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Electronic Quantum Transport in Mesoscopic Semiconductor Structures

With 90 Illustrations, 5 in Full Color

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