The GEMS project: X-ray analysis and statistical properties of the group sample

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ABSTRACT

The GEMS project involves a multi-wavelength study of a sample of 60 galaxy groups, chosen to span a wide range of group properties. Substantial ROSAT PSPC observations, available for all of these groups, are used to characterise the state of the intergalactic medium in each. We present the results of a uniform analysis of these ROSAT data, and a statistical investigation of the relationship between X-ray and optical properties across the sample. Our analysis improves in several respects on previous work: (a) we distinguish between systems in which the hot gas is a group-scale medium, and those in which it appears to be just a hot halo associated a central galaxy, (b) we extrapolate X-ray luminosities to a fixed overdensity radius (r500) using fitted surface brightness models, in order to avoid biases arising from the fact that cooler systems are detectable to smaller radii, and (c) optical properties have been rederived in a uniform manner from the NASA Extragalactic Database, rather than relying on the data in the disparate collection of group catalogues from which our systems are drawn.

The steepening of the $L_{\rm X}$-$T_{\rm X}$ relation in the group regime reported previously is not seen in our sample, which fits well onto the cluster trend, albeit with large non-statistical scatter. A number of biases affect the fitting of regression lines under these circumstances, and until the impact of these has been thoroughly investigated it seems best to regard the slope of the group $L_{\rm X}$-$T_{\rm X}$ relation as being poorly determined. A significant problem in comparing the properties of groups and clusters is the derivation of system radii, to allow different systems to be compared within regions having the same overdensity. We find evidence that group velocity dispersion ($\sigma_v$) provides a very unreliable measure of system mass (and hence radius), with a number of groups having remarkably low values of $\sigma_v$, given that they appear from their X-ray properties to be collapsed systems. We confirm that the surface brightness profiles of groups are significantly flatter than those of clusters – the maximum value of the $\beta_{\rm M}$ parameter for our sample is 0.58, lower than the typical value of 0.67 seen in clusters – however, we find no significant tendency within our sample for cooler groups to show flatter profiles. This result is inconsistent with simple universal preheating models. The morphology of the galaxies in the GEMS groups is correlated to their X-ray properties in a number of ways: we confirm the very strong relationship between X-ray emission and a dominant early-type central galaxy which has been noted since the early X-ray studies of groups, and also find that spiral fraction is correlated with the temperature of the hot gas, and hence the depth of the gravitational potential. A class of spiral-rich groups with little or no X-ray emission, probably corresponds to groups which have not yet fully collapsed.

Key words: X-rays: galaxies: clusters - galaxies: clusters: general - galaxies: general - galaxies: intergalactic medium - galaxies: formation - galaxies: evolution

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1 INTRODUCTION

The principle that we are nowhere special, which is fundamental to cosmology, also applies to galaxies. The majority of galaxies are, like our own, located within bound systems, mostly containing just a handful of bright galaxies (Tully 1987). These are characterised as galaxy groups, which are distinguished rather arbitrarily from richer and rarer galaxy clusters. These systems are evolving, as they turn round from the Hubble expansion, virialise, and grow through mergers and accretion. This dynamical evolution modifies the environment of their constituent galaxies, and can in turn have profound effects on the evolution of the galaxies themselves. On the other hand, energetic galaxy winds can have a substantial impact on the surrounding intergalactic medium (IGM) within groups and clusters (e.g. Pildis, Bregman & Evrard 1995; Mulchaey et al. 1996; Mulchaey & Zabludoff 1998; Helsdon & Ponman 2000a,b; Mulchaey et al. 2003). Any meaningful study of the relationship between groups and galaxies needs to acknowledge this fact. We have therefore commenced a study of the properties of a substantial sample of 60 galaxy groups, and the galaxies they contain, with a view to clarifying the different stages of group evolution, and the ways in which this is related to galaxy properties. This GEMS (Group Evolution Multi-wavelength Study) project involves optical photometry and spectroscopy to study the galaxies, radio observations to explore the HI content of galaxies and to look for cool intergalactic gas, and X-ray studies to probe the hot gas which dominates the baryonic content of at least some galaxy groups, and also provides a valuable indicator that a group is truly a dense system in 3-dimensions.

Given the value of X-ray data, all groups in our sample have been selected to have high quality ROSAT observations available – though we have not selected only groups which are detected in the X-ray. The present paper describes the analysis of these ROSAT PSPC data, and the properties derived from them, and combines these with other properties of these systems and their galaxies drawn from the literature, and in particular from the NASA-IPAC Extragalactic Database (NED). There have been a number of previous studies of samples of galaxy groups based primarily on pointed ROSAT observations (e.g. Pildis, Bregman & Evrard 1995; Mulchaey et al. 1996; Ponman et al. 1996; Mulchaey & Zabludoff 1998; Helsdon & Ponman 2000a,b; Mulchaey et al. 2003). The present work improves on these in a number of respects:

- it is one of the largest samples for which the X-ray data have been analysed in a uniform manner,
- it includes systems with low X-ray luminosity, and some which are entirely undetected in the X-ray,
- systems showing intergalactic X-ray emission have been distinguished from those in which the X-ray emitting gas appears to constitute only hot halo associated with the central galaxy,
- galaxy membership and internal velocity dispersion of the groups have been rederived in a consistent way, using NED data and a sigma-clipping approach, within a projected overdensity radius,
- fitted models have been used to extrapolate X-ray luminosity to a fixed overdensity radius, to compensate for systematic trends with temperature in the radial extent to which X-ray data are available.

The only other studies which share some (but not all) of these features, are those of Helsdon & Ponman (2000a,b) and Mulchaey et al. (2003), with which we make a number of comparisons below.

Throughout this paper we use \( H_0 = 70 \text{ km s}^{-1} \text{ Mpc}^{-1} \), and all errors correspond to 1\( \sigma \).

2 THE SAMPLE

We have sought to assemble the largest sample of galaxy groups for which an X-ray analysis can be performed. We have therefore compiled a list of 4320 groups from 10 optical catalogues (Hickson 1982; Huchra & Geller 1982; Geller & Huchra 1983; Fouque et al. 1992; Garcia 1993; Nolthenius 1993; Bacon et al. 1996; Ramella, Pisani & Geller 1997; Giudici 1999; White et al. 1999) and compared it to the ROSAT PSPC observation log. Groups with a recessional velocity in the range 1000 < \( v < 3000 \text{ km s}^{-1} \) were then selected from this list if there was a PSPC pointing with \( t > 10000 \text{ s} \), within 20′ of the group position. This was to ensure the availability of good quality ROSAT data and that the system was neither so close as to overfill the PSPC field of view nor so distant as to make an X-ray detection unlikely.

Duplicate entries resulting from the overlap between catalogues were removed, along with 7 groups in or around the Hydra and Virgo clusters. One further system, NGC7552 (drawn from Huchra & Geller 1982), was excluded after a calculation of the optical membership described in Section 1 revealed that, although the catalogue group position adhered to all of the above criteria, the group galaxies are all located at radii > 20′ from the ROSAT PSPC pointing, so that none of them actually lie within the mirror shell support ring of the PSPC.

To the resulting sample of 45 selected groups, we added a further 13 which had previously been studied with the PSPC by Helsdon & Ponman (2000a,b), who in turn assembled their sample from those of Nolthenius (1993): Ledlow et al. (1996), Mulchaey & Zabludoff (1998), and two additional Hickson compact groups (HCG 4 and HCG 40) for which we had collected useful optical data. The resulting ensemble of groups is clearly not a true statistical sample, but is chosen to represent a wide range of group properties.

Details of the full sample of 60 groups can be found in Table 1 where the names given are taken from the optical catalogues which have been used, and generally (apart from the Hickson compact groups) correspond to the name of a prominent galaxy within the group. The group positions given in Table 1 were defined in the following way: (a)
where X-ray emission is present (i.e. most cases) the position is that of the galaxy most centrally located within this emission, (b) where no X-rays are detected, the catalogued group position was used. Note that, following these rules, group positions do not always correspond to the location of the galaxy whose name appears in the first column of Table I.

We have further segregated our sample into 3 subsamples according to the presence and nature of their X-ray emission, since it is important to distinguish between emission which is genuinely intergalactic, and that which appears to be associated with the halo of an individual galaxy. It has been shown that the emission from X-ray bright groups is typically characterised by a two-component surface brightness profile (Mulchaey & Zabludoff 1998), where the extended component corresponds to the group emission, and the central component to either the central galaxy, or a bright group core. Therefore, the presence of two such components confirms that a group contains intergalactic hot gas. Unfortunately, poor statistics can often make fitting a two-component model difficult, even if the distribution is truly two-component, and in such cases a one-component model may be all that is available. Hence some other criterion is required, which can discriminate between group-scale and galaxy halo emission, even in the case of poor quality data. Two simple criteria were investigated: the detectable extent of group emission ($r_{\text{ext}}$, Section 4.1), and the ratio of X-ray luminosity to the luminosity of the central BGG ($L_X/L_{BGG}$). The former was found to give more satisfactory results, in that a simple threshold in $r_{\text{ext}}$ of 60 kpc was found to result in the classification all two-component systems as X-ray groups. We therefore assumed that any systems with one-component fits, which had emission more extensive than 60 kpc, also possessed intergalactic gas, but that poor quality data did not permit a two-component fit.

The implication of our extension threshold, is that individual galaxies should not have X-ray halos extending to more than 60 kpc in radius. To check this, it would be useful to compare our threshold value of $r_{\text{ext}}$ with the radii derived from a sample of isolated early-type galaxies (late-type galaxies have much less extended hot gas halos). Unfortunately, isolated early-type galaxies are rare, and very few have been studied with X-ray instruments. O’Sullivan et al. (2003) studied ROSAT data from a sample of 39 early-type galaxies, of which 8 were neither BGGs, nor brightest cluster galaxies. The X-ray radii of these galaxies ranged from ~3 to 9 kpc - much smaller than our threshold. A recent study, by O’Sullivan & Ponman (2004), of a rather X-ray bright isolated elliptical galaxy, NGC4555, detected emission extending to just 60 kpc. Hence this would have (just) been correctly classified by our extension criterion.

As a further check, we also examined $L_X/L_{BGG}$ for all groups, and found one case in which we felt that our extension criterion had failed. In HCG 22, the X-ray emission is centred on a rather faint elliptical ($L_B = 10^{9.29} L_\odot$), and the BGG lies outside the main X-ray emitting region. Using this dimmer central galaxy to calculate $L_X/L_B$, results in a value of $10^{31.39}$ erg s$^{-1}$ L$^{-1}_\odot$, which is significantly higher than the maximum value for any other galaxy halo system ($L_X/L_{BGG} = 10^{30.75}$ erg s$^{-1}$ L$^{-1}_\odot$). We have therefore altered the classification of this system from galaxy halo to group emission, to reflect its high value of $L_X$, relative to its optically dim central galaxies.

Finally, groups with an X-ray flux ($L_X$, Section 4.2), less than 3σ above the background level, have been classed as X-ray undetected groups. We therefore have the following 3 subsamples:

- G-sample: 37 groups (36 with $r_{\text{ext}} > 60$ kpc + HCG 22)
- H-sample: 15 groups with $r_{\text{ext}} \leq 60$ kpc
- U-sample: 8 groups with $L_X < bg + 3\sigma(bg)$

Selection effects in our sample originate from the requirement to have ROSAT archive data available, the velocity cut we have used, and the sample of Helsdon & Ponman (2004) from which a large fraction of our groups have been taken. It is not clear what biasing is inherent in the ROSAT pointing agenda. Some of our targets were observed serendipitously by ROSAT, which reduces any bias involved, but most were the subject of direct pointed observations. Our sample should therefore be viewed as diverse (and in particular it is not restricted to X-ray bright systems) rather than statistically representative. Details of the 60 groups in our full sample are given in Table I.

### 3 OPTICAL PROPERTIES

Our groups have been assembled from a large number of catalogues, and in order to reduce the inhomogeneity in our optical data, we have rederived their galaxy membership in a uniform manner. Group galaxies were selected from the NASA/IPAC Extragalactic Database (NED) using the algorithm described below, and optical properties such as total B-band luminosity, morphological type, velocity and position were extracted. There will however remain a degree of inhomogeneity in the NED data, due to the range of sources from which the data have been compiled. We discuss some checks on the effects of this heterogeneity, later in this section.

For each group we have searched NED for galaxies within a projected radius $r_{500}$ of the group position, defined above, and in a velocity range of $v \pm 3\sigma_v$. Values of $r_{500}$ were calculated from temperature ($T_X$, Section 4.2) using a relation derived from simulations by Evrard, Metzler & Navarro (1996).

$$r_{500}(T_X) = \frac{124}{H_0} \sqrt{\frac{T_X}{10 \text{ keV}}} \text{ Mpc},$$  
where $T_X$ is the temperature in keV and $H_0$ is the Hubble constant in km s$^{-1}$ Mpc$^{-1}$. Where no value of $T_X$ was available, a relation between $r_{500}$ and $L_B$ was derived using Equation (1) and a regression fit in the $L_B-T_X$ plane for the systems with group-scale emission (Section 4.3),

$$r_{500}(L_B) = \frac{124}{H_0} \sqrt{\frac{1}{10} \left( \frac{L_B}{10^{11.17}} \right)^{1/3}} \text{ Mpc}.$$  
A value of $r_{500}$ can also be estimated from galaxy velocity dispersion, using the virial theorem. Assuming energy equipartition between gas and galaxies (i.e. $\beta_{\text{spec}} = 1$, see Section 4.2), Equation (1) can be rewritten in terms of $\sigma_v$,

$$r_{500}(\sigma_v) = \frac{0.096\sigma_v}{H_0} \text{ Mpc},$$  

(3)
than this. In cases where no value of velocity dispersion were taken from the respective catalogues, and are rederived in Table 2 for use in the present work. Groups where the catalogue is marked with * have been included from the Heisler & Ponman (2000) sample and parameters were taken from that paper. Velocity dispersions of Hickson compact groups are taken from Ponman et al. (1994).

**Table 1.** The sample listed in order of right ascension (Section 2). RA and Dec are defined as discussed in the text. $\sigma_v$ and $N_{gal}$ are taken from the respective catalogues, and are rederived in Table 2 for use in the present work. Groups where the catalogue is marked with * have been included from the Heisler & Ponman (2000) sample and parameters were taken from that paper. Velocity dispersions of Hickson compact groups are taken from Ponman et al. (1994).

where $\sigma_v$ is the velocity dispersion in km s$^{-1}$. However we find evidence that this method is unreliable at low values of $\sigma_v$, as discussed in Section 5.

Starting values of $v$ and $\sigma_v$ were taken from the respective catalogues. It has been that a virialised group should have $\sigma_v \geq 100$ km s$^{-1}$ (Mamon, 1994) and as such we have constrained our starting value of $\sigma_v$ to be no less than this. In cases where no value of velocity dispersion was available from the source catalogue we have used 200 km s$^{-1}$.

Optical data resulting from the galaxy extraction were used to recalculate $v$ and $\sigma_v$, where

$$\sigma_v = \sqrt{\frac{\sum (v - \bar{v})^2}{N - \frac{1}{2}}} \pm \frac{\sigma_v}{\sqrt{2(N - \frac{1}{2})}} \text{ km s}^{-1},$$

and the updated values used to redefine our search cri-
The denominator includes a correction for the effects of biasing in systems with a small number of galaxies (Helsdon & Ponman 2004). The selection and recalculation were then repeated until the values of \( v \) and \( \sigma_v \) became stable. If the final number of galaxies within a group was less than 3, then the membership calculation was repeated with the starting value of \( \sigma_v \) set to 200 km s\(^{-1}\). Distances (\( D \)) were calculated from velocities after correcting for infall into Virgo and the Great Attractor.

For two of our systems it was necessary to adjust the membership calculation in order to reduce contamination from nearby clusters. NGC 4261 is in the vicinity of two clusters (WBL 392 & WBL 397) and to prevent the \( \sigma_v \) from increasing to include cluster galaxies, we have used only one iteration of the membership calculation. HCG 48 is falling into the cluster Abell 1060, and to reduce contamination we have used a group radius equivalent to the distance away of the minimum in the galaxy density distribution between the centre of the two systems.

We improve the completeness of our sample by applying a luminosity cut to the optical selection. The value of luminosity was chosen so as to include 90% of the B-band luminosity of the galaxy population, as described by a Schechter function of the form:

\[
\phi(L) dL = \phi_\star \left( \frac{L}{L_\star} \right)^{\alpha} \exp \left( -\frac{L}{L_\star} \right) \frac{dL}{L_\star},
\]

where \( L \) is the galaxy luminosity and \( \phi(L) dL \) is the number of galaxies with a luminosity between \( L \) and \( L + dL \) per Mpc\(^3\). Free parameters are the slope at the faint end (\( \alpha \)), the characteristic Schechter luminosity (\( L_\star \)) and the normalisation (\( \phi_\star \)). We have taken values of \( \alpha \) and \( L_\star \) from [Zabludoff & Mulchaey (2000)], and applied a correction of B-R = 1.57 to convert from R-band to B-band magnitudes ([Fukugita, Shimasaku & Ichikawa 1995]) giving \( \alpha = -1.3 \), \( L_* = 1.60 \times 10^{10} \ L_\odot \), and a minimum luminosity of \( L_{\text{cut}} = 5.28 \times 10^{10} \ L_\odot \) (corresponding to \( M_B = -16.32 \)). We investigate the completeness obtained by applying this cut in our comparison with [Miles et al. (2004)] below. The assumed value of B-R is appropriate for early-type galaxies, and in the case of late types, it will typically result in a luminosity cut which is too low by about 0.5 magnitudes. However, no correction has been applied for the effects of extinction on our galaxy magnitudes, and for typical spirals this amounts to \( \sim 0.5 \) in the B-band. Hence the two effects approximately cancel, and our galaxy membership cut should be reasonably accurate.

We have applied this cut following the membership calculation, and as such it does not affect the calculated values of \( v \) and \( \sigma_v \), which are based on the full sample of galaxies associated with each group. Data surviving the cut were used to calculate total optical luminosity \( L_B \), corrected for the effect of the magnitude cut, spiral fraction by number, \( f_{\text{sp}} \), and mean galaxy density, \( \rho_{\text{gal}} \), assuming a spherical volume of radius \( r_{500} \). The brightest galaxy within 0.25\( r_{500} \) of the the group position was designated as the brightest group galaxy (BGG) and its luminosity (\( L_{\text{BGG}} \)) was divided by the luminosity of the second brightest galaxy to define the dominance of the BGG (\( L_{12} \)). The results of the membership calculation are shown in Table 2. The number of galaxies (\( N_{\text{gal}} \)) is quoted both before and after the luminosity cut. Systems with \( N_{\text{gal}} < 4 \) before the luminosity cut have been excluded from the statistical analysis, on the grounds that (a) many of the optical properties of interest to us are poorly defined for these systems, and (b) such very poor systems are quite likely to be line-of-sight projections, rather than genuinely overdense in 3-dimensions (Frederic 1995). This richness cut excludes 6 groups, two of which have group-scale X-ray emission, but with statistical quality too poor to derive an X-ray temperature. These 6 systems are included in the main data tables, but are flagged with daggers in Tables 2, 3 and 4.

Hence our sample for statistical analysis in the present paper consists of 54 GEMS groups, which are divided into three subsets according to their X-ray properties. We refer to these below as the G-sample (35 systems) which have group-scale emission, the H-sample (13 systems) with galaxy halo emission, and the U-sample (6 systems) which are undetected in X-rays.

As discussed above, the optical data drawn from NED are inevitably inhomogeneous. To investigate the effects of this on our optical luminosities, we have compared our optical results to those of [Miles et al. (2004)], who obtained B-band photometry for a subset of 25 of the GEMS groups. Figure 1 shows a comparison between our galaxy luminosities, and those of [Miles et al. (2004)]. The solid line represents equality.

![Figure 1. A comparison between our galaxy luminosities, and those of [Miles et al. (2004)]. The solid line represents equality.](image-url)
Figure 2. A comparison between our galaxy luminosity function (filled pentagons) and that of [Miles et al. (2004)] (open stars), for the subset of GEMS groups covered by the latter study. The dashed line represents the luminosity cut at $M_B = -16.32$.

A further check on the completeness of our sample close to the cut is obtained by comparing the total light in galaxies above two different cuts. Using Equation\[A\] we calculate the luminosity above which 50% of the optical light should lie, to be $1.34 \times 10^{43}$ erg s$^{-1}$ ($M_B = -20.55$). If our sample were complete to the 90% cut then we would expect the ratio of total light above the two cuts to be $\frac{\sum L_B(90\%)/\sum L_B(50\%)}{\sum L_B(90\%)} = 1.8$. In practice this ratio is found to be 1.9 for our data, suggesting that our completeness is still very high down to the 90% cut, under the assumption that our galaxy luminosity function is well represented by the adopted Schechter function.

4 X-RAY DATA ANALYSIS

ROSAT PSPC datasets were prepared for analysis by first eliminating sources of contamination such as particle emission and solar X-ray emission scattered from the Earth’s atmosphere. Detectors aboard the spacecraft identify and exclude sources of contamination such as particle emission and reflected solar X-rays can be identified by an increase in the background event rate exceeded by 3σ above the background, the dataset was deemed to contain detected X-ray emission.

It was often useful during the course of this data reduction to examine images of the groups in question. Quantitative results, such as the emission radii calculated in Section\[B\] could be examinined and confirmed using such images. We have therefore produced optical images, with X-ray contours overlaid, for all of the groups in our sample. Background variance maps were created assuming Poissonian statistics, smoothed in the usual way and divided into smoothed images to produce significance maps. Contours were drawn on at $5 \times 2\sigma$ sigma above the background ($n = 0,1..10$) and overlaid onto optical images taken from the Digitised Sky Survey (DSS). Figure\[C\] shows an X-ray/optical overlay of NGC524 which has $r_{cut} = 56$ kpc (represented by the dashed circle) and as such is identified with emission from a galactic halo. NGC533 (Figure\[D\]) has $r_{cut} = 372$ kpc indicating group-scale emission.

We have sought to characterise the surface brightness properties of our sample of groups by fitting their emission with a 2-dimensional $\beta$-model, of the form

$$S(r) = S_0 \left(1 + \left(\frac{r}{r_{core}}\right)^2\right)^{-\frac{3+\beta_{fit}+0.5}{\beta_{fit}}}.$$  (6)

It has been shown that fitting such a profile in one dimension can lead to an overestimate of the $\beta_{fit}$ parameter in systems with particularly elongated or offset components.
Table 2. The optical data (section B). Group membership was calculated using a position/velocity search for each group, and a luminosity cut of $L_{\text{cut}} = 2.73 \times 10^{11}$ erg s$^{-1}$. The number of galaxies is given before and after the cut. Groups marked with $^\dagger$ have $N_{\text{gal}} < 4$ before the cut, and have been excluded from the statistical analysis.

(Helou & Pomarajan 2000a). An image in the band 0.5 to 2 keV was extracted from all datasets containing a detection, and data outside $r_{\text{cut}}$ removed. Remaining data were then fitted with a single component $\beta$-model.

Models were convolved with the PSF at an energy determined from the mean photon energy of the data, and free parameters were the central surface brightness $S_0$, core radius ($r_{\text{core}}$), slope ($\beta_{\text{gal}}$) and the co-ordinates of the centre of emission. We also allowed our fits to be elliptical by introducing the axis ratio ($\epsilon$) and position angle as additional free parameters.

In cases where a single component $\beta$-model was inadequate in describing the emission, a second component was added to the model. Such an inadequacy was identified by examining a radial profile for each group in the G-sample, and looking for a shoulder in which the single $\beta$-model significantly departed from the data. In marginal cases a fit using the two component model was attempted. In order to
limit the number of free parameters in our two-component fits, we have fixed the axis ratio and position angle of the central component, thus constraining it to be circular. Surface brightness models were used to correct bolometric fluxes for the removal of point sources and other contamination. For each group the fitted \( \beta \)-model (two-component where available) was taken and used to generate a model image from which a count rate was extracted. Regions of contamination, as defined in Section 4, were then removed, and the reduced count rate combined with the original count rate to derive a correction factor for the luminosity. Groups with no fitted \( \beta \)-model were corrected by taking an image with the regions removed and patching over the holes using a local mean. A correction factor was obtained and applied in the same way. Results of the spatial analysis are presented in Table 3.

### 4.2 Spectral Analysis

We have performed a spectral analysis for all pointings containing a detected galaxy group. A spectrum was obtained by removing all data outside \( r_{\text{cut}} \), and projecting the cube along its spatial axes. Each spectrum was then fitted with a single component MEKAL hot plasma model (Mewe, Lemen & van den Oord 1982), and a multiplicative absorption component with the neutral hydrogen column density fixed at a value taken from HI radio observations (Dickey & Lockman 1990).

A spectral fit was considered reliable if the error on the temperature was less than the fitted value of temperature. Where this was not the case, the value of metal abundance was fixed at 0.3 \( Z_{\odot} \), and the fitting repeated. If the fit remained unreliable then the value of temperature was fixed at 1 keV and the normalisation fitted. Unabsorbed bolometric fluxes were obtained from all spectral models by setting the neutral hydrogen column density to zero. We have calculated an upper limit on the flux from undetected groups, by taking the same fixed model and fitting the normalisation to \( 3\sigma \) above the background level. Values of flux were then converted to luminosities, \( L_X \), using the optically derived distance, \( D \) (Section 3). Results of the spectral analysis are presented in Table 3.

The poor spectral resolution of the ROSAT PSPC means that values of metal abundance \( (Z) \) can often be misleading, even when the value of temperature is deemed reliable. However simulations have shown us that fixing this value can bias the fitted temperature by up to approximately 20%. We found that fitting a one-component spectral model to variable temperature emission results in a greatly underestimated metal abundance, whilst still producing a reliable value for temperature.

We have produced simple projected temperature profiles for all groups with sufficiently good statistics. For each group we extracted spectra from concentric annuli of increasing radius from the group position, and fitted MEKAL hot plasma models to them. The neutral hydrogen column density was fixed as before, and \( Z \) was allowed to vary in cases where the data quality had allowed a global value to be fitted. Spectral profiles including more than 3 bins, and showing a significant drop in temperature in the centre were deemed to demonstrate a cool core. In these cases (9 systems), data within the central cool region were removed and the global spectrum refitted, to derive a “cooling-corrected” temperature. This correction was found to be small – the average drop in \( T_X \) being only 4%, and lying well within the statistical error on \( T_X \). In these cases the X-ray luminosity was corrected for any central data excised, using the fitted surface brightness model.

Spectral data were combined with optical data to calculate two compound parameters: the ratio of X-ray luminosity to optical luminosity \( (L_X/L_B) \), and the spectral index \( (\beta_{\text{spec}}) \) defined by

\[
\beta_{\text{spec}} = \frac{\mu \sigma_v^2}{kT} = 6.26 \times 10^{-6} \left( \frac{\sigma_v^2}{T_X} \right),
\]

where \( \sigma_v \) is the line-of-sight velocity dispersion in \( \text{km} \ \text{s}^{-1} \) and \( T_X \) the temperature in keV.

We have used the fitted \( \beta \)-models to calculate a luminosity \( (L_X) \) within \( r_{500} \), and Figure 5 shows this extrapolated luminosity \( (L_X/L_B) \) plotted against \( L_X \). Errors in \( L_X(r_{500}) \) plotted in the Figure, and listed in Table 4, are extrapolated from errors in \( L_X \), ignoring any errors arising from uncertainties in \( r_{\text{core}} \) or \( \beta_{\text{fit}} \). In cases where no fitted \( \beta \)-model was available, a standard model with the average values of \( r_{\text{core}} = 6 \text{ kpc} \) and \( \beta_{\text{fit}} = 0.5 \) (Table 4), was used instead. As expected, the greatest correction to the luminosity occurs within the lowest luminosity systems, where it can be as large as a factor of \( \sim 3 \).

To investigate the impact on \( L_X(r_{500}) \) of errors in \( r_{\text{core}} \) and \( \beta_{\text{fit}} \), we performed a full Monte-Carlo analysis, incorporating a Gaussian spread in normalisation, \( r_{\text{core}} \) and \( \beta_{\text{fit}} \), for the system (NGC 720), which has fairly typical parameter values. The total derived error on \( L_X(r_{500}) \) was 8%, a factor of 2 greater than the value of 4% based on the normalisation error alone.

### 4.3 Correlations in Properties

We have derived 18 group parameters, listed in Table 5, which we use for our statistical analysis. All parameters were cross-correlated and any significant relationships identified by examining the resulting plots and the Kendall’s rank co-
relation coefficient ($K$), which corresponds to a correlation significance in units of Gaussian sigma. Trends were parameterised by taking the bisector between two orthogonal least squares regression fits, as calculated by the SLOPES software (Freigelson & Babu 1992). We prefer to use an unweighted orthogonal regression, since the scatter observed in the properties of galaxy groups is primarily non-statistical (Helsdon & Ponman 2000). It is therefore inappropriate to weight points by their statistical errors when fitting regression lines.

The regression parameters are summarised in Table 5 and relationships listed in Table 6. These results are presented and discussed in the following sections. In all figures, filled squares represent X-ray groups (G-sample), open circles X-ray galactic-halos (H-sample), and crosses X-ray non-detections (U-sample).

Table 3. Results of the spatial analysis (Section 4.1). Groups marked with † have $N_{gal} < 4$ before the luminosity cut and have been excluded from the statistical analysis.
hereafter referred to as MDMB), includes 109 ROSAT source catalogues (Figure 7).

Figure 3. ROSAT PSPC contours for NGC524 overlaid on an optical DSS image. The dashed circle represents \( r_{\text{cut}} = 56 \) kpc. This system has rather compact X-ray emission which we classify as a galaxy halo (H-sample).

Figure 4. ROSAT PSPC contours for NGC533 overlaid on an optical DSS image. The dashed circle represents \( r_{\text{cut}} = 372 \) kpc. This extensive hot halo is clearly associated with the group as a whole (G-sample).

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<th>Min.</th>
<th>Max.</th>
<th>N</th>
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<td>25</td>
<td>651</td>
<td>54</td>
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<tr>
<td>( D ) (Mpc)</td>
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<td>10</td>
<td>127</td>
<td>54</td>
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<tr>
<td>( r_{500} ) (Mpc)</td>
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<td>0.23</td>
<td>0.88</td>
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</tr>
<tr>
<td>( r_{500}(\sigma_x) ) (Mpc)</td>
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<td>0.10</td>
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</tr>
<tr>
<td>( \rho_{\text{gal}} ) (Mpc(^{-3}))</td>
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<td>6</td>
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<tr>
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<td>10.32</td>
<td>11.80</td>
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<tr>
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<td>0.00</td>
<td>1.00</td>
<td>54</td>
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<tr>
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<td>9.44</td>
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<tr>
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<td>( r_{\text{core}} ) (kpc)</td>
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<tr>
<td>( \beta_{\text{fit}} )</td>
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</tr>
<tr>
<td>( \epsilon )</td>
<td>1.52</td>
<td>1.04</td>
<td>3.16</td>
<td>34</td>
</tr>
<tr>
<td>( \tau_X ) (keV)</td>
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<td>0.19</td>
<td>1.52</td>
<td>43</td>
</tr>
<tr>
<td>( Z ) (Z_\odot)</td>
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<td>0.00</td>
<td>2.00</td>
<td>43</td>
</tr>
<tr>
<td>( L_X ) (log erg s(^{-1}))</td>
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<td>39.69</td>
<td>43.51</td>
<td>48</td>
</tr>
<tr>
<td>( L_X(r_{500}) ) (log erg s(^{-1}))</td>
<td>42.55</td>
<td>40.34</td>
<td>43.57</td>
<td>48</td>
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<td>( \beta_{\text{spec}} )</td>
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<td>0.01</td>
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<td>( L_X/L_B ) (log erg s(^{-1}) ( L_\odot^{-1} ))</td>
<td>31.07</td>
<td>29.14</td>
<td>32.09</td>
<td>43</td>
</tr>
</tbody>
</table>

Table 5. A summary of the parameters investigated in the statistical analysis. \( N \) is the number of datapoints used in each calculation.

5 COMPARISON WITH PREVIOUS WORK

We compare our derived values of \( N_{\text{gal}} \) and \( \sigma_x \) to those given in the group catalogues from which our groups are drawn. Figure 5 shows a reasonable agreement between values of \( N_{\text{gal}} \) in all but the compact groups, where we typically find many more galaxy members, since the original compact group search included only a compact core of galaxies in what is generally a much larger group (e.g. Zabludoff & Mulchaey 1998). We also find a reasonable match between our values of \( \sigma_x \), and those taken from the source catalogues (Figure 7).

The recently published atlas by Mulchaey et al. (2003, hereafter referred to as MDMB), includes 109 ROSAT-observed groups, larger than present sample, with X-ray emission detected from 61. X-ray fluxes in this study have not been corrected to \( r_{500} \), and optical properties have been drawn from a variety of group catalogues, rather than reextracted in a uniform manner as in our sample. However, Mulchaey et al. subject all their groups to a uniform X-ray data analysis similar in many ways to ours, so that comparisons with our results provide a valuable check. In particular they adopt the same procedure for choosing \( r_{\text{cut}} \), and quoted luminosities are bolometric. In the spectral fitting the natural hydrogen column density is fixed at the galactic and unconstrained metallicities are fixed at 0.3 solar.

There is an overlap of 43 groups between the two samples. Plotting \( L_X \) against \( L_X \) (MDMB) (Figure 6) shows a good agreement for X-ray bright groups, and reasonable agreement amongst groups with lower luminosity, but with a good deal of scatter in the latter. The reason for this scatter is not clear. It does not, in general, appear to be related to the radius out to which emission has been integrated in the two studies, nor (see below) to systematic differences in the spectral properties derived. We explored the comparison in more detail for three of the groups for which the disagreement with MDMB was strongest. NGC 315 has a value of \( 10^{41.88} \) erg s\(^{-1}\). However this difference is accounted for by the removal of the central AGN in our analysis (Section 4).

Our \( L_X \) for HCG 48 is a factor of \( \approx 2 \) less than the MDMB value of \( 10^{41.70} \) erg s\(^{-1}\). This value has been extracted from a circular region with a value of \( r_{\text{cut}} \) equivalent to 60% of the MDMB radius of 72 kpc. We have used a smaller radius in order to minimise X-ray contamination from the nearby cluster Abell 1060 and it is this difference which accounts for the deficit in \( L_X \). NGC 4636 has \( L_X \) a factor of \( \approx 5 \) less than the MDMB value of \( 10^{42.19} \) erg s\(^{-1}\), and is extracted from a similar size region. Furthermore the diffuse emission
is so extensive that replacing the central AGN only changes the overall $L_X$ by a small proportion. The value of $L_X$ derived by $200 \times 10^{42}$ erg s$^{-1}$ for the same system is $10^{42.16}$ erg s$^{-1}$, in good agreement with the MDMB value. However both of these studies take the group velocity from the source catalogue, and applying our iterative membership calculation decreases this catalogue value (and hence the distance inferred from it) by a factor of $\sim 2$, accounting for the majority of the discrepancy in $L_X$. Our value of distance is also in much better agreement with that of the BGG, NGC 4636 ($D = 10$ Mpc).

We find a good agreement between our values of $T_X$ and those taken from MDMB (Figure 9), though the latter have not been corrected for cool cores. Since the MDMB
studied is based on the same ROSAT data that we are using, this comparison does not address the issue of the whether ROSAT spectra yield reliable temperatures. The results of Hwang et al. (1994) suggest that for hot plasmas with $T_X > 1.5$ keV, ROSAT PSPC temperatures are biased low (by about 30%) relative to those derived using the superior spectral capabilities of ASCA, whilst for cooler systems temperatures from the two instruments are in reasonable agreement. Since the hottest system in our sample has $T_X = 1.52$ keV, any such bias should have only minor effects on our study.

6 THE RADIUS OF GALAXY GROUPS

As discussed in Section 4, we have sought in this study to extract group properties within a consistently defined overdensity radius, corresponding to 500 times the critical density of the Universe at the current epoch. The best way to define such a radius for each group would be to derive total mass profiles, to directly measure the radius within which the desired mean density is obtained. This could be done (under the assumption of hydrostatic equilibrium) if gas density and temperature profiles could be extracted from our data. Unfortunately, the quality of the data does not permit reliable gas temperature profiles to be extracted for most of these groups, and in no case could such a profile be extended to $r_{500}$. Failing this, three methods for estimating $r_{500}$ were considered, as described in Section 8 based on the use of X-ray temperature, galaxy velocity dispersion or total optical (blue) luminosity. The principle behind all these, is that a system virialising at $z = 0$ should have a given mean density within its virial radius, and hence all overdensity radii should scale as the third power of system mass. Total optical luminosity ($L_B$) can be used to estimate system mass under the assumption that star formation efficiency, and mean mass-to-light ratio of galaxies, are independent of other group properties.

Unfortunately, these assumptions are debatable. Semi-analytical models of galaxy formation predict a correlation between $M/L$ and halo size. For example, Benson et al. (2000) find that $M/L$ drops by a factor ~3 in their models, between halos of mass $10^{14}$ $M_\odot$ and $10^{12}$ $M_\odot$, i.e. in the group and galaxy regime. Observational evidence on this issue is mixed. Most X-ray studies, such as those by Hranecky et al. (2000) and Sanderson & Ponman (2003), have found the mass-to-light ratio and star formation efficiency in groups and clusters to be essentially independent of temperature. However, the study of Hoekstra et al. (2003), based on the weak lensing signal from a set of stacked groups, found $M/L$ lower than that in clusters, and a compilation of a variety of measurements on group to cluster scales, led Bahcall & Cenfard (2002) to conclude that $M/L$ rises gently, as $T_X^{0.3}$, across the temperature range from 1 keV to 12 keV.

Alternatively, for a system in virial equilibrium, the characteristic velocity dispersion of the galaxies, and the gas temperature, should be related to system mass via the virial theorem. This leads to

$$T_X \propto \sigma_v^2 \propto M/R \propto M^{2/3},$$

where the final step involves the assumption of constant mean density for newly-virialised systems. Results from cosmological simulations suggest that a scaling relation $M \propto T_X^{1.5}$ can give a robust and reliable measure of mass. Evrard et al. (1996), in an analysis of an ensemble of simulated clusters (including some incorporating feedback), found that mass estimates using a $T_X^{1.5}$ formula with an appropriate normalisation, scattered about the true masses, with a standard deviation of only 15%. On the other hand, a number of studies (e.g. Finoguenov, Reiprich & Böhringer 2001) find that the $M-T_X$ relation has a slope steeper than 1.5, and Sanderson et al. (2003) find observational evidence, by comparing X-ray derived masses with the results obtained from simple scaling formulae, that a $T_X^{0.5}$ scaling can overestimate virial radii, especially in cool systems, by up to 40%, leading to a corresponding overestimate in virial mass.

It is known from previous studies (c.f. Section 4) that the energy per unit mass in gas tends to be higher than that in galaxies (i.e. $\beta_{pec} < 1$) for poor clusters and groups, and that in groups there appears to be a great deal of scatter in $\beta_{pec}$. This implies that either $T_X$ or $\sigma_v$ (or both) is an unreliable indicator of system mass. A priori one could think of reasons to suspect either parameter: $\sigma_v$ is usually statistically poorly determined in groups, due to the low number of galaxy redshifts available, and might also be affected by a variety of biases and physical effects, whilst $T_X$ could be vulnerable to the effects which are believed to have raised

<table>
<thead>
<tr>
<th>$\log L_X$</th>
<th>$\log T_X$</th>
<th>$\log \sigma_v$</th>
<th>$\log f_{sp}$</th>
<th>$\log f_{sp}$</th>
<th>$\log T_X$</th>
<th>$\log L_X$</th>
</tr>
</thead>
<tbody>
<tr>
<td>2.75 ± 0.49</td>
<td>42.38 ± 0.10</td>
<td>-0.97 ± 0.11</td>
<td>2.56 ± 0.66</td>
<td>35.73 ± 1.68</td>
<td>4.94</td>
<td></td>
</tr>
<tr>
<td>2.05 ± 0.21</td>
<td>19.13 ± 2.41</td>
<td>4.78</td>
<td></td>
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</tr>
<tr>
<td>1.28 ± 0.34</td>
<td>26.82 ± 3.66</td>
<td>0.12</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
| 2.47 ± 0.19 | 14.25 ± 2.15 | 5.978

Table 6. A summary of the relationships discussed in the following sections. Values of slope and intercept describe an unweighted orthogonal regression fit to all data, and the G-sample (bold) and H-sample seperately. K is Kendall’s rank correlation co-efficient, corresponding to a significance in units of Gaussian sigma.
The GEMS project: X-ray analysis and statistical properties of the group sample

Figure 6. A comparison between our values of $N_{\text{gal}}$, and those taken from the source catalogues (Table 1). Filled squares represent the G-sample, open circles the H-sample and crosses non-detections. The solid line represents equality.

Figure 7. A comparison between our values of $\sigma_v$, and those taken from the source catalogues (Table 1). Filled squares represent the G-sample, open circles the H-sample and crosses non-detections. The solid line represents equality.

Figure 8. A comparison between our values of $\log N_{\text{gal}}$, and those taken from the source catalogues (Table 1). Filled squares represent the G-sample, open circles the H-sample and arrows represent upper-limits from non-detections. The solid line represents equality.

Figure 9. A comparison between our values of $L_X$, and those taken from the source catalogues (Table 1). Filled squares represent the G-sample and open circles the H-sample. The solid line represents equality.

Figure 10. A comparison between our values of $\log \rho_{\text{gal}}$, and those taken from the source catalogues (Table 1). Filled squares represent the G-sample, open circles the H-sample and arrows represent upper-limits from non-detections. The solid line represents equality.

Figure 11. A comparison between our values of $T_X$, and those taken from the source catalogues (Table 1). Filled squares represent the G-sample and open circles the H-sample. The solid line represents equality.

the entropy of the gas in groups relative to that expected on the basis of what is seen in clusters (Ponman et al. 1999).

To explore this further, we tried both methods (Equations 1 and 3) for the evaluation of $r_{500}$, and extracted the group members for each of the two resulting definitions. It is instructive to consider the mean density of galaxies,

$$\bar{\rho}_{\text{gal}} = \frac{N_{\text{gal}}}{V_{500}} = \frac{N_{\text{gal}}}{\frac{4}{3} \pi r_{500}^3} \text{ Mpc}^{-3},$$

for the GEMS sample, computed by each method. Histograms showing the distribution of $\bar{\rho}_{\text{gal}}$ values obtained are shown in Figure 10. For comparison, we calculated the expected mean galaxy density within $r_{500}$ from the average Sloan Digital Sky Survey (SDSS) luminosity function of Blanton et al. (2003), by integrating their Schechter function down to our luminosity cut, giving a predicted mean galaxy density

$$\bar{\rho}_{\text{gal}}(\text{pred}) = \frac{500}{\Omega_m} \int_{L_{\text{cut}}}^{\infty} \phi(L) dL = 27 \text{ Mpc}^{-3},$$

where $\Omega_m$ is the density of ordinary matter, as a fraction of the critical density, and is assumed to be 0.3. The predicted mean galaxy density is marked in Figures 10 and 11.

It can be seen that using the $T_X$-based estimate of $r_{500}$, the expected density is close to the median of our derived values ($\bar{\rho}_{\text{gal}} = 25$), whilst the $\sigma_v$-based estimates lead to a much wider scatter in $\bar{\rho}_{\text{gal}}$, with some values (mostly for very poor groups) over an order of magnitude higher than expected. The standard deviations in the $\bar{\rho}_{\text{gal}}$ distributions for the $T_X$ and $\sigma_v$-based estimates are 21 Mpc$^{-3}$ and 115 Mpc$^{-3}$, respectively.

In Figure 11 we compare the derived densities for the two methods, plotted against total optical luminosity of the groups. It can be seen that not only does the $T_X$-based analysis give a smaller scatter in $\bar{\rho}_{\text{gal}}$, but that the inferred densities show no discernable trend with $L_B$. It seems that any
effects of non-self-similar entropy scaling are not acting to systematically raise $T_X$ in lower mass systems, otherwise we would see a trend towards lower apparent $\rho_{gal}$ in the poorest systems.

The good agreement between our observed and expected galaxy densities, appears to conflict with the conclusions of the Sanderson et al. (2003) analysis, discussed above, since a 40% overestimate in $r_{500}$ would lead to our densities being underestimated by a factor of 2.7, which does not seem consistent with the results shown in Figure 11. Moreover a number of recent studies (e.g. Nevalainen, Markevitch & Forman 2000; Sato et al. 2000; Finoguenov et al. 2001), have indicated that the $M-T_X$ relation for clusters and groups is significantly steeper than the self-similar ($M \propto T_X^{1.5}$) relation, although Allen, Schmidt & Fabian (2001) find a relation consistent with self-similarity from a high-quality Chandra study of a small sample of rich, relaxed clusters, with a 2500 overdensity radius. If the $M-T_X$ relation does have a slope steeper than 1.5, then it follows that the $T_X^{0.5}$ scaling for $r_{500}$ is too flat, and will presumably tend to overestimate the radius in the group regime.

It should be noted that the good agreement between our median value of galaxy density and the expected value, assumes that galaxies are not biased relative to mass on group scales. Recent results from the 2dF galaxy redshift survey (Verde et al. 2002) suggest that light is essentially unbiased relative to mass on scales larger than 5 Mpc. However, as we discussed earlier in this section, there is some evidence from both observations and simulations (e.g. Bahcall & Comerford 2002; Benson et al. 2003) that light may be biased on smaller scales. A recent study of the K-band mass-to-light ratio (Lin, Mohr & Stanford 2003), based on 2MASS luminosities which provide a measure of the stellar mass relatively unaffected by recent star-formation history, coupled with mass estimates based on X-ray temperatures, found that $M/L_X$ dropped by a factor $\sim 2$ over the mass range $M(r_{500}) \sim 10^{15} M_\odot$ to $\sim 10^{14} M_\odot$. It may therefore be that the apparent good agreement between our derived galaxy densities and the prediction from the universal mean is fortuitous, and that our application of Equation 11 leads to an overestimate of $r_{500}$, and hence an underestimate of $\rho_{gal}$, which cancels the factor of $\sim 2-3$ by which these densities are biased upward relative to the Universal mean. Derivation of reliable X-ray masses with XMM-Newton may eventually resolve this issue.

Our conclusion is that the use of Equation 11 appears to provide a more stable estimate of $r_{500}$ than the use of a $\sigma_v$-based scaling relation, although there is some danger that all our radii may be somewhat overestimated by the $T_X^{0.5}$ formula. Where no value of $T_X$ is available, we adopt an estimate based on the scaling of scaling of mass with $L_B$, using Equation 2. In the latter case, an iterative process is involved, since $L_B$ depends upon the group membership within $r_{500}$, whilst $r_{500}$, in turn, depends on $L_B$.

7 GLOBAL SCALING RELATIONS

Scaling relations between the major global parameters of galaxy systems -- $L_X$, $T_X$, $\sigma_v$ and $L_B$ -- are of great interest in studying the extent to which groups are related to clusters through simple similarity scalings. Previous work (Helsdon & Ponman 2000; Xue & Wu 2000; Mulchaey 2000) has shown that even where scaling relations follow self-similar forms for rich clusters, this behaviour does not usually extend to the group regime. In terms of X-ray properties, we are interested here in the scaling properties of the hot IGM, so we concentrate primarily on those systems designated as having "group" emission. In order to compare with cluster properties, we make use of the sample of Horner (2001), based on a homogeneous analysis of data from the ASCA observatory. We remove cool ($T_X < 2$ keV), low luminosity ($L_X < 2 \times 10^{43}$ erg s$^{-1}$) groups from the systems studied by Horner, to give a sample of 230 clusters, 105 of which have velocity dispersions available. The X-ray luminosities for these systems were corrected to $r_{500}$ by Horner, assuming a standard $\beta$-model with $\beta = 0.67$, and core radius which scales as $L_X^{0.28}$, following the empirical result of Böhringer et al. (2000). We have used the same model to correct each of these cluster luminosities instead to $r_{500}$, for comparison with our group values. Temperatures for these clusters have been derived by Horner from MEKAL model fits to integrated ASCA spectra from within some extraction radius. Although no attempt was made to remove any emission from a central cool core, we have seen that this has had only a small effect on our own temperatures, so that the two samples can reasonably be compared. Velocity dispersions for a subset of his clusters were collected by Horner from the literature. These will therefore be derived in a heterogeneous fashion. However, for all but three of the clusters, these velocity dispersions are based on more than 10 redshifts.

7.1 The $L_X-T_X$ Relation

Strong correlations exist between X-ray luminosity and both gas temperature and velocity dispersion, reflecting the fact that deeper potential wells generally contain more hot gas.
It has been clear for many years that the \( L_X-T_X \) relation for clusters does not follow the \( L_X \propto T_X^2 \) law expected for self-similar systems radiating bremsstrahlung X-rays. Most authors (e.g. White, Jones & Forman 1997; Arnaud & Evrard 1992) have found logarithmic slopes close to 3 in the cluster regime, though attempts to remove the effects of central cooling flows (Allen & Fabian 1998; Markevitch 1998) have produced rather flatter relations. Studies of the relation for galaxy groups have mostly found considerably steeper slopes. Helsdon & Ponman (2000a) obtained a slope of 4.9±0.8 for a sample of X-ray bright loose groups, and 4.3±0.5 for a larger sample (36 systems) including both loose and compact groups. Xue & Wu (2000), found a slope of 5.6±1.8 from data for 38 groups drawn from the literature.

Our result from the GEMS sample, shown in Table 6 and Figure 11 for the subsample of 45 groups with fitted temperatures, is significantly flatter than the above group results, and appears close to the slope seen in clusters. This is especially striking if we restrict our attention to G-sample systems (slope = 2.75±0.46) and flattens still further (2.50±0.42) if we use \( L_X \) values extrapolated to \( r_{500} \).

In Figure 11, we plot the G-sample systems, with extrapolated luminosities, alongside the Horner cluster sample. The parameters for the three trend lines are given in Table 7 and that for the G-sample groups is actually somewhat flatter than the cluster relation. Can we conclude from this that the earlier results of a steeper \( L_X-T_X \) relation in groups were incorrect?

To explore the origin of the differences from our own earlier results, we examined the subset of 16 of our GEMS groups which overlap with the sample of 24 groups studied by Helsdon & Ponman (2000a). Our regression line through these 16 systems has a slope of 4.3±0.9, close to the result of Helsdon & Ponman (2000a). The use of luminosities extrapolated to \( r_{500} \) flattens this regression line only slightly, to a slope of 3.7±1.0. These tests strongly suggest that the flatter slope from our G-sample systems is primarily related to differences in the group sample used here, rather than in the analysis techniques employed. The systems studied by Helsdon & Ponman (2000a) were selected on the basis of significant X-ray flux, and therefore constitute a sample of X-ray bright groups, whereas the GEMS sample was deliberately designed to cover a wider spectrum of X-ray properties, as discussed in Section 2. As a result, our present sample includes a much larger number of cool groups (\( T_X < 0.7 \) keV) than that of Helsdon & Ponman (2000a), and most other previous studies. Two groups in particular, HCG 10 and NGC 3557, have \( T_X < 0.25 \) keV, and yet have moderately high X-ray luminosities.

In the present study, we are also pushing closer to the statistical limits of what can be achieved with ROSAT data. It is well-established that there is considerably larger real scatter in the scaling relations for galaxy groups than is seen in clusters. This scatter introduces three sources of bias into our regression process. Firstly, the result of truncating this scattered trend at low \( L_X \) (since we will either reject systems with very low \( L_X \) as galaxy halo sources, or fail to detect them altogether) will be to flatten the fitted relation. Secondly there is a logarithmic bias whereby the scatter in \( L_X \) (which dominates the statistical scatter about the trend line) will be asymmetric (if the scatter in \( T_X \) is fairly symmetric) with larger scatter towards lower \( L_X \) since we will either reject systems with very low \( L_X \) or fail to detect them altogether. Finally, there is an additional bias which couples with the scatter in \( T_X \). At temperatures towards the bottom of the ROSAT bandpass, and close to the absorption cut-off due to interstellar gas and dust, the unabsorbed bolometric flux corresponding to a given PSPC count rate rises quite sharply as \( T_X \) falls (e.g. for an absorbing column of \( 4 \times 10^{20} \) cm\(^{-2} \) it rises by 67% as \( T_X \) falls from 0.6 keV to 0.3 keV). Thus it follows that points in the \( L_X-T_X \) plane which scatter down in temperature, will scatter up in \( L_X \), which further magnifies the flattening effect discussed above. Since all three of these biases are related to the large scatter in the data, we investigated the effect of clipping the outliers. Iteratively discarding G-sample points which lie more than 2 sigma from the regression line does indeed steepen the fitted slope, from 2.5 to 3.0 where 8 of the 33 points are clipped in this analysis. Note, however, that this steeper slope is still fully consistent with the cluster \( L_X-T_X \) relation.

One final source of bias which becomes important when pushing the sample down to very poor groups, is the im-

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**Figure 11.** The relationship between \( \rho_{gal} \) and \( L_X \) using (top) gas temperature, and (bottom) galaxy velocity dispersion, to calculate \( r_{500} \) and derive group membership. Filled squares represent the G-sample, open circles the H-sample and crosses non-detections. The expected mean density of galaxies down to our luminosity cut is shown as a horizontal dashed line.
Table 7. A comparison of scaling relations between groups and clusters. Group relations are derived from the G-sample and cluster relations from the sample of Horner (2001).

Figure 12. The relationship between $L_X$ and $T_X$ for the GEMS groups. Filled squares represent the G-sample and open circles the H-sample. The solid line represents an unweighted orthogonal regression fit to all points, and the dashed line to the G-sample only.

Figure 13. The relationship between $L_X(r_{500})$ and $T_X$ for the GEMS groups (squares and circles) and the Horner clusters (stars). The dashed line represents a fit to the G-sample, dotted line to the clusters, and solid line to clusters plus the G-sample. The H-sample is excluded from the fitting, but is plotted for comparison.

Figure 14. The relationship between $L_X$ and $\sigma_v$ for the GEMS groups. Filled squares represent the G-sample, open circles the H-sample and arrows represent upper-limits from non-detections. The solid line represents an unweighted orthogonal regression fit to all points, and the dashed line to the G-sample only.

Figure 15. The relationship between $L_X(r_{500})$ and $\sigma_v$ for the GEMS groups (squares, circles and arrows) and the Horner clusters (stars). The dashed line represents a fit to the G-sample, dotted line to the clusters, and solid line to clusters plus the G-sample. The H-sample and non-detections are excluded from the fitting but are plotted for comparison.

The impact of contamination from point sources which are unresolved by ROSAT. Since the fractional contribution of such sources will tend to be larger in the lowest luminosity groups, it will tend to flatten the $L_X$-$T_X$ relation. Helsdon, Ponman & Mulchaey (2004) find, from a comparison of Chandra and ROSAT results for two very cool groups, that the level of unresolved point source contribution to the diffuse flux derived from the PSPC analysis is 30-40%. So this effect is smaller than the correction (a factor 2-3 for
such poor systems) arising from extrapolation to $r_{500}$, and
works in the opposite direction.

A further difference in our present analysis, compared to
earlier studies, is that we separate off systems in which the
X-ray emission appears to be related to a central galaxy,
rather than to the group as a whole. In studying the prop-
erties of groups, for comparison with clusters, this seems
the appropriate thing to do. As can be seen from Figure 12
and Table 1 these halo sources do fall at the bottom of the
$L_X$-$T_X$ relation, and their inclusion steepens the fitted $L_X$-$T_X$
relation. However, this will have had little impact on the
earlier work of Helsdon & Ponman (2000a), since their X-
ray bright sample contained very few objects which might
be classified as galaxy halo sources.

In summary, we conclude that although the $L_X$-$T_X$ re-
lation obtained from our G-sample groups is close to con-
tinuous with the cluster relation, albeit with increased scatter,
this may be a misleading result, since we have identified a
number of biases, all of which work towards flattening the
fitted $L_X$-$T_X$ relation in the low $T_X$, low $L_X$ regime. Extin-
tion of the data towards lower $L_X$ would be necessary to
reduce these biases and establish definitively whether the
$L_X$-$T_X$ relation does steepen in groups. This may ultimately
be possible with $XMM$-$Newton$, but will not be straight-
forward, in a regime where luminosities are comparable to
those of individual halos around early-type group member
galaxies. What is clear from our results, is that groups show
a considerably larger real scatter about the mean $L_X$-$T_X$
trend than is seen in clusters – spanning at least a factor of
30 in $L_X$, at a given value of $T_X$, or a factor 3-4 in $T_X$ at
given $L_X$.

### 7.2 $L_X$-$\sigma_X$ relation

Our relationship between $L_X$ and $\sigma_X$ (Figure 14) has a
slope of 2.96±0.56 for the G-sample, which is flatter
than the value of 4.5±1.1 found by Helsdon & Ponman
(2000a). Although there is general agreement that the
$L_X$-$\sigma_X$ relation does not steepen in groups, unlike the
$L_X$-$T_X$ relation, there is disagreement between studies
(e.g. Ponman et al. 1994; Mulchaey & Zabludoff 1998;
Helsdon & Ponman 2000a; Mahdavi 2001), which find that
groups are consistent with the cluster-relation slope of
≈ 4, and those (Mahdavi et al. 1997; Xue & Wu 2000;
Helsdon & Ponman 2000b; Mahdavi et al. 2000) which find
significantly flatter relations in groups. The result from the
GEMS sample is clear (Figure 15) substantially flatter
than the cluster trend, and has a slope in good agree-
ment with that of Helsdon & Ponman (2000a) (2.4±0.4) and
Xue & Wu (2000) (2.35±0.21). Extrapolation of the lumin-
osity to $r_{500}$ results, as expected, in a slightly lower slope,
of 2.31±0.62 (Table 4).

As with the $L_X$-$T_X$ relation, biases are at work which
will tend to lead to some spurious flattening of our regression
results. Since the groups with lowest $L_X$ tend to be
the poorest, and hence to have the largest fractional er-
rors in $\sigma_X$, three of the four sources of bias discussed in
the last section (the truncation and logarithmic biases, and
point source contamination) will also apply to the $L_X$-$\sigma_X$
relation. Nonetheless, there are some groups in our sample
with remarkably low velocity dispersion, which appear to
show group-scale emission. This is hard to understand, since
such X-ray emission presumably implies that a group is col-
lapsed, if not virialised, and as Mamon (1994) has argued,
the requirement that collapsed systems should have some
minimum overdensity sets a lower bound (at a given mass
or radius) to the velocity dispersion which they can have.
This bound is $\sim 100-200$ km s$^{-1}$ for poor groups. A study
with Chandra (Helsdon et al. 2004), of two of the low $\sigma_X$
systems in our sample, NGC 1587 and NGC 3665, has con-
firmed that the diffuse X-ray emission identified by $ROSAT$
is not grossly misleading, although point source contami-
nation and inaccurate spectral characterisation can lead to
overestimation of $L_X$ by $\sim 30-40\%$.

The fact that groups with such low values of $\sigma_X$ can
contain a significant IGM, with properties which accord rea-
sonably well with the other groups, strongly suggests that
the observed values of $\sigma_X$ are not reflecting the depth of
the potential well in the way one expects. We will return to this
in the following section.

### 7.3 $\sigma_X$-$T_X$ and $\beta_{\text{spec}}$

A number of previous studies have found that the re-
lation between velocity dispersion and gas temperature
departs slightly from the virial theorem expectation
($\sigma_X \propto T_X^{0.5}$) in clusters (Bird, Mushotzky & Metzler 1995;
Girardi et al. 1998; Wu, Xue & Fan 1999). The evidence
for groups is more controversial, with some authors (e.g.
Xue & Wu 2000; Mulchaey 2000) finding that groups fall
on the cluster trend, and others (Helsdon & Ponman 2000a)
finding that the relation steepens in groups with $T_X < 1$ keV,
to a slope $\geq 1$. Our result, presented in Figure 16, shows that
there is a great deal of non-statistical scatter in the groups,
in addition to the large statistical errors in both $T_X$, and
especially $\sigma_X$, in the poorest systems. This appears to be
the origin of the controversy over whether the relation does
or does not steepen in the group regime. Formally, we find
that it does, with a best fit slope to the GEMS G-sample
systems of 1.15±0.29. However it is clear that the best fit
line to the combined group+cluster sample (with a slope of
0.71±0.05) passes through the centre of the scatter of group
points, and also represents the trend in the cluster regime
quite adequately. This slope is somewhat steeper than that
found in most previous studies.

Comparison with the line $\beta_{\text{spec}} = 1$ in Figure 16 shows
that many of the G-sample groups are actually consistent
with this energy equipartition line (as are many clusters),
but that there is a significant subsample of points which
scatter well below it. These systems have velocity dispersions
typically a factor 3 below what would be expected for their
$X$-ray temperatures. All of the groups with $\sigma_X < 1$0 km s$^{-1}$
fall into this category.

Figure 17 shows clearly that high X-ray luminosity ($L_X$
$> 10^{46} \text{ erg s}^{-1}$) groups have $\beta_{\text{spec}} \sim 1$, whilst groups with
$L_X \lesssim 10^{45.5} \text{ erg s}^{-1}$ scatter widely in $\beta_{\text{spec}}$, spanning the range
$0.1-1.0$. The evidence discussed in Section 6 above,
leads us to the conclusion that $T_X$ gives a much more reliable
measure of system mass and radius than does $\sigma_X$. It follows
from this that the “problem” in some of the poorest systems,
which leads to their remarkably low values of $\beta_{\text{spec}}$, lies not
with $T_X$, but with $\sigma_X$. Some of these groups, from both G and
H-samples, have extremely low velocity dispersions, giving
such statistical biases cannot provide anything approaching a bias to the derived value of the group potential well. This galaxy will not contribute to the sum of squared deviations from the mean velocity, but will be included in the denominator. For a group with only four members, this reduces the $v_\sigma$ by over 20%. However, such statistical biases cannot provide anything approaching the large factors (~2-3) by which we infer that $v_\sigma$ has been reduced in some of these groups.

Physical effects which might lead to such low values of $v_\sigma$, are discussed in greater detail in Helsdon et al. (2004). Observed galaxy velocity dispersions might be reduced if (a) galaxy orbits decay due to dynamical friction, (b) orbital energy is converted into internal energy of the galaxies via tidal heating, or (c) orientation effects result in most of the galaxy velocity vectors for some systems lying close to the plane of the sky. The last of these has, perhaps, the greatest potential to achieve really substantial reductions in observed line-of-sight velocity dispersions.

7.4 Scaling between $L_B$ and X-ray properties

In an ensemble of self-similar groups with constant mean density, the X-ray luminosity would scale linearly with galaxy mass, and hence with optical luminosity. Helsdon & Ponman (2003) found a much steeper relation, $L_X \propto M_{B}^{2.69\pm0.29}$. Our fitted relation for our full sample of X-ray detected systems is consistent with this (Table 6).

The trend for the G-sample systems (Figure 18) is somewhat flatter (2.05±0.21), but still much steeper than the self-similar expectation. This could be explained in any of three ways:

(a) $f_{\text{gas}}$ rises with system mass,
(b) gas density is higher in more massive systems,
(c) star formation is more efficient in poorer groups.

There are indications that all three of these factors may contribute, but the results of Ponman et al. (1999) and Sanderson et al. (2003) suggest that the dominant effect is probably a reduction in gas density in the inner regions of poor systems, relative to richer ones.

If $T_X$ gives a reliable measure of group size ($R \propto T_X^{0.5}$) and hence mass, as we are assuming here (since we use this relation to define our value of $R_{\text{500}}$), then $L_B \propto T_X^{1.7}$ would result if star formation efficiency were independent of system mass. Our observed relation (Figure 19) has a slope of 1.28±0.19, somewhat flatter than the slope of 1.64±0.23 found by Helsdon & Ponman (2003), but still consistent with the value of 1.5 expected from self-similarity and constant SFE. If, however, the $M$-$T_X$ relation has a slope steeper than the value of 1.5, then our $L_B$-$T_X$ slope of 1.28 suggests a star formation efficiency which is significantly higher in lower mass systems, as discussed in Section 6.

8 $\beta$ AND THE ROLE OF HEATING

Mulchaey & Zabludoff (1998) and Helsdon & Ponman (2003a) found that most X-ray bright groups with data of sufficiently high quality, require two-component $\beta$-models to adequately represent their surface brightness distributions. The central component is identified either with a halo associated with the brightest cluster galaxy (BCG) with Mulchaey & Zabludoff (1998), or a central group cooling region (Helsdon & Ponman 2003b), whilst the outer...
component clearly arises from a group-scale intergalactic medium. Helsdon & Ponman (2000a) investigated the effect of fitting a single component $\beta$-model to a group where a two-component model is more appropriate, and found that the value of $\beta_{\text{fit}}$ obtained with a single-component model typically scattered by $\sim 0.1$ (but in extremis by up to 0.3), either upward or downward from the value for the group component given by a two-component fit. We therefore place more credibility in the two-component results from our present fits.

The largest value of $\beta_{\text{fit}}$ obtained for any of the GEMS groups is 0.58, and the median value from our G-sample fits is 0.45, in good agreement with the value of 0.46 derived by Helsdon & Ponman (2000a). This is clearly well below the typical value, $\beta_{\text{fit}} \approx 0.67$, found in rich clusters (Arnaud & Evrard 1999; Mohr, Mathiesen & Evrard 1999). A trend towards lower values of $\beta_{\text{fit}}$ in poorer clusters has been reported by a number of authors. However, Mohr et al. (1999) found that this trend disappeared when the systems in their study (which all had $T_X \gtrsim 2$ keV) were fitted with two-component models, and hence concluded that the effect was spurious. This explanation cannot account for the low values of $\beta_{\text{fit}}$, obtained here, nor in the studies of Helsdon & Ponman (2000a) or Mulchaey et al. (2003), since two-component fits are employed wherever possible, and found to give $\beta_{\text{fit}} \sim 0.4-0.5$.

However, some uncertainty arises due to the fact that X-ray emission in groups can typically be traced only to a modest fraction of the radii to which they should be virialised (Mulchaey 2000). It has been argued on the basis of simulations (Navarro, Frenk & White 1995), and analytical models (Wu & Xue 2002), that gas density profiles steepen progressively, and hence that low values of $\beta_{\text{fit}}$ naturally arise when profiles are fitted only within $r \sim 0.3 r_{200}$. However there is some evidence that this is unlikely to explain the low values of $\beta_{\text{fit}}$ we observe. Sanderson et al. (2003) examined the effects of truncating the data for galaxy clusters when fitting $\beta$-models, and found little evidence for any significant drop in $\beta_{\text{fit}}$. Moreover observed radial surface brightness profiles are generally found to be modelled remarkably well by simple power laws, outside the central core.

Vikhlinin, Forman & Jones (1999) studied a sample of rich clusters out to $r \sim r_{200}$ with the ROSAT PSPC, and found only a slight steepening (by $\Delta \beta \approx 0.05$) in the outer regions of typical clusters. Rasmussen & Ponman (2004) were able to trace the emission from two rich groups ($T_X \sim 2$ keV) out to $r_{200}$, and found no evidence for steepening of the profiles beyond the simple $\beta$-model fits.

Whilst the $\beta_{\text{fit}}$ values of groups appear to be lower than those of clusters, no previous studies have detected any significant correlation between $\beta_{\text{fit}}$ and $T_X$ within the group regime. Figure 20 shows the relationship between these two variables for the GEMS groups. Results from two-component fits are marked as larger symbols. No correlation is apparent for the G-sample systems; in fact a weak ($1.4 \sigma$) anti-correlation is present in these data. The results for groups with two-component fits (i.e. the most reliable values), show no significant trend at all.

It is interesting to compare the values of $\beta_{\text{fit}}$ and $\beta_{\text{spec}}$ for the GEMS groups, and this is plotted in Figure 21. In the simple case of an isothermal hot gas, and a set of galaxies with isotropic velocity dispersion, both in equilibrium in the gravitational potential of a mass distribution having the $\beta$-model form, one would expect to find $\beta_{\text{fit}} = \beta_{\text{spec}}$. Even though the assumptions underlying this model are restrictive and unrealistic, one might in general expect to find a correlation between the two $\beta$s if heating of the IGM is affecting the gas density profiles, as is often assumed (Cavaliere, Menci & Tozzi 1999; Balogh, Babul & Patton 1999), since energy input into the gas is expected to directly reduce $\beta_{\text{spec}}$, and also to flatten the gas profile, lowering $\beta_{\text{fit}}$ (c.f. Muawong et al. 2002). In practice, no such relationship is seen. $\beta_{\text{spec}}$ covers a much wider range than $\beta_{\text{fit}}$, with many systems having $\beta_{\text{spec}} \sim 1$, and some having extremely low values $\beta_{\text{spec}} \sim 0.1$. However, the latter do not have remarkably low values of $\beta_{\text{fit}}$.

How can we understand the lack of significant correlations involving $\beta_{\text{fit}}$? If group mass, coupled to a simple universal preheating model, were responsible for the flatter profiles in groups compared to clusters, then strong correlations would be seen. Hence, one plausible suggestion

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**Figure 18.** The relationship between $L_X$ and $L_B$. Filled squares represent the G-sample, open circles the H-sample and arrows represent upper-limits from non-detections. The dashed line represents a fit to the G-sample.

**Figure 19.** The relationship between $L_B$ and $T_X$. Filled squares represent the G-sample and open circles the H-sample. The dashed line represents a fit to the G-sample.
is that additional properties peculiar to individual groups, such as star formation efficiency or merger history, play a substantial role, and introduce a large amount of non-statistical scatter. Flat X-ray surface brightness profiles are associated with lower central gas densities and consequently with higher entropy compared to self-similar expectations. Recent results (Ponman, Sanderson & Finoguenov 2003, Pratt & Arnaud 2003, Sun et al. 2003, Mushotzky 2003) suggest that the earlier hypothesis (Ponman et al. 1999) of a universal “floor” value of entropy was incorrect. It appears (Ponman et al. 2003) that entropy scales in a non-self-similar way with system mass, and that there is also significant scatter (Sun et al. 2003, Mushotzky 2003) between the magnitude of the entropy in groups of a given mean temperature. This would lead to scatter in the value of $\beta_{\text{fit}}$, making it hard to detect any trend with temperature without a large and accurately modelled sample. Since biases are present where only one-component fits are performed, we actually have only 15 reliable values of $\beta_{\text{fit}}$ in our sample.

The lack of correlation between $\beta_{\text{fit}}$ and $\beta_{\text{spec}}$, is not obviously explained by this explanation of individual scatter. What is required is some way of breaking the link between the two $\beta$ values. The obvious way to do this is through effects on $\sigma_v$, since the expectation that the two $\beta$s should be related, is based on the assumption that $\sigma_v$ provides a measure of the gravitational potential. We have already seen, from the discussion in Sections 6 and 7.3, that there is good reason to doubt this assumption.

9 GALAXY MORPHOLOGY

9.1 Spiral fraction in groups

Strong correlations between $f_{sp}$ and both $L_X$ and $T_X$ are seen in clusters (Edge & Stewart 1991a). In groups, such trends have proved to be surprisingly weak (Ponman et al. 1996; Mulchaey 2000; Helsdon & Ponman 2003b), despite the strong correlation between X-ray emission and the morphology of the central group galaxy (discussed below). For the G-sample systems, we also find only a weak (1σ) tendency for $f_{sp}$ to be higher in low $L_X$ groups, but the correlations of $f_{sp}$ with $T_X$ and $\sigma_v$ (see Table 6) are stronger, though they still show a large amount of scatter (Figures 22 and 23). This is consistent with what Ponman et al. (1996) found in their study of Hickson compact groups. Since $T_X$ and $\sigma_v$ are primarily determined by the depth of the potential well, whilst $L_X$ is related to the mass and density of hot gas, the relative strengths of these correlations, now found for both loose and compact groups, is that galaxy morphology is related to the depth of the potential rather than its gas content.

Comparing the $f_{sp}$-$T_X$ correlation with that seen in clusters (Edge & Stewart 1991a), there is a large offset between the two relations. The cluster relation shows $f_{sp}$ rising from $\sim 0.1$ in hot clusters like Coma, to $\sim 0.5$ in systems like Virgo, with $T_X = 2-3$ keV. In contrast, a best fit trend through the G-sample $f_{sp}$-$T_X$ data, is fitted by $f_{sp} = 0.26 - 0.93 \log T_X$, corresponding to a typically low value of $f_{sp}$ for groups with $T_X > 1$ keV. Proper comparison of the group and cluster samples requires the application of consistent absolute magnitude limits to all systems, and lies beyond the scope of the present paper, but would be very worthwhile.

Although the relationship between $f_{sp}$ and $L_X$ is not strong within the G-sample, when the full sample is considered, it becomes a great deal stronger (3.5σ), as shown in Figure 24. It is clear that galaxy halo sources, and X-ray undetected sources (which of course have lower $L_X$ than most G-sample groups) tend to have systematically higher $f_{sp}$ than do X-ray bright groups. It seems that the presence of detectable hot intergalactic gas is related to galaxy morphology much more strongly that its luminosity.

In general, metallicities derived from ROSAT PSPC spectra must be regarded with considerable caution, since the spectral resolution of the instrument is very limited, and it is well known that serious biases can result if multi-temperature gas is fitted with a single-temperature hot plasma model (Buote & Fabian 1998). Nonetheless, the 3σ
Figure 22. The relationship between $f_{\text{sp}}$ and $T_X$. Filled squares represent the G-sample and open circles the H-sample. The dashed line represents a fit to the G-sample.

Figure 23. The relationship between $f_{\text{sp}}$ and $\sigma_v$. Filled squares represent the G-sample, open circles the H-sample and crosses non-detections.

Figure 24. The relationship between $f_{\text{sp}}$ and $L_X$. Filled squares represent the G-sample, open circles the H-sample and arrows represent upper-limits from non-detections.

Figure 25. The relationship between $f_{\text{sp}}$ and $Z$. Filled squares represent the G-sample and open circles the H-sample.

Figure 26. The relationship between $f_{\text{sp}}$ and $\bar{\rho}_{\text{gal}}$. Filled squares represent the G-sample, open circles the H-sample and crosses non-detections.
anticorrelation between metallicity and spiral fraction (Figure 25) is sufficiently strong to be worthy of comment. Taken at face value, this would seem to imply that most of the intergalactic metals have their origin in early-type galaxies. Such a result can be understood if the formation of early-type galaxies, either by galaxy merging or through some primordial collapse (or more likely early-eon multiple merging) picture, results in the ejection of much of the enriched interstellar medium of the galaxy due to energy input from type II supernovae (Matteucci & Tornambe 1987; Kauffmann & Charlot 1998). However, the role of biases in ROSAT metallicity estimates is potentially sufficiently serious that this result requires careful checking with CCD quality spectra. This is underway at present.

Finally, in Figure 26 we show the relationship between spiral fraction and mean galaxy density. It was shown by Helsdon & Ponman (2003) that groups display a morphology-density relation rather similar to clusters, in the sense that galaxies in regions of high surface density are more likely to be of early type. Here we see the opposite effect, in terms of the mean density of groups as a whole: there is a tendency, with a great deal of scatter, but significant at the 2.5σ level (Table 6), for groups with the highest mean density to have higher $f_{sp}$. This is not necessarily in conflict with the Helsdon & Ponman (2003a) result, which was a local effect. If all these groups had virialised recently, we would actually expect them all to show the same mean density (as discussed in Section 3 above), so that no correlation at all would be expected between $f_{sp}$ and $\rho_{gal}$, even if a local morphology-density relation were present. The fact that we see a systematic trend, suggests that the range of values of $\rho_{gal}$ that we observe (which span a factor of $\sim 30$) is not simply due to statistical scatter, but is subject to some systematic effects, which are related to the morphological mix in groups. For example, most of the groups with high mean densities significantly higher than the expected value (marked in the Figure) have reasonably high values of $f_{sp}$. This could result from underestimation of their $r_{500}$ values, which are based on gas temperatures for most groups. One explanation could be that these groups are not fully virialised, so that their gas temperature has not yet risen to its final value.

9.2 Brightest group galaxies

The most striking correlation between the X-ray properties of groups, and their galaxy contents, which has been noted since early ROSAT studies of groups (Ebeling, Voges & Boehringer 1994), is the presence of a bright early-type galaxy at the centre of the X-ray emission in virtually every X-ray bright group. This phenomenon is clearly apparent in the GEMS sample, as can be seen from Figure 27. Of our 35 G-sample systems, 32 have an early-type BGG, and in all but four of these, this galaxy lies at the centre of the group’s X-ray halo. As described in Section 3.3 we have defined our “brightest group galaxy” (BGG) to be the most optically luminous within 0.25$r_{500}$ of the group centre, in order to avoid picking up outlying galaxies which may have recently fallen into a group. With this definition, we find that all but three of the systems with group-scale emission (hatched regions) have early-type BGGs. These three exceptions are HCG 16, HCG 48 and HCG 92. HCG 16 is well known as an unusual group dominated by spirals which shows significant intergalactic hot gas (Ponman et al. 1996; Dos Santos & Mamon 1999), and probably corresponds to a system which is collapsed but not yet virialised (Belsome et al. 2003). HCG 92 is the well studied system Stephan’s Quintet, which contains a number of strongly interacting galaxies. None of the member galaxies lie at the centre of the X-ray emission, and high resolution observations (Pietsch et al. 1997; Sulentic et al. 2001) have shown sharp features in the X-ray emission, interpreted as intergalactic shocks. Like HCG 16, this appears to be a newly collapsed group. Finally, in HCG 48 the late-type BGG does appear to lie at the centre of the diffuse X-ray emission, although a bright elliptical is seen 71 kpc away in projection. The unusual properties of this group may be related to the fact that it appears to be falling into the nearby cluster Abell 1060, and its X-ray morphology is distorted into a coma-like shape.

The distribution of spiral fraction in detected and undetected groups can be seen from Figure 27 to differ primarily in that there is a set of groups with high $f_{sp}$ and late-type BGGs, which almost invariably show no group-scale X-ray emission. It can be seen from Figure 28 that these systems (and indeed all groups without detectable group-scale hot gas) also have low velocity dispersions. It seems very likely that these systems are not yet fully collapsed and virialised, so that their IGM has not been heated and compressed to a point where it radiates detectable X-rays. Note however (e.g. from Figure 27 that these H and U-sample systems do not in general have low inferred mean densities. This is not entirely surprising, since they have been selected from group catalogues which are compiled using techniques which rely on a significant overdensity in the inferred 3-dimensional density, typically corresponding, for the catalogues we draw from, to a threshold factor of $\sim 20-80$, relative to the mean density of the Universe – although all our systems appear to lie well above this threshold.

Figure 28 shows a highly significant (6σ, including all points in the plot) tendency for brighter BGGs to be found in richer groups (i.e. with higher total $L_{B}$). A similar, but less significant (2.5σ), correlation exists between $L_{B}$ and $L_{X}$. These relationships are similar in character to those seen in the BCGs, found in richer systems, and represent an extension towards poorer systems of the trends with X-ray luminosity and temperature reported by (Edel 1993). Studies of the K-band luminosities of BCGs (Burke, Collins & Mann 2004; Brough et al. 2004) in clusters spanning a range of redshifts and X-ray luminosities, show a correlation between $L_{X}$ and $L_{B}$, although Brough et al. (2004) argue that this relation is weak in low redshift ($z < 0.1$) clusters. Ours is a low redshift sample, and yet clearly does show such a correlation. This is in accord with the results of Burke et al. (2000), who found BCGs in the most X-ray luminous clusters to be standard candles, whilst for poor clusters ($L_{X} < 10^{44}$ erg s$^{-1}$ in our cosmology) they find that lower luminosity clusters tend to contain less bright BCGs. Our results show that this trend continues through the group regime.

It seems very likely (Dubinski 1998) that BCGs and BGGs are primarily assembled through galaxy merging. This idea is also supported, from the present study, by the fact that early-type BGGs tend to be more luminous (on average by a factor 1.8) than late-type BGGs. Since (other
to their merger into a central remnant (Jones et al. 2003). It has been suggested that the high $L_X/L_B$ ratios may result from high gas density (and hence high $L_X$) resulting from an early formation epoch (Jones et al. 2003), or from an unusually low star formation efficiency, leading to low $L_B$ (Vikhlinin et al. 1999). One might hope to derive some insights into the origin and properties of fossil groups from a study of the optical luminosity ratio between the first and second ranked galaxies ($L_{12}$) in the GEMS sample.

Only one of the GEMS systems qualifies as a fossil group, according to the definition of Jones et al. (2003), which requires $L_X > 10^{42} \, h_{50}^{-2} \, \text{erg s}^{-1}$ ($h_{50} = H_0/50$) and $L_{12} > 6.3$ (2 magnitudes). This system is NGC 741, which safely passes both thresholds. However, it does not display the feature of high $L_X/L_B$, which is a feature of previously studied fossil groups, nor does it display a high $L_X$ for its temperature, which suggest may be another characteristic property of fossil systems. A study of the relationship between $L_{12}$ and other statistical parameters, across the GEMS sample, reveals nothing very striking. For example, given the hypothesised link to merging, one might have expected to see a relationship with the spiral fraction or velocity dispersion of groups. However, neither of these shows any significant correlation (the relationship with $f_{sp}$ is shown in Figure 34), nor is there any very substantial difference between the distribution of $L_{12}$ values for systems with early-type and late-type BGGs.

On the other hand, a parallel optical study of the luminosity function (Miles et al. 2004) has shown the presence of a distinctive dip in the luminosity function at $M_B \sim -18$ (which can be seen in Figure 2), especially in low $L_X$ groups. A study of the structure of GEMS galaxies (Khosroshahi et al. 2004), provides further motivation for the suggestion that this dip might be generated by the effects of galaxy merging, which will generate brighter galaxies, whilst leaving the dwarfs relatively unaffected (due to their small merger cross-sections). If this is the case, then it appears that the opening up of a dip at intermediate magnitudes is not reflected strongly in the difference between first and second ranked galaxies, until the fossil stage is reached. This is understandable if merging affects all the brighter galaxies in a group, rather than simply the central BGG.

10 CONCLUDING DISCUSSION

Although the GEMS groups cannot be regarded as a proper statistically-selected sample, they do span a wider range in group properties than any previous sample subjected to a thorough X-ray analysis and statistical investigation. This has resulted in a number of new results, and some challenges to findings from earlier work. Here we summarise and discuss some of the most important of these.

10.1 $L_X$-$T_X$

It has become widely accepted that the $L_X$-$T_X$ relation steepens in the group regime, following in part the results of Ponman and co-workers, and much theoretical effort has been expended in trying to reproduce this steepening. It therefore comes as something of an embarrassment that the GEMS $L_X$-$T_X$ relation is consistent with an extrapolation

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**Figure 27.** A histogram showing the distribution of $f_{sp}$ for systems dominated by a late type galaxy, and those dominated by an early type galaxy. The shaded region represents the G-sample.

**Figure 28.** A histogram showing the distribution of $\sigma_z$ for systems dominated by a late type galaxy, and those dominated by an early type galaxy. The shaded region represents the G-sample.
of the \( L_X \propto T_X^3 \) trend seen in clusters. As we discussed in Section 7.1 this flatter \( L_X-T_X \) slope cannot be regarded at present as a secure result, since a number of biases resulting from the large scatter in the properties of poor groups, coupled with the observational selection effect against detecting groups with very low \( L_X \), conspire to systematically flatten the fitted relation. However, earlier results (e.g. Helsdon & Ponman 2000) based on X-ray-selected group samples, showing a slope of 4-5, must now be regarded as questionable. The origin of the flatter relation found here, appears to be primarily the inclusion of more groups with very low temperatures, some of which have surprisingly high X-ray luminosities.

Recent developments from studies of the entropy of groups and clusters tend to support the idea of a greater continuity in properties between the IGM in groups and clusters. The idea of a universal “entropy floor” (Ponman et al. 1999), which could have led to an isentropic IGM in the poorest systems (Babul et al. 2002), and hence to an \( L_X-T_X \) slope of \( \sim 5 \), has now been shown to be incorrect in two ways. Firstly, individual groups do not show isentropic cores, as would be expected in such a simple preheating model (Pratt & Arnaud 2003; Ponman et al. 2003; Sun et al. 2003; Mushotzky 2003; Rasmussen & Ponman 2004; Khosroshahi, Jones & Ponman 2004), and secondly the scaling properties of entropy in clusters and groups appears to take the form of a “ramp”, rather than a “floor” (Ponman et al. 2003) - following the non-self-similar power law form \( S \propto T_0^{0.65} \), rather than breaking from the self-similar slope of unity at a well-defined temperature \( T_X \sim 1-2 \) keV, as was previously suggested (Lloyd-Davies, Ponman & Cannon 2000). Given this continuity of properties, a (non-self-similar) power law form for the \( L_X-T_X \) relation is what one would expect.

### 10.2 \( \sigma_v \)

We find several indications that the velocity dispersions of some poor groups are anomalously low. There are groups in our sample, such as HCG 16, HCG 22 and NGC 3665, which appear to have diffuse X-ray emission from a hot IGM (confirmed in the case of NGC 3665 and NGC 1587 by the Chandra observations of Helsdon et al. 2004), and yet have velocity dispersions so low (\(< 100 \) km s\(^{-1}\)) that it is hard to understand how they can be virialised. These groups also have very low values of \( \beta_{\text{spec}} (\lesssim 0.3) \), and if \( \sigma_v \) is used to calculate their overdensity radii, then the inferred values of galaxy density tend to be very high (Figure 10). In Section 7.3 we discussed a number of statistical and physical effects which might lead to low values of \( \sigma_v \), however, statistical scatter cannot account for the lack of poor systems with high values of \( \beta_{\text{spec}} \), and statistical biases seem too weak to account for the very low values we observe. A more detailed investigation is required to determine whether alignment effects or tidal interactions can produce velocity dispersions as low as those observed.

### 10.3 Group radii

In order to make meaningful comparisons between the properties of groups and clusters, it is important to derive physi-
cal values within some well-defined overdensity radius. However, it has become apparent in the present study just how difficult it is to define a reliable value of $r_{200}$ ($r_{200}$ is even more difficult) in galaxy groups. Their low surface brightness prohibits the mapping of gas pressure (which would allow the mass to be inferred) out to large radii, even in X-ray bright groups. Virial analyses are unreliable due to the sparse galaxy populations, and lensing studies unfeasible on individual groups due to their low projected mass densities.

Having investigated the use of scaling formulae based on $\sigma_v$, $T_X$ and $L_B$, we have reservations about all three. $\sigma_v$ appears to be the worst of the three, due to the large unexplained biases in velocity dispersion in some poor groups, discussed above. $T_X$ gives a much more stable and satisfactory estimate of group sizes, but there is some evidence that it may overestimate $r_{200}$ by up to 40% throughout the group regime. $L_B$ also appears to give fairly stable results, but since there are both theoretical and observational reasons to believe that the mass-to-light ratio may drop in low mass systems, a scaling formula based on constant star formation efficiency seems unwise. More work employing deep XMM-Newton observations, to clarify the relationships between group masses and the value for $T_X$ and $L_B$ would be of great value for future scaling studies.

10.4 $\beta_{nt}$

As was discussed in Section 5, it seems curious that the lower value of $\beta_{nt}$ compared to clusters, which we believe to be a robust result, is not reflected in any significant correlation between $\beta_{nt}$ and $T_X$ within the GEMS sample. This appears to be another nail in the coffin of simple preheating models, which would lead to systematically flatter gas density profiles in the shallower potential wells of cool groups. We suggest that in our sample, such a weak trend may be obscured by fluctuations in the values of gas entropy between groups. This in turn may be driven by differences in the merger and star formation histories.

10.5 $f_{sp}$

GEMS groups typically contain a much higher fraction of early-type galaxies than would be expected if one extrapolates the trends between $f_{sp}$ and $T_X$ or $L_X$ established for clusters. This result is almost certainly related to the results of Helsdon & Ponman (2003), who found that X-ray bright groups have lower $f_{sp}$ than clusters, at a given projected density, and even at a given inferred 3-dimensional density. They interpreted this result as evidence that galaxy morphology may be related to the effects of galaxy interactions and mergers, which are enhanced in low velocity dispersion systems.

It seems clear (Figures 24 and 25) that there is a class of groups with low $\sigma_v$, and fairly high spiral fraction (including, in most cases, a late-type BGG) which show no group-scale X-ray emission. Since a hot, X-ray emitting IGM requires a collapsed group, both to heat the gas, and to raise its density to the point where its emission becomes detectable, it seems very probable that these undetected groups are not yet virialised, and represent late-forming groups. In a study of galaxy photometry for a subsample of 25 of the GEMS groups, Miles et al. (2004) find that groups with $L_X < 5 \times 10^{41}$ erg s$^{-1}$ (including some which are undetected) show a pronounced dip in their galaxy luminosity functions, which may result from the effects of recent galaxy merging activity taking place in these low $\sigma_v$ virialising systems.

10.6 BGGs

We confirm the very strong relationship between the presence of intergalactic X-ray emission, and the presence of a centrally located luminous early-type galaxy, which has been noted by many previous authors. This points strongly to the effects of galaxy merging having played an important role during the evolution of these systems. We do, however, find four groups from our G-sample, for which the early-type BGG does not lie at the centre of the X-ray emission, and a further three systems in which the BGG is of late-type, as discussed in Section 5.2 above. The presence of a small fraction of systems in which the BGG is offset is not surprising, given that groups are expected to experience mergers, during which their gravitational potentials will be perturbed. The three G-sample systems with late-type BGGs are all groups with compact cores. Two of them appear to be systems in the process of virialisation, in which the gas has been recently heated, but a luminous early-type BGG has yet to form. The status of HCG-48 is still problematical, and warrants more detailed study with better quality X-ray data.

Our richer groups tend to have more luminous BGGs (Figures 29 and 30), continuing a trend which has been noted in moderately rich clusters. Given the likelihood that these dominant early-type galaxies have been formed through multiple mergers, coupled with the strong inverse dependence of the merger cross-section on $\sigma_v$ (Makino & Hut 1997), the positive correlation seen in Figure 30 strongly suggests that much of this merging has taken place at earlier epochs, in substructures which have since merged to form the groups we observe today, since at the present epoch merging should be more effective in groups with low values of $\sigma_v$.

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