BEAM DIAGNOSTICS FOR ACCELERATORS

H. Koziol

Abstract

This introductory course aims at a reasonably complete coverage of beam diagnostic devices used in linear and circular accelerators and in primary beam lines. The weight is on the concepts and the indication of variants, while for technical details the reader is referred to the literature. The present updated version replaces those from previous General Accelerator Physics Courses.

Course given at the CERN Accelerator School, Loutraki, Greece
October, 2000

CERN, Geneva, Switzerland
8 May, 2001
CONTENTS

1. INTRODUCTION

2. DESCRIPTION OF DIAGNOSTIC DEVICES (with commonly used abbreviations)

   2.01 Beam Transformers (BT)
   2.02 Wall-Current Monitors (WCM)
   2.03 Pickups (PU)
   2.04 Faraday Cup
   2.05 Secondary Emission Monitors (SEM)
   2.06 Wire Scanners (WS)
   2.07 Multiwire Chambers (MWC)
   2.08 Ionization Chambers
   2.09 Beam Loss Monitors (BLM)
   2.10 Gas Curtain
   2.11 Residual-Gas Profile Monitors
   2.12 Scintillator Screens
   2.13 Optical Transition Radiation (OTR)
   2.14 Synchrotron Radiation
   2.15 Compton Scattering
   2.16 Scrapers and Measurement Targets
   2.17 Beamscope

3. SOME MORE COMPLEX MEASUREMENT SYSTEMS

   3.01 Q-Measurement
   3.02 Schottky Scans
   3.03 Emittance Measurement
   3.04 Measurement of Energy, Spectrometer
   3.05 Polarimetry

4. CONCLUDING REMARKS

5. ACKNOWLEDGEMENTS

6. APPENDICES

   6.01 Signal-Level on an Electrostatic Pickup
   6.02 Coulomb-Interaction of Beam Particles with Matter
   6.03 Statistical Limit on Secondary Emission Signals & Similar
   6.04 Vanishing Width of Schottky Sidebands

7. LITERATURE
1. INTRODUCTION

Beam diagnostics is an essential constituent of any accelerator. These systems are our organs of sense that let us perceive what properties a beam has and how it behaves in an accelerator. Without diagnostics, we would blindly grope around in the dark and the achievement of a beam for physics-use would be a matter of sheer luck. As the saying goes: an accelerator is just as good as its diagnostics.

Beam diagnostics is a rich field that makes use of a great variety of physical effects. Imagination and inventiveness find a wide playground. Therefore, there exists today a vast choice of different types of diagnostic devices, each usually in many variants.

A few hours of lecture time do not permit an in-depth coverage of all devices on the market, but to present only a selection would not fulfill the purpose of a general course. The choice was made to aim at a reasonably complete coverage of diagnostic devices currently used, at the expense of detail. We will thus concentrate on the concepts and indicate the variants that exist, and for details refer to the appended "List of Helpful Literature" (no references are made in the text).

Also, we will limit ourselves to diagnostics used on accelerators and on ejected primary beams and leave aside detectors for secondary beams, on their way from the target to a particle physics experiment. As a further economy measure, we will also leave aside associated electronics, analogue signal processing and digital data treatment, although these are fields of great importance to beam diagnostics.

There are subjects which were treated in other lectures, e.g. synchrotron radiation, which permits us to be briefer on those. Very specialized measurements, such as beam polarization or those at the final focus of colliding linacs, are beyond the aim of an introductory course and are just mentioned for completeness.

When setting out to describe a large number of diagnostic devices, one first tries to establish a systematic order. One could proceed according to the properties measured (intensity, position, etc.). Or one could class the devices as electromagnetic, using secondary emission, etc., or as destructive and non-destructive. However, none of that makes much sense. Many devices can measure more than one property, their variants may make use of different physical principles, and the distinction between destructive and non-destructive often depends on circumstances.

I have therefore drawn up a matrix (Table 1) listing the devices to be discussed and the properties they can measure. And now we will forget about classification and get on with the description in a sequence that is didactically convenient.
### Table 1
Diagnostic devices and beam properties measured

<table>
<thead>
<tr>
<th>PROPERTY MEASURED</th>
<th>transverse</th>
<th>longit.</th>
<th>Effect on beam</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Intensity/charge</td>
<td>Position</td>
<td>Size/shape</td>
</tr>
<tr>
<td>Beam transformers</td>
<td>●</td>
<td>●</td>
<td>●</td>
</tr>
<tr>
<td>Wall-current monitors</td>
<td>●</td>
<td>●</td>
<td>●</td>
</tr>
<tr>
<td>Pick-ups</td>
<td>●</td>
<td>●</td>
<td>●</td>
</tr>
<tr>
<td>Faraday cup</td>
<td>●</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Secondary emission monitors</td>
<td>●</td>
<td>●</td>
<td>●</td>
</tr>
<tr>
<td>Wire scanners</td>
<td>●</td>
<td>●</td>
<td>●</td>
</tr>
<tr>
<td>Wire chambers</td>
<td>●</td>
<td>●</td>
<td>●</td>
</tr>
<tr>
<td>Ionization chambers</td>
<td>●</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Beam loss monitors</td>
<td>●</td>
<td>●</td>
<td>●</td>
</tr>
<tr>
<td>Gas curtain</td>
<td>●</td>
<td>●</td>
<td>●</td>
</tr>
<tr>
<td>Residual-gas profile monitors</td>
<td>●</td>
<td>●</td>
<td>●</td>
</tr>
<tr>
<td>Scintillator screens</td>
<td>●</td>
<td>●</td>
<td>●</td>
</tr>
<tr>
<td>Optical transition radiation</td>
<td>●</td>
<td>●</td>
<td>●</td>
</tr>
<tr>
<td>Synchrotron radiation</td>
<td>●</td>
<td>●</td>
<td>●</td>
</tr>
<tr>
<td>LASER-Compton scattering</td>
<td>●</td>
<td>●</td>
<td>●</td>
</tr>
<tr>
<td>Polarimetry</td>
<td>●</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Scrapers and measurement targets</td>
<td>●</td>
<td>●</td>
<td>●</td>
</tr>
<tr>
<td>Beamscope</td>
<td>●</td>
<td>●</td>
<td>●</td>
</tr>
<tr>
<td>Q-measurement</td>
<td>●</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Schottky scans</td>
<td>●</td>
<td>●</td>
<td>●</td>
</tr>
<tr>
<td>Emittance measurement</td>
<td>●</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Measurement of energy</td>
<td>●</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Effect on beam: N none, - slight, negligible, + perturbing, D destructive

Only the most basic measured properties are shown. There are many more, less basic, which can be derived: coupling, dispersion, chromaticity, etc. Note that to determine emittance (transverse or longitudinal), knowledge other than that obtained from the basic measurement is required. The oscillatory behaviour of the beam is observed through the time-dependance of properties (like position, size/shape, energy), often on a very fast time scale.
2. DESCRIPTION OF DIAGNOSTIC DEVICES

2.01 Beam Transformers (BT)

Apart from the sheer proof of its existence, the most basic measurement on a beam is that of its intensity. A widely used device is the "beam transformer" (an older name is Rogowski coil) which allows one to determine the electric current that a beam constitutes or, depending on the circumstances, the electric charge contained in a burst of beam. Figure 1 shows the principle.

![Fig. 1 Principle of the BT.](image)

In order for the BT to see the magnetic field produced by the beam, it must be mounted over a ceramic insert in the metallic vacuum chamber. The ferromagnetic core is wound of high-permeability metal tape or made of ferrite, to avoid eddy currents. Bandwidths exceeding 100 MHz can thus be achieved. An idealized BT with a secondary winding of inductance L and connected to an infinite impedance would deliver as signal a voltage

\[ V = L \frac{dI_b}{dt} \]

which, as Fig. 2 shows, is "differentiated" and not very practical to use.

In reality, the ferromagnetic core has losses proportional to \( f^2 \) (\( f \) = frequency), the secondary has a stray capacity \( C_s \) and is terminated with a finite resistance \( R \) (Fig. 3).

![Fig. 2 Signal from an idealised BT into an infinite impedance.](image)

![Fig. 3 Real BT with stray-capacity \( C_s \) and termination \( R \).](image)
The signal now shows a much more useful behaviour (Fig. 4). Provided the length of a beam bunch is longer than the BT rise time and shorter than its droop time, the signal will be a good reproduction of the bunch shape. Here, one is confronted with the "L-dilemma" (for a short rise time, one wants L to be small; for a long droop time, one wants L to be large) and has to pick the best compromise.

![Diagram of primary and secondary pulses with rise and droop times](image)

Fig. 4 Signal from real BT.

When, instead of a single bunch, a long string of bunches passes through the BT, as is also the case with a circulating beam, the droop will affect the base-line (Fig. 5). When equilibrium has been reached, equal areas of signal will be above and below zero. Thus, the level of the base-line is a measure for the dc component of the beam current.

![Diagram of droop of base-line in BT signal](image)

Fig. 5 Droop of base-line in the BT signal.

For a beam circulating in a machine, the succession of bunches seen by the BT will be much longer than its droop time. Therefore, to obtain a signal representing the beam intensity, one has to treat electronically the BT signal such that the effective droop time is much longer than the time that the beam circulates. At the same time, this increases the signal rise time, so that the bunch structure will disappear. Such a treatment is often called "low-pass" or "integration". Figure 6 shows three commonly used methods.

Since integration makes the bunch structure disappear, it produces an intensity signal also for an unbunched beam, without any longitudinal density structure, provided that signal observation begins before injection of the beam.

Adding a simple RC may sometimes suffice, but in general, the time constants will be too short and/or the signal too attenuated. Feedback integrators allow time constants above 1000 s to be achieved, while maintaining a good signal level. They are widely used on circular accelerators, where cycle times are of the order of seconds.
In a storage ring, however, the beam may circulate for hours. Indeed, 999 h, or 42 days, is the longest a beam has circulated uninterrupted (in the Antiproton Accumulator at CERN). No integrator can cope with that, and a true dc beam-current measurement is needed. Such a device was developed for the ISR (the CERN Intersecting Storage Rings), the first machine to sustain beams for hours. Figure 7 shows its principle.

A modulator sends a current at several 100 Hz through the excitation coils of two ferromagnetic rings, such that they are excited in opposite directions. The pick-up coils mounted on the rings are connected in series, so that their sum signal, $V_s$, will be zero. The rings are made of a material with rectangular hysteresis. When a beam current $I_b$ passes through the rings, it introduces a bias in the excitation of the cores, $V_s$ will no longer be zero and the second harmonic of the modulator frequency will appear in it, which the demodulator converts into a dc voltage. This controls a power supply, sending a current $I_c$ through a compensating winding on the two rings. Equilibrium is reached when the compensating
current $I_c$ cancels the beam current $I_b$. The final measurement is that of $I_c$. Proton currents of over 50 A have been measured with such a dc-BT. A resolution of better than 1 μA has been achieved, and the zero drift over a week is of the same order.

Such dc-BTs have become commercially available, for various ranges of current and sensitivity. Typically, their resolution is in the μA-range. In recent years, the "Cryogenic Current Comparator", using superconducting transducers (SQUIDs), has extended the resolution to the nA-range.

### 2.02 Wall-Current Monitors (WCM)

One may want to observe the bunch shape at frequencies far beyond the few 100 MHz accessible with BTs. The bunches may be very short, as is often the case with electrons or positrons, or they may have a structure in their line density, caused by intentional processes or by instabilities.

WCMs with a bandwidth of several GHz have been built. Their principle is quite simple (Fig. 8a):

![Fig. 8a] Principle of a WCM. b) Separate pick-up of signals to observe beam position.

A modulated beam current $I_b$ is accompanied by a "wall-current", $I_W$, of equal magnitude and opposite direction, which it induces in the vacuum chamber. An insulating gap forces the wall-current to pass through the impedance of a coaxial cable. The gap may also be bridged with resistors, across which a voltage is picked up. To avoid perturbation through circumferential modes, the wall-current (or the gap-voltage) is picked up at several points around the circumference and summed. When the beam is not at the centre of the vacuum chamber, the wall-current will be unequally distributed around the circumference of the chamber. Separate pick-up and separate observation (Fig. 8b) will thus also show the beam position with GHz bandwidth.

![Fig. 9] Gap of WCM with shield and ferrite loading.

A conducting shield must be placed around a WCM. Without it, troublesome electromagnetic radiation from the beam would leak out through the gap, and the monitor
itself would be perturbed from the outside. Of course, the shield constitutes a short-circuit at low frequencies and thus severely limits the lower end of the monitor's bandwidth. Loading the volume of the shield with ferrite increases the inductance and the cut-off can be lowered to some 100 kHz, sufficient for undifferentiated observation of bunch shape in most accelerators.

2.03 Position Pickup Monitors (PU)

The measurement of transverse beam position is a field of particularly great diversity. A glance at Table 1 shows a host of detectors, based on various physical effects. Three kinds are treated in this chapter:

- electrostatic,
- magnetic,
- electromagnetic.

The electrostatic PU is widely used, in particular on circular accelerators with not too short bunches. In its simplest form it resembles a diagonally cut shoe-box (Fig. 10 a, b). A combination of a horizontal and a vertical PU is shown in Fig. 11.

\[
x = \frac{w}{2} \frac{U_R - U_L}{U_R + U_L}
\]

where \( w \) is the total width of the PU, as shown in Fig. 10b. Due to capacitive coupling between the electrodes, the PU will have an effective width, larger than the geometric value of \( W \). The position \( x \) of the beam thus determined, is that of the centre of gravity of the electric charge contained in it.

Frequently, the jargon terms "\( \Delta \)" and "\( \Sigma \)" are used: \( \Delta = U_R - U_L \) and \( \Sigma = U_R + U_L \). Using them:
\[ x = \frac{w \Delta}{2 \Sigma} \]

Fig. 11 Combination of a horizontal and a vertical PU, mounted in the vacuum chamber of the Antiproton Accumulator at CERN.

The linear relation holds for any shape of the electrodes, as long as the length of the electrodes, projected onto the plane in which the position is measured, is a linear function of the distance from the axis. Hence, the shape of the electrodes may be deformed to suit practical requirements. A variation is shown in Fig. 10c, where the free gap allows placing two further electrodes in the orthogonal plane. However, although \( U_R - U_L \) still depends linearly on beam position, \( U_R + U_L \) is no longer independent of it. For normalization, the sum of all four electrodes must be used.

Edge effects at the ends of the electrodes may impair the linearity. To avoid them, one either designs the electrodes to have the same cross-section as the vacuum chamber at either end, or one provides cross-sectional continuity by adding guard electrodes at both ends.

In electron and positron machines, no electrodes can be tolerated in the mid-plane, where they would be hit by the synchrotron radiation and the resulting secondary electron emission would perturb the signal. So-called "button" electrodes are used, housed in recesses (Fig. 12a).

![Fig. 12 a) PU with "button" electrodes. b) Magnetic PU.](image)

Compared with the shoe-box PU, for the measurement of horizontal position \( U_1 + U_3 \) replaces \( U_L \), and \( U_2 + U_4 \) replaces \( U_R \), similarly the sums \( U_1 + U_2 \) and \( U_3 + U_4 \) for the
vertical plane. The response to position is not linear and the two planes are interdependent. Careful calibration and consequent data treatment on the signals is necessary.

In proton machines too, secondary emission from the electrodes can be a problem when strong beam loss occurs. In such a situation, a magnetic PU may be chosen (Fig. 12b).

In single-ring colliders, two beams, one of particles, the other of anti-particles, are circulating simultaneously, in opposite directions. "Directional couplers" permit the selective observation of only one of the beams in the presence of the other. The principle is shown in Fig. 13a.

The beam acts in two ways on the strip electrodes of the coupler. Firstly, the electric charge of the passing beam induces a charge on them. Secondly, part of the magnetic field, created by the beam current, passes between the strip and the vacuum chamber and induces a voltage. These two effects add for the direction of the beam shown in Fig. 13a, and cancel for a beam of opposite direction.

Four strips (Fig. 13 b), after suitable formation of sums and differences of the signals, give the horizontal and vertical beam position. The sensitivity of such a PU depends on frequency, as $|\sin f|$, with the maximum where the strip length corresponds to a quarter wave length. The response can be influenced by giving the strips more sophisticated shapes.

A "wave-guide coupler" (Fig. 14), can be used, usually on electron and positron linacs, to observe extremely short bunches ($\ll 1$ nsec). The beam passing through it sets off a wave which propagates to the left and the right, where it is picked up by small loops on the inside of the wave guide. The position is not derived by comparing the magnitude of $U_L$ and $U_R$, but by comparing their phase: $x \sim \Delta \phi$.

---

Fig. 13 a) Principle of directional coupler. b) Cross-section with four coupler strips. c) Frequency response.

Fig. 14 Wave-guide coupler. Beam position affects the right/left path-lengths of the induced
wave, resulting in a phase difference between $U_L$ and $U_R$.

To measure the closed orbit in a circular accelerator, many PUs are arranged around the circumference. A rule-of-thumb says that at least four position measurements per betatron wavelength are required to see closed orbit distortions sufficiently well. For example, a Q-value around 3.5 demands at least 14 PUs, uniformly spaced not in linear length but in betatron phase advance. From that minimum, one will then go up to the nearest number that fits with the periodicity of the machine for a regular installation pattern.

Special kinds of PU have been conceived to obtain information on the shape of the beam, in terms of aspect ratio between its horizontal and vertical size. This is a very tricky task and quantitatively satisfactory results are difficult to obtain. "Quadrupole PUs" have been developed for quantitative observation of beam shape oscillations. With these, one can verify betatron matching, after injection into a circular machine.

### 2.04 Faraday Cup

Conceptually the simplest way to measure beam current is to capture the beam and let the current flow through some kind of meter. Historically, this was also the first method used. It is still employed at low energies, where the obvious condition of the thickness of the collector plate being greater than the stopping range of the beam particles can be easily fulfilled. Here are some ranges for protons in copper:

<table>
<thead>
<tr>
<th>Energy</th>
<th>Collector Type</th>
<th>Thickness</th>
</tr>
</thead>
<tbody>
<tr>
<td>500 keV</td>
<td>pre-accelerator: Cockcroft-Walton or RFQ</td>
<td>0.003 mm</td>
</tr>
<tr>
<td>5 MeV</td>
<td>van de Graaff generator</td>
<td>0.08 mm</td>
</tr>
<tr>
<td>50 MeV</td>
<td>injector linac</td>
<td>4 mm</td>
</tr>
<tr>
<td>200 MeV</td>
<td>injector linac</td>
<td>43 mm</td>
</tr>
<tr>
<td>1 GeV</td>
<td>small synchrotron</td>
<td>520 mm</td>
</tr>
</tbody>
</table>

Capture of the beam with a simple collector plate suffers from perturbation due to secondary electron emission. Electrons liberated from the collector surface escape into the surroundings, thereby contributing in an uncontrolled way to the current flowing through the meter. The use of a Faraday Cup (Fig. 15) prevents this. The collector is housed in a box with a hole to let the beam in and at a negative potential of a few 100 V to drive the secondary electrons back onto the collector.

![Diagram](image.png)

**Fig. 15** a) Simple collector; b) Proper Faraday Cup.

### 2.05 Secondary-Emission Monitors (SEM)

At this point, the reading of Appendices 6.02 and 6.03 is recommended. They cover aspects common to the detectors described in this and several following sections.
A SEM makes use of the phenomenon that under the impact of the beam particles on some solid material, electrons are liberated from the surface, thus producing a flow of current.

Fig. 16 a) Basic SEM: foil with clearing electrodes, seen sideways. b) A SEM consisting of an array of ribbons, seen in beam direction. c) Transverse beam profile obtained from an array of ribbons or wires.

When the intercepting material is a foil (Fig. 16 a), electrons are liberated from both sides. Since this is a surface phenomenon, the secondary emission coefficient will not only depend on the material but also, often even critically, on the state of cleanliness of its surface.

The provision of a "clearing field" of a few 100 V/cm is essential to ensure that the liberated electrons are rapidly cleared away. Otherwise, an electron cloud may form over the foil surface and impede further emission.

Fig. 17 A SEM made of thin ribbons attached to contacts on a ceramic frame.

A SEM in the form of an array of thin ribbons (Figs. 16b and 17) is a much-used device to measure transverse density distribution. A sequential display of the signals from the ribbons gives the beam profile (Fig. 16c). To enhance the signal strength, either the individual ribbons or the whole array may be inclined with respect to the beam direction, thus presenting a greater effective surface. When signal strength is not a problem, the array and the clearing electrodes may be made of thin wires. This makes it an almost non-destructive profile monitor (at least for single passage, not for a circulating beam).

Secondary emission being a surface effect, it can be greatly altered (usually enhanced) through surface contamination. Rigorous cleaning procedures must be applied to obtain long-term stability of the monitors.

2.06 Wire-Scanners
When a SEM, made of several wires, disturbs the beam too much, mostly through multiple Coulomb scattering, a single wire may be moved across the beam. This can be done in steps and readings taken, e.g., at every pulse of a linac.

A fast-moving wire can be used even on a circulating beam. Speeds of 20 m/s have been obtained with thin Be or C wires, which allowed profiles to be measured on an 800 MeV proton beam, causing an acceptably small emittance increase (Fig. 18).

![Fast wire-scanner](image18.png)

Fig. 18 Fast wire-scanner. The wire, stretched between the tips of the lightweight arms, is actually a twisted strand of 15 C wires, each 6 µm in diameter, and thus barely visible.

Wire-scanners too need a clearing field in order to obtain a consistent signal. The clearing electrode will be situated well outside the beam cross-section.

An alternative is not to use the secondary emission current, but to place radiation detectors at the outside of the vacuum tank in which the wire moves, and observe the products of the collisions between beam particles and wire material (γ and secondary particles). This may require thin parts in the wall of the tank, and the signal from two or more radiation detectors to be summed to render the sensitivity independent of wire position.

### 2.07 Multi-Wire Chambers

These detectors, taken over from high-energy physics, find some application on beams of very low intensity. For example at LEAR (the CERN Low Energy Antiproton Ring), from which in an "ultra-slow extraction" as little as 1 antiproton was ejected on average per revolution, yielding beams of less than 10⁶ ̅π/s.

![Multi-wire chamber](image19.png)

Fig. 19 Multi-wire chamber. Typically, the distance between the cathode foils is 10 mm, the distance between wires 1 mm, their diameter 5 to 50 µm and their potential +5 kV.

Electrons produced in the gas by the passing beam particles will travel towards the
nearest wire. In the high gradient close to the wire they experience strong acceleration and create an avalanche. A wire chamber can be used in counting or in proportional mode. The distribution of counting rate or signal height over the wires represents the beam profile.
2.08 Ionization Chamber

This is a gas-filled, thin-walled chamber with a collector electrode inside. Particles passing through it will ionize the gas; the ions will travel towards the cathode, the electrons towards the anode, and a current can be measured (Fig. 20). The voltage should be in the "plateau" region where all charges are collected but no avalanche occurs.

![Ionization Chamber](image)

Fig. 20 a) Ionization chamber. b) Collection efficiency vs. voltage.

Ionization chambers are used to measure very low beam intensities and as beam loss detectors (see section 2.09).

2.09 Beam Loss Monitors (BLM)

Although they do not measure a beam property, the information which they supply is most valuable for the practical operation, of high-intensity machines in particular. Here the loss of a minute fraction of the beam, too small to be reliably measured with beam transformers, causes intolerable levels of radiation and/or induced radioactivity of components. High-intensity machines are therefore equipped with a large number of BLMs around their circumference to indicate the location and magnitude of losses for remedial action, sometimes in a fast, automatic way.

In accelerators employing superconducting magnets, the heat deposited in the superconductors by the loss of even minute fractions of the beam can cause a "quench", that is the loss of superconductivity of a part of the magnet coil, with potentially disastrous consequences. Here, BLMs are indispensible elements in the safety chains which dump the beam in a safe way before the losses can rise to dangerous levels.

Calibration in terms of number of particles lost is usually obtained by intentional loss of a measured fraction of the beam, but is neither easy nor very precise. Besides the pure statement of loss, BLMs with a fast response yield information on its cause and mechanism.

Three widely used kinds of BLM will be described briefly:

- Ionization chamber (see section 2.08),
- Aluminium Cathode Electron Multiplier (ACEM),
- Scintillator plus photomultiplier (PM).

An ACEM is similar to a PM, with a thin aluminium layer on the inside of the glass tube serving as the cathode. Electrons are produced from the cathode through secondary
emission when it is struck by a stray beam particle, a $\gamma$-ray, or some secondary particle resulting from beam loss. As with a PM, the gain is high and adjustable over a wide range, and an ACEM is cheap, robust and radiation-resistant.

Another very cheap and effective BLM is a combination of a scintillator and a PM as shown in Fig. 21. The primary effect here is the production of light.

Fig. 21 A photomultiplier immersed in scintillator oil is a cheap and fast beam loss monitor.

With this type, bandwidths of 100 MHz are possible, allowing one to see details, such as loss from only part of the bunch length, as happens, for example when a kicker magnet is incorrectly triggered. Fast BLMs can be usefully employed to study any beam dynamics phenomena connected with beam loss.

2.10 Gas-Curtain

In section 2.06 we have seen that a fast wire scanner can measure the transverse profile of a beam circulating in an accelerator, once or twice per cycle. In a storage ring, where one wants to measure the profile repeatedly over the many hours that a beam circulates, a wire scanner would cause too much scattering and emittance increase. Only a gas constitutes a sufficiently transparent interceptor. Figure 22 shows the gas-curtain profile-monitor developed for the CERN Intersecting Storage Rings (ISR).

Fig. 22 Sodium-curtain beam profile monitor, seen in the direction of the Na-jet.

An ultrasonic 2-dimensional jet of atomic Na is produced in an oven followed by a collimation system. The Na-jet is inclined at 45° to the beam direction. Electrons from the ionization of Na atoms by beam particles are accelerated by a vertical electric field, while being focused along the lines of a magnetic field, also in the vertical direction. On the top of
the tank there is a quartz window which on its inner side carries a layer of scintillator (incorrectly often called phosphor), covered with a very thin metal layer as the anode for the electric field. The accelerated electrons will traverse the metallization and produce light in the scintillator, thus forming a 2-dimensional image of the beam cross-section. This image can be viewed with an image-intensifier TV camera for direct display or with some other device for further data treatment.

All this sounds easy but in practice is very difficult to realize because of the stringent boundary conditions. The magnetic field needs to be compensated by additional coils on either side of the detector, so as not to perturb the closed orbit. The Na-jet must be extremely well collimated and entirely collected on the other side to avoid contamination of the vacuum. Its density must be controlled to constitute only a small increase in the average pressure of the ring. Consider the circumference of the ISR of 1 km and an average pressure of $10^{-11}$ Torr. A Na-curtain 1 mm thick and of an equivalent pressure of $10^{-5}$ Torr would have doubled the average pressure around the circumference!

The ISR have been dismantled and the Na-curtain monitor with them. It will probably remain the only one of its kind, but many lessons have been learnt from its design and operation.

### 2.11 Residual-Gas Monitors

When neither the residual gas pressure nor the beam intensity are too low, ionization of the "natural" residual gas may supply electrons in sufficient number, so that a gas-curtain is not needed. Otherwise the device is identical to the one shown in Fig. 22. However, the image appearing on the scintillator will not be 2-dimensional, as it is the projection of the beam density distribution onto one plane. Two devices are needed for a horizontal and a vertical profile.

Instead of collecting electrons from the ionization, one can also observe the light from de-excitation of the residual gas atoms. This is achieved more easily at the low energies of a pre-injector (500-800 keV) combined with the prevalent modest vacuum.

### 2.12 Scintillator Screens

Scintillators were the first particle detectors, more than a century ago. When accelerators, instead of cosmic radiation and radioactive samples, began to deliver particles, scintillators were the prime means to detect the existence of a beam and its location. Although many people turn up their nose at them as an old-fashioned relic from pioneer days, scintillator screens are still alive and not beaten in their simplicity, cheapness and power of conviction. Even today, where everything gets digitized, data-treated, fitted, smoothed, enhanced and finally displayed, there is nothing as convincing as a flash of light, dead on the centre of a scintillator screen.

Fig. 23 shows a typical arrangement for measuring beam position and, less quantitatively, size. A scintillator screen (often incorrectly called phosphorescent, fluorescent or luminescent) is moved into the path of the beam. It is inclined at $45^\circ$ to the beam, carries a graticule and is illuminated through a small window in the tank. Through another window, at
90° to the beam direction, a TV camera will see a 2-dimensional image of the beam cross-section. Figure 24 shows a vertically movable screen in its tank.

The most common scintillator used to be ZnS powder which, with some binder, was painted onto a metal plate. Such screens deliver green light and have high efficiency but are unfit for use in high vacuum and burn out at some $10^{14}$ protons/cm$^2$ at GeV energies.

A great step forward was the formation of thick Cr-doped Al$_2$O$_3$ layers on aluminium plates. This is chemically the same as ruby and the light emitted is red. These screens are fit for ultra-high-vacuum and have a long lifetime ($10^{20}$ to $10^{21}$ p/cm$^2$ at 50 MeV).

![Fig. 23 Typical arrangement for observation of beam position and size with a movable scintillator screen and a TV camera.](image)

![Fig. 24 Scintillator screen made from a Cr-doped Al$_2$O$_3$ plate with imprinted graticule.](image)

The most frequently used screens are thin plates (1 mm or less) of Cr-doped Al$_2$O$_3$ which can be obtained from industry in all sizes. A graticule and other references can be printed directly on their surface. The screen in Fig. 24 is of that kind. Figure 25 shows another
one, mounted on the antiproton production target of the CERN Antiproton Accumulator. It has received some $10^7$ pulses of $10^{13}$ protons at 26 GeV in a spot of about 3 mm diameter (every 2.4 s during some 6000 h of operation in 1 year), i.e. over $10^{20}$ p/cm$^2$. This was and still is the most important means of keeping the beam on the target with a precision of ± 0.5 mm.

![Scintillator plate mounted on the antiproton production target of the CERN Antiproton Accumulator.](image)

Fig. 25 Scintillator plate mounted on the antiproton production target of the CERN Antiproton Accumulator.

Several aspects of the TV camera deserve attention. Often it needs to be radiation-resistant. The model developed at CERN uses nuvistors and withstands $10^6$ Gray. Ordinary lenses turn brown under radiation. Catadioptric optics do a bit better, but when radiation is really a problem, one has to buy expensive lenses developed for use in nuclear reactors.

For very weak beams a combination of Image Intensifier plus Vidicon is used. Beams of $10^9$ protons of GeV-energy in a cross-section of a few cm$^2$ are clearly visible. Also, CCD-cameras offer high sensitivity, but have poor radiation resistance.

TV images may be digitized and stored, for more convenient observation or image treatment to extract more quantitative information.
2.13 Optical Transition Radiation (OTR)

When a fast particle crosses the boundary between two media of different dielectric constant, it emits radiation called "Optical Transition Radiation". The effect has been known since 1946, but its use for beam diagnostics has become more widespread only over the last decade.

With respect to scintillator screens, usually about 1 mm thick, OTR has the advantage that it can be obtained from very thin foils, with much less scattering of the beam particles, and therefore less emittance increase. OTR is emitted from both sides of the foil. Fig.27 shows the situation at the entrance side.

For reasons of optical imaging, one wants the angle $\theta$ to be small, and therefore the use of OTR is limited to particles of reasonably high energy ($\gamma > 1$), say above 20 GeV for protons. Otherwise, OTR is used and treated as the light from a scintillator screen.

2.14 Synchrotron Radiation

What is a curse for the acceleration of electrons and positrons is a blessing for diagnostics. Synchrotron radiation, similar to Schottky noise, is a fairly ideal source of information, which is there for the taking (although the taking may be quite expensive).

Despite the subject's great importance for diagnostics, we will be brief here, since it is described elsewhere in these proceedings. Let us just recall two essential features: at almost all electron synchrotrons the spectrum includes the visible range; and the light is emitted into a very small angle, roughly $E_0/E$. 
For diagnostic purposes, light is extracted from the accelerator and transported to the measuring equipment by means of various optical elements, such as windows, mirrors, lenses and fibres. The receivers are TV cameras, CCDs, photo diodes (single or in an array), etc. The information obtained may be a simple, but very instructive, TV image on which one can visually follow the evolution of beam size; it may be a precise profile measurement; it may be a bunch length measurement with ps resolution which needs extremely fast oscilloscopes or a streak camera (that’s where it gets expensive).
In the context of synchrotron radiation, because of the dependence on \((E/E_0)^4\), one tends to think only of electrons. However, at the highest energies achieved in the last decades, even protons come up against this effect. Not so much yet that it would be a curse, but some blessing is already there. Synchrotron radiation induced by the abrupt change of field at the ends of the bending magnets was detected at the 400 GeV CERN SPS and used for profile measurement. The addition of an undulator provided the necessary enhancement of emission for continuous profile monitoring of the proton and antiproton beams, when the SPS was used as a 270 GeV \(p - \bar{p}\) collider.

### 2.15 LASER Compton Scattering

Compton scattering is the exchange of energy between a photon and a particle when they encounter each other, as shown in Fig. 28a. In a collision with an energetic moving particle, the highest gain of energy for the photon will occur in a head-on collision, for which the angle \(\alpha\) goes to zero. A photon of a few eV, in the visible range, encountering a multi-GeV electron or positron, may thus have its energy increased to several GeV. This case, in which it is the photon that gains energy, is often referred to as "Inverse Compton Scattering".

When one shines LASER light on an electron beam, the resulting high-energy photons travel with the beam until the next bending magnet, where they will fly straight on (Fig. 28 b). By detecting only the photons of highest energies, one selects those which have the same direction as the electron which they had encountered. One can thus measure the density distribution of the electron beam, either by scanning the beam with a fine LASER beam, or by illuminating it fully and evenly.

Fig. 28 a) The mechanism of Compton scattering. b) Shining LASER light on an electron beam produces high energy photons, which fly straight on at the next bending magnet.

Compton scattering is used with success for the measurement of electron and positron beam profiles. For proton beams its use is hindered by the fact that the cross-section for head-on events, in which the photon gains high energies in the particle-forward direction, is proportional to \(1/E_0^2\) (\(E_0\) the rest-mass of the particle).
2.16 Scrapers and Measurement Targets

Incremental destruction of a beam with scrapers permits the determination of the betatron amplitude distribution of the particles. A scraper with four movable blades (Fig. 29a), used in conjunction with a dc-BT, allows measurement in the horizontal and vertical plane in a storage ring, where there is time to move the blades towards and into the beam.

![Fig. 29 a) Scraper with four blades for horizontal and vertical measurement. b) Beam intensity vs. blade position. c) Amplitude distribution.](image)

Observing the decrease of beam intensity as a blade advances, one obtains the beam size for a given fraction of the total intensity and, through differentiation, the amplitude distribution. In principle, a single blade in each plane would suffice, but for independent and consistent determination of the beam centre, one blade on each side is needed. This will also diagnose a "hollow" beam, in which there are no particles with zero or small betatron amplitudes. In the horizontal plane, the distribution of the particles is given by the spread in betatron amplitude and by the spread in momentum. Either one places the scraper where the dispersion is zero, or one has to unfold the two spreads.

Although scrapers are destructive and slow, they are valuable for their precise and reliable information. They can serve for the calibration of non-destructive emittance measurements, such as Schottky scans of betatron bands (see section 3.02), and for intentional limitation of machine acceptance.

The beam particles are not stopped in the scraper blades, they are merely scattered. After several traversals of the blades their betatron amplitude has grown beyond the machine acceptance and they are lost somewhere around the ring. Energy loss in the blades usually plays a lesser role.

On accelerators with short cycle time and fast-shrinking beam size, scrapers as described above are not applicable. The same principle can still be employed by driving the beam into a stationary blade by means of a pulsed closed orbit distortion (the so-called "Beamscope"). Fast measurement targets have also been built (Fig. 30). The position of the two blades is pre-adjusted and then the target is flipped into the beam in a movement perpendicular to the plane of measurement. Interception times of only a few ms are thus achieved.
3. SOME MORE COMPLEX MEASUREMENT SYSTEMS

3.01 Q-Measurement

Q, the number of betatron oscillations per revolution in a circular machine, is really a property of the machine rather than of the beam (although an intense beam, through the forces which its own charge produces, can influence it). The exact value of Q is of great importance in storage rings, in which beams may be kept circulating for hours while being subjected to strong non-linear forces, caused by their own charge or from the second beam in a collider. Sometimes, variations of Q by a few 0.0001 of an integer decide about the well-being of the beam.

A straightforward way to measure Q is to let a bunch of particles perform a coherent transverse oscillation, e.g. by misadjusting injection conditions, and measure the beam position on all PUs around the ring for one turn. Subtracting from these readings the previously-measured closed orbit positions, normalizing to the square-root of the betatron function at each PU and plotting the result as a function of betatron phase, one obtains a sine-curve, the frequency of which is easily judged to 0.05 of an integer. A merit of this method is that it yields the full value of Q. That is no mean feature, as there have been cases where even the integral part of Q was not as expected.

A similar method is to deform the closed orbit by means of a single dipolar bump. The change in closed orbit, treated as above, yields a sine-curve with a kink at the location of the bump.

Usually, Q is measured by observing the signal from a single PU which, at each revolution, records the position of the beam, excited somehow to perform a coherent betatron oscillation (Fig. 31).

Fig. 31 A single PU records the position of an oscillating beam at every revolution.
As an example, Fig. 32 shows in large dots the position of an oscillating bunch on six subsequent turns. Intuitively, one would draw a sine-curve through the data points and obtain the one labelled 0.23. However, sine-curves of other, higher, frequencies also pass through the same data points. Two, labelled -0.77 and 1.23, are shown, but it is true for all frequencies $f_m$

$$f_m = (m \pm Q) f_{rev}$$

where $f_{rev}$ is the revolution frequency and $m$ the mode. These are also the "betatron sidebands" of section 3.02 and Fig. 38.

![Fig. 32 Beam position on six subsequent turns and the three lowest-frequency fits.](image)

Analysis of the signal from a single PU can deliver very precise results, to a few $0.0001$ of an integer, but says nothing about the value of $m$. Consequently, the integral part, $[Q]$, remains unknown and one cannot even distinguish between $q = Q-[Q]$ and its complement $1-q$ (0.23 and 0.77 in Fig. 32). In order to determine whether $q$ is above or below 0.5, one may change the focusing properties of the machine (e.g. the current in the F- and D-quadrupole-lenses) and observe in which direction this shifts the frequencies $f_m$, or one resorts to one of the two first-mentioned methods.

The methods using the signal from a single PU are many. They differ in the way in which the beam is excited and in which the signal is analyzed. Historically, the first method was to excite a beam by applying an rf voltage to a transverse kicker (a pair of electrode plates, Fig. 33a). Scanning with the rf generator, one searched for the frequencies $f_m$ at which beam loss occurred, hence the term "rf knock-out". Today, one does it more gently, by detecting resonant excitation at harmlessly small amplitudes.

Often the beam is excited by a single kick lasting for a fraction of the revolution time, (Fig. 33 b). A filter selects a suitable $f_m$ for measurement with a counter, after a delay to allow the filter transients to die away. In selecting the band $f_m$ to be measured, one must consider length and shape of the kick, since the "response function" depends on them. As can be seen in Fig. 34, it may vanish for certain combinations of parameters, and there will be no signal at the output of the filter.
Fig. 33 Q-measurement. a) RF excitation; a feedback loop may provide lock-on. b) Application of a single short kick.

Alternatively, one may digitize the raw signal from the PU and obtain the frequencies \( f_m \) through mathematical analysis of the data, usually by Fast Fourier Transform (FFT).

No excitation at all is needed when one observes the Schottky noise, see section 3.02.

Fig. 34 Response function (vertical axis) for a rectangular kick, as a function of \( f_m/f_{\text{rev}} \) (left axis) and \( t_{\text{kick}}/t_{\text{rev}} \) (right axis).

3.02 Schottky Scans

This technical jargon term means scans in frequency (using a spectrum analyzer), of the Schottky signals emanating from a circulating beam. Schottky signals are at the basis of stochastic cooling but their great potential for diagnostic purposes was soon recognised. This subject has become quite vast and here we can only point out some salient features, for unbunched beams only.

Consider a single particle, circulating in a storage ring and observed with an ideal PU of
infinite bandwidth. The signal delivered by the PU is a series of delta-function-like spikes, spaced by 1 revolution period \( t_{\text{rev}} \), as shown in Fig. 35 a. A spectrum analyzer then displays what is shown in Fig. 35 b: a series of spectral lines, spaced by the revolution frequency \( f_{\text{rev}} \).

![Fig. 35](image)

Fig. 35  a) Time domain : signal on a PU from a single circulating particle  
b) Frequency domain : corresponding spectrum.

In a beam there are many particles and since there is a spread in their momentum, there will also be a spread in their revolution frequency. The observed Schottky signal can be regarded as the sum of all individual signals or as the noise stemming from statistical density fluctuations. The spectrum will be as in Fig. 36, with bands instead of lines, their width proportional to \( \Delta f = hf/f_{\text{rev}} \) and, provided the vertical coordinate is the spectral power density, of equal area. From such a scan, \( f_{\text{rev}} \), \( \Delta f_{\text{rev}} \) and (assuming \( \eta = \frac{[df/f]}{[dp/p]} \) is known) \( \Delta p \) are immediately obtained.

![Fig. 36](image)

Fig. 36 Schottky scan of a many-particle beam with a spread in momentum and therefore in frequency.

The area of each band is a measure of beam intensity. Extremely low beam intensities can thus be diagnosed with Schottky scans, after calibration against a BT at higher intensities. At the CERN Antiproton Accumulator, where \( 10^6 \) to \( 10^8 \ \overline{p} \) were injected per pulse, the reproducibility in the intensity measurement by Schottky scan corresponded to \( 10^4 \ \overline{p} \). The most sensitive measurement to date was performed on an experimental cooling ring, ICE. In the course of an experiment to set a new lower limit on the lifetime of the \( \overline{p} \), a beam of 250 \( \overline{p} \) was made to circulate and after 86 h there remained 85 \( \overline{p} \). The error on these numbers was estimated to \( \pm 13 \ \overline{p} \).

As a further illustration of what can be seen with Schottky scans, Fig. 37 beautifully demonstrates stochastic momentum cooling in before/after scans.

Schottky scans are usually made at high harmonics of \( f_{\text{rev}} \). Firstly, for a given resolution in \( \Delta f_{\text{rev}} \), the required scan time is proportional to \( 1/f \). Secondly, one often uses the signal from a PU that drives the stochastic cooling. There, a high bandwidth is desired and therefore the PU is made more sensitive at high frequencies.
Fig. 37 Schottky scans before and after momentum cooling of $6 \times 10^6 \overline{p}$ in the Antiproton Accumulator. The scan is made around $h = 170$, at 314 MHz.

A position-sensitive PU will deliver Schottky signals from the incoherent betatron oscillations of the individual particles. With a beam centred in the PU, perfect balance of sensitivity, and perfect linearity, the harmonics of $f_{\text{rev}}$ will not be present. The spectrum (Fig. 38) consists of bands centred at the values

$$f_m = (m \pm Q)f_{\text{rev}}$$

where $m$ is the mode number, 0, 1, 2, ....

Fig. 38 The signal from a position-sensitive PU contains the frequencies $f_m$ of the "betatron sidebands". Here, the non-integer part of $Q$ is 0.35 or 0.65.

The non-integer part of $Q$ (or its complement to 1, see section 3.01) is thus measured. The width of the bands, together with the knowledge of $\Delta p$ and the chromaticity of the machine, $\xi$, yields $\Delta Q$. It is an interesting exercise to show that a particular relation between $m$, $Q$, $\eta$ and $\xi$, leads to a vanishing width of the band at $f_m$ (Appendix 6.04).

### 3.03 Emittance Measurement

Any beam-size measurement on a circulating beam is at the same time an emittance measurement by virtue of the relation

$$\varepsilon = a^2/\beta$$

where $\varepsilon$ is the emittance, $a$ the half-width or -height of the beam and $\beta$ the value of the beta-function at the place where $a$ is measured. The definition of $\varepsilon$ and $a$ is often a source of confusion and needs to be specified clearly.

On beams circulating in storage rings, one can observe the betatron bands in the
Schottky noise. The area of a band is a measure of the rms betatron amplitude and an emittance can be derived after calibration, e.g. with a scraper, see section 2.16.

In transport lines, more than one beam-size measurement is required. For an unambiguous determination of size and orientation of the emittance ellipse, the beam size needs to be known at least at three locations, with known transfer matrices between them and, optimally, a betatron phase advance of 60°. A particularly simple case, as occurs around a "waist", is shown in Fig. 39. One might think that, because of the symmetry, two measurements would suffice. The third measurement is needed however, to verify that a symmetric situation has indeed been obtained. The most-used device for this purpose is the SEM-grid (see section 2.05).

![Diagram](image_url)

Fig. 39 Emittance ellipses at three locations: at a waist and 60° in betatron phase to either side. Transforming the size-defining lines a₁, a₂, c₁, c₂ to location b, defines the emittance there.

At lower energies, e.g. at the output of a 50 MeV linac, the technique of phase space scanning can be used (Fig. 40). One arranges for the beam to be fairly wide in the plane in which the emittance is to be measured. A slit selects a narrow slice in x, the transverse coordinate. That slice is left to diverge over a drift space. Its extension in x' is thus transformed into an extension in x, measured with a profile detector, e.g. a SEM-grid. Scanning the beam over the slit by means of two bending magnets, for every x the extension in x' at the slit is obtained, and the emittance, whatever its shape may be, can be reconstructed.
3.04 Measurement of Energy

In a circular machine with well-known orbit length, the energy may be derived from the measurement of revolution frequency (either by counting, when the beam is bunched, or from Schottky scans, when the beam is coasting), and the exact knowledge of the circumference.

The energy spread, $\Delta E$, of a bunched beam can be inferred from the bunch length, knowing the rf voltage and the factor $\eta$ (see section 3.02). For coasting beams it is the width, $\Delta f$, of a harmonic band, together with $\eta$ which gives $\Delta E$. All this is basic accelerator physics.

Spectrometers are the standard means of measuring the energy and its spread at the output of linacs.

Let us follow the beam as it makes its way through the set-up shown in Fig. 41. The axis of the beam, $x = 0$, is the path taken by a particle of central momentum, $p_0$. To begin with, one produces a wide beam, from which a slit selects a small sample (a). After a drift space, a D-quadrupole-lens greatly increases the divergence of the sample (b) which, after a further drift space, permits an F-lens to rotate the sample such that its width is large and its divergence small (c). This is the situation at the entrance to the bending magnet. At its exit we show three beams: the middle one represents the particles with momentum $p_0$; the one above, those with momentum $p_0 - \Delta p$, more strongly bent; the one below, those with momentum $p_0 + \Delta p$, less strongly bent; $\Delta p$ is shown as the smallest resolved momentum bite. One sees immediately that for good resolution one needs a small sample emittance $\varepsilon$, a large beam width $w$ in the bending magnet and a large angle $\phi$:

$$\Delta p = \frac{\varepsilon}{w \phi}$$

which explains what we have done to the beam so far. The separation in $x'$ of the three
representative beams must now be converted into a separation in x, so that it can be measured. First, an F-lens introduces a strong convergence (e) and after a final drift space the desired separation in x is achieved at a profile detector placed there (f). Overall, one might see this as a highly chromatic imaging of the slit onto the profile detector.

Such spectrometry is relatively easy to perform on 50 MeV protons but becomes difficult with increasing energy. Not only because the magnets will necessarily be bigger, but, more basically, because it becomes impossible to make a slit which, on the one hand, is thick enough to stop the particles outside the wanted sample, and, on the other hand, constitutes a limit only in x and not in x'.

Fig. 41 Above: Basic layout of a spectrometer. D : defocusing lens, F : focusing lens, B : bending magnet. Underneath : the situation in phase space at the six significant locations a - f.

3.05 Polarimetry

Sometimes the experimental physicists delight in polarized beams and the accelerator physicists strive to provide them. A beam is said to be fully polarized, $P = 1$, when the spin of all particles is pointing in the same direction, up or down. A beam is unpolarized, $P = 0$, when the spins of the particles do not have a preferred orientation; half of them will be up, the other half down.

Polarized beams are not easy to produce. Also, polarization may be lost during acceleration, on so-called depolarizing resonances. P is therefore a quantity to be monitored all along the beam's path, from the source until delivery to the physics experiment. As
mentioned in the introduction, this is too specialized a subject for an introductory course. We will just mention three methods and refer to the literature.

Firstly, P can be measured in the physics experiment itself, through the asymmetry in the scattering of the beam particles or in the products of their collisions with target nucleons. This accurate determination can serve as a calibration for other methods.

Secondly, a thin fibre can be brought into the beam, even into the fringe of a circulating beam, and the asymmetry in the scattered particles observed (Mott scattering).

Thirdly, the cross section for Compton scattering depends on the polarization of both the particles and the photons. By shining polarized LASER light onto a circulating beam, P can be determined.

4. CONCLUDING REMARKS

I would like to conclude with some advice, first on the technical-operational level.

It is important that calibration, automatic or on demand, can be performed remotely and without interruption to the operation of the accelerator. This applies particularly to beam transformers and position pick-ups.

Status signals must indicate the good order of a device and permit remote fault diagnosis.

For data treatment and the display of results, diagnostic systems usually rely on a small local computer or are linked to a larger central controls computer. I consider it important that the software, which contains the understanding of the measurement and determines the way in which the desired information is extracted, be conceived (and perhaps even written) by the person who has conceived the diagnostic device.

Lastly, and this is true for all components of a machine: good documentation is indispensable for efficient use of the systems and for their maintenance.

In a more general vein, it is no idle advice that before designing the diagnostic equipment for a machine, one should first acquaint oneself with the machine and its possible modes of operation, and with the properties and behaviour the beam may show under various conditions. One will take into account not only the "nominal" beam, but also what it might be like in an early stage, the running-in of the machine, and under abnormal conditions, when one is particularly dependent on diagnostics.

One will think of tricky measurements the machine experimenters will want to carry out in order to improve performance and basic knowledge, but equally consider the need for precise, unfailing and easily perceived information during routine operation.

Often diagnostic equipment is added at an advanced state in the design of an accelerator. That is wrong. Diagnostic systems must be included in the design at an early stage, otherwise only too often one finds that no space is left at the best-suited locations.

Another important aim, when building a new accelerator, is to have a complete set of diagnostic systems tested and ready for use on the day of first beam. Not only is adequate
diagnostic equipment essential for an efficient running-in of the accelerator, it is also an economic investment in terms of time, pain and simply cost of electricity that it helps to save.

5. ACKNOWLEDGEMENTS

My thanks go to those students of previous courses, who, over the years, have helped me by pointing out weak spots; to some colleagues who will recognise themselves, for their helpful comments; and to Mrs. L. Ghilardi for her patient and careful preparation of this paper.

6. APPENDICES

6.01 Signal Level on an Electrostatic PU

It is instructive to make an estimate of voltage levels obtained on the electrodes of a PU, for realistic beam conditions. Consider a rectangular shoe-box configuration, with dimensions typical for medium-sized storage rings. The PU is inserted in a vacuum chamber, also of rectangular cross-section.

![Fig. 42 Rectangular shoe-box PU inside a rectangular vacuum chamber. The dimensions are those of the electrodes.](image)

With the dimensions shown in Fig. 42, the capacity of the whole PU is approximately $C = 100 \text{ pF}$, i.e. $C_1 = 50 \text{ pF}$ for the left or right electrode.

We first consider a fairly weak beam of $10^9$ protons, close to the speed of light, in a bunch of parabolic longitudinal density distribution and a total length of 80 ns. The peak line-density is then

$$\lambda = \frac{10^9 \times 1.6 \times 10^{-19} \text{Cb}}{80 \times 10^{-9} \text{s} \times 3 \times 10^{10} \text{cm/s}} \times 1.5 = 10^{-13} \text{Cb/cm}$$

where the final factor 1.5 is the ratio in height between a rectangle and a parabola of equal area and length. Exceptionally, we use 'Cb' instead of 'C' for 'Coulomb'.

The charge induced on the two electrodes of the PU is equal to the charge of the beam within its length. For a beam passing through the centre of the PU, the charge on one electrode, left or right, is
\[ Q_1 = \frac{J}{2} \times \ell = \frac{1}{2} \times 10^{-13} \text{Cb/cm} \times 20\text{cm} = 10^{-12} \text{Cb} \]

and the peak-voltage \[ U_p = \frac{Q_1}{C_1} = \frac{10^{-12} \text{Cb}}{50 \times 10^{12} \text{F}} = 20 \text{mV} \]

With a high input-impedance amplifier, directly connected to the feedthrough, this is a signal level just sufficient for forming a difference signal with adequate resolution.

At the other extreme, consider an intense beam of \(10^{12}\) protons in a bunch, also of parabolic shape, but only 4 ns total length. We now find

\[ U_p = 400 \text{ V} \]

and the problem will rather be the protection of the head-amplifier.

### 6.02 Coulomb Interactions of Beam Particles with Matter

Several kinds of detectors rely on the interaction of the beam particles with matter, gaseous or solid. The effects made use of are:

- ionization of gas (residual or molecular jet),
- "secondary emission" of electrons from surfaces,
- production of light (scintillation; in gases, liquids and solids).

These effects are all due to the same basic mechanism, the transfer of energy through Coulomb-interaction from a beam particle to a shell electron, and therefore exhibit a common functional behaviour.

Consider a beam particle passing close to an atom, at high speed, such that the particle's direction and the "impact parameter" \(b\) (i.e. the minimum distance between the particle and the concerned shell electron, see Fig. 43), change little during the encounter.

\[ \text{Fig. 43} \quad \text{Encounter between a beam particle and a shell electron. } F : \text{Coulomb force, } b: \text{impact parameter.} \]

Integrated over the encounter, the longitudinal component, \(F_x\), of the Coulomb force averages to zero, whereas the transverse component, \(F_y\), does not and will impart a transverse momentum, \(p_y\), to the electron:

\[ \int_{-\infty}^{+\infty} F_y \, dt = p_y \]
thus exciting, or even ionizing the atom.

From this simple picture we learn the first important fact: electrons are mostly produced at right angles to the direction of the beam (head-on collisions, for which \( b \) is very small, and which produce forward-electrons, are very rare). The distribution of electron energies extends to very high values, but the bulk of the electrons have energies below 20 eV. On average, a relativistic proton loses some 100 eV per encounter.

The Bethe formula describes the rate at which the beam particle loses its energy. In Gaussian units:

\[
\frac{dE}{ds} = 4\pi NZ \frac{z^2e^4}{m\beta^2c^2} \ln\left(\frac{2m\gamma^2\beta^2c^2}{I}\right) - \beta^2
\]

where

- \( N \) atoms/cm\(^3\)
- \( Z \) atomic number
- \( I \) ionization potential
- \( z \) charge number
- \( \beta, \gamma \) relativistic parameters
- \( m \) electron mass
- \( e \) elementary charge
- \( c \) velocity of light

A crude simplification, to highlight the functional behaviour (using density \( \rho \) for NZ, which is only true within a factor 2), gives:

\[
\frac{dE}{ds} = \text{const.} \rho \frac{z^2}{\beta^2} \ln\left(\frac{p^2}{I}\right)
\]

This formula reveals the second important fact, namely the dependence on \( z^2 \). An ion with charge \( z \) will produce \( z^2 \) as much light in a scintillator (or \( z^2 \) as many secondary electrons from a foil) as a proton of the same speed \( \beta c \). In terms of electrical beam current, the factor is \( z \).

The third important information is the dependence of \( dE/ds \) on the particle’s energy. Figure 44 shows this in the often-used definition of "\( dE/dx \)", normalized to the density of the material traversed. For most materials the minimum \( dE/dx \) is around 2 MeV/g/cm\(^2\). The sharp increase with decreasing energy is characteristic (the reason for the so-called "Bragg peak" at the end of the particle’s range), which makes low energy particles much more efficient.
Fig. 44. Typical energy loss of a proton in matter, as a function of kinetic energy.

6.03 Statistical Limit in Profile Measurements

Transverse beam profiles are often measured by collecting electrons or photons, produced by the beam's particles in a gas, from a foil or on a scintillator. The collection occurs into channels, the width of which is given either by the design or by the spatial resolution of the device.

When the beam is very weak, one increases the gain of the amplifiers, with the limit usually seen in the electrical noise of the circuits involved. There is, however, a much more basic limitation due to the finite number of electrons or photons collected and the statistical nature of their production.

Let us assume that the projection of the beam's 2-dimensional density distribution onto one plane has a Gaussian shape (Fig. 45), with $\sigma$ the standard deviation or rms-width.

$$\frac{dn}{dx} = \frac{1}{\sigma \sqrt{2\pi}} e^{-\frac{x^2}{2\sigma^2}}$$

with

$$\int_{-\infty}^{+\infty} \frac{dn}{dx} \, dx = 1$$

Fig. 45 Distribution of a Gaussian profile over channels $0.2\sigma$ wide.

Within a certain time interval, which may be the desired measurement time or simply the time that the beam lasts, the total number of electrons or photons reaching the detector is
Let us take a channel width of $\Delta x = 0.2 \sigma$. The 20 channels between $x = -2 \sigma$ and $x = +2 \sigma$ will collect $0.95 N_{\text{tot}}$ electrons or photons. Consider the central channel, from $x = 0$ to $x = 0.2 \sigma$. The number it collects is

$$N_c = 0.083 N_{\text{tot}}$$

The statistical fluctuation on $N_c$ is $\sqrt{N_c}$ and is also called "sampling fluctuation". As an example, let us demand a 5% accuracy on the measurement of central density:

$$\sqrt{N_c} / N_c = 0.05 \quad \text{therefore} \quad N_c = 400$$

Since $N_{\text{tot}} = N_c / 0.083$, we need for a "good" profile measurement at least

$$N_{\text{tot}} = 4800 \quad \text{electrons or photons.}$$

Similar exercises can be carried out for other criteria for a "good" profile measurement, resulting in specific compromises between spatial and time resolution.

### 6.04 Schottky Side Bands of Vanishing Width

In paragraph 3.02 we saw that the spectrum of the signal from a position-sensitive PU contains the frequencies

$$f_m = (m \pm Q)f_{\text{rev}} \quad \text{mode number: } m = 0, 1, 2, \ldots \quad (1)$$

These are not lines but rather bands of a certain width $\Delta f_m$, because the beam particles do not all have the same momentum and both $f_{\text{rev}}$ and $Q$ depend on momentum. With $\Delta p$ the momentum spread of the particles:

$$\Delta f_m = \Delta p \frac{df_m}{dp}$$

We mentioned the interesting fact that under certain conditions the width of these bands may shrink to very small values, or indeed vanish. This happens when the dependence of $f_{\text{rev}}$ and the dependence of $Q$ on momentum (the chromaticity) just cancel each other, so that $df_m / dp = 0$. Differentiating Eq.(1) with respect to momentum $p$:

$$\frac{df_m}{dp} = (m \pm Q)\frac{df_{\text{rev}}}{dp} \pm f_{\text{rev}} \frac{d(m \pm Q)}{dp} \quad (3)$$

$$= (m \pm Q)\frac{df_{\text{rev}}}{dp} \pm f_{\text{rev}} \frac{dQ}{dp} \quad (4)$$

We introduce the chromaticity

$$\xi = \frac{dQ}{dp} / p \quad (5)$$

and the relation

$$\eta = \frac{df_{\text{rev}} / f_{\text{rev}}}{dp / p} \quad (6)$$
\( \eta \) is a function of energy, \( \gamma = E/E_0 \), and of the transition energy \( \gamma_{tr} \), a property of the machine lattice:

\[
\eta = \left| \frac{1}{\gamma^2} - \frac{1}{\gamma_{tr}^2} \right| \tag{7}
\]

Inserting Eqs. (5) and (6) into Eq. (4):

\[
\frac{df_m}{dp} = [(m \pm Q) \eta \pm \xi] \tag{8}
\]

which will be 0 when

\[
(m \pm Q) \eta = \xi \tag{9}
\]

or

\[
(m - Q) \eta = \xi. \tag{10}
\]

When condition (10) is fulfilled, the width \( \Delta f_m \) of the betatron band will vanish. Looking for that line in the spectrum and knowing \( \eta \), one obtains the chromaticity \( \xi \) (or vice versa).

7. LIST OF HELPFUL LITERATURE

As said in the Introduction, the wide coverage of the subject brings with it a lack of depth. A particularly extensive list of literature should compensate for that and help CAS-students and readers of this report to find the way to the necessary details.

7.01 Previous CAS Lectures on Beam Diagnostics


GENERAL ACCELERATOR PHYSICS
K. Potter, Beam Profiles, p.301
K. Potter, Luminosity Measurements, p.318
P. Wolstenholme, Control Systems of Accelerators, Instrumentation, p.519.

ADVANCED ACCELERATOR PHYSICS
D. Boussard, Schottky Noise and Beam Transfer Function Diagnostics, p.416

SECOND GENERAL ACCELERATOR PHYSICS COURSE
P. Strehl, Beam Diagnostics, p.99

ADVANCED ACCELERATOR PHYSICS
D. Boussard, Schottky Noise and Beam Transfer Function Diagnostics, p.90.
JOINT US-CERN SCHOOL ON PARTICLE ACCELERATORS
FRONTIERS OF PARTICLE BEAMS; OBSERVATION, DIAGNOSIS AND CORRECTION
Capri, 1988, Lecture Notes in Physics Nb.343, Springer-Verlag,
Berlin/Heidelberg, 1989; many articles on beam diagnostics.

THIRD GENERAL ACCELERATOR PHYSICS COURSE
H. Koziol, Beam Diagnostics, p.63; superseded by the present version.

FOURTH GENERAL ACCELERATOR PHYSICS COURSE
M. Serio, Tune Measurements, p.136.

FIFTH GENERAL ACCELERATOR PHYSICS COURSE
H. Koziol, Beam Diagnostics, p.565; superseded by the present version.

FIFTH ADVANCED ACCELERATOR PHYSICS COURSE
A. Verdier, Chromaticity, par. Measurements, p.98
D. Boussard, Schottky Noise and Beam Transfer Function Diagnostics, p.749
A.C. Melissinos, Energy Measurement by Resonant Depolarization, p.1051

SYNCHROTRON RADIATION AND FREE ELECTRON LASERS
A. Hofmann, Characteristics of Synchrotron Radiation
A. Hofmann, Diagnostics with Synchrotron Radiation

7.02 Workshops and Schools

"European Workshops on Beam Diagnostics and Instrumentation for Accelerators" (DIPAC)

"Accelerator Instrumentation" (AIW), Annual Workshops, US
AIP Conference Proceedings, Particles and Fields

"Beam Instrumentation Workshops" (BIW), US
AIP Conference Proceedings, Particles and Fields
Santa Fe, 1993, No.319; Vancouver, 1994, No.333; Argonne, 1996, No.390;
"Transverse Emittance Preservation and Measurement", 4th ICFA Mini-Workshop, CERN,

7.03 Literature by Subject

In addition to the quotations in 7.01, this selective list intends to provide first contact with a subject and complementing details to the sketchy presentations in the General CAS Course. Selection criteria are: ease of retrieval; introductory or review character; didactic value; presentation of an interesting variant; recent state of the art. Articles of complex presentation, or treating intricate details, are not included, neither those published as internal reports only. From 8 authors on, only the name of the first one is given. Titles are sometimes shortened to their essential part and the following abbreviations are used:

EPAC : European Particle Accelerator Conference
HEACC : International Conference on High Energy Accelerators
PAC : US Particle Accelerator Conference
DIPAC : European Workshop on Beam Diagnostics and Instrumentation for Particle Accelerators
AIW : Accelerator Instrumentation Workshop
BIW : Beam Instrumentation Workshop
NIM : Nuclear Instruments and Methods

BEAM TRANSFORMERS

WALL CURRENT MONITORS
PICKUPS

SECONDARY EMISSION MONITORS

BUNCH-LENGTH MONITORS
WIRE SCANNERS

BEAM LOSS MONITORS

GAS-CURTAIN and RESIDUAL-GAS PROFILE-MONITORS

SCINTILLATOR SCREENS

OPTICAL TRANSITION RADIATION

SCHOTTKY SIGNALS

SYNCHROTRON RADIATION

Q-MEASUREMENT, CHROMATICITY

EMITTANCE MEASUREMENT

COMPTON SCATTERING (beam size measurement)
POLARIZATION MEASUREMENT

COULOMB INTERACTION OF BEAM PARTICLES WITH MATTER