An abstract graphic consisting of several thick, black, curved lines that intersect and overlap, creating a complex, web-like pattern. The lines originate from the left side of the cover and extend towards the right, with some lines curving upwards and others downwards.

P R I N C I P L E S O F

Radiation Interaction

IN Matter and Detection

Claude Leroy

University of Montreal, Montreal, Canada

Pier-Giorgio Rancoita

Istituto Nazionale di Fisica Nucleare, Milan, Italy

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