Continuum and CO/HCO$^+$ Emission from the Disk Around the T Tauri Star LkCa 15

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ABSTRACT

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We present OVRO Millimeter Array $\lambda = 3.4 - 1.2$ mm dust continuum and spectral line observations of the accretion disk encircling the T Tauri star LkCa 15. The 1.2 mm dust continuum emission is resolved, and gives a minimum diameter of 190 AU and an inclination angle of $57 \pm 5^\circ$. There is a noticeable, but at present poorly constrained, decrease in the continuum spectral slope with frequency that may result from the coupled processes of grain growth and dust settling. Imaging of the fairly intense emission from the lowest rotational transitions of CO, $^{13}$CO and HCO$^+$ reveals a rotating disk substantially larger than that observed in the dust continuum. Emission extends to $\sim 750$ AU and the characteristic radius of the disk is determined to be $\sim 425$ AU (HWHM), based on model fits to the CO velocity field. The measured line ratios demonstrate that the emission from these species is optically thick, while that from C$^{18}$O and H$^{13}$CO$^+$ is optically thin, or nearly so. The disk mass derived from the CO isotopologues with “typical” dense cloud abundances is still nearly two orders of magnitude less than that inferred from the dust emission, the most probable explanation being extensive molecular depletion in the cold, dense disk midplane. Thus, while CO, HCO$^+$ and their isotopologues are excellent tracers of the disk velocity field, they are not reliable tracers of the disk mass.

$N_2H^+$ $1\rightarrow 0$ emission has also been detected which, along with HCO$^+$, sets a lower limit to the fractional ionization of $10^{-8}$ in the near-surface regions of protoplanetary disks. This first detection of $N_2H^+$ in circumstellar disks has also made possible a determination of the $N_2$/CO ratio ($\sim 2$) that is at least an order of magnitude larger than those in the envelopes of young stellar objects and dense clouds. The large $N_2$/CO ratio indicates that our observations probe disk layers in which CO is depleted but some $N_2$ remains in the gas phase. Such differential depletion can lead to large variations in the fractional ionization with height in the outer reaches of circumstellar disks, and may help to explain the relative nitrogen deficiency observed in comets.

Subject headings: stars: individual (LkCa 15) — stars: circumstellar matter — planetary systems: protoplanetary disks — radio lines: stars — ISM: molecules

1. Introduction

LkCa 15, located in the Taurus-Auriga complex at a distance of 140 pc, is rapidly becoming one of the best studied T Tauri stars at millimeter wavelengths. A K5 star with an optical/near-infrared luminosity of $\sim 0.8 \, L_\odot$ (elias78, neuhaeuser95, simond01), LkCa 15 is well isolated from
through far-infrared excess is consistent with the presence of a circumstellar disk (strom89) whose mass and wave interferometric observation to be some $0.024 M_\odot$ and 650 AU, respectively (chiang01, simon01).

Age estimates for LkCa 15 range from 3 Myr (simon01) to 12 Myr (thi01). These timescales are similar to the timescales of other T Tauri stars.

The large size and mass of the disk, combined with the age of LkCa 15, make this an important system for further study since it may represent an important transitional phase in which viscous disk spreading and dispersal competes with planetary formation processes. Further, the outer disk can be studied in detail with existing (sub)millimeter-wave telescopes. Single dish observations have already revealed readily detectable emission from several molecules (vanzadelhoff01, thi01), while aperture synthesis imaging has the potential to shed light on the chemistry of the disk.

Our initial millimeter-wave observations of LkCa 15 have concentrated on species that are typically abundant in dense molecular clouds. Here we present Owens Valley Radio Observatory (OVRO) millimeter array observations of the disk encircling LkCa 15 in dust continuum emission and the lowest rotational transitions of various isotopologues of CO and HCO$^+$. An upper limit to the emission from the $^{13}$CO$^+$ ion is noted. N$_2$H$^+$ was also observed to constrain the fractional ionization and molecular depletion beyond 100 AU. Due to the limited angular extent of the disk, small scale gradients were largely smoothed out by the spatial resolution achieved, and the resultant line intensities should be considered as an “average” over the outer disk. Nevertheless, these interferometric observations suffer from substantially less beam-dilution than those with single telescopes; and this, combined with the inherent stability of cross-correlation measurements, provides a powerful means of studying the weak emission from species such as N$_2$H$^+$ and C$^{18}$O. While arrays under development will provide substantially improved sensitivity and spatial resolution, observations at the ≤ few arcsecond level form the first and necessary step to understanding depletion and ionization within the disks of T Tauri stars. Future publications will present more detailed analyses of these and other data acquired in an extensive millimeter-wave interferometric spectral line survey of LkCa 15 (qi03,kessler03). In what follows, §2 includes a brief overview of the observations, while in §3 we discuss the results and the important effects of gas-phase depletion and fractional ionization on the physical and chemical structure of the disk around LkCa 15. A brief summary of our results and the role of future observations may be found in §4.

2. Observations

All measurements were made between 1997 October and 2000 April using the OVRO Millimeter Array at Big Pine, California. The array consists of six 10.4 meter telescopes with
an rms surface precision of 35 microns. The pointing accuracy is about 4″, except for brief excursions at sunrise and sunset. Combinations of five array configurations were used to map LkCa 15, with antenna spacings ranging from 20 to 400 m east-west and from 25 to 440 m north-south. Cryogenic SIS receivers on each telescope produced average single sideband system temperatures of 450, 1300, and 1200 K at the frequencies of the $^{13}$CO $1\rightarrow0$, CO $1\rightarrow0$, and CO $2\rightarrow1$ lines, respectively. The receivers were tuned for double sideband operation so that both the upper and lower sidebands could be used for molecular line studies.

The receiver IF output is sent over fiber optic transmission lines to a pair of 1 GHz bandwidth analog correlators and a 512 lag digital correlator with four separately configurable modules. Spectral line and continuum measurements are made simultaneously and can be carried out in both the $\lambda = 3$ and 1.3 mm atmospheric windows with a single local oscillator set up. During the $^{13}$CO $1\rightarrow0$ and HCO$^+$ $1\rightarrow0$ observations of LkCa 15, the digital correlator was configured into two bands of $64 \times 0.125$ MHz channels to provide a velocity resolution of 0.17 and 0.21 km s$^{-1}$, while the CO $2\rightarrow1$ measurements were made using $256 \times 0.125$ MHz channels for a velocity resolution of 0.16 km s$^{-1}$.

Calibration of the visibility phases and amplitudes was achieved with observations of the quasars 0528+134 and 0507+179, typically at intervals of 20–30 minutes. Measurements of Uranus, Neptune, 3C 273 and 3C 454.3 provided an absolute scale for the calibration of flux densities. All data were phase- and amplitude-calibrated using the MMA software package, developed specifically for OVRO (scoville93). Continuum and spectral line maps were generated and CLEANed.

### 2.1. Continuum Emission

Figure 1 shows the spectral energy distribution of the continuum emission from LkCa 15. A noticeable, but at present poorly constrained, decrease in the continuum spectral slope with frequency has been found, as discussed further in §3.1. The dust emission is spatially resolved, but only in the highest resolution OVRO 1.2 mm images. The ($u, v$)-plane fits of a two-dimensional gaussian to the highest quality visibilities yield a deconvolved size of $(1.35 \pm 0.12) \times (0.74 \pm 0.06)$ at a position angle (PA) of $66 \pm 5^\circ$, which corresponds to a minimum size of the dust disk of $189 \pm 17$ AU. Assuming the disk is circular, the measured ellipticity indicates an inclination angle of $57 \pm 5^\circ$ ($0^\circ$ being the inclination of a face-on disk). This inclination is somewhat larger than the value obtained by Duvert et al. (2000), $34^\circ$, but smaller than the value of $66^\circ$ obtained by Kitamura et al. (2002) with their NMA 2 mm continuum observations, probably due to differences in the synthesized beams. Nevertheless, it is in good agreement with both the OVRO and Plateau de Bure measurements of the disk properties as traced by CO (simond01).
2.2. CO/HCO$^+$ Observations

Figure 2 shows the integrated intensity and intensity-weighted mean velocity maps of the CO $2\rightarrow1$ emission toward LkCa 15. As shown in the left panel, the molecular gas emission appears much more extended than the dust. Solid grains no doubt exist at similar radii, but are undetectable due to the more rapid fall-off in dust emissivity (Sargent, 1987, Lay, 1997). Conversely, the molecular emission from the innermost region of the disk ($R_{\text{d}}$=30−50AU) is sufficiently beam-diluted even at 1−2'' resolution that no direct information on this size scale can be obtained of the sightvelocity component of the outer disk via Doppler shifts, as is shown by the intensity-weighted mean gas velocity map in Figure 2 (right panel). Molecular gas southwest (SW) of the star is blue-shifted, whereas that to the northeast (NE) is red-shifted, consistent with gas orbiting in a disk inclined with an inclination angle of $i_{\text{disk}}=58^\circ \pm 10^\circ$. The outer Gaussian component has a HWHM of 425 AU and a cut-off radius of 750 AU. These values are in good agreement with optical and infrared photometry (Bouvier, 1995), PdBICO observations (Simon, 2001) and with our resolved 1.2 mm continuum observations. An scan of the 2→1 spectral line maps of LkCa 15. The size of the gas disk is thus well determined both from the image and the spectral data cube, and is much larger than the dust disk size as determined from continuum emission. In what follows, important disk physical properties are fixed at the values derived from the dust (disk mass) and CO (disk size and orientation) emission.

For robust measurements of the abundance and excitation of CO, it is necessary to derive observational estimates of line opacities. These can be obtained by examining a range of transitions and isotopologues. Visibilities from several configurations were therefore combined to examine the $^{13}$CO, C$^{18}$O, HCO$^+$, and N$_2$H$^+$ J=1→0 transitions; results are
presented in Figure 5 and Figure 6. The velocity patterns observed in both $^{13}$CO and HCO$^+$ are entirely consistent with those seen in CO, with red-shifted emission to the NE and blue-shifted emission to the SW. The C$^{18}$O and N$_2$H$^+$ 1$→$0 data cubes have lower signal-to-noise values, and so no velocity analysis was carried out for these transitions. The integrated line intensities and the corresponding column densities for the above transitions were derived with the assumptions of local thermodynamic equilibrium (LTE) and optically thin emission at an excitation temperature of 30 K as presented in Table 1. Only upper limits have been obtained for H$^{13}$CO$^+$.

3. Discussion

3.1. Disk Structure and Grain Properties

Two of the most important global properties of a disk are its mass and temperature distribution. At sufficiently short wavelengths, the entire disk is optically thick, and the density distribution does not affect the emission. At wavelengths longer than about 300 µm, however, the thermal emission from circumstellar disks becomes optically thin. Thus, continuum observations at millimeter wavelengths provide an excellent way to measure disk masses directly via the equation:

$$F_\nu = \int I_\nu d\Omega = \int S_\nu \tau_\nu d\Omega \approx \int \frac{2kT}{\lambda^2} \kappa_\nu \Sigma d\frac{\sigma}{D^2} = \frac{2k < T >}{\lambda^2 D^2} \kappa_\nu M,$$

where $M = \int \Sigma d\sigma$, $F_\nu$ is flux density, $\kappa_\nu$ is the mass opacity, $\Sigma$ is the surface density and $\sigma$ is the surface area of the disk (beckwith s 90). The dust temperatures $T$ are almost always sufficiently high (typical Jeans assumption valid), so the total emission is proportional to a product of the total mass and the average temperature. Theoretically, $\kappa_\nu$ is expected to vary as a power of the frequency $\nu$: $\kappa_\nu = \kappa_0 \left( \frac{\nu}{230 \text{GHz}} \right) ^\beta$. Following Beckwith et al. (1990), we adopt a fiducial value of 0.02 cm$^2$g$^{-1}$ and calculate the total gas mass assuming $M_{\text{gas}}/M_{\text{dust}} = 100$. The disk mass of LkCa 15 is calculated to be $\sim 0.01 M_\odot$.

More detailed constraints for the density and temperature structure can be derived by fitting the spectral energy distributions (SED) of young star/disk systems. Figure 1 shows the flux density as a function of frequency of the millimeter wavelength emission from LkCa 15. Because the continuum and molecular lines were observed simultaneously, the frequencies of the continuum observations at 1.3 and 2.7 mm vary slightly depending on the local oscillator frequency required for the molecular line observations. In Figure 1, the spectral index, $\alpha$, as defined by $F_\nu \approx \nu^\alpha$, is 2.65, consistent with IRAM PdBI observations (duvert g 00). A separate analysis of the data in each atmospheric window, however, suggests that the slope of the
3.51) is considerably steeper than that for the 1.3 mm fluxes ($\alpha = 2.34$), although the error bars are large.

In order to examine this issue further, we compare our OVRO 3.4 – 1.2 mm continuum fluxes with those obtained at 870 $\mu$m and 7 mm by the JCMT and VLA, respectively. The JCMT SCUBA flux lies along a spectral index $\alpha$ of 2.65 with respect to the OVRO data, and so is consistent with the local slope derived from the OVRO 1.3 mm continuum emission measurements. No simple extrapolation of the sub-millimeter data can explain the VLA non-detection at 7 mm (D. Wilner, private communication), which requires $\alpha$ values similar to or even larger than those measured at 3 mm. The coincidence of the 1.3 and 3 mm data observed by Duvert et al. (2000) with the fits to our OVRO data indicate that the observed change in the spectral index at millimeter wavelengths is not likely to be due to errors in flux calibration.

Several physical mechanisms, notably optical depth effects and grain growth, can contribute to the observed behavior. As mentioned above, $\kappa_\nu$ is expected to vary as $\nu^\beta$, where $\beta$ is the opacity index. Assuming optically thin emission in the Rayleigh-Jeans limit, the opacity index $\beta (=\alpha - 2)$ varies from 1.51 to 0.34 for the LkCa 15 disk, while $\beta$ is approximately 2 for dust in the diffuse interstellar medium.

How reasonable is this assumption of optically thin continuum emission? Following Beckwith et al. (1990):

$$\alpha - 2 = \frac{\beta}{1 + \frac{\beta}{(2-q)\ln(\frac{2-pq}{(2-p)\tau})}}$$

where $\frac{\beta}{(2-q)\ln(\frac{2-pq}{(2-p)\tau})}$ is the ratio of optically thick to optically thin emission and depends on the disk structure, $\tau_\nu = \frac{\kappa_\nu M_D}{\cos \theta} \frac{\nu}{R_D^2}$ is the average optical depth at frequency $\nu$, and $M_D$ is the mass of the disk. Given the dust disk radius of 190 AU and an $M_D$ of 0.01 $M_\odot$ (derived above from $F_\nu$), the average optical depth at 230 GHz is $\lesssim 0.03$. Thus, for any reasonable disk density and temperature distribution, the optical depth correction does not appear to be sufficient to explain the observed change in the LkCa 15 spectral index with a single $\beta$.

One means to solve this dilemma is for the mass opacity coefficient $\kappa_\nu$ to decrease by nearly an order of magnitude between 1.2 and 3.4 mm. Recent detailed models of irradiated T Tauri disks, including dust grain growth (dalessio01), conclude that when grains grow from $\mu$m to mm sizes, the mass opacity coefficient $\kappa_\nu$ changes significantly between 1.3 and 3 mm. Indeed, observations of circumstellar disks (beckwith90, mannings94, wilner96) indicate typical values of $\beta = 2$, as opposed to the steeper frequency dependence of $\kappa_\nu$ ($\beta = 2$) found in the general interstellar medium (hildebrand83).

As indicated by chiang01, the disk mass and grain size distribution cannot be uniquely constrained by the very detailed models of irradiated T Tauri disks, including dust grain growth (dalessio01), conclude that when grains grow from $\mu$m to mm sizes, the mass opacity coefficient $\kappa_\nu$ changes significantly between 1.3 and 3 mm. Indeed, observations of circumstellar disks (beckwith90, mannings94, wilner96) indicate typical values of $\beta = 2$, as opposed to the steeper frequency dependence of $\kappa_\nu$ ($\beta = 2$) found in the general interstellar medium (hildebrand83).
\( \mu m \) since the disk intercepts less stellar radiation. Dust settling can help explain the relative paucity of large disks to which the powerful technique of scattered light coronography can be applied and specifically the lack of any detectable reflection nebulosity in HST WFPC2GTO observations of LkCa 15 (krist97). Thus, the most likely explanation for the observed change in the spectral indices

3.2. Radiative Transfer and Molecular Line Emission

The observed line intensities in circumstellar disks are a complex function of the physical structure of the disk and of the line/continuum optical depth. If we assume that circumstellar disk abundances are similar to those found in dark clouds, the emission lines from parent isotopologues of common species such as CO, HCO\(^+\), HCN, etc., should be highly optically thick. Our observed ratios of \(^{12}\)CO/\(^{13}\)CO emission reveal that \(^{12}\)CO is indeed optically thick, but say little about \(^{13}\)CO. Several LkCa 15 transits were therefore devoted to a local oscillator setting containing the \(^{18}\)O \(J=1 \rightarrow 0\) transition, the results of which are presented in Figure 5. The observed beam-matched flux density ratio is 5, only somewhat lower than the isotope ratio \([^{13}\text{C}]/[^{18}\text{O}]\) of 8.3. The \(^{13}\)CO \(J=1 \rightarrow 0\) transition is therefore only somewhat optically thick, and that of \(^{18}\)O is optically thin, and should therefore provide a more reliable estimate of the disk mass, provided it remains in the gas phase. van Zadelhoff et al. (2001) indicate that, for standard HCO\(^+\) abundances, the \(1 \rightarrow 0\) line is again optically thick in the outer layers, whereas that of H\(^{13}\)CO\(^+\) is close to being optically thin throughout the disk. Further, the low-J HCO\(^+\) lines are predicted to probe densities of order \(10^5 - 10^6 \text{ cm}^{-3}\), below the critical density of the \(4 \rightarrow 3\) transition (so that LTE cannot be safely assumed). For H\(^{13}\)CO\(^+\), the populations will be closer to thermal equilibrium because its emission arises primarily from regions with densities of \(10^7 - 10^8 \text{ cm}^{-3}\) (vanzadelhoff01). Parent isotopologues are therefore likely to be optically thick for many species in disks.

The observations described above indicate the need for detailed calculation of disk radiative transfer. Furthermore, the complex geometry within the disk demands that flexible and efficient radiative transfer techniques be utilized, and of the many techniques available the Monte Carlo approach has shown great promise (choi95). Since Monte Carlo techniques utilize integration over one-dimensional (1D) and two-dimensional (2D) Monte Carlo treatments of the line radiative transfer based on the homogeneous layer passive disk models outlined above have now begun to appear (hogerheijde00, vanzadelhoff01). In 2D implementations are necessary to quantitatively treat inclined disks. For this reason we have used an accelerated 2D Monte Carlo model (hogerheijde00) to examine the radiative transfer and disk mass. In this model, we assume spherical, compact dust grains with a power law size distribution with a mass of \(1 M_\odot \text{ yr}^{-1}\), with the inner radius of the disk set at 5 AU and the outer radius at 425 AU, which is consistent with that derived above for LkCa 15. The inclination (58 degrees)
and turbulent velocity width (0.1 km s\(^{-1}\)) are found by fitting the observed CO 2→1 line profile with the model spectrum, using \(N_{\text{CO}}=10^{-4}N_{\text{H}}\)\(^6\) as shown in Figure 3. For each transition observed, a suite of models with the parameters described above were created, but with the molecular abundances relative to hydrogen varied until a match with the observed integrated line intensity was obtained. Integrated intensity is a useful quantity for comparison because the column density is approximately constant as a function of radius (Willacy00, Aikawa99) at the larger radii \(r>50\text{AU}\) to which we are sensitive with the OVRO millimeter array.

The resulting column densities are shown in Table 1. The column densities calculated using this non-LTE radiative transfer model are 1-2 orders of magnitude larger than those calculated in the Willacy & Langer (2000) models of disk chemistry, but consistent with those calculated by Aikawa et al. (2002) – except that \(N_2\text{H}^+\) is an order of magnitude larger than the model prediction. As indicated in the last column of Table 1, for CO 2→1, \(^{13}\text{CO}\) 1→0, HCO\(^+\) 1→0 and \(N_2\text{H}^+\) 1→0 emission the column densities are smaller when calculated using the LTE assumption. This is due to the fact that the emission from these transitions is optically thick (see discussion above). The LTE calculations assume that the gas is optically thin and that the entire disk is being probed by observation of this line emission and thus result in an underestimation of the total amount of CO, HCO\(^+\) and \(N_2\text{H}^+\) present. In the case of the \(^{18}\text{O}\) 1→0 and H\(^{13}\text{CO}\)\(^+\) 1→0 emission, which are believed to be optically thin, and for the conditions in the near-surface regions of disks beyond 50 AU, the column densities are overestimated when thermal equilibrium is assumed. This supports the conclusion that conditions in the emitting region are not at LTE, and that both radiative and collisional processes play a part in the excitation. The population of higher energy rotational states is thus much lower than would be the case if collisions were dominant; and the assumption of thermal equilibrium therefore results in an overestimation of the population of the upper states and thus in the total column density, which at LTE is directly proportional to the density of the upper state.

Both the results presented above and observations of high-J transitions of CO, HCO\(^+\), and HCN toward LkCa 15 by van Zadelhoff et al. (2001) suggest that the molecular emission from the major isotopologues is optically thick and that the inferred densities in the region are not sufficient to thermalize all transitions. The line ratios presented in van Zadelhoff et al. (2001) further indicate temperatures and densities typically associated with warm layers lying above the disk midplane. Additionally, if we ignore depletion of gas phase species onto grains, and assume cosmic fractional abundances for CO \((10^{-5}–10^{-4} N_{\text{H}})\) and hydrogen

\(^6\)This model assumes that CO and H\(_2\) have similar radial and vertical distributions. Chemical models (i.e. Aikawa et al. (2002)) indicate that this is not strictly the case, and variations in the vertical distribution of CO will be explored in future work.
column densities of $10^{23}$ cm$^{-2}$, the resulting CO column density is an order of magnitude greater than that observed here ($10^{18}$ cm$^{-2}$). Thus, for any disk in which the gas and dust are well mixed and there is no depletion, even species such as C$^{18}$O are predicted to be optically thick at molecular cloud abundances. The low column densities derived here and the high-$J$/low-$J$ line ratios therefore indicate that the disk midplane (heights below several tens AU) is not being probed by the observed emission and that the column densities presented in Table 1 are only applicable to the warm layers of the disk.

3.3. Ionization Balance

The theory of the ionization balance in molecular clouds and the relevant ion-molecule chemistry has been widely used for determinations of the electron abundances in dense clouds (langer85). Theoretical chemical models indicate that ion-molecule reactions are also efficient in the outer regions of protoplanetary disks (aikawa98). Photoionization, cosmic ray ionization, and possibly X-ray ionization of H$_2$ rapidly lead to the formation of H$_3^+$, the pivotal species in ion-molecule models of molecular cloud chemistry. The low proton affinity of H$_2$ ensures that H$_3^+$, which has no rotational spectrum, will undergo proton transfer reactions with abundant neutral species such as CO and N$_2$. In disks, gaseous CO and N$_2$ exist in regions well removed from the midplane, where the temperature warms enough for sublimation of these molecules ($T \approx 20$-30 K). The isoelectronic ions HCO$^+$ and N$_2$H$^+$ were observed here and can therefore be used to estimate the fractional ionization in the warm layer of the LkCa 15 disk.

The volume density in the emitting region can be constrained from line ratios obtained from the results presented here and previous single dish observations of molecules with high dipole moments (e.g. HCO$^+$, HCN). An LVG analysis for LkCa 15, performed by van Zadelhoff et al. (2001), indicates that the lines arise from regions with $n_{H_2} \sim 10^5$-$10^7$ cm$^{-3}$. We use $10^6$ cm$^{-3}$ as the number density of H$_2$ in the calculations below, which is also the number density at a height of ~150 AU and a radius of 350 AU in the D’Alessio disk model. The mean kinetic temperatures are less well constrained, but the analysis of multiple transitions of CO (van Zadelhoff et al. 2001) suggests that $T_{kin} \sim 20$-40 K for LkCa 15. We therefore adopt a single kinetic temperature of 30 K. Also, for the reasons discussed in §3.2, we use the column densities resulting from the non-LTE radiative transfer model summarized in Table 1 for all observed species. Because H$_2$ cannot be observed directly at millimeter wavelengths, the column density is highly model dependent. Typical values vary from $10^{23}$ to $10^{24}$ cm$^{-2}$ for R~300 AU, the distance corresponding to the typical beam size of our observations. van Zadelhoff et al. (2001) investigate the level of molecular depletion by statistical equilibrium calculations as compared to the gas column densities predicted by
dust continuum observations, and find depletion by a factor of 3–40 for CO in the disk of LkCa 15. We therefore adopt $10^{-5}$ as the fractional abundance of CO, by assuming depletion by a factor of 10 from the nominal value of $f$(CO) in molecular clouds. In our calculations we also assume that the warm layers in the disk are in local (chemical) equilibrium and that the abundances of CO, HCO$^+$ and N$_2$H$^+$ peak within these layers (Aikawa et al. 2002), although the vertical distributions of these species are not identical [cf. Figure 4 of van Zadelhoff et al. (2003) and Figures 4 and 5 of Willacy & Langer (2000)].

To simplify the calculations presented here, we first consider only the ionization balance determined by HCO$^+$, H$_3^+$, N$_2$H$^+$ and electrons in steady state, for which

$$k_1[H_3^+][CO] = k_e(HCO^+)[HCO^+][e] - k_2[N_2H^+][CO]$$

(3)

$$k_e(H_3^+)[H_3^+][e] + k_3[N_2][H_3^+] + k_1[H_3^+][CO] = \frac{\zeta}{n(H_2)}$$

(4)

$$k_3[N_2][H_3^+] = k_2[N_2H^+][CO] + k_e(N_2H^+)[N_2H^+][e]$$

(5)

where $k_e(H_3^+) = 1.15 \times 10^{-7} \left(\frac{T}{300}\right)^{-0.65}$ cm$^3$s$^{-1}$, $k_e(HCO^+) = 2.0 \times 10^{-7} \left(\frac{T}{300}\right)^{-0.75}$ cm$^3$s$^{-1}$ and $k_e(N_2H^+) = 1.7 \times 10^{-7} \left(\frac{T}{300}\right)^{-0.9}$ cm$^3$s$^{-1}$ are the dissociative recombination rate coefficients of H$_3^+$, HCO$^+$ and N$_2$H$^+$, $k_1 = 6.56 \times 10^{-10} \left(\frac{T}{300}\right)^{-0.5}$ cm$^3$s$^{-1}$ and $k_2 = 8.8 \times 10^{-10}$ cm$^3$s$^{-1}$ are the reaction rate coefficients of CO with H$_3^+$ and N$_2$H$^+$, respectively, $k_3 = 1.8 \times 10^{-9}$ is the rate coefficient for the reaction $N_2 + H_3^+ \rightarrow N_2H^+ + H_2$ (all rate coefficients have been adopted from the UMIST database for astrochemistry (millar97)), and the bracket $[]$ represents the fractional abundance of the species and $\zeta$ the ionization rate due to cosmic rays, X-rays, and UV radiation.

A lower limit to the electron fraction follows directly from the observed HCO$^+$ and N$_2$H$^+$ column densities, but can also be obtained more “locally” by noting that the right side of equation 3 must be larger than 0, or:

$$\frac{[e]}{[CO]} \geq \frac{k_2[N_2H^+]}{k_e(HCO^+)[HCO^+]} \sim 1 \times 10^{-3}$$

(6)

The lower limit of the fractional ionization $[e]$ is therefore $\geq 10^{-8}$, given $[CO] \sim 10^{-5}$, in the near-surface region of the disk. This value is fairly high compared to that of cold, dark clouds at $n_{H_2} \sim 10^6$ cm$^{-3}$ where for example, Caselli et al. (2002) obtained fractional ionization of $10^{-9}$ in the center of L1544, and we note that the ionization fraction in
LkCa 15 may be enhanced relative to other T Tauri stars. The ROSAT All-Sky Survey of young stars in Taurus (neuhaeuser, 1995) shows that the probability of the existence of an X-ray source for LkCa 15 is 98% and the upper limit for its X-ray luminosity is $4.1 \times 10^{29}$ ergs$^{-1}$. Ionization from the resulting high-energy radiation may have important effects on the disk (feigelson, 1999). The high HCO$^+$ abundance and CN/HCN ratio observed (Qi, Kessler & Blake, 2003) indicate that LkCa 15 could possess similar chemistry to the intense X-ray source TW Hya, another Sun-like star with strong molecular emission from its attendant disk (kastner, 1997).

Understanding the ionization rate near the disk surface is important because the electron fraction scales linearly with the ionization rate. A full 3D calculation of X-ray transport and ionization in axially asymmetric disks has been developed by Igea & Glassgold (1999) using a Monte Carlo approach. They calculate the ionization rate at $R = 1$ AU in a minimum mass solar nebula disk model with $L_x = 10^{29}$ erg s$^{-1}$, which can be scaled to other X-ray luminosities and disk radii and is found to be relatively insensitive to changes in disk parameters. Scaling their values at $R = 300$ AU with $N(H_2) \sim 10^{23}$ cm$^{-2}$, we calculate an X-ray ionization rate of $\sim 10^{-16}$ s$^{-1}$ near the surface of the LkCa 15 disk. This is nearly a factor of ten larger than the galactic cosmic ray ionization rate, and shows that X-rays can play an important role in the disk ionization balance. The enhanced ionization can drive additional chemical activity, and the inclusion of X-rays within the context of dust settling models developed for LkCa 15 may well account for much higher abundances of molecules observed toward this source as compared with the DM Tau disk, for which “standard” disk chemistry models produce good agreement with observations (aikawa, 2002).

By considering the balance of all the molecular ions present in the disk, even tighter constraints can be placed on the electron fraction. We consider two conditions with differing abundances of metal ions, as discussed in Langer (1985). When the abundances of metal ions are low, H$_3^+$, HCO$^+$ and N$_2$H$^+$ become the major cations within the disk. Because HCO$^+$ and N$_2$H$^+$ have fractional abundances that are only $\lesssim 10^{-10}$ while the lower limit to the electron fraction is closer to $10^{-8}$, H$_3^+$ dominates. In this case, the electron abundance can be calculated simply from $[e] \simeq (\frac{\zeta}{k_{en}(H_2)})^{\frac{1}{2}} \sim 1.4 \times 10^{-8}$ (langer, 1985), which yields values similar to that derived above. However, the high resulting abundance of H$_3^+$ drives rapid protonation of CO, that is $k_1[H_3^+][CO] \gg k_e(HCO^+)[HCO^+][e]$, and makes HCO$^+$ balance (equation 3) impossible within the confines of the simple model.

It is therefore reasonable to examine the contribution of metal ions to the fractional ionization because they are destroyed very slowly and can comprise a significant fraction of the ion abundance even though their elemental abundances are small. Fromang et al. (2002) calculate the ionization fraction of protostellar disks, taking into account vertical
temperature structure and the possible presence of trace metal atoms, and find that a tiny fraction of the cosmically available metals can dramatically affect the ionization balance. Considering the model above, but now with $[H_3^+] + [HCO^+] + [N_2H^+] \ll [e]$, we can solve for the 3 unknown variables $[N_2]$, $[H_3^+]$ and $[e]$ in order to balance equations 3,4,5. Using equations 4 and 5, removing the term $k_3[N_2][H_3^+]$, and inserting the value of $H_3^+$ derived from the equation 3, the equation for $[e]$ becomes:

$$k_e(HCO^+)[e] + B[e] - \frac{\zeta}{n(H_2)} k_1[CO] = 0$$

(7)

where $B = -k_2k_e(H_3^+)[CO][N_2H^+] + k_1k_e(HCO^+)[CO][HCO^+] + k_1k_e(N_2H^+)[CO][N_2H^+]$. This equation can be solved using the observed column densities of CO, HCO$^+$, and $N_2H^+$ and an assumed density of $H_2$. The $N_2/CO$ ratio can also be derived from equations 5 and 7 under such conditions, and Figure 7 presents the solutions for a range of $H_2$ column densities. Not surprisingly, the electron fraction is calculated to be larger than the metal free case ($\sim 10^{-8}$), which, as we stress above, can only be applied for the physical conditions prevailing near the warm surface layer(s) of the disk.

Transport processes in the outer disk likely depend critically on the degree of ionization. Efficient coupling between the neutral material and magnetic fields is thought to be provided by fractional ionizations of $\gtrsim 10^{-8}$ (feigelson99). As we have outlined above, photons, X-rays, and cosmic rays can produce the ionization needed to couple the magnetic field to the neutral disk material.

### 3.4. CO Depletion and the $N_2/CO$ Ratio

If CO remains primarily in the gas phase, it is sufficiently chemically stable that its abundance will be little altered from dark cloud values. CO would therefore be a good tracer of the disk gas mass, but depletion onto grain mantles in the cold disk is likely to substantially reduce the gas phase column density of CO and many other species. Thus, estimates of the degree of depletion of volatile molecules such as CO and $N_2$ onto grains will greatly improve
our understanding of disk chemistry. For CO, depletion factors can be measured directly from infrared spectroscopy of edge on disks (boogert02), or more generally by using observations of the dust continuum along with several isotopically-substituted molecules (e.g. $^{12}$CO, $^{13}$CO, C$^{18}$O) to distinguish depletion from optical depth effects. From the column density of CO ($1.7 \times 10^{18}$ cm$^{-2}$) obtained with the detailed 2D Monte Carlo radiative transfer model (Table 1), a disk gas mass of only $\sim 10^{-4}$ M$_\odot$ is derived, a value in agreement with that derived from single dish observations of $^{13}$CO higher-J transitions (thi01) using the JCMT and CSO but nearly two orders of magnitude less than the mass derived from dust emission – far more than can be accounted for by errors either in the dust mass opacity coefficient or in the spectral line radiative transfer. Depletion thus appears to be a dominant effect and while CO and its isotopomers are therefore excellent tracers of the disk velocity field, it is clear that they are not reliable tracers of the disk mass. In the models of Aikawa and co-workers (aikawa96, aikawa99), CO depletes onto grains at radii greater than 200–300 AU. Inside this radius, the temperature is 20 K and the gas phase column density rises substantially. If thermal sublimation is the main desorption mechanism, the depletion patterns in disks should be strongly correlated with volatility. We have observed strong emission from non-volatile species such as HCN and CN toward LkCa 15 with spatial distributions that are not well correlated with CO (Qi, Kessler & Blake 2003). Additional mechanisms are therefore likely to be important in maintaining the observed gas-phase abundances.

As a closed shell homonuclear diatomic molecule, N$_2$ has no electric dipole allowed rotational transitions and so cannot be observed directly at millimeter wavelengths. However, from our N$_2$H$^+$ observations and the model presented above, we can estimate the N$_2$/CO ratio, and find it to be $\sim 2$ (Figure 7). This is much higher than the ratios inferred for typical dark clouds at moderate densities, which are $\sim 0.01–0.1$ (womack92, bergin01). In the dark cloud IC 5136, BephalasedepletionandalteredCO/N$_2$ ratios in the densest portions, where CO exhibits a significant abundance reduction and N$_2$H$^+$ is relatively undepleted – although in their models the abundance of N$_2$ is still less than that of CO.

Within disks, Aikawa & Herbst (1999) investigated the two-dimensional chemical structure within the so-called Kyoto minimum mass solar nebula model (hayashi81), and predicted much lower abundances of N$_2$ than CO at all vertical scales. Because they adopted an artificially low sticking probability to reproduce the spectra of CO available at that time, without specifying any non-thermal desorption processes or modifying the temperature distribution in the Kyoto model, such an approach might not account for the known differential desorption of CO and N$_2$. Further, the vertical temperature gradients of actual protoplanetary disks should be more complex than those in the Kyoto model (cg97, dalessio97). Willacy & Langer (2000) investigated the molecules in the superheated layer of the Chiang and G and its chemical product N$_2$H$^+$ trace dense gas in the disk where CO is largely depleted but
N$_2$ is not, and that this region is protected by an overlying warm layer that protects N$_2$ from ultraviolet radiation, in order to produce the high N$_2$/CO ratio observed.

Deriving absolute fractional abundances is more difficult, but from the N$_2$/CO ratio and our Monte Carlo radiative transfer calculations we estimate a fractional abundance for N$_2$ of $\sim 2 \times 10^{-5}$. N$_2$ would therefore represent a substantial fraction of the cosmically available nitrogen, this plus the gas phase N$_2$/CO ratio inferred for LkCa 15 provides a direct observational connection to comets. The abundance of N$_2$ in comets is an important guide to their volatile content because it is trapped and released by amorphous ice in a manner similar to that of Ar (bar-nun$_8$). This process has implications for understanding the role of comets for delivery of volatile materials to the terrestrial planets, relative to that of the sun. The laboratory experiments performed by Bar-Nun et al. (1988) showed that in amorphous ice formed at 50 K and Owen & Bar-Nun (1995) predicted that in icy planetesimals forming in the solar nebula at about 50 K, N$_2$/CO $\approx 0.06$ in the gases trapped in the ice provided N$_2$/CO $\approx 1$ in the nebula itself, a value quite consistent with our data.

Wyckoff & Theobald (1989) reported N$_2$/CO $\sim 2 \times 10^{-3}$ in Halley’s comet, whereas Lutz et al. (1993) found N$_2$/CO $\sim 2 \times 10^{-2}$ in Comet Bradfield, and N$_2$/CO $\sim 3 \times 10^{-2}$ in Comet Kohoutek. The observations are actually of the two molecular ions (CO$^+$ and N$_2^+$) and the conversion from the ion abundances to those of the neutrals is dependent on poorly constrained photodestruction branching ratios. Wyckoff & Theobald (1989) argued that the ion ratio must be multiplied by a factor of 2, while Lutz et al. (1993) find no factor necessary. Large amounts of gaseous N$_2$ may thus be required in the outer solar nebula, as we find in the disk of LkCa 15, in order to explain the N$_2$/CO ratios found in comets. This can be confirmed by measurements of the N$_2$/CO ratio in dynamically new comets, which should have higher values than those in short-period comets (owen$_9$).

4. Summary

We have detected molecular gas and continuum emission from the disk encircling the T Tauri star LkCa 15 at frequencies between 85 and 260 GHz. The 1.2 mm dust continuum emission is resolved in our 1.35 $\times$ 0.74 beam with a minimum diameter of 190 AU and an inclination angle of $\sim 57^\circ$. A noticeable decrease in the continuum spectral slope with frequency may result from the combination of grain growth and dust settling. Sensitive observations at longer wavelengths and submillimeter continuum images are needed to confirm the trend. Based on Keplerian rotation model fits to the CO velocity field, the gas emission extends to $\sim 750$ AU while the characteristic radius of the disk is determined to be closer to 425 AU from Gaussian fits to the CO 2$\rightarrow$1 spectral data cube.

We have also presented molecular images of various isotopologues of CO and the HCO$^+$
and N$_2$H$^+$ ions in the disk. Our observations show that most of the molecular emission from the dominant species of common molecules is optically thick. Different molecules and even different transitions of one molecule will therefore probe different layers of the disk; most of the emitting region detected is near the disk surface. Detailed radiative transfer modelling indicates that LTE is not appropriate in these regions. With this 2D model and the column densities from the detection of the HCO$^+$ and N$_2$H$^+$ ions, we derive a lower limit to the fractional ionization of $10^{-8}$ and an N$_2$/CO ratio of 2, which reveals a region where CO is heavily depleted but N$_2$ is not. This zone must be well protected by the efficient shielding of ultraviolet radiation by an overlying disk layer. Additional discussions concerning the UV field and its impact on disk chemistry will be presented in forthcoming papers.

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Table 1. Observed molecular intensities and column densities toward LkCa 15

<table>
<thead>
<tr>
<th>Transition</th>
<th>Beam (arcsec)</th>
<th>$\int T dv$ (K km s$^{-1}$)</th>
<th>N(30K,LTE) (cm$^{-2}$)</th>
<th>N(Model) (cm$^{-2}$)</th>
<th>Model Ratios N(Model)/N(30K,LTE)</th>
</tr>
</thead>
<tbody>
<tr>
<td>CO 2→1</td>
<td>$1.81 \times 1.49$</td>
<td>12.5</td>
<td>7.28(15)</td>
<td>1.68(18)</td>
<td>230</td>
</tr>
<tr>
<td>$^{13}$CO 1→0</td>
<td>$2.74 \times 2.41$</td>
<td>6.39</td>
<td>1.11(16)</td>
<td>3.04(16)</td>
<td>2.74</td>
</tr>
<tr>
<td>C$^{18}$O 1→0</td>
<td>$5.05 \times 3.59$</td>
<td>1.90</td>
<td>3.31(15)</td>
<td>1.40(15)</td>
<td>0.42</td>
</tr>
<tr>
<td>HCO$^+$ 1→0</td>
<td>$7.74 \times 5.64$</td>
<td>3.30</td>
<td>9.25(12)</td>
<td>2.31(13)</td>
<td>1.79</td>
</tr>
<tr>
<td>H$^{13}$CO$^+$ 1→0</td>
<td>$6.30 \times 4.41$</td>
<td>&lt;0.88</td>
<td>&lt;2.60(12)</td>
<td>&lt;1.12(12)</td>
<td>0.43</td>
</tr>
<tr>
<td>N$_2$H$^+$ 1→0</td>
<td>$3.51 \times 3.17$</td>
<td>3.83</td>
<td>1.71(13)</td>
<td>3.07(13)</td>
<td>1.80</td>
</tr>
</tbody>
</table>
Fig. 1.— Measured millimeter/submillimeter continuum emission fluxes toward LkCa 15. The 850 $\mu$m point was acquired with SCUBA, whose image of LkCa 15 is consistent with a point source (G. Sandell, private communication). The two squares depict the 3 and 1.3 mm continuum fluxes measured with the Plateau de Bure interferometer (duvert00). The spectral slope as determined by all of the available data is shown by the solid line, individual spectral upper limit is inconsistent with an extrapolation of the spectral index derived from the millimeter/submillimeter fluxes.
Fig. 2.— CO 2→1 emission toward LkCa 15. The integrated intensity is shown in contours at left, overlayed on the highest resolution continuum image in gray scale. Contours start at 30% of the peak value of 2.66 Jy km s\(^{-1}\) and increase 10% thereafter. The intensity-weighted mean velocity field over the observed emission region is shown at right (\(v_{\text{LSR}}\) units in m s\(^{-1}\)). The synthesized beam is shown at lower left.
Fig. 3.— The disk averaged spectrum of CO $2\rightarrow 1$ (solid histogram), compared with the model CO emission for a 430 AU radius disk inclined at 58° (dotted line). Details of the calculation may be found in §3.2.
Fig. 4.— Spectral-line maps of the CO 2→1 emission toward LkCa 15, obtained with OVRO in steps of 0.65 km s\(^{-1}\), shown adjacent to simulations of the emission predicted by a kinematic model of a disk in Keplerian rotation with parameters as described in the text. The velocities are referred to the stellar(systemic) velocity of \(V_{lsr} = 6.3\) km s\(^{-1}\).
Fig. 5.— Top: The integrated intensity maps of $^{13}\text{CO}$ (left, contours start at 0.16 Jy beam$^{-1}$ km s$^{-1}$ and are spaced by 0.08 Jy beam$^{-1}$ km s$^{-1}$) and C$^{18}$O (right, contours start at 0.1 Jy beam$^{-1}$ km s$^{-1}$ and are spaced by 0.05 Jy beam$^{-1}$ km s$^{-1}$) $1 \rightarrow 0$ emission. Bottom: The integrated intensity maps of HCO$^+$ (left, contours start at 0.16 Jy beam$^{-1}$ km s$^{-1}$ and are spaced by 0.08 Jy beam$^{-1}$ km s$^{-1}$) and N$_2$H$^+$ (right, contours start at 0.1 Jy beam$^{-1}$ km s$^{-1}$ and are spaced by 0.05 Jy beam$^{-1}$ km s$^{-1}$) $1 \rightarrow 0$ emission. All steps correspond to the rms noise level in each map.
Fig. 6.— Disk averaged spectra of the molecules in Figure 5, obtained over boxes of $6'' \times 7''$ for $^{13}$CO, $8'' \times 5''$ for C$^{18}$O, $6'' \times 7''$ for HCO$^+$, and $6'' \times 6''$ for N$_2$H$^+$. 
Fig. 7.— Fractional abundances ($f(X) = N(X)/N(H_2)$) of $N_2$ and electrons versus the $H_2$ column density for the simple fractional ionization model discussed in §3.3.