Centrality dependence of proton and antiproton spectra in Pb+Pb collisions at 40A GeV and 158A GeV measured at the CERN SPS


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Abstract

The yields of (anti-)protons were measured by the NA49 Collaboration in centrality selected Pb+Pb collisions at 40A GeV and 158A GeV. Particle identification was obtained in the laboratory momentum range from 5 to 63 GeV/c by the measurement of the energy loss $dE/dx$ in the TPC detector gas. The corresponding rapidity coverage extends 1.6 units from mid-rapidity into the forward hemisphere. Transverse mass spectra, the rapidity dependences of the average transverse mass, and rapidity density distributions were studied as a function of collision centrality. The values of the average transverse mass as well as the midrapidity yields of protons when normalized to the number of wounded nucleons show only modest centrality dependences. In contrast, the shape of the rapidity distribution changes significantly with collision centrality, especially at 40A GeV. The experimental results are compared to calculations of the HSD and UrQMD transport models.

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I. INTRODUCTION

It is generally accepted that heavy ion collisions at ultra-relativistic energies result in a fireball of matter with high density and temperature. Such conditions prevail, when the incoming nucleons deposit enough of their kinetic energy in the reaction zone. Little is known about this stopping process and about possible differences between the stopping of the incident nucleons in elementary nucleon-nucleon interactions and nucleus-nucleus collisions. In a simple microscopic picture each nucleon interacts only once in elementary interactions, whereas in central nuclear collisions multiple interactions prevail. There are three methods to study nuclear stopping. In proton-nucleus (p+A) collisions the difference between the c.m.-energies of the incident and the most forward going nucleon is a good measure of the stopped energy. This type of analysis has been pioneered in reference [1]. Another approach to study effects due to multiple projectile nucleon collisions employs symmetric collisions of nuclei of different size. The resulting distributions of participating nucleons in terms of longitudinal and transverse momenta may vary with the size of the incident nuclei. Such differences reflect the change of stopping power as a function of system size. Finally, the effective system size can be changed by varying the impact parameter in collisions between heavy nuclei. Here again the momentum distribution of participating nucleons may be different in central and peripheral collisions as a consequence of changes in the stopping behavior.

Energy loss in central collisions was studied as a function of beam energy at AGS in Brookhaven [2], at CERN SPS in Geneva [3] and at RHIC in Brookhaven [4]. It was found that the rapidity distribution changes from a convex to a concave form from AGS to RHIC via SPS energies. At AGS energies the energy loss was also studied as a function of collision centrality [2]. A strong centrality dependence was observed. This topic has also been addressed by NA49 in two previous publications. The first one presents the net-proton distribution for central Pb+Pb collisions at 158A GeV [3]. The second one describes the measurement of midrapidity proton and antiproton yields in Pb+Pb collisions at various energies from 20A to 158A GeV as well as for different centralities at 158A GeV [5]. At RHIC the PHOBOS collaboration has published the centrality dependence of the rapidity density at midrapidity and the transverse mass spectra of net protons [6] at $\sqrt{s_{NN}} = 62.4$ GeV and charged particle pseudorapidity distributions [7, 8] at $\sqrt{s_{NN}} = 19.6$ GeV, 62.4 GeV, and 130 GeV. Data on centrality dependent particle production at $y = 0$ and $y = 1$ in
Au+Au collisions at $\sqrt{s_{NN}} = 200$ GeV \cite{9} are available from the BRAHMS collaboration. The STAR collaboration has published Au+Au data on the centrality dependence of proton and antiproton production for $|y| < 0.5$ at $\sqrt{s_{NN}} = 130$ GeV \cite{10}.

In this paper we present the centrality dependence of proton and antiproton transverse mass and rapidity distributions in Pb+Pb collisions at 40$A$ GeV and 158$A$ GeV as obtained with the NA49 detector \cite{11}. The phase space coverage extends in center-of-mass rapidity $y$ from mid-rapidity 1.6 units into the forward hemisphere and ranges from zero to 2.0 GeV/c in transverse momentum $p_T$. Net-proton distributions at 158$A$ GeV are obtained from those of all protons by subtracting the distributions of antiprotons. This analysis supplements the NA49 data on $\pi$, K, $\phi$, $\Lambda$ production as function of beam energy at the CERN SPS \cite{12–14}. Pion and kaon production in Pb+Pb collisions at 40$A$ GeV and 158$A$ GeV is analyzed as function of centrality with the same method and is the subject of a separate paper \cite{15}.

II. EXPERIMENTAL SETUP AND DATA SETS

The NA49 detector is a large acceptance hadron spectrometer at the CERN SPS \cite{16}. The main components are four large time projection chambers (TPCs) and two super-conducting dipole magnets with a 1 m vertical gap, aligned in a row, and a total bending power of 9 Tm. Two 2 m long TPCs (VTPCs) inside the magnets each with 72 pad-rows along the beam direction allow for precise tracking, momentum determination, vertex reconstruction, and particle identification (PID) by the measurement of the energy loss ($dE/dx$) in the detector gas. The other two TPCs (MTPCs) have large dimensions (4m x 4m x 1.2m, 90 pad-rows) and provide additional momentum resolution for high momentum particles as well as PID by $dE/dx$ measurement with a resolution of around 4%. Two time-of-flight scintillator arrays of 891 pixels each, situated just behind the MTPCs symmetrically on either side of the beam axis, supplement particle identification in the momentum range from 1 to 10 GeV/c. A Veto Calorimeter (VCAL), which is placed further downstream along the beam and covers the projectile spectator phase space region, is used to select event centrality. The NA49 detector is described in detail in reference \cite{16}. The Pb beam had a typical intensity of $10^4$ ions/s and impinged on a target Pb foil with a (areal) density of 224 mg/cm$^2$. It passed through a quartz Cherenkov detector from which the start signal for the time-of-flight measurement was obtained, and three stations of multi-wire proportional chambers which measured the trajectories of individual beam particles. A minimum bias trigger was derived from the signal
TABLE I: Cross section fractions in % centrality, average numbers of wounded nucleons \( \langle N_w \rangle \), and numbers of analyzed events for the five centrality classes at 40A GeV and 158A GeV. Only systematic errors are quoted.

<table>
<thead>
<tr>
<th>centrality class</th>
<th>centrality [ % ]</th>
<th>( \langle N_w \rangle )</th>
<th>analyzed events</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td></td>
<td>40A GeV</td>
</tr>
<tr>
<td>C0</td>
<td>0-5</td>
<td>351 ± 3</td>
<td>13034</td>
</tr>
<tr>
<td>C1</td>
<td>5-12.5</td>
<td>290 ± 4</td>
<td>22971</td>
</tr>
<tr>
<td>C2</td>
<td>12.5-23.5</td>
<td>210 ± 6</td>
<td>34035</td>
</tr>
<tr>
<td>C3</td>
<td>23.5-33.5</td>
<td>142 ± 8</td>
<td>32668</td>
</tr>
<tr>
<td>C4</td>
<td>33.5-43.5</td>
<td>93 ± 7</td>
<td>32071</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>158A GeV</td>
</tr>
<tr>
<td>C0</td>
<td>0-5</td>
<td>352 ± 3</td>
<td>15306</td>
</tr>
<tr>
<td>C1</td>
<td>5-12.5</td>
<td>281 ± 4</td>
<td>23548</td>
</tr>
<tr>
<td>C2</td>
<td>12.5-23.5</td>
<td>196 ± 6</td>
<td>37053</td>
</tr>
<tr>
<td>C3</td>
<td>23.5-33.5</td>
<td>128 ± 8</td>
<td>34554</td>
</tr>
<tr>
<td>C4</td>
<td>33.5-43.5</td>
<td>85 ± 7</td>
<td>34583</td>
</tr>
</tbody>
</table>

of a gas Cherenkov device right behind the target. Only interactions which reduce the beam charge and thus the signal seen by this detector by at least 10% are accepted. The interaction cross section thus defined is 5.7 b. The contamination by background events remaining after cuts on vertex position and quality amounts to less than 5% for the most peripheral collisions and is negligible for near-central collisions (see [17]). The resulting event ensemble was divided into five centrality classes C0, C1, C2, C3, and C4 (see Table I and [17]). The centrality selection is based on the forward going energy of projectile spectators as measured in VCAL. The number of projectile spectator nucleons and the average number of interacting (wounded) nucleons \( \langle N_w \rangle \) were calculated from the selected cross section fractions using the Glauber approach. The track finding efficiency and \( dE/dx \) resolution were optimized by track quality criteria. To be accepted, a track must have at least 50 (out of a maximum of 90) potential points in the MTPCs and have at least 5 measured and 10 potential points in one of the VTPCs. Finally, tracks were required to have azimuthal angles within +/- 30 degrees with respect to the bending plane in order to minimize reconstruction inefficiencies.
and to optimize the accuracy of the $dE/dx$ measurements.

III. ANALYSIS METHOD

![Graph](image)

**FIG. 1:** a) The most probable specific energy loss $\hat{\epsilon}$ for particle species $\pi^+$, $K^+$ und $p$ as a function of total momentum $p$. The points show results extracted from data whereas the lines indicate the Bethe-Bloch parametrizations optimized for the NA49 measurement. b) The ratios of the Bethe-Bloch parametrizations ($e_i$) to $\hat{\epsilon}_i$ from data are shown as function of laboratory momentum. The index $i$ stands for $p$ and $\bar{p}$.

The protons are identified by the measurement of their specific energy loss in the relativistic rise region. As an appropriate measure of $dE/dx$ we calculated for each track the truncated mean of the distribution of charges measured in each pad row of the MTPCs. Their raw yields were extracted by fitting the function $F$ to the $dE/dx$ distribution of all positively charged particles in narrow bins of total momentum $p$ and transverse momentum $p_T$ [18]. Antiproton yields are determined from the $dE/dx$ distributions of all negatively charged particles with the same method at 158A GeV. At 40A GeV the antiproton statistics was very low and did not allow reliable extraction of yields. The shape of $F$ is assumed to be the sum of Gaussians. Their parameters depend on the particle masses and the measured track lengths. We modified the Gaussian functions by means of an extra asymmetry parameter to account for tails of the Landau distributions which are still present even after truncation.

The function $F$ reads

7
\[
F \left( \frac{dE}{dx} \right) = \sum_{i=d,p,K,e} A_i \frac{1}{\sum_l n_l} \frac{n_l}{\sqrt{2\pi \sigma_{i,l}}} \exp \left[ -\frac{1}{2} \left( \frac{e_i(p) - \hat{e}_i(p)}{(1 \pm \delta)\sigma_{i,l}} \right)^2 \right].
\]  

(1)

Here \( \frac{dE}{dx} \) (abbreviated \( e \)) is the measure of specific ionization, and \( \hat{e} \) is its most probable value. The other parameters of the function are:

- \( A_i \): the raw yield of the particle \( i \) under consideration in a given phase space bin.

- \( n_l \): the number of tracks in a given track length interval \( l \). The second sum together with the normalization \( \sum_l n_l \) forms the weighted average of the track ensembles in each phase space interval.

- \( \sigma_{i,l} \): the width for the asymmetric Gaussian of particle type \( i \) in length interval \( l \).

- \( \delta \): the asymmetry parameter.

The amplitude parameters \( A_i(p,p_T) \) were determined by a maximum likelihood fit to the \( dE/dx \) histogram in each \( p, p_T \) bin. The peak positions \( \hat{e}_i(p) \) are considered to be \( p_T \) independent and were determined by fits to the \( p_T \) integrated distributions in all \( p \) bins. The fitted peak positions \( \hat{e}_i(p) \) for \( \pi^+, K^+ \) and \( p \) are compared to a parametrization of the momentum dependence of the most probable energy loss determined for the NA49 detector in Fig. 1a. The relative differences between fitted (anti-)proton positions and the Bethe-Bloch parameterization are smaller than 5\% (see Fig. 1b). We have verified that the peak positions do not depend on centrality. The widths of the Gaussians \( \sigma_{i,l} \) depend on the particle type \( i \) and on the track length \( l \) according to \( \sigma_{i,l} = \sigma \cdot (\hat{e}_i/e_\pi)\alpha(1/\sqrt{l}) \). The exponent \( \alpha \) \((= 0.625)\) was extracted from simultaneous fits to \( m^2 \) distributions from

FIG. 2: Raw yields of protons at 40A GeV (a), protons (b) and antiprotons (c) at 158A GeV are shown as function of center-of-mass rapidity \( y \) and \( p_T \) for centrality class C2.

The amplitude parameters \( A_i(p,p_T) \) were determined by a maximum likelihood fit to the \( dE/dx \) histogram in each \( p, p_T \) bin. The peak positions \( \hat{e}_i(p) \) are considered to be \( p_T \) independent and were determined by fits to the \( p_T \) integrated distributions in all \( p \) bins. The fitted peak positions \( \hat{e}_i(p) \) for \( \pi^+, K^+ \) and \( p \) are compared to a parametrization of the momentum dependence of the most probable energy loss determined for the NA49 detector in Fig. 1a. The relative differences between fitted (anti-)proton positions and the Bethe-Bloch parameterization are smaller than 5\% (see Fig. 1b). We have verified that the peak positions do not depend on centrality. The widths of the Gaussians \( \sigma_{i,l} \) depend on the particle type \( i \) and on the track length \( l \) according to \( \sigma_{i,l} = \sigma \cdot (\hat{e}_i/e_\pi)\alpha(1/\sqrt{l}) \). The exponent \( \alpha \) \((= 0.625)\) was extracted from simultaneous fits to \( m^2 \) distributions from
TOF and to $dE/dx$ distributions from the TPCs [18]. The momentum averaged widths $\langle \sigma \rangle$ were determined for each centrality bin by fits to the data in the whole $p$ range. These momentum averaged widths $\langle \sigma \rangle$ turned out to be approximately 4% for each centrality bin. $\delta$ was studied by fits with the asymmetric Gaussians. Since it did not show any significant variation with centrality, total and transverse momentum [11], this parameter was fixed to a constant value (0.071). The total number of fit parameters for each $p$, $p_T$ bin is 9. The raw yields were transformed from a fine grid in $\log(p)$, $p_T$ to a coarser grid in $y$, $p_T$. Examples of the transformed results for centrality class C2 are shown in Fig. 2.

A. Acceptance and inefficiency

The raw particle yields have to be corrected for losses due to tracks which do not pass through the detectors or which do not fulfill the acceptance criteria (acceptance losses) and tracks which are not properly reconstructed (efficiency losses). The acceptance was calculated by generating a sample of (anti-)protons with flat distributions in transverse momentum and rapidity. The generated particles were propagated through the detectors (and the magnetic field) using the programs provided in the GEANT 3.21 [19] package. Along the resulting trajectories realistic detector signals were generated and processed in exactly the same way as the experimental data. The ratio of generated to accepted particle tracks in each $y$, $p_T$ bin is the acceptance correction factor. In addition to the well-defined corrections necessary to correct for the limited and constrained acceptance, the raw spectra may be subject to losses due to detector occupancy and thus centrality dependent inefficiencies. These losses were minimized by restricting the analysis to tracks with azimuthal emission angles within $\pm$ 30 degrees with respect to the bending plane and in the bending direction. The remaining losses were determined by the following procedure: Ten GEANT generated (anti-)proton tracks and their signals were embedded into raw data of real events. Only those tracks are embedded which pass all acceptance criteria. These modified events are reconstructed with the standard reconstruction chain. The ratio of all generated tracks to those reconstructed constitutes the applied correction factor for reconstruction inefficiencies. The resulting efficiencies vary with centrality by less than 5% and are over 95% in most $y$, $p_T$ bins. In the further analysis the bin size in rapidity of the antiproton spectra (see Fig. 2c) was doubled in order to reduce the statistical errors. The one in $p_T$ was also doubled at 40A GeV.
B. Feed-down corrections

The measured (anti-)proton yield contains (anti-)protons from weak hyperon decays, namely of the Λ (¯Λ), the Σ⁰ (¯Σ⁰), and the Σ⁺ (¯Σ⁻). The (anti-)proton contribution from Σ⁺ (¯Σ⁻) decays is determined by scaling the estimated feed-down correction coming from Λ (¯Λ) by the ratio Λ / Σ⁺ (¯Λ/ ¯Σ⁻) derived from a statistical hadron gas model [20] thus assuming the same phase space distributions for Λ (¯Λ) and Σ⁺ (¯Σ⁻) hyperons. To determine the feed-down correction $n_{fd}$ from Λ (¯Λ) in each measured phase space bin, we used a similar procedure as for the efficiency calculation. Λ (¯Λ) were generated according to distributions measured by NA49 [14, 21] and embedded into real events. Those (anti-)protons from embedded Λ (¯Λ) decays, which are reconstructed and accepted by the track selection cuts as such, have to be subtracted from the (anti-)proton yield after proper normalization per event (see Eq. (2)). In reference [14, 21] the measured Λ (¯Λ) include the Λ (¯Λ) from electromagnetic decays of Σ⁰ und ¯Σ⁰. The feed-down correction is given by:

$$n_{fd}(y, p_T) = \frac{N_{Λ(¯Λ)}^{found}(y, p_T)}{N_{Λ(¯Λ)}^{sim}(y, p_T)} Y_{tot}(y, p_T)$$

where $N_{Λ(¯Λ)}^{found}(y, p_T)$ is the average number of reconstructed (anti-)protons per event from embedded Λ (¯Λ) decays, $N_{Λ(¯Λ)}^{sim}(y, p_T)$ is the number of simulated Λ (¯Λ) and $Y_{tot}(y, p_T)$ the multiplicity of Λ (¯Λ) in the phase space interval from reference [14, 21] scaled for the contributions from Σ⁺ (¯Σ⁻). The lowest and the two highest rapidity bins in the 404 GeV data (see Fig. 2a) were removed due to low statistics in too many $p_T$ bins.

C. Systematic Errors

One of the sources for systematic errors is the uncertainty in the procedure of unfolding the $dE/dx$ distributions. Studies of the sensitivity to small changes of the fit parameters showed that the systematic errors are of the same order as the statistical errors. The largest contribution to the systematic error was traced to the deviations of the peak positions from the predicted values (see Fig. 1). They reach up to 4% in the yields in the low momentum bins. The next source of systematic errors is the uncertainty related to acceptance, inefficiencies and feed-down correction calculations. To estimate the magnitude of these errors cut parameters were varied such that significantly different correction factors were obtained. The resulting final results varied only within the statistical errors. Overall it appears that
the systematic uncertainties resulting from the correction procedures are of the order of 3% or less.

The determination of the rapidity density distributions required extrapolations of the transverse momentum distributions. Their contribution is negligible for most of the rapidity bins except the rapidity bins \( y \geq 1.2 \), where the extrapolation factors reached values of 1.3. Single and double exponentials were used to describe the shape of the transverse momentum distributions in this region. The resulting differences of \( p_T \)-integrated yields are smaller than 2%. Finally, the results from the \( dE/dx \) analysis in this paper and the TOF-results [5] agree within 5% in the common acceptance region at all centralities. We conclude from these studies that each data point carries a systematic uncertainty of approximately 7%.

IV. RESULTS AND COMPARISON WITH MODELS

A. Transverse momentum spectra

![Graphs showing invariant \( m_T \) spectra of protons at 40\( A \) GeV (a) and 158\( A \) GeV (b) as well as antiprotons at 158\( A \) GeV (c) for five centrality bins in Pb+Pb collisions. The respective center-of-mass rapidity intervals are \(-0.02 < y < 0.18\), \(-0.12 < y < 0.08\), \(-0.12 < y < 0.08\). The data at different centralities are scaled down by the factors indicated in the figures. The new NA49 measurements (full symbols) are compared, whenever available, to results of an earlier analysis using TOF information for particle identification [5] (open symbols). Only statistical errors are shown if larger than the symbol size. For the systematic errors see section IIIC.]

Transverse momentum distributions of (anti-)protons were determined in 10 (11) bins of rapidity at 40\( A \) GeV (158\( A \) GeV) as shown in Fig. 2. The range covered in trans-
verse momentum extends from $p_T$ equal zero to 0.8 GeV/c at high rapidity and up to 1.5 GeV/c (2 GeV/c) for $0.0 < y < 1.0$ at 40A GeV (158A GeV). Whenever necessary the $p_T$ spectra were extrapolated to 2 GeV/c (neglecting contributions at higher transverse momenta which have been accounted for in the systematic uncertainties) by taking the mean of the single and double exponential fits to the measured invariant spectra. At 40A GeV the extrapolation of the two bins around midrapidity were performed with the functional form obtained from the adjacent rapidity bin because of low statistics in the $p_T$ distributions. Using theses extrapolations $p_T$ integrated yields $(dn/dy)$ and mean $m_T$ values $(\langle m_T \rangle - m_0)$ as function of rapidity were calculated (see below). Midrapidity invariant $m_T$ spectra $(1/m_T \ d^2n/(dm_T \ dy))$ at 40A GeV and 158A GeV are compared in Fig. 3 with the results of a TOF based analysis published previously [5]. We find agreement within errors except for some of the two lowest $m_T$ points with deviations up to 20% in the 158A GeV data. These differences can be traced to the feed-down corrections, which relied

**FIG. 4:** $(m_T) - m_0$ for (anti-)protons as function of rapidity for five centrality intervals in Pb+Pb collisions. We show in the upper row (a) protons at 40A GeV, in the middle row (b) protons at 158A GeV, and in the lower row (c) antiprotons at 158A GeV. The open symbols are obtained by reflection at mid-rapidity. Asterisks refer to results of an earlier analysis using TOF information for particle identification [5]. Only statistical errors are shown (if larger than the symbol size). For the systematic errors see section IIIC.
on different (older) parameterizations used for the MC input of (anti-)lambda phase space distributions in reference [5], but are based on recent measured data in this analysis (see above). However, this uncertainty has only a small effect on the value of $\frac{dn}{dy}$.

**FIG. 5:** $\langle m_T \rangle - m_0$ near mid-rapidity as function of $\langle N_w \rangle$ in Pb+Pb collisions. The leftmost panel (a) shows the proton data at 40A GeV, the middle panel (b) the proton data at 158A GeV, and the right panel (c) the antiproton data at 158A GeV. The results of this analysis (labelled dE/dx) are compared to previously published Pb+Pb data (labelled TOF) [5]. The ordinate has a suppressed zero. Only statistical errors are shown (if larger than the symbol size). For the systematic errors see section III C.

Since the shapes of all invariant $m_T$ spectra deviate significantly from single exponentials, we choose $\langle m_T \rangle - m_0$ instead of the inverse slope parameter of the transverse mass spectra to study the transverse activity as function of rapidity. Fig. 4 shows $\langle m_T \rangle - m_0$ of protons at 40A GeV (upper row) and 158A GeV (middle row), and antiprotons at 158A GeV (lower row) as function of cms rapidity. In the latter the bin size in rapidity was doubled to reduce the statistical errors on the data points. The $\langle m_T \rangle - m_0$ values near midrapidity are plotted in Fig. 5 as function of centrality. Also shown are the data points from the TOF analysis [5] and recent results from p+p interactions at the same energy [22]. A clear increase of $\langle m_T \rangle - m_0$ by roughly 30% is observed when comparing the values obtained in the most peripheral with the most central event sample. The increase is close to a factor of two when the results on p+p interactions are taken as reference. Similar observations have been made by NA49 for data on hyperons [21].
FIG. 6: $dn/dy$ of (net) protons for five different centralities. We show in the left panel (a) the proton distributions at 40A GeV and in the right panel (b) the difference between proton and antiproton spectra (i.e. the net proton spectra) at 158A GeV. The open symbols are obtained by reflection at mid-rapidity. Also shown are the results from an earlier analysis labelled TOF [5]. Only statistical errors are shown (if larger than the symbol size). For the systematic errors see section IIIC.

**B. Rapidity spectra**

The rapidity densities $dn/dy$ in each rapidity interval were obtained by summing the yields in the measured $p_T$ interval and the integrals of the extrapolation function above the highest measured $p_T$ bin. The additive correction was calculated as the average of the single and the double exponentials in the unmeasured $p_T$ region. The contributions of the extrapolation to $dn/dy$ are mostly of order of 3 % (6 %) for protons and below 5 % for antiprotons at 158A GeV (40A GeV) and contribute negligibly to the errors of the integrals. These extrapolations reach up to 25 % close to the limits of the accepted rapidity region.

The rapidity spectra of protons at 40A GeV (left) and net protons at 158A GeV (right) are presented in Fig. 6 for five different centrality selections (C0 - C4). We included the $dn/dy$ values obtained from the TOF analysis (asterisks) published earlier by NA49 [5] for comparison. At both energies the yields increase with centrality. No change in shape is apparent at 158A GeV beam energy, whereas at 40A GeV the form of the $dn/dy$ distribution evolves from a parabolic shape near to midrapidity ($|y| < 1$) in semi-peripheral to a double hump structure in central collisions. The $dn/dy$ values of protons at 40A GeV are given in Table II, those for protons at 158A GeV in Table III and for antiprotons in Table IV.
FIG. 7: Rapidity density distributions per wounded nucleon are shown for protons at 40A GeV (top panel), protons at 158A GeV (middle panel), and antiprotons at 158A GeV (bottom panel) for five centralities in Pb+Pb collisions. The open symbols are obtained by reflection at mid-rapidity. The solid lines represent results of single Gaussian fits. For the statistical errors see Fig. 6. For the systematic errors see section IIIC.

The trends in the evolution of the rapidity distributions are seen best, when the spectra are divided by the number of wounded nucleons as shown in Fig. 7. The proton spectra at 158A GeV (middle panel) change little. The normalized yields (at midrapidity) increase by roughly 15% from 0.065 to 0.075 when going from semi-peripheral to central collisions. At 40A GeV the scaled yields at midrapidity increase by 25% from 0.085 to 0.11 from semi-peripheral to central collisions. As to the shape it seems that with decreasing centrality additional protons populate the region $|y| < (y_{max} - 1.2)$. The shape of the antiproton distributions at 158A GeV resembles a Gaussian and does not change with centrality. The integrated and mid-rapidity yields normalized by $\langle N_w \rangle$ decrease by 20% with increasing centrality.

We present the dependences on centrality of the normalized antiproton multiplicity and of the width of their rapidity distribution in Fig. 8 together with NA49 data from elementary p+p interactions [22] both at 158A GeV. The mean multiplicities (total yield per event)
FIG. 8: The total multiplicities (per wounded nucleon) of $\bar{p}$ and $\bar{\Lambda}$ (upper panel) and the RMS$_y$ widths of the $dn/dy$ distributions of $\bar{p}$ and $\bar{\Lambda}$ (lower panel) for five centralities as function of the number of wounded nucleons $\langle N_w \rangle$ in Pb+Pb collisions at 158$A$ GeV. The $\bar{\Lambda}$ data are from [21]. Also shown are results on antiprotons obtained from p+p interactions [22]. Only statistical errors are shown (if larger than the symbol size). For the systematic errors see section IIIC.

of antiprotons for different centralities were calculated by integrating the measured rapidity spectra and by extrapolating into the unmeasured regions assuming a Gaussian shape (see Fig. 7). The magnitude of the corresponding extrapolation factors are in the range from 5%
to 10%. A double Gaussian fit is used to estimate the systematic errors of the extrapolation into the high $y$-region. The antiproton multiplicity normalized to $\langle N_w \rangle$, shown in the upper panel of Fig. 8, increases by nearly a factor 1.5 when going from mid-central Pb+Pb to inelastic p+p collisions and stays constant from mid-central to central Pb+Pb collisions. Although the properly weighted average of yields in p+p and n+n collisions would be the appropriate reference for this comparison, we consider the p+p midrapidity yield to be a good approximation. It is interesting to note that the antilambda multiplicity (from reference [21]), also shown in Fig. 8a, exhibits a centrality dependence similar to the one of the antiprotons. The lower panel of Fig. 8 shows the centrality dependence of the widths of the rapidity distributions for antiprotons and antilambdas (from reference [21]). No significant difference is observed between the values in different centrality bins of the Pb+Pb data. Only the width in p+p interactions seems to be slightly wider than those observed in Pb+Pb collisions.

Net-proton rapidity distributions for all five centralities are obtained by subtracting the antiproton distributions from those of the protons. The result at 158.4 GeV for central collisions (bin C0) is compared to data published earlier [3] in Fig. 9. The differences between the two measurements can be traced back to different analysis methods. The earlier analysis used a method in which distributions of negatively charged particles were subtracted from those of the positively charged ones assuming the proton mass for all particles. The resulting distributions were corrected for the then unmeasured differences between $\pi^+$ and $\pi^-$, as well as $K^+$ and $K^-$ yields by means of model calculations and detector simulations (see reference [3]). Here we identify the protons and antiprotons directly by means of their specific energy loss in the MTPCs. The new results should therefore be more reliable due to the smaller and better determined corrections leading to smaller systematic uncertainties. The two results are consistent within the systematic errors.

C. Model comparisons and conclusions

Net-proton spectra are compared with HSD [23] and UrQMD-2.3 [24] model calculations. Before addressing possible differences between the model results and Pb+Pb collision data, we check how well the models reproduce the rapidity distribution of net-protons in p+p interactions. It is important to note here that the model calculations include also elastic
FIG. 9: The net-proton rapidity distribution at 158A GeV for centrality bin C0 is compared with previously published data [3]. The full circles indicate results from the analysis presented in this paper, whereas the full squares show the previously published data. The open points result from reflection of the data points at midrapidity. The shaded bars represent the systematic uncertainties. Error bars represent statistical errors.

scattering whereas the experimental data represent inelastic interactions only. Fig. 10 reveals significant differences between the models and the experimental data. First, UrQMD [24] has more stopping than HSD [23] with a similar shape as the data, but a significantly higher yield at midrapidity. Second, HSD reproduces the midrapidity yield but fails to reproduce the shape. These shortcomings render comparison to Pb+Pb data questionable. The comparison is shown nevertheless in Fig. 11 for 40A GeV and in Fig. 12 for 158A GeV, in which the rapidity density distributions are divided by the average number of wounded nucleons \( \langle N_w \rangle \). Note that antiprotons were not subtracted in the 40A GeV data, since their yield is negligibly small compared to the proton yield (\(< 1\% \) at midrapidity). Overall we observe fair agreement between the HSD model calculation and the data in the rapidity region covered by the NA49 measurements. Larger disagreements are seen for the UrQMD predictions. The differences can be attributed either to known differences between the models (see below) or to the deficiencies in describing proton distributions in elementary p+p collisions.
interactions. The HSD [23] calculations describe the data always better than UrQMD [24] calculations. These significant differences in the rapidity distributions between HSD and UrQMD are due to a different definition of "formed" and "unformed" hadrons. In HSD a hadron is considered as "formed" only if the energy density (in the surrounding cell) drops below a critical value, which is taken to be 1 GeV/fm$^3$ in line with results from lattice QCD on the critical energy density for deconfinement. Otherwise the hadron is considered as "unformed" and unable to interact with other hadrons until the energy density drops to the critical value. This energy density criterion is not included in UrQMD which leads therefore to a substantial overestimate of the energy loss of participant nucleons in collisions in which high energy densities are reached [23].

In Pb+Pb collisions at 158A GeV we observe a parabolic shape near to midrapidity ($|y| < 1$) which is similar to the one seen in inelastic p+p interactions as well as in HSD calculations. This can be explained by an exponential decrease of the proton yield towards midrapidity (according to $\exp[-(y-y_{beam})]$), which in turn results from the approximately flat probability

FIG. 10: Rapidity distribution of net-protons from p+p-collisions at 158 GeV/c beam momentum [22]. The solid line represents the HSD [23] and the dashed line the UrQMD [24] calculation.
density distribution as a function of Feynman x \cite{1}. At 40A GeV the rapidity distributions are similar to those at 158A GeV for more peripheral collisions, while they develop a double hump structure for central collisions. The normalized mid-rapidity yield increases by about 25% at 40A GeV and 10% at 158A GeV from the most peripheral to the most central collisions in line with findings in earlier analyses of proton yields at mid-rapidity \cite{5} and recent results on hyperons \cite{21}. HSD calculations reproduce this trend quantitatively.

The significant differences between the proton distributions at 40A GeV and 158A GeV are at least partly due to the differences in experimental acceptances at the two energies. The change in shape which occurs away from midrapidity at 40A GeV is probably also present at the higher energy, however, in a range |y| < (\y_{\text{max}} - 1.2) which is outside the NA49 acceptance. Finally, the integral of the normalized net proton distributions over the measured region increases by 8% at 40A GeV and by 5% at 158A GeV with decreasing centrality. This is an indication that the spectrum of net protons contains nucleons not only from the nuclear overlap region specified in the Glauber model (which we call wounded nucleons) but also from the spectator remnants. Such an additional contribution to the proton spectra is confirmed in the results from the model calculations in which the coverage extends from target to beam rapidity (see Figs. 11 and 12). The origin of these
FIG. 12: The rapidity distributions scaled with $1/\langle N_w \rangle$ of net-protons for five different centralities at 158$A$ GeV are shown together with results of HSD (top) [23] and UrQMD (bottom) [24] calculations. For the statistical errors see Fig. 6. For the systematic errors see section IIIC.

"participating spectators" could be elastic and inelastic $N+N_{\text{spectator}}$ and $\text{meson}+N_{\text{spectator}}$ interactions ($N$ stands for nucleon). Since there is no way to separate the "participating" spectator protons from the wounded nucleons in the experimental data, it is difficult to draw conclusions on nuclear stopping from the study of net proton spectral shapes in centrality selected $\text{Pb}+\text{Pb}$ collisions. On the other hand this spectator contribution seems to be absent in the hyperon rapidity distributions [21], thus the e.g. $\text{meson}+N_{\text{spectator}}$ interactions are not violent enough to produce hyperons.

V. SUMMARY

The NA49 collaboration analysed proton and antiproton spectra in 40$A$ GeV and 158$A$ GeV $\text{Pb}+\text{Pb}$ reactions covering the 43.5% most central collisions. In the transverse mass spectra no strong variation with centrality is discernible, but the average $m_T$ increases by roughly 20% from peripheral to central collisions. The rapidity distributions at 158$A$ GeV have a common concave shape (Fig. 6b) which however gets shallower with increasing centrality, best seen if normalized to the number of participants as shown in Fig. 7. The rapidity distributions at 40$A$ GeV on the contrary exhibit a strong centrality depen-
dence starting with a concave or 'V' shaped structure at large impact parameters, which turns into a symmetric double hump shape for more central collisions. The minimum at the center, which is characteristic of the concave shape, persists at all centralities. Sizeable contributions from non-participants in the rapidity range $|y| < (y_{\text{beam}} - 1.2)$ are observed, which are probably due to secondary interactions of produced particles in spectator matter. Thus rapidity loss analyses of net proton spectra in nucleus-nucleus collisions have to account for this unwanted component of the spectrum. The midrapidity yield normalized to the number of participants varies only by 10% (5%) with centrality at 40A GeV (158A GeV) reaching its maximum for the most central collisions. As expected it decreases when going from 40A GeV to 158A GeV (by 25%). These finding may be compared to the corresponding data from AGS experiment E917 extracted from reference [2] using reference [25] to compute the number of participants. We find roughly a factor of two higher (normalized) yields at midrapidity with centrality variations of 3%, 5%, and 5% at 6A GeV, 8A GeV, and 10.8A GeV, respectively. Antiproton spectra could not be extracted at 40A GeV because of lack of statistics. At 158A GeV the normalized total (see Fig. 8) and midrapidity yields increase with impact parameter. Such a behavior is expected in case absorption plays a significant role or, equivalently, the baryon rich collision system approaches chemical equilibrium [20].

We chose to compare our findings to the transport model calculations from the HSD and UrQMD codes. Although both models reproduce rapidity density distributions in p+p collisions only with significant deviations as shown in Fig. 10, HSD gives a good description of the nuclear collision data at both energies (see upper rows in Figs. 11 and 12) in the region covered by NA49 measurements with deviations only at large rapidities. The UrQMD model calculations also fit the experimental distributions fairly well, although with larger discrepancies which are most pronounced at midrapidity and in central collisions.
TABLE II: Proton rapidity densities \( \frac{d n}{d y} \) at five different centralities and 40\( A \) GeV. The quoted errors are statistical. For the systematic errors see section IIIC.

<table>
<thead>
<tr>
<th></th>
<th>( \frac{d n}{d y}(C0) )</th>
<th>( \frac{d n}{d y}(C1) )</th>
<th>( \frac{d n}{d y}(C2) )</th>
<th>( \frac{d n}{d y}(C3) )</th>
<th>( \frac{d n}{d y}(C4) )</th>
</tr>
</thead>
<tbody>
<tr>
<td>(-0.02 \leq y \leq 0.18)</td>
<td>38.64( \pm )1.11</td>
<td>30.69( \pm )0.79</td>
<td>21.01( \pm )0.51</td>
<td>12.69( \pm )0.33</td>
<td>8.19( \pm )0.20</td>
</tr>
<tr>
<td>(0.18 \leq y \leq 0.38)</td>
<td>40.15( \pm )1.07</td>
<td>30.63( \pm )0.75</td>
<td>21.86( \pm )0.51</td>
<td>13.26( \pm )0.34</td>
<td>8.74( \pm )0.22</td>
</tr>
<tr>
<td>(0.38 \leq y \leq 0.58)</td>
<td>41.23( \pm )1.08</td>
<td>32.93( \pm )0.70</td>
<td>22.72( \pm )0.51</td>
<td>14.49( \pm )0.34</td>
<td>9.68( \pm )0.23</td>
</tr>
<tr>
<td>(0.58 \leq y \leq 0.78)</td>
<td>41.72( \pm )0.98</td>
<td>34.24( \pm )0.74</td>
<td>24.01( \pm )0.52</td>
<td>15.48( \pm )0.35</td>
<td>10.51( \pm )0.23</td>
</tr>
<tr>
<td>(0.78 \leq y \leq 0.98)</td>
<td>42.08( \pm )1.32</td>
<td>33.65( \pm )0.72</td>
<td>24.57( \pm )0.49</td>
<td>16.64( \pm )0.37</td>
<td>11.71( \pm )0.24</td>
</tr>
<tr>
<td>(0.98 \leq y \leq 1.18)</td>
<td>40.11( \pm )1.19</td>
<td>32.91( \pm )0.85</td>
<td>24.58( \pm )0.50</td>
<td>17.48( \pm )0.38</td>
<td>12.71( \pm )0.28</td>
</tr>
<tr>
<td>(1.18 \leq y \leq 1.38)</td>
<td>36.64( \pm )0.98</td>
<td>31.29( \pm )0.73</td>
<td>24.84( \pm )0.53</td>
<td>18.70( \pm )0.42</td>
<td>14.06( \pm )0.33</td>
</tr>
<tr>
<td>(1.38 \leq y \leq 1.58)</td>
<td>31.63( \pm )1.09</td>
<td>29.16( \pm )0.76</td>
<td>24.94( \pm )0.56</td>
<td>20.69( \pm )0.51</td>
<td>15.69( \pm )0.48</td>
</tr>
</tbody>
</table>

Acknowledgments

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TABLE III: Proton rapidity densities $dn/dy$ at five different centralities and 158$A$ GeV. The quoted errors are statistical. For the systematic errors see section IIIC.

<table>
<thead>
<tr>
<th>$-0.52 \leq y \leq -0.32$</th>
<th>$-0.32 \leq y \leq -0.12$</th>
<th>$-0.12 \leq y \leq 0.08$</th>
<th>$0.08 \leq y \leq 0.28$</th>
<th>$0.28 \leq y \leq 0.48$</th>
<th>$0.48 \leq y \leq 0.68$</th>
<th>$0.68 \leq y \leq 1.08$</th>
<th>$1.08 \leq y \leq 1.28$</th>
<th>$1.28 \leq y \leq 1.48$</th>
<th>$1.48 \leq y \leq 1.68$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$dn/dy(C0)$</td>
<td>25.63±1.41</td>
<td>27.49±1.24</td>
<td>27.51±1.09</td>
<td>28.07±1.01</td>
<td>29.20±0.89</td>
<td>31.30±0.88</td>
<td>30.51±0.85</td>
<td>32.35±1.05</td>
<td>38.84±3.43</td>
</tr>
<tr>
<td>$dn/dy(C1)$</td>
<td>22.17±0.74</td>
<td>22.32±0.61</td>
<td>20.97±0.52</td>
<td>21.81±0.51</td>
<td>22.91±0.50</td>
<td>23.96±0.49</td>
<td>25.10±0.49</td>
<td>26.88±0.57</td>
<td>28.82±0.58</td>
</tr>
<tr>
<td>$dn/dy(C2)$</td>
<td>14.36±0.43</td>
<td>15.14±0.38</td>
<td>14.79±0.33</td>
<td>14.96±0.31</td>
<td>16.27±0.30</td>
<td>17.4±0.31</td>
<td>17.87±0.32</td>
<td>19.22±0.39</td>
<td>21.46±0.43</td>
</tr>
<tr>
<td>$dn/dy(C3)$</td>
<td>9.28±0.30</td>
<td>9.46±0.25</td>
<td>9.46±0.23</td>
<td>9.34±0.21</td>
<td>9.92±0.23</td>
<td>10.97±0.23</td>
<td>11.53±0.24</td>
<td>12.25±0.26</td>
<td>13.63±0.28</td>
</tr>
<tr>
<td>$dn/dy(C4)$</td>
<td>5.84±0.21</td>
<td>6.03±0.18</td>
<td>6.07±0.19</td>
<td>5.98±0.16</td>
<td>6.39±0.16</td>
<td>7.05±0.17</td>
<td>7.55±0.19</td>
<td>8.43±0.20</td>
<td>9.52±0.22</td>
</tr>
</tbody>
</table>

TABLE IV: Antiproton rapidity densities $dn/dy$ at five different centralities and 158$A$ GeV. The quoted errors are statistical. For the systematic errors see section IIIC.

<table>
<thead>
<tr>
<th>$-0.52 \leq y \leq -0.12$</th>
<th>$-0.12 \leq y \leq 0.28$</th>
<th>$0.28 \leq y \leq 0.68$</th>
<th>$0.68 \leq y \leq 1.08$</th>
<th>$1.08 \leq y \leq 1.28$</th>
<th>$1.28 \leq y \leq 1.48$</th>
<th>$1.48 \leq y \leq 1.68$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$dn/dy(C0)$</td>
<td>1.61±0.13</td>
<td>1.75±0.12</td>
<td>1.76±0.11</td>
<td>1.31±0.10</td>
<td>0.60±0.10</td>
<td>1.61±0.13</td>
</tr>
<tr>
<td>$dn/dy(C1)$</td>
<td>1.37±0.09</td>
<td>1.37±0.08</td>
<td>1.43±0.07</td>
<td>1.11±0.07</td>
<td>0.57±0.09</td>
<td>1.37±0.09</td>
</tr>
<tr>
<td>$dn/dy(C2)$</td>
<td>0.92±0.06</td>
<td>1.06±0.05</td>
<td>0.96±0.05</td>
<td>0.80±0.05</td>
<td>0.37±0.05</td>
<td>0.92±0.06</td>
</tr>
<tr>
<td>$dn/dy(C3)$</td>
<td>0.78±0.05</td>
<td>0.80±0.04</td>
<td>0.70±0.04</td>
<td>0.54±0.038</td>
<td>0.21±0.03</td>
<td>0.78±0.05</td>
</tr>
<tr>
<td>$dn/dy(C4)$</td>
<td>0.51±0.04</td>
<td>0.55±0.03</td>
<td>0.49±0.03</td>
<td>0.36±0.03</td>
<td>0.31±0.06</td>
<td>0.51±0.04</td>
</tr>
</tbody>
</table>

[21] T. Anticic et al., NA49 Collaboration, Phys. Rev. C 80 (2009) 034906. The data on \( \bar{\Lambda} \) yield and rapidity width in p+p interactions are preliminary NA49 results which are subject to 7% systematical errors.