Measurement of the Cross Section for High-$p_T$ Hadron Production in Scattering of 160 GeV/$c$ Muons off Nucleons

The COMPASS Collaboration

Abstract

The cross section for production of charged hadrons with high transverse momenta in scattering of 160 GeV/$c$ muons off nucleons at low photon virtualities has been measured at the COMPASS experiment at CERN. The results, which cover transverse momenta from 1.1 to 3.6 GeV/$c$, are compared to a next-to-leading order perturbative Quantum Chromodynamics (NLO pQCD) calculation in order to evaluate the applicability of pQCD to this process in the kinematic domain of the experiment. The shape of the calculated differential cross section as a function of transverse momentum is found to be in good agreement with the experimental data, but the normalization is underestimated by NLO pQCD. This discrepancy may point towards the relevance of terms beyond NLO in the pQCD framework. The dependence of the cross section on the pseudo-rapidity and on the charge of the hadrons is also discussed.

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Most of the current knowledge about the structure of the nucleon has been derived from high-energy lepton-nucleon scattering experiments [1]. The theoretical framework for the interpretation of data from such experiments is perturbative Quantum Chromodynamics (pQCD). In the presence of a large momentum transfer in the reaction, pQCD relies on the collinear factorization of the cross section into non-perturbative collinear parton distribution functions (PDFs), hard partonic scattering cross sections calculable in perturbation theory, and non-perturbative collinear fragmentation functions (FFs) [2]. This Letter discusses the measurement of the cross section for production of charged hadrons with high transverse momenta $p_T$ in muon-nucleon ($\mu$-N) scattering at low photon virtualities, $\mu N \rightarrow \mu' h^{\pm} X$. In the pQCD framework, the lowest-order contributions to this reaction are (1) photon-gluon fusion (PGF), in which a virtual photon emitted by the lepton interacts with a gluon inside the nucleon via the formation of a quark-anti-quark pair, $\gamma g \rightarrow q\bar{q}$, (2) QCD Compton (QCDC) scattering, in which the photon interacts with a quark in the nucleon leading to the emission of a hard gluon, $\gamma q \rightarrow qg$, and (3) numerous resolved-photon processes, in which the photon fluctuates into a virtual vector-meson-like state before it interacts with the nucleon.

The ability of pQCD to correctly describe high-$p_T$ hadron production can be evaluated by comparing the calculated cross section to the experimentally measured one. This benchmark is sensitive to the accuracy, with which the partonic cross section can be calculated in perturbation theory, as well as to the validity of collinear factorization itself. For inclusive high-$p_T$ hadron or jet production in proton-proton ($p-p$) scattering, cross sections have been measured at FNAL [3,4,5], CERN [6] and BNL [7,8,9,10,11,12] at center-of-mass system (CMS) energies $\sqrt{s_{pp}}$ from 20 GeV to 200 GeV. The comparison of these data to next-to-leading order (NLO) pQCD calculations [13] shows that while there is good agreement at $\sqrt{s_{pp}} = 200$ GeV (RHIC), the theory increasingly underestimates the cross sections with decreasing $\sqrt{s_{pp}}$. The disagreement reaches up to an order of magnitude at 20 GeV. These discrepancies can be reconciled by the inclusion of all-order resummations of threshold logarithms [14], which are related to soft gluon emissions and are usually performed up to next-to-leading logarithmic (NLL) accuracy.

The electromagnetic probe in muon-lepton scattering has the advantage over $p-p$ scattering that the kinematics of the reaction is better known since the momentum and energy transfers to the nucleon can be measured for each event by analyzing the scattered lepton. In the regime of quasi-real photoproduction, i.e. at low photon virtualities $Q^2$, the cross section for high-$p_T$ hadron production in lepton-nucleon scattering can be calculated in NLO pQCD via the Weizsäcker-Williams formalism [15,16]. For dijet production at HERA at very high photon-nucleon CMS energies $142 \leq W_{\gamma N} \leq 293$ GeV, the NLO pQCD results agree well with the experimental data [17]. At the energy of fixed-target experiments, such a check of the applicability of pQCD to high-$p_T$ particle production at low $Q^2$ has not been done yet. The cross section for high-$p_T$ hadron production in the scattering of 28 GeV/c positrons off nucleons has been published by the HERMES Collaboration [18]. However, the measurement hardly exceeds $p_T$ values of 2 GeV/c, which sets rather low factorization and renormalization scales for pQCD calculations, and a comparison to NLO pQCD was not attempted. In this Letter, the measurement of the cross section for production of unidentified charged hadrons with high $p_T$ in scattering of 160 GeV/c muons off nucleons (CMS energy $\sqrt{s_{\mu \cdot N}} = 17.4$ GeV) at the COMPASS experiment [19] at low photon virtualities is presented. The cross section for this kinematic domain has been calculated in NLO pQCD [20].

The hadron-production cross section is measured in bins of $p_T$ and $\eta$ of widths $\Delta p_T$ and $\Delta \eta$, respectively, and is defined as

$$E \frac{d^3\sigma}{dp_T^3} = \frac{1}{2 \pi p_T} \frac{N_h}{\Delta p_T \cdot \Delta \eta \cdot L \cdot \varepsilon},$$

(1)

where $E$ and $p$ are energy and momentum of the hadron, respectively, $p_T = p \cdot \sin \theta$ is the transverse momentum of the hadron with respect to the direction of the virtual photon ($\theta$ is the angle between the virtual photon and the hadron momenta), and $\eta = -\ln \tan(\theta/2)$ is the pseudo-rapidity of the hadron, all measured in the laboratory system. The integrated luminosity is denoted by $L$, $N_h$ is the number of observed hadrons in a given bin of $p_T$ and $\eta$, and $\varepsilon$ is the acceptance-correction factor, which is determined
independently for both hadron charges for each bin of $p_T$ and $\eta$. This factor corrects the number of observed hadrons for geometrical acceptance and detection efficiency of the spectrometer as well as for kinematic smearing. The cross section is defined as a single-inclusive cross section, i.e. several high-$p_T$ hadrons per muon-scattering event are counted for the hadron yield $N_h$.

The experimental data were recorded in 2004 with the COMPASS spectrometer at CERN. In the experiment, a naturally-polarized 160 GeV/c $\mu^+$-beam scatters off a polarized, isoscalar target that consists of granulated $^6$LiD immersed in liquid helium. The small admixtures of H, $^3$He, and $^7$Li lead to an excess of neutrons of about 0.1%. The target is arranged in two oppositely polarized 60 cm long cells. The unpolarized cross section is obtained by averaging over the target polarizations. Since the azimuthal angles of the produced hadrons are integrated over, the cross section does not depend on the beam polarization. The integrated luminosity is determined via the direct measurement of the rate of beam muons crossing the target and is found to be equal to 142 pb$^{-1} \pm 10\%$(syst.) after correction for the dead time of the data acquisition system. As an independent cross check of the luminosity, the structure function of the nucleon $F_2$ is determined from this data set and compared to the NMC parametrization of $F_2$ yielding satisfactory agreement [22]. The high-$p_T$ analysis is based on events that were recorded by the quasi-real photoproduction trigger systems [23]. These triggers are based on the coincidence between the detection of the scattered muon at low scattering angles and an energy deposit exceeding about 5 GeV in one of the two hadronic calorimeters, to suppress background from muon-electron scattering and radiative elastic or quasi-elastic muon-scattering events. Events are accepted if the photon virtuality $Q^2 < 0.1 \text{(GeV/c)}^2$ and if the fractional energy transferred from the incident muon to the virtual photon is in the range $0.2 \leq y \leq 0.8$, where the acceptance of the trigger systems is largest. These selections result in the energy range $7.8 \leq W_{PN} \leq 15.5 \text{ GeV}$. The fraction of the virtual-photon energy transferred to the hadron $h$ is constrained by $0.2 \leq z \leq 0.8$. Moreover, hadrons are required to have momenta $p \geq 15 \text{ GeV/c}$ to ensure full trigger efficiency. The angle of the hadron with respect to the direction of the virtual photon has to be in the range $10 \leq \theta \leq 120 \text{ mrad}$, which corresponds to a range of muon-nucleon CMS pseudo-rapidities $2.4 \geq \eta_{\text{CMS}} \geq -0.1$. In addition to these kinematic criteria, the selection of reconstructed hadrons is subject to several geometrical cuts: the positions of the muon-scattering vertices are limited to the fiducial target volume, the hadron tracks must not cross the solenoid magnet of the polarized target, and the hadron tracks must hit one of the two hadronic calorimeters, excluding 3 cm wide margins around the edges (for full trigger efficiency).

The acceptance correction factors of Eq. (1) are determined with a Monte-Carlo (MC) simulation of $\mu$-N scattering in the COMPASS experiment. Events are generated with PYTHIA6 [24], the response of the spectrometer is simulated with a GEANT3-based program [25], and the data are reconstructed with the same software as the experimental data [19]. The acceptance factor for the bin $p_T \in [p_{T,1}, p_{T,2}]$ is defined as

$$\varepsilon = \frac{N_{\text{rec}}(p_T^{\text{rec}} \in [p_{T,1}, p_{T,2}])}{N_{\text{gen}}(p_T^{\text{gen}} \in [p_{T,1}, p_{T,2}])},$$

(2)

where $N_{\text{rec}}$ is the number of reconstructed hadrons in the bin of reconstructed transverse momentum $p_T^{\text{rec}}$, and $N_{\text{gen}}$ is the number of generated hadrons in the MC sample in the bin of generated transverse momentum $p_T^{\text{gen}}$. While both, $N_{\text{rec}}$ and $N_{\text{gen}}$ are subject to the above-listed kinematic selection criteria, the geometrical cuts are only applied to $N_{\text{rec}}$ so that the loss of hadrons due to these cuts is accounted for by the acceptance correction.

Hadrons that are created at the $\mu$-N vertex constitute the signal of the measurement and have to be separated from background hadrons, which are created in secondary interactions of other hadrons in the target material. This separation is performed by the vertex-reconstruction algorithm, which is however impaired by the fact that the angle between the incoming and outgoing muon tracks is very small at low $Q^2$. The background contamination can not be estimated directly from the MC data, because simulations with the two hadron-shower models available in GEANT3 (GHEISHA and FLUKA) give inconsistent results. Hence the background contribution is determined in each $p_T$ bin from the experimental data by
fitting the shape of the distribution of position differences between two-particle vertices formed by the incoming muon track and the outgoing muon track on the one hand, and the incoming muon track and the outgoing hadron track on the other hand [26]. The distribution for signal hadrons, originating from the same interaction as the outgoing muon track, has a symmetric shape, while for background hadrons there is a characteristic asymmetric shape. The results of these fits show that the background contribution to the experimental data is consistent with zero. However, cross checks with both MC data sets indicate that the background contribution can be systematically underestimated by 6% using this method. In addition, the described procedure is statistically limited for the highest $p_T$ bins because there are too few entries in the vertex-difference distributions to exclude a non-zero background contribution with high statistical accuracy. For the four highest $p_T$ bins, the background level $p_{\text{excl}}$ at which a non-zero background contribution can be excluded at 90% confidence level is greater than 6%. Therefore, the possible contribution of residual background to the hadron yield is conservatively estimated to be $2 \times 6\%$ for the six lowest $p_T$ bins and $p_{\text{excl}} + 6\%$ for the four highest $p_T$ bins. These values are used as systematic uncertainties of the acceptance factors.

A second contribution to the systematic uncertainties of the acceptance factors arises from the fact that they are determined in a one-dimensional way, i.e. by integrating over all kinematic variables other than $p_T$. The resulting uncertainty is quantified by calculating the acceptance correction binned in two variables, i.e. $p_T$ and one of the variables $Q^2, y, x_{ Bj}$ (Bjorken scaling variable), $W_{N}$, $z$, $\theta$. A comparison of the cross section calculated in two variables, summed up over the second variable, with the one-dimensional result yields deviations below 3%. This uncertainty is added in quadrature to the uncertainties from background contamination, resulting in the following definition of the upper ($\varepsilon_u$) and lower ($\varepsilon_d$) limits of the systematic error band of the acceptance factors:

$$\varepsilon_u = \varepsilon \cdot \left( 1 + \sqrt{0.03^2 + (0.06 + \max(0.06, p_{\text{excl}}))^2} \right)$$

$$\varepsilon_d = \varepsilon \cdot (1 - 0.03) .$$

Another systematic uncertainty of the cross section is the 10% normalization uncertainty from the luminosity determination.

The cross section for production of charged high-$p_T$ hadrons in $\mu/N$ scattering at $Q^2 < 0.1$ (GeV/c)$^2$ and $\sqrt{s_{\mu/N}} = 1.74$ GeV, integrated over the full kinematic range, is presented in Fig. 1 and listed in Tab. 1. The presented cross section is not corrected for QED radiative effects. The discrete $p_T$ values at which the cross section values from the binned analysis of Eq. (1) are drawn are calculated using the method of Lafferty & Wyatt [28] and are denoted by $\langle p_T \rangle_{\text{lw}}$ in Tab. 1. The cross section drops by about four orders of magnitude over the measured $p_T$ range. The only apparent deviation from an exponential shape is a slight hardening of the spectrum at about $p_T = 2.5$ GeV/c. In Fig. 1 the data are compared to the NLO pQCD calculation of Ref. [20], which has been updated [27] to implement the above-stated kinematic selections and the DSS FFs [29] for unidentified charged hadrons. The three curves correspond to different choices of the renormalization ($\mu_r$) and factorization ($\mu_f$) scales in the pQCD calculation. The standard choice for the scales in pQCD is $\mu_r = \mu_f = p_T$ and the scale uncertainty is estimated by varying the scale in the range $2p_T \geq \mu \geq p_T/2$. For $p_T \gtrsim 1.75$ GeV/c, the pQCD result at the standard scale $\mu = p_T$ underestimates the experimental cross section by a factor of three to four, but follows the shape of the differential cross section remarkably well. For $p_T \lesssim 1.75$ GeV/c the pQCD results should be discussed and interpreted very cautiously, because the factorization of the calculated cross section is expected to break down when reaching small scales $\mu$. The large scale uncertainty of the cross section shows that contributions beyond NLO are likely to be significant in the pQCD framework. The analogy to $p-p$ scattering at low CMS energies suggests that all-order resummations of threshold logarithms, once available, might reconcile the normalization discrepancy.

In Fig. 2 the $p_T$ dependence of the experimental cross section is presented in bins of $\eta_{\text{CMS}}$, together with the comparison to NLO pQCD. The steeper $p_T$ slopes of the cross section at forward rapidities as compared to central rapidity are well described by the pQCD curves, and the normalization difference
Fig. 1: Cross section for high-$p_T$ hadron production in $\mu$-$N$ scattering, integrated over the full kinematic range (see text). The data are compared to the NLO pQCD calculation [20, 27]. The error bars in the upper panel are the quadratic sums of statistical and systematic uncertainties. The middle panel shows the relative statistical and systematic uncertainties of the measurement. The normalization uncertainty of 10% from the luminosity measurement is not shown. The lower panel shows the ratio of the measured over calculated cross sections.

between the theoretical calculation ($\mu = p_T$) and the experimental values remains about the same for all rapidities. This is a positive indication for the consistency of the pQCD results. The charge ratio of the cross sections for the production of negatively over positively charged hadrons is displayed in Fig. 3. No strong $p_T$ dependence is observed within the statistical accuracy of the measurement. The charge ratio is sensitive to the contributions of the different partonic processes to the cross section. The QCDC process can lead to an excess of positively charged hadrons because the electromagnetic coupling to $u$ quarks is four times larger than to $d$ quarks, and $u$ quarks are more likely to produce positively charged mesons. The PGF process, on the other hand, is not expected to result in a charge asymmetry, assuming independent quark fragmentation. The NLO pQCD calculation, also shown in Fig. 3, features a charge ratio of about unity for $p_T = 1$ GeV/$c$ and a clear decrease with increasing $p_T$, in disagreement with the data.

In summary, the single-inclusive cross section for charged-hadron production in $\mu$-$N$ scattering at $\sqrt{s_{\mu-N}} = 17.4$ GeV was measured for photon virtualities $Q^2 < 0.1$ (GeV/$c)^2$ in the $\eta_{\text{CMS}}$ interval between -0.1 and 2.4 and for transverse hadron momenta up to 3.6 GeV/$c$. While the shape of the measured $p_T$-differential cross section agrees well with NLO pQCD over the full rapidity range, the present theoretical calculation underestimates the experimental cross section by a factor of three to four. Thus, the pQCD calculation at
NLO appears to be insufficient to fully describe high-$p_T$ hadron production in $\mu$-$N$ scattering at low $Q^2$ in the kinematic domain of COMPASS. The resummation of threshold logarithms beyond NLO might help to resolve this discrepancy. Once an agreement with the measured cross section has been established, the pQCD framework can be employed to constrain the polarization of gluons in the nucleon [20], using the double-spin asymmetry of single high-$p_T$ hadron production at low $Q^2$ extracted from the full COMPASS muon-scattering data set. This approach is complementary to previous measurements of the gluon polarization by COMPASS using polarized high-$p_T$ hadron-pair production [30] [31], which employ the MC generators PYTHIA and LEPTO [32], respectively, to quantify the contribution of PGF to the cross section.

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References

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Table 1: Measured cross section for high-$p_T$ hadron production in $\mu$-$N$ scattering at $\sqrt{s_{\mu N}} = 17.4$ GeV. The cross section is integrated over the full kinematic range defined in the text. The columns show: (1) $p_T$ range of the bin; (2) $p_T$ value of data point in Fig. 1; (3) differential cross section summed over hadron charges (please note that there is an additional 10% normalization uncertainty from luminosity); and (4) charge ratio of the cross section.

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\begin{array}{cccccc}
[p_T, p_T', (\text{GeV/c})] & \langle p_T \rangle_{\text{res}} (\text{GeV/c}) & \frac{d\sigma}{dp_T} = \int_{p_T}^{p_T'} \frac{d\sigma}{dp_T} (\text{pb GeV}^{-1} c^{-\frac{2}{2}}) & \frac{d\sigma}{dp_T} (h^-) / \frac{d\sigma}{dp_T} (h^+) \\
[1.125, 1.375] & 1.239 & 2.810 \pm 0.006 \text{ (stat.)} & 0.874 \pm 0.004 \text{ (stat.)} \\
[1.375, 1.625] & 1.489 & 9.87 \pm 0.04 \text{ (stat.)} & 0.864 \pm 0.007 \text{ (stat.)} \\
[1.625, 1.875] & 1.739 & 3603 \pm 23 \text{ (stat.)} & 0.850 \pm 0.011 \text{ (stat.)} \\
[1.875, 2.125] & 1.989 & 1261 \pm 14 \text{ (stat.)} & 0.829 \pm 0.018 \text{ (stat.)} \\
[2.125, 2.375] & 2.239 & 421 \pm 8 \text{ (stat.)} & 0.800 \pm 0.030 \text{ (stat.)} \\
[2.375, 2.625] & 2.489 & 148 \pm 5 \text{ (stat.)} & 0.85 \pm 0.06 \text{ (stat.)} \\
[2.625, 2.875] & 2.739 & 55.9 \pm 3.0 \text{ (stat.)} & 0.83 \pm 0.09 \text{ (stat.)} \\
[2.875, 3.125] & 2.989 & 21.7 \pm 1.9 \text{ (stat.)} & 0.78 \pm 0.14 \text{ (stat.)} \\
[3.125, 3.375] & 3.239 & 9.08 \pm 1.25 \text{ (stat.)} & 0.80 \pm 0.23 \text{ (stat.)} \\
[3.375, 3.625] & 3.490 & 3.40 \pm 0.80 \text{ (stat.)} & 1.0 \pm 0.5 \text{ (stat.)}
\end{array}
\]