Fluctuations of fragment observables

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Abstract. This contribution presents a review of our present theoretical as well as experimental knowledge of different fluctuation observables relevant to nuclear multifragmentation. The possible connection between the presence of a fluctuation peak and the occurrence of a phase transition or a critical phenomenon is critically analyzed. Many different phenomena can lead both to the creation and to the suppression of a fluctuation peak. In particular, the role of constraints due to conservation laws and to data sorting is shown to be essential. From the experimental point of view, a comparison of the available fragmentation data reveals that there is a good agreement between different data sets of basic fluctuation observables, if the fragmenting source is of comparable size. This compatibility suggests that the fragmentation process is largely independent of the reaction mechanism (central versus peripheral collisions, symmetric versus asymmetric systems, light ions versus heavy ion induced reactions). Configurational energy fluctuations, that may give important information on the heat capacity of the fragmenting system at the freeze out stage, are not fully compatible among different data sets and require further analysis to properly account for Coulomb effects and secondary decays. Some basic theoretical questions, concerning the interplay between the dynamics of the collision and the fragmentation process, and the cluster definition in dense and hot media, are still open and are addressed at the end of the paper. A comparison with realistic models and/or a quantitative analysis of the fluctuation properties will be needed to clarify in the next future the nature of the transition observed from compound nucleus evaporation to multi-fragment production.

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1 Fluctuations and phase transitions

Since the first inclusive heavy ion experiments, multifragmentation has been tentatively associated to a phase transition or a critical phenomenon. This expectation was triggered by the first pioneering theoretical studies of the nuclear phase diagram [1] which contains a coexistence region delimited, at each temperature below an upper critical value, by two critical points at different asymmetries [2, 3].

Even more important, the first exclusive multifragmentation studies have shown that multifragmentation is a threshold process occurring at a relatively well defined deposited energy [4, 5, 6, 7]. The wide variation of possible fragment partitions naturally leads to important fluctuations of the associated partition sizes and energies.

Different observables have been proposed to measure such fluctuations. Using the general definition of the $n$–th moment as

$$M_n = \sum_{Z_i \neq Z_{\text{max}}} Z_i^n \cdot n_i(Z_i),$$

the variance of the charge distribution is measured by the second moment $M_2$ or by the normalized quantity [8]:

$$\gamma_2 = \frac{M_2 M_0}{M_1^2}.\quad (2)$$

The root mean square fluctuation per particle

$$\sigma_m = \sqrt{\langle (Z_m/Z_0 - \langle Z_m/Z_0 \rangle )^2 \rangle} \quad (3)$$

of the distribution of the largest fragment $Z_m$ detected in each event completes the information. We will also consider the total fluctuation

$$\Sigma_m^2 = \langle Z_0 \rangle \sigma_m^2 \quad (4)$$

and the fluctuation

$$\sigma_k^2 = \langle (E_p/A_0 - \langle E_p/A_0 \rangle )^2 \rangle \quad (5)$$

of the configurational energy per particle associated to each fragment partition $(k)$

$$E_p^{(k)} = \sum_{i=1}^{m_k} (BE)_i + \alpha^2 \sum_{i,j=1}^{m_k} \frac{Z_i Z_j}{|r_i - r_j|} \quad (6)$$
where \( m_k \) is the multiplicity of event \( k \), \( BE \) is the ground state binding energy of each fragment, and \( \langle |r_i - r_j| \rangle \) is the average interfragment distance at the formation time. The quantities \( A_0, Z_0 \) in eqs. (3), (5) represent the reconstructed charge and mass of the fragmenting system, \( Z_0 = \sum_{i=1}^{m_0} Z_i, A_0 = \sum_{i=1}^{m_0} A_i \).

In a simple statistical picture the fluctuation of any observable can be related to the associated generalized susceptibility by

\[
\chi = -\frac{\partial \langle A \rangle}{\partial \lambda} = \langle A^2 \rangle - \langle A \rangle^2
\]

where \( \lambda \) is the intensive variable associated to the generic observable \( A \). Since the intensive variable associated to a particle density \( N/V \) is the susceptibility \( \chi = \partial \langle N \rangle / \partial \mu \), then the large variance of the charge distribution observed in multifragmentation experiments could be connected to the diverging critical point fluctuation which would signal a diverging susceptibility and a diverging density correlation length. The apparent self-similar behavior and scaling properties of fragment yields \( ^9 \) tends to support this intuitive picture.

### 1.1 Finite size effects

Many different effects can however blur this simple connection. First of all, since fragmenting sources cannot exceed a few hundred nucleons, we have certainly to expect finite size rounding effects, which smooth the fluctuation signal \( ^8 \). Not only the transition point is expected to be loosely defined and shifted in the finite system as shown in the three-dimensional percolation model in Figure 1, but also the signal is qualitatively the same for a critical point, a first order transition or even a continuous change or cross over.

Finite size effects have other consequences on the distribution than the simple smoothing of the transition. It has been shown on different model calculations that the presence of conservation constraints as well as the use of different event sorting procedures can sensibly distort the fluctuation observables. To give a simple example, the presence of a peak in the largest fragment’s size fluctuation as a function of the energy deposit is trivially produced by the baryon number conservation constraint which forces this fluctuation to decrease with increasing average multiplicity \( ^{10} \). In the case of a genuine critical behavior as for the percolation model, the fact of sorting events according to the percolation parameter \( p \) or according to some other correlator observable, as for instance the total cluster multiplicity, modifies \( ^{10, 5} \) the behavior of \( m_2, \gamma_2 \), and all other related moments \( ^{11} \) measuring the fluctuation properties of the system. All these effects can be understood in the general framework of the non-equivalence of statistical ensembles for finite systems, which we will discuss in the next chapter.

![Fig. 1. Second moment of the size distribution (see \( ^{11} \) for a precise definition) as a function of the average fragment multiplicity for the three-dimensional percolation model for different lattice sizes. Figure is taken from \( ^{8} \).](image)

### 1.2 Thermal invariance properties

Another problem when trying to connect a fluctuation peak to a phase transition or a critical behavior in a finite system is given by the possible existence of thermodynamic ambiguities. It has been observed by different independent works that in the framework of equilibrium fragmentation models the fluctuation behavior is qualitatively independent of the break up density \( ^{12, 13, 14, 15} \). An example is given in Figure 2 which gives the second moment of the charge \( (S_2 = M_2 - M_1^2) \) and of the energy \( (C_2) \) distribution as a function of temperature in the Lattice Gas model for different break-up densities in the subcritical regime.

A peak in the fluctuation observables can be seen at all densities, at a temperature which is systematically below the critical temperature of the system and close to the first order transition temperature in the thermodynamic limit. A similar behavior has been observed in different fluctuation observables and also at supercritical densities along the Kertesz percolation line, where the system does not present any phase transition. Table 1 gives, as a function of the lattice size, the inverse temperature at which the variable \( S_2 \) shows a maximum in the three-dimensional IMF model \( ^{13} \) at different densities. As a general statement, the fluctuation peak as well as the global scaling properties of the size distribution \( ^{15, 16} \) in these models can be found along a curve in the \( T(p) \) diagram passing through the thermodynamic critical point but extending in the subcritical as well as supercritical region \( ^{17} \). The subcritical behavior can be understood as a finite size effect, when the correlation length, close to the first order transition point, becomes comparable to the linear size of the system, while the supercritical behavior is linked to the definition of clusters in dense and hot media \( ^{17} \). For the subcritical region, a clusterization algorithm has been sug-
It is clear that fluctuations on a given observable $A$ will be suppressed if a constraint is applied to a variable correlated to $A$. This trivial fact has a deep thermodynamic meaning and is linked to the non equivalence of statistical ensembles in finite systems. Indeed the basic statistical relation between a fluctuation and the associated susceptibility eq. (7) is only valid in the ensemble in which the fluctuations of $A$ are such as to maximise the total entropy, under the constraint of $\langle A \rangle$ (“canonical” ensemble). The thermodynamics in the ensemble where the generic observable $A$ is controlled event by event (“microcanonical” ensemble), or in the ensemble where $\sigma_A$ is externally fixed (“gaussian” ensemble) is a perfectly defined statistical problem, but the thermodynamic relationships have to be explicitly worked out. As an example we show in Figure 3 the correlation between the size of the largest cluster $A_{\text{big}}$ and the total energy in the isobar Lattice Gas model at the transition temperature. The presence of two energy solutions at the same temperature and pressure clearly shows that the transition is in this case first order. The $A_{\text{big}}$ fluctuation properties are very different in the canonical ensemble (left part) and in the microcanonical ensemble (right part) at the same (average) total energy. Because of the important correlation between the total energy and the fragmentation partition, fragment size fluctuations can be compared only for samples with comparable widths of the energy distribution.

From the experimental viewpoint, different constraints apply to fragmentation data and have to be taken into account. Apart from the sorting conditions, the collisional dynamics can also give important constraints to the fragmentation pattern (e.g. flows, deformation in r-space and p-space). This means that fluctuations have to be compared with calculations performed in the statistical ensemble corresponding to the pertinent experimental constraints.

2.2 Fluctuations and susceptibilities

In the last subsection we have stated that a connection between a fluctuation and the associated susceptibility can always be in principle worked out if the constraints acting


3

Fig. 2. Second moment of the charge ($S_2$) and of the energy ($C_v$) distribution as a function of temperature in the Lattice Gas model for different densities for a system of linear dimension $L=7$. Arrows: first order transition temperature in the thermodynamic limit. Figure taken from ref. [14].

Table 1. Inverse temperature at which the second moment $S_2 = M_2 - M_1^2$ is maximal for different densities and lattice sizes in the three-dimensional IMFM model. Taken from ref. [13].

<table>
<thead>
<tr>
<th>$L$</th>
<th>$\beta_c (\rho = .3)$</th>
<th>$\beta_c (\rho = .5)$</th>
<th>$\beta_c (\rho = .7)$</th>
</tr>
</thead>
<tbody>
<tr>
<td>10</td>
<td>.2560(5)</td>
<td>.225(3)</td>
<td>.1942</td>
</tr>
<tr>
<td>16</td>
<td>.2440(2)</td>
<td>.223(5)</td>
<td>.1984</td>
</tr>
<tr>
<td>20</td>
<td>.2396(10)</td>
<td>.227(4)</td>
<td>.1990</td>
</tr>
<tr>
<td>24</td>
<td>.2367(3)</td>
<td>.227(2)</td>
<td>.2005</td>
</tr>
</tbody>
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on the observable are known. In the case of sharp constraints (e.g. fixed total mass, charge, deposited energy), the connection between the fluctuation on a variable correlated to the constraint (e.g. size or charge of the largest fragment, configurational energy) and the associated susceptibility are in many cases analytical [27, 28, 29]. If a conservation constraint $A = A_1 + A_2 = \text{cst}$ applies and the system can be split into two statistically independent components such that $W(A) = W(A_1)W(A_2)$, then the partial fluctuations are linked to the total susceptibility by

$$\frac{\chi_i}{\chi} = 1 - \frac{\sigma_i^2}{\sigma_{\text{ref}}^2},$$

where $\chi_{\text{ref}}^{-1} = \partial^2 A / \partial W_i$, $\sigma_{\text{ref}}^2$ is the fluctuation of $A_1$ in the ensemble where only the average value $\langle A \rangle$ is constrained, and we have approximated the distribution of $A_1$ with a Gaussian [24]. The case of the total energy constraint has been particularly studied in the literature. Indeed the total energy deposit can be (approximately [30]) measured event by event in $4\pi$ experiments, allowing to experimentally construct a microcanonical ensemble by sorting. For classical systems with momentum independent interactions the potential energy fluctuation $\sigma_A^2$ at a fixed total energy is linked to the total microcanonical heat capacity by

$$\frac{C_k}{C} = 1 - \frac{\sigma_k^2}{\sigma_{\text{can}}^2},$$

where $C_k, C$ are the kinetic and total heat capacity, $\sigma_k^2 = \sigma_A^2$ and $\sigma_{\text{can}}^2 = k_B T^2$ is the kinetic energy fluctuation in the canonical ensemble. Apart from the microstate equiprobability inherent to all statistical calculations, the above formula is obtained in the saddle point approximation for the partial energy distributions. The contribution of non gaussian tails can be also analytically worked out [28] and has been found to be negligible in all theoretical as well as experimental data samples analyzed so far [21]. An example of the quality of the approximation is given in Figure 4 which gives the temperature, normalized potential energy fluctuation and heat capacity in the isobar Lattice Gas model for a system of 108 particles.

Fig. 3. Center: correlation between the largest fragment’s size and the total energy in the isobar Lattice Gas model close to the transition temperature, for a system of 216 particles. Left side: projection over the $A_{\text{big}}$ direction. Right side: same as the left side, but only events within a narrow energy interval around the average energy have been retained.

Fig. 4. Temperature, normalized binding energy fluctuation and heat capacity in the microcanonical isobar Lattice Gas model as a function of the total energy for a system of 108 particles. In the lower panel the heat capacity estimated from fluctuations via eq. (9) (dots) is compared to the exact expression from the entropy curvature (line). Figure is taken from [31].

3 Experiment

3.1 Effect of the sorting variable

In this section we turn to compare different sets of experimental data available in the literature. A special attention has been paid by different collaborations to the largest fragment fluctuation $\sigma_m$ eq. (3) and to the $\gamma_2$ observable eq. (2) [31, 32, 33, 34, 35, 36]. For all data sets of comparable total size these observables, as well as the others we will show in the next subsections, show a well defined peak at comparable values of the chosen sorting variable. This is an important and non trivial result considering that data are taken with different apparata and the multifragmenting systems are obtained with very different reaction mechanisms. The effect of the sorting variable is explored in table 2 that gives the maximum value of $\gamma_2$ and $\sigma_m$ with different data sets sorted in bins of the total measured bound charge $Z_{\text{bound}}$, total measured charged particles multiplicity $m$, or calorimetric excitation energy $\gamma_2$. Even if the systematics should certainly be completed and errors should definitely be evaluated, we can observe from table 2 that different data sets show a reasonable agreement when the same sorting is employed.

We can also note that a higher $\gamma_2$ is systematically obtained when data are analyzed in bins of total charge multiplicity, with respect to a sorting in $Z_{\text{bound}}$. This can be qualitatively understood if we recall that $\gamma_2$ measures the variance of the charge bound in fragments, and this quantity is obviously strongly correlated with $Z_{\text{bound}}$ and loosely correlated with $m$. The calorimetric excitation energy sorting leads to comparable results to the multiplicity
The effect of the system size is further analyzed in table 3. All presented data are sorted in bins of calorimetric excitation energy. The fluctuation properties of quasi-projectile decay appear to be largely independent of the target. This well-known behavior at relativistic energy\[5\] appears confirmed in the case of the Nimrod experiment\[37\] which was performed with a beam energy as low as 47 MeV/A. This suggests that a quasi-projectile emission source can be extracted\[7\] in spite of the important midrapidity contribution in the Fermi energy regime\[19\].

To conclude, we have seen that fluctuations can vary of a factor two changing the sorting variable. This stresses the need of confronting the experimental data with statistical predictions containing the same constraints, i.e. performed in the adapted statistical ensemble. Interesting enough, when the same sorting is adopted the different available data sets agree within \( \approx 15\% \) both in the value of the peak and in the position where the peak is observed. More data are needed to confirm these trends.

### 3.3 Configurational energy fluctuations

One of the most interesting aspects of studying fluctuation observables, is their possible connection with a susceptibility or a heat capacity via eq.\[9\]. Configurational energy fluctuations have been studied at length by the Multics collaboration\[38, 39, 40\] and by the Indra collaboration\[39, 41-43\] on Au sources. The observable used in these studies is an estimation of the energy stored in the configurational degrees of freedom at the time of fragment formation, defined as follows

\[
E_I = \sum_{i=1}^{N_{imf}} Q(Z_i^p, A_i^p) + \sum_{i=1}^{N_{imf}} Q(Z_i, A_i) M_i^p + V_{coul} \langle \{Z_i^p\}, V_{FO} \rangle
\]

where \( Q \) indicates the mass defects and \( V_{coul} \) the coulomb energy. The measured fragment charges \( Z_i \) and lcp multiplicities \( M_i \) are corrected in each event to approximately account for secondary decay

\[
Z_i^p = Z_i + \langle M_{He}^v + 2M_{He}^v \rangle \frac{Z_i}{\sum_{i=1}^{N_{imf}} Z_i} \quad (11)
\]

\[
M_i^p = M_i - \langle M_i^v \rangle \quad (12)
\]

where \( \langle M_i^v \rangle \) is the estimated multiplicity of secondary emitted light charged particles for each calorimetric excitation energy bin.

Three quantities need to be estimated in each excitation energy bin to compute \( E_I \).
The fluctuation in the canonical ensemble can be written as:

\[ \sigma^2_{\text{can}} = c_k T^2 \]

The kinetic heat capacity \( c_k \) is calculated from the measured fragment yields. We can see that the fluctuation peak overcomes the upper classical limit \( c_k = 3/2 \) suggesting a negative heat capacity as expected in a first order phase transition analyzed in the micro-canonical ensemble.

The same analysis performed on Indra data of central Xe+Sn collisions at different bombarding energies leads to compatible temperatures and volumes and a fluctuation estimation that agrees within 25% with the presented Multics results, as shown for the 32 A.MeV data in figure [9] (upper part). In the absence of isotopic resolution for fragments, Coulomb repulsion cannot be distinguished from a radial collective expansion due to a possible initial compression. If an important radial flow component is assumed for these central collisions, data can also be compatible with a bigger freeze out volume (lower part of the figure) leading to a shift of the abnormal fluctuation behavior towards lower energy. This volume/flow ambiguity in central collisions can only be solved with third generation multidetectors.

Indra data on the same Au quasi-projectile analyzed by the Multics collaboration lead to a fluctuation measurement about 40% lower, see figure [8]. This difference is tentatively explained as an effect of emission from the neck which leads to a reduced occupation of the available phase space.

Recent Nimrod data on the fragmentation of a much lighter system show a similar value for the energy corresponding to the fluctuation peak, but fluctuation a factor 10 lower than for Multics data, as shown in figure [9]. If we consider the global fluctuation \( \langle A_0 \rangle \) without the normalization to the estimated temperature, this factor is reduced to about a factor 4. These results go in the same direction as the general behavior of \( \sigma^2_{\text{can}} \) that we have analyzed in section 4.2. Recall that the fluctuation of the biggest fragment for the quasi-Au source is a factor 6.8 higher than for the quasi-Ar. This fluctuation reduction seems then to be a general feature of light systems fragmentation and has been tentatively explained as an effect of the higher temperature that light systems can sustain.

In this interpretation, a higher temperature region of the phase diagram, possibly above the critical point, is explored in the fragmentation of light systems, and the first order phase transition observed in heavy nuclei becomes a smooth cross over.

As a general remark, the configurational energy fluctuation signal is a very interesting one due to its possible connection with a heat capacity, but it is also a very...
indirect and fragile experimental signal which needs precise calorimetric measurements, a careful data analysis, extensive simulations to assess the effect of the different hypotheses in the event sorting and reconstruction procedure. Moreover the different techniques to exclude or minimize pre-equilibrium and neck emission seem to have a strong influence in the absolute value of fluctuations.

The evaluation of systematic errors in fluctuation measurements is necessary to achieve a quantitative estimation of fluctuations: some first encouraging results in this direction have been presented in ref. \[40\]. The confirmation (or infirmation) of the fluctuation enhancement is certainly one of the most important challenges of the field in the next years with third generations multidetectors.

4 Open questions

The possibility of accessing a thermodynamic information on the nuclear phase diagram from measured fragment properties entirely relies on the representation of the system at the freeze out stage as an ideal gas of fragments \[26\] in thermal equilibrium. This is true for fluctuation observables as well as for all other thermodynamic analyses \[44,9\]. This is an important conceptual point which is presently largely debated in the heavy ion community.

A first open question concerns the structure of the systems at the freeze out stage, i.e. at the time when fragments decouple from each other. Contrary to the ultra-relativistic regime \[50\], we do not expect much difference between the chemical and kinetic decoupling times due to the small collective motions implied in these low energy collisions. We can therefore speak at least in a first approximation of a single freeze out time. If at this time the system is still relatively dense, the cluster properties may be very different from the ones asymptotically measured, and the question arises \[17\] whether the energetic information measured on ground state properties can be taken backward in time up to the freeze out. Calculations from classical molecular dynamics \[51\] show that the ground state Q-value is a very bad approximation of the interaction energy of Hill clusters in dense systems. This is due both to the deformation of clusters when recognized in a dense medium through the Hill algorithm, and to the interaction energy among clusters in dense configurations where clusters surfaces touch. As a consequence, comparable fluctuations are obtained in the subcritical and supercritical region of the Lennard-Jones phase diagram. This result is shown in fig. \[13\]. Calculations in a similar model, the Lattice Gas model, show that even in the supercritical...
regime the correct fluctuation behavior can be obtained if both the total energy and the interaction energy are consistently estimated with the same approximate algorithm as it is done in the experimental data analysis [52]. Indeed the high value of the estimated configurational energy $Q$ fluctuations is essentially due to the spurious fluctuation of the total energy $E_K + E_I$ obtained when $E_I$ is estimated through $Q$: such an effect is eliminated if data are analyzed in bins of $E_K + Q$. This calculation is shown in fig. 11.

A second related question which needs further work is the relevance of the equilibrium assumption at freeze out. Molecular dynamics models applied to study the time evolution of the reaction [21, 53–55] predict that the decoupling between fragment degrees of freedom (freeze out) occurs very rapidly during the reaction. At this stage however the configuration is considerably diluted due to the early presence of collective motions [21, 20]. An example taken from classical molecular dynamics for an initially equilibrated compact configuration freely evolving in the vacuum, is shown in fig. 12. At this reaction stage cluster energies may be well approximated (within a side feeding correction) by their asymptotically measured values, but it is not clear whether this configuration can correspond to an equilibrium, more precisely whether the hypothesis of equiprobability of the different charge partitions holds.

5 Conclusions and outlooks

In this paper we have presented a short review of the experimental as well as theoretical studies of fluctuation observables of fragments produced in a multifragmentation heavy ion reaction. The aim of these studies is the understanding of the nature of the nuclear fragmentation transition as well as the thermodynamic characterization of the finite temperature nuclear phase diagram. This vast and ambitious program is still in its infancy. Many promising results already exist, but the analyses are not yet conclusive and need to be intensively pursued in the future.
The nuclear fragmentation phenomenon, well documented by a series of independent experiments\[7\], presents many features compatible with a critical phenomenon\[11\] or a phase transition\[9,25\]. Only a careful study of fluctuation properties will allow to discriminate between the different scenarios. Even more important, the phase diagram of finite nuclei is theoretically expected to present an anomalous thermodynamics\[49,48\] which should be characteristic of any non extensive system undergoing first order phase transitions in the thermodynamic limit. Once the difficulties linked to the imperfect detection and sorting ambiguities will be overcome, fluctuation observables will be a unique tool to quantitatively study this new thermodynamics with its interdisciplinary applications\[49,48,56\].

From the theoretical point of view, the theoretical connections between fluctuations and susceptibilities in the different statistical ensembles are well established, and the different experimental contraints can be consistently adressed by the theory. However, the evaluation of a thermodynamics for a clusterized system opens the difficult theoretical problem of cluster definition in dense quantum media. To produce quantitative estimations of measurable fluctuation observables the pertinence of classical models has to be checked through detailed comparisons with microscopic\[54\] and macroscopic\[26\] nuclear models.

On the experimental side, multiplicities and size fluctuations agree reasonably well if comparable size fragmentations are studied, even if the effect of the system size has to be clarified. Configurational energy fluctuations are especially interesting because of their possible connection with a heat capacity measurement. The methodology to extract such fluctuations from fragmentation data is presently under debate, in particular a careful analysis of systematic errors is presently undertaken\[40\]. From a more conceptual point of view, the influence of the different time scales in the reaction dynamics has to be clarified. Configurational energy fluctuations may be subject to strong ambiguities since they use information from all the particles of the event, and this information is integrated over the whole reaction dynamics. In this respect, an interesting complementary observable may be given by fluctuation of the heaviest cluster size\[25,29\].

To solve the existing ambiguities we need full comparisons with a well defined protocol and consistency checks between different data sets. The simultaneous measurement of fragments mass and charge on a 4π geometry\[57\] will be essential to measure the basic variable of any thermodynamic study, namely the deposited energy. No definitive conclusion about the occurrence of a thermodynamic phase transition and its order can be drawn without this detection upgrade.

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