two criteria should be fulfilled for any proposed pulsar/SNR association. Application of the third and fifth ones for evaluating proposed associations is not so straightforward, since they are based on the assumption that the SN explosion site coincides with the geometrical centre of the SNR. This assumption could be erroneous in the case of a density-stratified interstellar medium (e.g. Lozinskaya 1992, Frail et al. 1994b) or in the case of a cavity SN explosion (Gvaramadze 2002). A mechanical application of these two criteria could result in the rejection of genuine associations (Gvaramadze 2002). The fourth criterion should be considered for those claimed associations where the pulsar is located not far (at least in projection) from the SNR’s shell. To some extent this situation takes place in the case considered in this paper – the pulsar is superposed on the bright radio arc.

3.1. The distance estimates

The most reliable distance estimate for PSR B 1706−44 was derived by Koribalski et al. (1995) using a kinematic method. This estimate ranges from 2.4 ± 0.6 to 3.2 ± 0.4 kpc, in quite reasonable agreement with the dispersion measure distance of 1.8 ± 0.5 kpc derived from the Taylor & Cordes’ (1993) model for the Galactic electron density distribution, given the uncertainties inherent in both methods. The kinematic distance measured by Koribalski et al.
The characteristic age of PSR B1706–44 is \( \tau = P/(n - 1) \tilde{P} \), where \( P \) is the spin period of the pulsar, \( \tilde{P} \) is the period derivative, and \( n \) is the braking index. For \( P = 0.102 \) s, \( \tilde{P} = 9.3 \times 10^{-14} \) s s\(^{-1} \) (Johnston et al. 1992), and assuming that \( n = 3 \), one has \( \tau \approx 17500 \) yr. This age can be compared with the age estimate for G 343.1–2.3 of 5000–6000 yr, derived (McAdam et al. 1993, Nicastro et al. 1996) on the basis of the Sedov-Taylor solution (i.e. from the diameter-age relationship, e.g. Clark & Caswell 1976). But the diameter-age relationship cannot be applied to SNRs originating from cavity SN explosions. In what follows we assume that the true age of the pulsar is equal to \( \tau \) and that the SNR is as old as the pulsar. We realize, however, that the system could be younger (if the pulsar was born with a spin period close to the current one; in this case \( \tau \) overestimates the true age of the pulsar) or older (see Sect. 3.3.1), but the actual age of the system is not fundamental to the results presented in this paper.

3.2. The age estimates

The implied pulsar transverse velocity, i.e. the velocity inferred from the angular displacement of PSR B 1706–44 from the geometrical centre of the bright arc, about 20′ north of the pulsar, is

\[
V_{\text{imp}} \simeq 700 \theta_{20} D_{2.1} \tau_{17.5}^{-1} \ km \ s^{-1},
\]

where \( \theta_{20} \) is the angular displacement in units of 20′, \( D_{2.1} \) is the distance to the pulsar in units of 2.1 kpc, and \( \tau_{17.5} \) is the characteristic age of the pulsar in units of 17.5 kyr. In principle this high transverse velocity is not impossible. It could be even higher if the true age of the pulsar is less than \( \tau \) (see Sect. 3.2). However it can be reduced if one assumes that the true age of the pulsar is much larger than the characteristic one [e.g. due to the low value of the pulsar braking index (e.g. Camilo 1996) or due to a secular (e.g. Blandford & Romani 1988) or short-term (e.g. Gvaramadze 1999b, 2001a) increase of the braking torque]. The implied velocity can also be reduced if the true SN explosion site is offset from the geometrical centre of the SNR. Such offsets naturally arise if the SN exploded in a density-stratified medium (e.g. Lozinskaya 1992, Frail et al. 1994b) or inside a cavity created by the wind of the moving SN progenitor star (Gvaramadze 2002). We favour the last possibility (Sect. 2.2) and suggest that the pulsar transverse velocity could be less than the implied one (see Sect. 3.3.2).

The implied transverse velocity should be compared with the measured one. Nicastro et al. (1996) derived the pulsar velocity from the scintillation measurements and found that it is anomalously low, about twenty times less than \( V_{\text{imp}} \). They used this inconsistency to suggest that the pulsar did not originate from the apparent centre of SNR, and that the pulsar and SNR are not associated. We agree with their first suggestion (see Sect. 2.2) and therefore believe that the implied velocity can be reduced.

On the other hand we have found (Sect. 3.3.2) that if the turbulent material of the reaccelerated former wind-driven shell (the bright arc of SNR G 343.1–2.3) is responsible for nearly all the scattering of PSR B 1706–44, then the pulsar transverse velocity can be as large as the transverse velocity of the portion of the arc projected on the pulsar. If so, one can show that the pulsar (transverse) velocity should indeed be less than \( V_{\text{imp}} \), though it can be much larger than that calculated by Nicastro et al. (1996).

3.3. The pulsar velocity

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3.3.2. The scintillation velocity

It is known that pulsar velocities derived from scintillation measurements show good correlation with proper-motion–derived ones (e.g. Gupta 1995). However, scintillation velocities are derived under several assumptions, some of which are not necessarily suitable for individual pulsars. It is usually assumed that the scattering material is homogeneously distributed along the line of sight and that its transverse velocity is negligible. These assumptions could be erroneous if a considerable fraction of the scintillations is due to a localized region of enhanced scattering existing along the line of sight in addition to the distributed scattering medium and if the transverse velocity of this region is nonzero (e.g. Cordes & Rickett 1998). In this case the scintillation velocity of the pulsar is not equal to the proper motion velocity. In the following we assume that the turbulent material associated with the bright arc of the SNR G 343.1–2.3 is the main scatterer of PSR B 1706–44.

The scintillation velocity for an asymmetrically placed thin scattering screen is (e.g. Gupta 1995):

\[
V_{\text{iss}} = 3.85 \times 10^{4} \left( \frac{\nu_{d,\text{MHz}} D_{\text{pc}} x}{f_{\text{GHz}} t_{d}} \right)^{1/2} \ km \ s^{-1}, \tag{1}
\]

where \( \nu_{d,\text{MHz}} \) and \( t_{d} \) are the scintillation bandwidth and the time-scale measured respectively in MHz and seconds, \( D_{\text{pc}} \) is the distance from observer to pulsar in kpc, \( x = D_{o}/D_{p}, D_{o} \) and \( D_{p} \) are the distances from observer to screen and from screen to pulsar, and \( f_{\text{GHz}} \) is the frequency of observation in units of GHZ. Note that the numerical coefficient in Eq. (1) is about three times larger than that used by Nicastro et al. (1996; see, however, Johnston et al. 1998). With \( \nu_{d,\text{MHz}} = 15, t_{d} = 2287, f_{\text{GHz}} = 1.52 \), and assuming that \( x = 1 \) (Nicastro et al. 1996), one has for
PSR B1706−44 that $V_{\text{iss}} = 62D_{\odot}^{-2.1} \text{ km s}^{-1}$. Although this value is few times larger than that calculated by Nicastro et al. (1996), it is still at the lower limit of the pulsar velocity distribution (e.g. Blaauw & Ramachandran 1998, Lorimer et al. 1997). However, the pulsar velocity estimate can be further increased if one takes into account the transverse velocity of the scattering screen. In the observer’s reference frame the scintillation velocity is connected with the pulsar (transverse or proper motion) velocity $V_p$ by the following relationship (Gvaramadze 2001b; cf. Gupta et al. 1994, Cordes & Rickett 1998):

$$V_{\text{iss}} = \left[ x V_p^2 - 2x(1+x)V_p V_{\text{scr},\|} + (1+x)^2 V_{\text{scr},\|}^2 \right]^{1/2},$$

where $V_{\text{scr},\|}$ and $V_{\text{scr},\perp}$ are the components of the transverse velocity of the screen, correspondingly, parallel and perpendicular to the vector of the pulsar proper motion velocity. In (2) we neglected for simplicity contributions from the differential Galactic rotation and the Earth’s orbital motion around the Sun. If $V_{\text{scr}} = 0$ [as assumed by Nicastro et al. (1996)], one has $V_p = V_{\text{iss}}/x = 62x^{-1/2}D_{\odot}^{-2.1} \text{ km s}^{-1} \approx 0$ (note that $x \approx 100$). But, if $V_{\text{scr}} \neq 0$, one can solve Eq. (2) for $V_p$:

$$V_p \approx V_{\text{scr},\|} \pm \left( V_{\text{iss}}^2/x^2 - V_{\text{scr},\perp}^2 \right)^{1/2}.$$

This solution is physically meaningful only for $V_{\text{scr},\perp} \leq V_{\text{iss}}/x$ ($\approx 0$), i.e. if the pulsar moves in the same direction and with nearly the same (transverse) velocity as does the part of the SNR responsible for the scattering of the pulsar: $V_p \approx V_{\text{scr},\|}$.

Although the existing observational data do not allow us to estimate the expansion velocity of the bright arc, we can constrain it by setting an upper limit on the expansion velocity of the “half” of the SN blast wave propagating inside the cloud. This constraint can be derived from the non-detection of the soft (0.1–2.4 keV) X-ray emission from the SNR. For the column density towards the SN of $\sim 2 - 5 \times 10^{21} \text{ cm}^{-2}$ (Becker et al. 1995), the interstellar medium transmits essentially no X-ray emission with energies below 0.3 keV (e.g. Gorenstein & Tucker 1976), therefore the expansion velocity of the blast wave is less than $\sim 500 \text{ km s}^{-1}$. On the other hand, it is obvious that the former wind-driven shell lagging behind the blast wave (whose angular extent is about two times larger) expands at least two times more slowly. These arguments show that if the bright arc is the main scatterer of the pulsar’s radio emission, then the pulsar transverse velocity should indeed be less than $V_{\text{imp}}$, though it could be as large as 200 km s$^{-1}$.

### 3.4. Interaction between the pulsar and the SNR

We mentioned above that despite the apparent proximity of PSR B1706−44 to the bright arc of the SNR G343.1−2.3 there are no morphological signatures of interaction between these two objects. This has given some authors a basis to question their association (Frail et al. 1994a; see also Nicastro et al. 1996). But this inconsistency can be easily removed if the SN exploded within a mushroom-like wind-driven cavity (Sect. 2.2).

### 3.5. Orientation of the pulsar proper motion vector

The proper motion vectors of neutron stars born in off-centred cavity SN explosions can be oriented arbitrarily with respect to the geometric centres of the associated SNRs (Gvaramadze 2002); they can even be directed towards the geometric centres of the SNRs! In Sect. 3.3 we showed that if the scintillations of PSR B1706−44 are due mostly to the scattering in the turbulent material associated with the bright arc of SNR G343.1−2.3, then the pulsar proper motion should be parallel to the expansion velocity of this material, i.e. the pulsar should move from the northeast to the southwest; this should be tested observationally.

### 3.6. On statistical studies of pulsar/SNR associations

Now we discuss the statistical argument against the association between PSR B1706−44 and the SNR G343.1−2.3 mentioned by Nicastro et al. (1996). This argument is based on the result of a statistical study of pulsar/SNR associations by Gaensler & Johnston (1995), which suggests that young ($< 25,000$ yr) pulsars cannot overrun their parent SNR shells (we recall that the spin-down age of PSR B1706−44 is $\approx 17,500$ yr). Although it is now clear that PSR B1706−44 is located (at least in projection) well within the SNR G343.1−2.3 (Dodson et al. 2001), it should be mentioned that Gaensler & Johnston (1995) did not consider two very important effects: modification of the ambient medium by the ionizing emission and stellar wind of massive stars (the progenitors of most SNe), and the proper motion of SN progenitor stars. Taking into account these two effects allows it to be shown that even a young pulsar moving with a moderate velocity ($\approx 200 \text{ km s}^{-1}$) is able to escape the SNR’s shell, provided that it was born not far from the edge of the wind-driven bubble (Gvaramadze 2002). Alternatively, the apparent location of a pulsar on the edge of a SNR’s shell can be due simply to the effect of projection in non-spherically-symmetric SNRs (see Fig. 1).

### 3.7. On the wind nebula around PSR B1706−44

The large angular extent of the pulsar wind nebula was used by Frail et al. (1994a) to consider an association between the pulsar and the SNR unlikely. Assuming that

2 Perhaps exactly this situation takes place in the case of the pulsar PSR B0656+14, which is moving approximately towards the centre of the SNR Monogem Ring (Thompson & Córdova 1994).
the pulsar moves (with a velocity of 670 km s\(^{-1}\)) through the interstellar medium (of number density 1 cm\(^{-3}\)) and that the pulsar wind nebula is confined by the ram pressure of the ambient medium, they found that the characteristic radius of the nebula, \(r_{\text{PWN}}\), should be about two orders of magnitude less than observed. Based on this argument Frail et al. suggested that G343.1–2.3 could be a background object, while PSR B1706–44 could be a low-velocity pulsar. We agree with their last suggestion, but propose that the pulsar wind nebula is instead confined by the interaction with the hot, tenuous material which fills the interior of the SNR:

\[
\frac{|\dot{E}|}{4\pi c r_{\text{PWN}}^3} \simeq n(2kT + \mu m_H v_p^2),
\]

where \(|\dot{E}| = 3.4 \times 10^{36} \text{ergs s}^{-1}\) is the pulsar spin-down luminosity, \(c\) is the speed of light, \(n\) and \(T\) are, respectively, the number density and the temperature inside the SNR, \(k\) is the Boltzmann constant, \(\mu = 1.3\) is the mean molecular weight, \(m_H\) is the mass of a hydrogen atom, and \(v_p\) is the full (i.e. three-dimensional) pulsar velocity. For \(r_{\text{PWN}} \simeq 0.9 D_{2.1}^{-1} \text{pc}\) and \(v_p \simeq 200 \text{km s}^{-1}\), and assuming that \(T \simeq 10^7 \text{K}\), one has from Eq. (3) a quite reasonable estimate for the number density, \(n = 3.2 \times 10^{-4} \text{cm}^{-3}\). Note that this estimate could be somewhat altered should the pulsar velocity have a significant radial component (a case not constrained by the considerations of this paper). For example, if \(v_p = 500 \text{km s}^{-1}\), then one has \(n = 1.4 \times 10^{-4} \text{cm}^{-3}\) (i.e. also a reasonable value).

4. Conclusion

We have analyzed the available observational data on the pulsar PSR B1706–44 and the SNR G343.1–2.3 and suggested that these objects could be the remnants of a SN which exploded within a mushroom-like cavity created by the SN progenitor wind breaking out of the parent molecular cloud. This accounts for the disparity between the measured and implied velocities of the pulsar. Our suggestion implies that in addition to the known bright “half” of the SNR G343.1–2.3 there should exist a more extended and weaker component, so that the actual shape of G343.1–2.3 is similar to that of the well-known SNR VRO 42.05.01. We have found such a component in archival radio data. Further observations, such as those discussed in Sect. 2.2, would be useful to confirm or reject the association between this component and the SNR G343.1-2.3.

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